

Non-Gaussian beam dynamics in low energy antiproton storage rings

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Abstract

In low energy antiproton facilities, where electron cooling is fundamental, the cooling forces together with heating phenomena causing emittance blow-up, such as Intra Beam Scattering (IBS), result in highly non-Gaussian beam distributions. In these cases, a precise simulation of IBS effects is essential to realistically evaluate the long term beam evolution, taking into account the non-Gaussian characteristics of the beam. Here, we analyse the beam dynamics in the Extra Low ENergy Antiproton ring (ELENA), which is a new small synchrotron currently being constructed at CERN to decelerate antiprotons to energies as low as 100 keV. Simulations are performed using the code BETA-COOL, comparing different models of IBS.

Keywords: Beam dynamics; Low energy storage rings; Antiprotons; Intra-beam scattering; Numerical simulations

1. Introduction

Antiprotons, stored and cooled at low energies in a storage ring or at rest in traps, are highly desirable for the investigation of a large number of basic questions on fundamental interactions, on the static structure of exotic antiprotonic atomic systems or of (radioactive) nuclei as well as on the time-dependent quantum dynamics of correlated systems. The Antiproton Decelerator (AD) at CERN [1] is currently the world's only low energy antiproton factory dedicated to antimatter experiments. The development of new antiproton facilities, such as the Extremely Low ENergy Antiproton ring (ELENA) [2] to further decelerate

27 beams from the AD in a well controlled manner, will open a unique possibility
28 to provide cooled, high-quality beams of extra-low energy antiprotons.

29 ELENA is a small synchrotron equipped with an electron cooler, which is
30 currently being constructed at CERN to further decelerate antiprotons from the
31 AD from 5.3 MeV to kinetic energies as low as 100 keV with a beam population
32 of $\sim 10^7$ cooled antiprotons. At such low energies it is very important to care-
33 fully take contributions from electron cooling (e-cooling) and heating effects into
34 account. Among these heating effects is Intra-Beam Scattering (IBS), which is
35 one of the main limiting processes for the performance of typical low energy ion
36 storage rings.

37 For simplicity, initial Gaussian beam distributions are usually assumed for
38 beam dynamics simulations in low energy ion rings. For instance, for ELENA
39 beam dynamics simulations of the cooling process in presence of rest gas scatter-
40 ing and IBS have been done in [3, 4]. In both cases, initial Gaussian antiproton
41 beam distributions were assumed and a standard IBS model (the so-called Mar-
42 tini model [5]) was used. In [3, 4] simulations led to an overcooling of the beam
43 core and highly populated long amplitude tails. We suspect that this overcooling
44 result is unphysical and an artefact of considering standard IBS models.

45 Standard algorithms to estimate IBS are based on the growth of the rms
46 parameters of Gaussian distributions [5–8] and, thus, allow long term evolu-
47 tions of emittances only if the beam remains Gaussian. However, in many of
48 these facilities, where electron cooling is a fundamental part, the cooling forces
49 result in highly non-Gaussian beam distributions. In these cases, other algo-
50 rithms applicable for a non-Gaussian distribution of IBS effects are required to
51 realistically evaluate the long term beam evolution.

52 To address this matter we have investigated the e-cooling process in ELENA
53 by means of beam dynamics simulations using the code BETACOOOL [9] and
54 comparing different models of IBS for the first cooling plateau at the interme-
55 diate beam momentum 35 MeV/c. A particularity of these studies is the use
56 of input beam distributions based on real measurements of beam profiles in the
57 AD. Our final goal is to make a more precise description of the beam evolution

58 during the cooling process under more realistic assumptions.

59 2. ELENA cycle

60 In ELENA electron cooling will be used to counteract the emittance and the
61 relative momentum spread blow-up caused by the deceleration process. This
62 will increase the efficiency of typical experiments capturing the antiprotons in
63 traps by one to two orders of magnitude.

64 The ELENA deceleration cycle is schematically shown in Fig. 1. There
65 are two cooling plateaus: the first cooling plateau lasts approximately 8 s at
66 35 MeV/c momentum, and the second one is applied for 2 s at 13.7 MeV/c. In
67 both cases the cooling is applied to a coasting beam. A third cooling at 13.7
68 MeV/c will be applied to bunched beams prior to extraction.

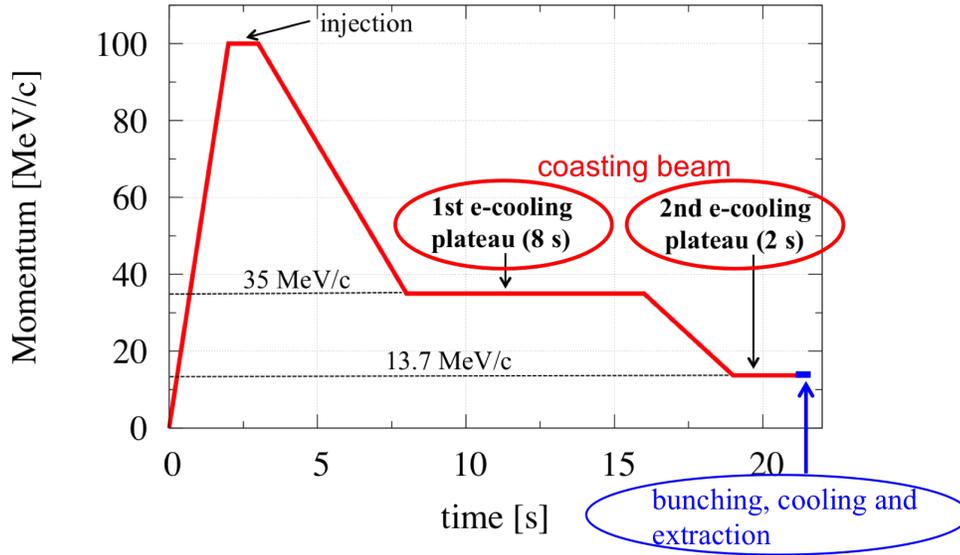


Figure 1: Basic ELENA deceleration cycle.

69 The ELENA optics layout, matched using the accelerator design code MAD-
70 X [10], is depicted in Fig. 2 and is described in detail in [2, 11]. In Table 1 we
71 display some relevant nominal parameters.

Table 1: ELENA nominal machine and beam parameters.

Circumference (m)	30.4
Nominal (dynamic) vacuum pressure (Torr)	3×10^{-12}
Machine tunes Q_x/Q_y	2.3/1.3
Repetition rate (s)	≈ 100
Kinetic energy range (MeV)	5.3 – 0.1
Momentum range (MeV/ c)	100 – 13.7
Beam intensity (number of \bar{p})	$\sim (1 - 3) \times 10^7$
Transverse acceptance (μm)	75
Ejected emittance (rms) $\epsilon_{x,y}$ (π mm mrad)	~ 1
Ejected relative momentum spread (rms) σ_p/p (%)	~ 0.05
Number of ejected bunches	4
Ejected bunch length (m)	1.3

72 3. Beam distribution at injection

73 Beam profile measurements in the AD in the past [12] have shown non-
74 Gaussian transverse beam distributions with compact core and extended tails,
75 generated during the beam cooling process (stochastic cooling and e-cooling).
76 Figure 3 shows an example of beam distribution measurements performed by
77 scraping in the AD at 100 MeV/ c momentum. A scraper blade, located in a
78 position with zero dispersion, has been moved into the beam in small steps
79 to measure the remaining beam current. This allows us to obtain cumulative
80 distribution functions. The differentiation of these cumulative functions corre-
81 sponds to the density of the beam distribution. Actually, the measurement in
82 Fig. 3 represents half of the beam distribution. For this set of measurements
83 approximate physical rms emittances of $\epsilon_x = 0.2$ to $0.5 \mu\text{m}$ were inferred for the
84 horizontal phase space, and $\epsilon_y = 0.15$ to $0.3 \mu\text{m}$ for the vertical phase space.

85 In recent years, such a core-tail beam structure in the AD has been confirmed
86 using Gas Electron Multiplier (GEM) based beam profile monitors [13, 14].

87 For the beam dynamics simulations in ELENA we use measured parameters

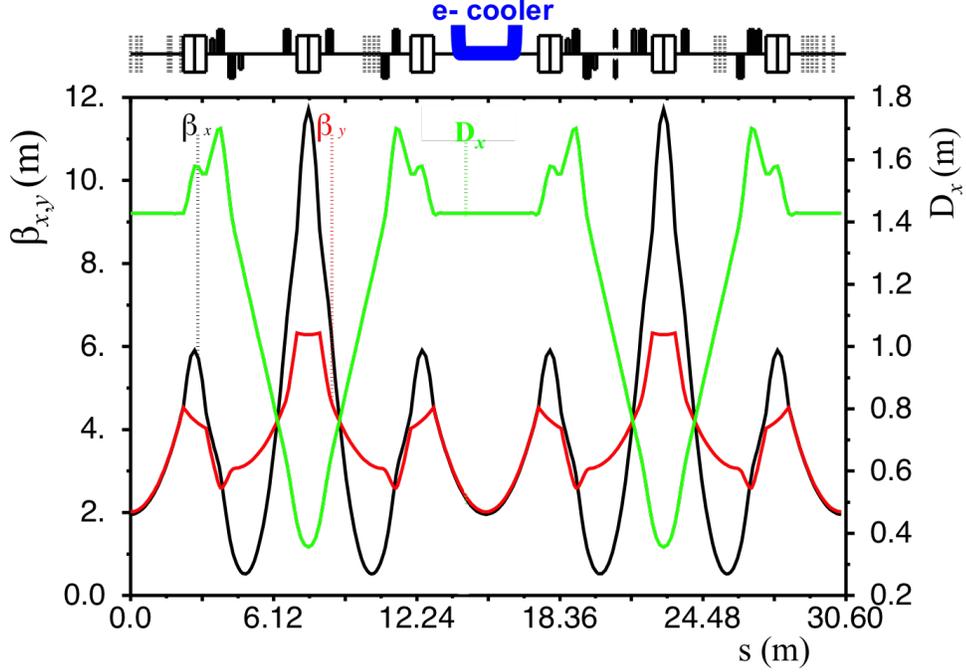


Figure 2: ELENA ring optics.

88 in the AD as a reference to generate an input distribution of macro-particles to
 89 be injected into the ELENA ring. For it, a Python script is used to create an
 90 input core-tail distribution based in the sum of two Gaussian functions in phase
 91 space centered at zero mean values:

$$g(x, x') = N \left\{ (1 - w) \frac{1}{2\pi\epsilon_c} \exp \left[-\frac{I(x, x')}{2\epsilon_c} \right] + w \frac{1}{2\pi\epsilon_t} \exp \left[-\frac{I(x, x')}{2\epsilon_t} \right] \right\}, \quad (1)$$

92 where ϵ_c stands for the core emittance and ϵ_t for the emittance of the Gaussian
 93 phase space representing the tails; N is the total number of macro-particles, and
 94 the parameter w represents a relative weight. The term $I(x, x')$ is the so-called
 95 Courant-Snyder invariant,

$$I(x, x') = \gamma_x x^2 + 2\alpha_x x x' + \beta_x x'^2, \quad (2)$$

96 with β_x , α_x and $\gamma_x \equiv (1 + \alpha_x^2)/\beta_x$ the Courant-Snyder parameters.

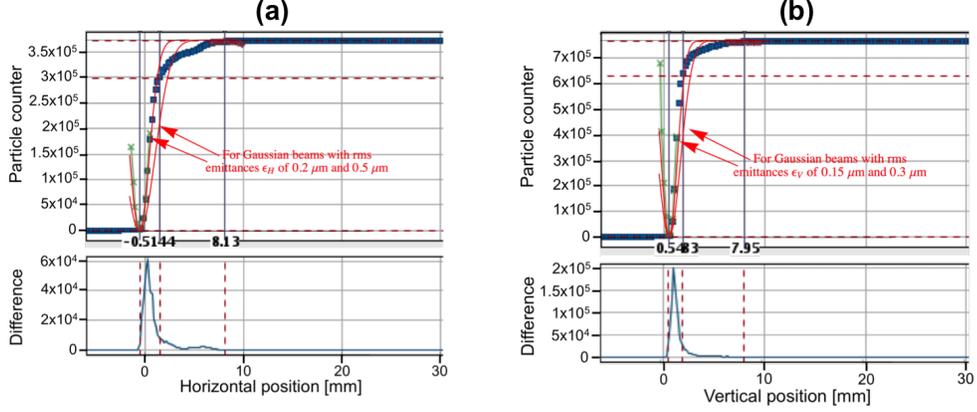


Figure 3: Horizontal (a) and vertical (b) half beam profile measured using a scraper in the AD at 100 MeV/c, taken in 2011. Courtesy of T. Eriksson.

97 Here, the emittance can be given in terms of the standard deviation $\sigma_{c,t}$ for
 98 the betatronic beam width for the core and the tail, respectively, and the optics
 99 parameter β_x : $\epsilon_{c,t} = \sigma_{c,t}^2 / \beta_x$.

100 A similar distribution $g(y, y')$ is assumed for the vertical phase space, with
 101 the corresponding optics parameters β_y , α_y and γ_y .

102 A Gaussian longitudinal phase space is considered for injection from AD
 103 to ELENA. Figure 4 shows a typical longitudinal profile measurement using
 104 tomography techniques in the AD [15]. In this sample the following parameters
 105 were measured: rms bunch length $\sigma_\tau = 125$ ns; rms kinetic energy spread $\sigma_E =$
 106 4 keV; and relative rms momentum spread $\sigma_p/p = (1/2)\sigma_E/E_0 = 0.38 \times 10^{-3}$
 107 (with the nominal energy $E_0 = 5.3$ MeV at the end of the AD cycle).

108 Figure 5 depicts the initial distribution of macroparticles at injection used for
 109 the particle tracking simulations in ELENA, based on the above assumptions.
 110 The following conservative values have been taken into account:

- 111 • For the transverse phase space, based on Eq. (1), we use the following
 112 emittance values: $(\epsilon_c)_{inj} = 0.5 \mu\text{m}$, and the tail is extended to $3 \times (\sigma_t)_{inj} \approx$
 113 10 mm, for both vertical and horizontal planes. For simplicity, here the
 114 same number of macroparticles in the core and in the tail is assumed, i.e.

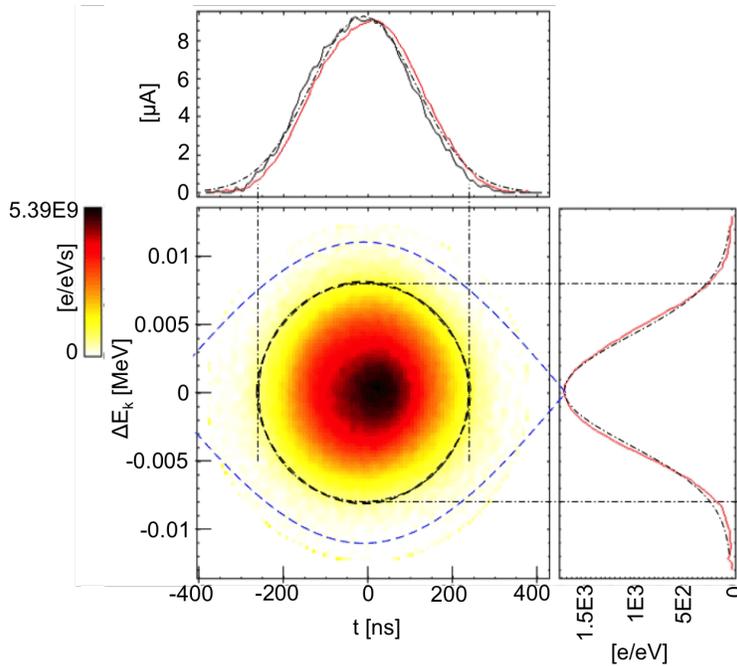


Figure 4: Longitudinal beam profile (kinetic energy spread versus time structure) measurement in the AD at 100 MeV/c, taken in 2011. Courtesy of T. Eriksson.

115 $w = 0.5$.

- 116 • For the longitudinal phase space, the ELENA bunch must be scaled by a
- 117 factor 0.8 from the AD bunch. For example, scaling from the bunch in
- 118 Fig. 4 one finds $(\sigma_\tau)_{\text{inj}} \approx 100$ ns rms bunch length (in units of time) and
- 119 $(\sigma_p/p)_{\text{inj}} \approx 0.3 \times 10^{-3}$ for the relative rms momentum spread.

120 4. Beam dynamics simulations

121 After injection from the AD to ELENA, the beam is decelerated for 5 s from
 122 a momentum of 100 MeV/c down to an intermediate momentum of 35 MeV/c.
 123 Assuming deceleration with constant RF voltage¹, the physical emittances of

¹For simplicity, we have assumed no increase of RF voltage for beam transfer from injection to the start of the first deceleration ramp, and, therefore, no variation of relative

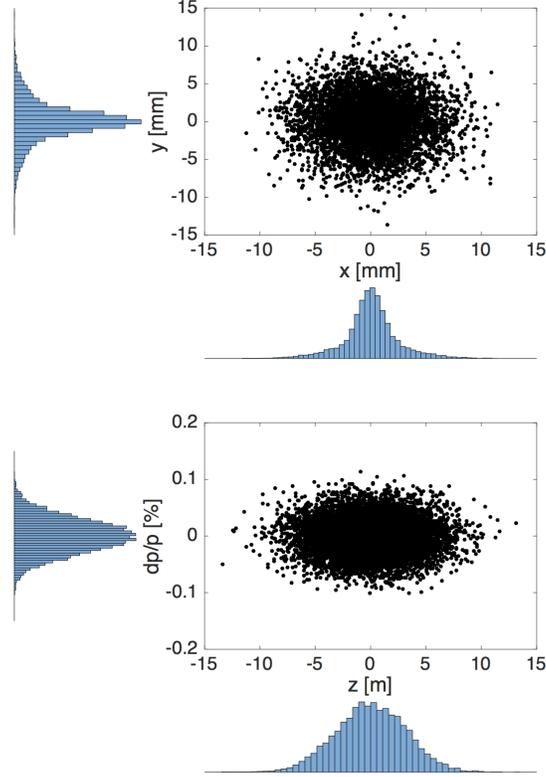


Figure 5: Transverse (top) and longitudinal (bottom) beam profile injected from the AD to ELENA at 100 MeV/c momentum. Distribution of 10000 macroparticles.

124 the beam and the relative momentum spread increase adiabatically by a factor
 125 $f_a = (\beta\gamma)_1/(\beta\gamma)_2 \simeq 2.86$, where β_1 refers to the relativistic velocity factor at
 126 the beginning ($p = 100$ MeV/c) and β_2 at the end ($p = 35$ MeV/c) of the
 127 deceleration ramp, respectively; γ is the corresponding Lorentz factor ($\gamma \approx 1$ at
 128 low energies).

129 Then, the antiproton beam is iso-adiabatically debunched prior to electron
 130 cooling. This debunching process implies a blow-up by approximately a factor

momentum spread at this stage. A more detailed description of the different scenarios of the RF gymnastics for ELENA can be found in [2].

131 $\pi/2$ for the longitudinal emittance [16], and a momentum spread reduction ² by
 132 a factor:

$$f_{\text{iso}} = \frac{\pi^2}{2} \sqrt{\frac{\pi}{2}} \frac{(\sigma_\tau)_b}{T_{\text{rev}}} \simeq 0.65, \quad (3)$$

133 where $(\sigma_\tau)_b = f_a \cdot (\sigma_\tau)_{\text{inj}} \simeq 286$ ns is the bunch length (in units of time) before
 134 debunching.

135 Then, e-cooling is applied for 8 s (first cooling plateau, see Fig. 1) to the
 136 coasting antiproton beam. Figure 6 shows a distribution of 10^4 macroparticles
 137 at the beginning of the e-cooling process at 35 MeV/ c . The beam dimensions of
 138 this distribution are given by: $f_a^{1/2} \cdot (\sigma_c)_{\text{inj}} \simeq 1.73$ mm, $f_a^{1/2} \cdot (\sigma_t)_{\text{inj}} \simeq 5.64$ mm,
 139 and $f_{\text{iso}} \cdot f_a \cdot (\sigma_p/p)_{\text{inj}} \simeq 0.56 \times 10^{-3}$, where the blow-up scaling factors f_a
 140 and f_{iso} are taken into account as described before with respect to the values
 141 at injection. This ensemble of macroparticles is used as an input for the code
 142 BETACOOOL [9]. This code allows us to calculate the evolution of arbitrary
 143 beam distributions under the action of cooling forces and different scattering
 144 effects, such as rest gas scattering and IBS. The code BETACOOOL has been
 145 benchmarked with measurements in the past, for example in the context of the
 146 low energy ion ring ELISA [17], giving a reasonable agreement.

147 4.1. Electron cooling

148 The electron cooling is a well consolidated technique to obtain high-quality
 149 ion beams by means of increasing the 6D phase space density through the dissi-
 150 pative force created by Coulomb interaction of the beam particles with a lower
 151 temperature electron distribution [18].

152 The electron cooling systems employed at low-energy coolers are typically
 153 based on an electron beam immersed in the longitudinal magnetic field of a

²The corresponding momentum spread reduction due to bunching/debunching can be calculated using the typical longitudinal emittance definitions: $\epsilon_L = 4\pi\beta c\sigma_p\sigma_\tau$ for bunched beam and $\epsilon_L = 4(2/\pi)^{1/2}\beta c\sigma_p T_{\text{rev}}$ for coasting beam, where $T_{\text{rev}} = C/(\beta c)$ is the beam time revolution, with C the ring circumference.

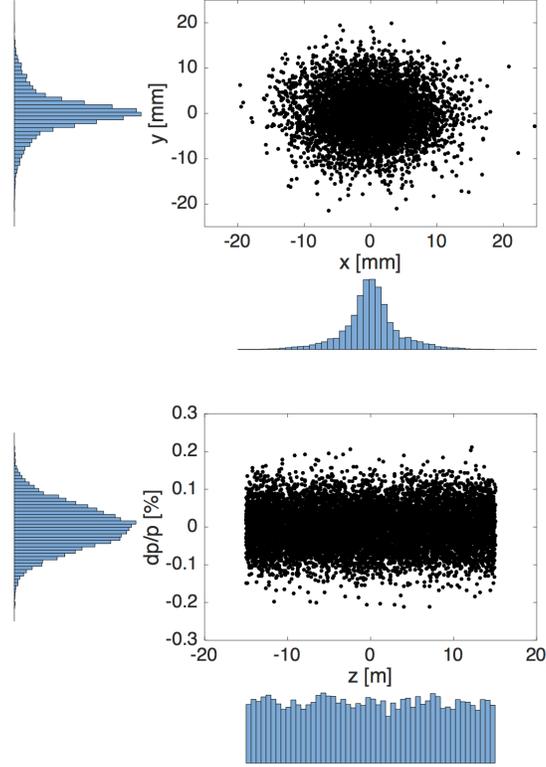


Figure 6: Transverse (top) and longitudinal (bottom) beam profile at the beginning of the first e-cooling plateau at 35 MeV/c momentum. Distribution of 10000 macroparticles.

154 solenoid (magnetised electron beam). For magnetised electron distributions,
 155 several theoretical models for the e-cooling friction force have been proposed in
 156 the literature, see e.g. [19–22]. A comparison of different electron cooling models
 157 is outside the scope of this paper. An exhaustive analysis of the different models,
 158 their validity ranges and limitations, can be found in [23]. Here, for the ELENA
 159 e-cooler simulations, to account for the finite value of the magnetic solenoidal
 160 field, we have used the so-called Parkhomchuk empirical expression [22]:

$$\vec{F} = -\vec{V} \frac{4Z^2 e^4 n_e}{m_e} \frac{L_M}{\left(V^2 + \Delta_{e,\text{eff}}^2\right)^{3/2}}, \quad (4)$$

161 where Z is the ion charge number, e is the electron charge, n_e is the electron
 162 density, m_e is the electron mass, \vec{V} is the relative ion velocity, $\Delta_{e,\text{eff}}$ is the
 163 effective velocity spread of the electrons, and L_M is the Coulomb logarithm,
 164 which is defined as:

$$L_M = \ln \left(\frac{\rho_{\text{max}} + \rho_{\text{min}} + \rho_L}{\rho_{\text{min}} + \rho_L} \right), \quad (5)$$

165 with ρ_{max} and ρ_{min} the maximum and minimum impact parameters, respec-
 166 tively; $\rho_L = m_e c \Delta_{e,\perp} / (eB)$. For ELENA we can approximate $L_M \cong 10$.

167 The expression (4) has been benchmarked with measurements [24], showing
 168 a reasonable agreement, and it seems sufficiently accurate to be used for a simple
 169 estimate of the e-cooler performance. Among others, Eq. (4) is implemented in
 170 the BETACOOOL code.

171 Here, we consider a cylindrical uniform electron beam distribution with
 172 transverse temperature $k_B T_{e\perp} = 0.01$ eV and longitudinal temperature $k_B T_{e\parallel} =$
 173 0.001 eV (with k_B the Boltzmann constant). The space charge in the e-beam is
 174 also taken into account. It generates a parabolic distribution of e-beam veloc-
 175 ities. Relevant parameters of the ELENA e-cooler are summarised in Table 2.
 176 A complete description of the ELENA e-cooler can be found in [2, 3].

177 4.2. Intra-beam scattering

178 IBS is one of the main heating processes limiting the performance of low
 179 energy ion rings. It becomes especially stronger when the phase space volume
 180 of the beam is reduced by cooling, thus limiting the achievable final emittances,
 181 which are determined by an equilibrium state between IBS and cooling.

182 IBS is a beam heating effect produced by multiple small-angle Coulomb
 183 scattering of charged particles within the beam itself. It causes an exchange of
 184 energy between the transverse and longitudinal degrees of freedom, thus leading
 185 to the growth of the phase space area occupied by the beam.

186 Many of the theories of IBS extensively described in the literature, e.g. [5–
 187 8], and frequently used in simulations to calculate the IBS growth rates and its
 188 effect on the beam are only valid for Gaussian distributions, which is unlikely

Table 2: ELENA electron cooler parameters

Beam momentum [MeV/ c]	35 – 13.7
Velocity factor, $\beta = v/c$	0.037 – 0.015
Electron beam energy [eV]	355 – 55
Electron current, I_e [mA]	5 – 2
Electron beam density, n_e [10^{12} m^{-3}]	1.38 – 1.41
Magnetic field in the gun, B_{gun} [G]	1000
Magnetic field in the drift, B_{drift} [G]	100
Expansion factor	10
Cathode radius [mm]	8
Electron beam radius, r_b [mm]	25
Betatron functions, $\beta_{x,y}$ [m]	2.103, 2.186
Horizontal dispersion, D_x [m]	1.498
Flange-to-flange length [m]	1.93
Solenoid length [m]	1.0
Effective length (good field region) [m]	0.7
Electron beam transverse temperature, $k_B T_{e\perp}$ [eV]	0.01
Electron beam longitudinal temperature, $k_B T_{e\parallel}$ [eV]	0.001

189 in many cases. For instance, during the e-cooling process the beam distribution
190 can quickly deviate from a Gaussian, resulting in a very dense core with long
191 tails. In addition, the injected beam from a previous machine of the decelerator
192 chain may be highly non-Gaussian, as likely the beam injected from the AD to
193 ELENA will be.

194 In ELENA, previous simulations of the cooling process, assuming an input
195 Gaussian beam and using a standard IBS model (the Martini model [5]) pointed
196 out an overcooling of the core and highly populated long tails [3, 4]. This core
197 overcooling looks unphysical and a product of a simulation artefact due to the
198 assumption of the Gaussian approximation.

199 Although the Gaussian approximation is still useful for a relative analysis,
200 for a more realistic estimate of the beam evolution it would be more correct
201 to pay attention to the non-Gaussian structure of the beam. In this case, it is
202 necessary to apply IBS induced kicks based on diffusion coefficients which are
203 different for particles inside and outside of the core.

204 Different IBS models for non-Gaussian distributions have been proposed
205 in the literature [25–30], and implemented in the code BETACOOOL [31]. A
206 preliminary study of the intra-beam scattering effects in ELENA using a core-
207 tail model was presented in [32].

208 Here, we compare results using the following IBS models:

- 209 • Standard model: here, we use the so-called Martini model [5]. This model
210 is an extended version of Piwinski’s model [6], taking into account lattice
211 derivatives. The computation process can basically be summarised as
212 follows: rms emittances and momentum spread are computed from the
213 input macro-particle distribution; the growth rates are calculated at each
214 element of the lattice along the ring, assuming Gaussian beams with these
215 rms parameters; and, finally, random IBS kicks are then applied to the
216 full macro-particle distribution based on the calculated growth rates.
- 217 • Simplified kinetic model: based on the three-dimensional approximate al-
218 gorithm described in [29]. This model is based on a numerical solution of

219 the Fokker-Planck equation, assuming the following approximations: (1)
220 the friction force has a linear dependence on momentum; (2) the compo-
221 nents of the diffusion tensor are constant. The components of the diffusion
222 tensor are calculated in accordance with the Bjorken-Mtingwa formulae
223 [7]. This model also assumes that most of the IBS interactions take place
224 inside the beam core, which is usually close to a Gaussian distribution.

- 225 • Local model [30]: this algorithm takes into account the local density of
226 particles after establishing an array of particles in the total beam dis-
227 tribution. It calculates the diffusion tensor components locally through
228 the Coulomb scattering of a test particle with the nearest particles. The
229 diffusion components are calculated at each optical element of the ring.
230 This algorithm can be applied to any arbitrary particle distribution and
231 is very suitable to precisely describe IBS effects during cooling processes
232 in hadron storage rings. However, this algorithm requires much longer
233 computation times than the previous models.

234 *4.3. Beam evolution*

235 Figure 7 illustrates our beam dynamics simulation sequence. A distribution
236 of 10^4 macro-particles is tracked through the ELENA lattice using the model
237 beam algorithm of BETACOOOL to study the beam evolution with e-cooling at
238 35 MeV/c \bar{p} momentum. For this study the initial beam structure is shown in
239 Fig. 6, based on the bi-Gaussian function of Eq. (1) and applying the corre-
240 sponding scaling factors, as described in previous sections. The optics lattice
241 information is generated by the code MAD-X [10] and read by BETACOOOL.

242 The beam is cooled down for 8 s by e-cooling. In addition, IBS is switched
243 on. In these simulations we have also taken into account the effect of rest gas
244 scattering, considering the nominal vacuum pressure $P = 3 \times 10^{-12}$ Torr, and
245 the following outgassing species: 95% H₂, 2% CO, 2% CO₂ and 1% CH₄ with
246 a total gas density (at room temperature) of 9.6×10^{10} m⁻³ [33]. Although
247 included in these simulations for the sake of completeness, for ELENA with the

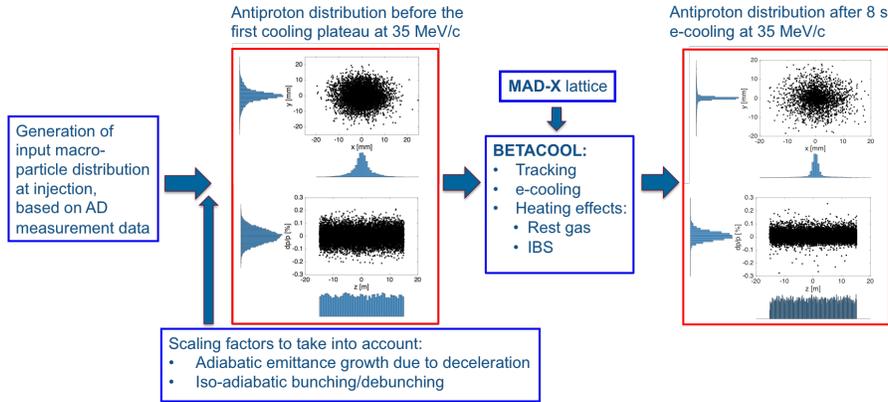


Figure 7: Schematic description of the simulation sequence of the Monte Carlo multiparticle tracking in the ELENA ring applying e-cooling and different heating scattering effects. The transverse and longitudinal beam profiles at the beginning of the first e-cooling plateau at 35 MeV/c momentum are shown on the left hand side. The resulting beam profiles after 8 s e-cooling are shown on the right hand side.

248 nominal vacuum pressure of 3×10^{-12} Torr, the effect of rest gas scattering has
 249 been estimated to be practically negligible in comparison with IBS [4, 34].

250 In principle, a local IBS model will allow us to make a self-consistent estimate
 251 of the beam evolution. In these simulations the integration time step is 0.5 s.
 252 To apply the IBS effect locally we have established cells with dimensions of 0.1 σ
 253 and 100 local particles each. For the IBS simulations the friction and diffusion
 254 coefficients are calculated at each optical element of the lattice.

255 The rms emittance and momentum spread evolution is shown in Fig. 8, where
 256 the e-cooling process is compared in presence of three different IBS models:
 257 local, kinetic and standard IBS (see Sec. 4.2 for details). One can see that
 258 applying a local IBS model results in slightly higher rms emittances. On the
 259 other hand, for the cases of the kinetic and the standard IBS models, the results
 260 are practically similar.

261 In Fig. 8 there is also an interesting feature of the evolution of the relative
 262 rms momentum spread (σ_p/p) for the case of e-cooling plus the local IBS model.
 263 Around 5 s there is a sudden increase of σ_p/p (rms). If we looked at the scatter

264 plots of the transverse and longitudinal beam profiles after 8 s cooling (Fig. 9),
 265 one can see that a few macroparticles have been kicked to high momentum
 266 spread, $|\Delta p/p| > 0.5\%$. In the transverse plane, some macroparticles can even
 267 be scattered outside the effective physical aperture of the machine (60 mm
 268 diameter), and get lost. Of course, these few macroparticles at high amplitude
 269 increase significantly the rms parameters of the distribution.

270 The emittance as a rms quantity is biased by strong tails. Therefore, in
 271 order to calculate the rms parameters concentrating the relevant part of the
 272 distribution, cuts on the final distribution must be applied. In this case, we
 273 can establish the following amplitude cuts: $-30 \text{ mm} < x, y < 30 \text{ mm}$ and
 274 $-0.5\% < \Delta p/p < 0.5\%$. Alternatively, we can use the emittance definition
 275 according to the value that encompasses a specific percentage of the beam.
 276 For example, to follow just the evolution of the dense core we could calculate
 277 the emittance within 68% of the distribution and, to extend the study to the
 278 core-tail evolution, we could evaluate the beam invariants within 95% of the
 279 distribution. Figure 10 shows the evolution of the transverse emittances and
 280 relative momentum spread for half beam widths containing 68% and 95% of the
 281 particles, respectively.

282 After 8 s cooling, $\epsilon_{x,y}$ (68%) and σ_p/p (68%) approach to equilibrium values,
 283 while $\epsilon_{x,y}$ (95%) monotonically decreases far from achieving equilibrium values.
 284 The narrow core (68%) will reach a cooling-IBS equilibrium faster than the high
 285 amplitude tails (within 95%), which will require much longer time.

286 Table 3 summarises the emittances and relative momentum spread values
 287 for the ELENA first cooling plateau for the different algorithms studied.

288 The beam profiles at the end of the cooling process for 35 MeV/c beam
 289 momentum are shown in Fig. 11, comparing the results for the three IBS
 290 under study. On the one hand, the cooling of the core is smoother if an IBS
 291 local model is applied and, likely, it describes more accurately the actual process,
 292 since it is beam shape-independent. On the other hand, applying the standard
 293 model and the simplified kinetic model results in an overcooling of the beam
 294 core.

Table 3: Emittance and relative momentum spread before and after 8 s e-cooling at the intermediate (35 MeV/c) plateau of the ELENA cycle. The rms values and values based on the enclosed particles within 68% and 95% of the antiproton distribution are shown for simulations using different algorithms of IBS.

Beginning first cooling plateau	
ϵ_x / ϵ_y (rms) [π mm mrad]	8.4 / 8.23
σ_p/p (rms)	0.56×10^{-3}
ϵ_x / ϵ_y (68%) [π mm mrad]	14.09 / 13.67
σ_p/p (68%)	0.56×10^{-3}
ϵ_x / ϵ_y (95%) [π mm mrad]	71.21 / 69.82
σ_p/p (95%)	1.1×10^{-3}
After 8 s e-cooling + Standard IBS	
ϵ_x / ϵ_y (rms) [π mm mrad]	3.28 / 3.2
σ_p/p (rms)	0.25×10^{-3}
ϵ_x / ϵ_y (68%) [π mm mrad]	0.08 / 0.076
σ_p/p (68%)	9.92×10^{-5}
ϵ_x / ϵ_y (95%) [π mm mrad]	43.72 / 42.57
σ_p/p (95%)	0.67×10^{-3}
After 8 s e-cooling + Kinetic IBS	
ϵ_x / ϵ_y (rms) [π mm mrad]	3.29 / 3.28
σ_p/p (rms)	0.24×10^{-3}
ϵ_x / ϵ_y (68%) [π mm mrad]	0.12 / 0.57
σ_p/p (68%)	8.73×10^{-5}
ϵ_x / ϵ_y (95%) [π mm mrad]	44.64 / 42.44
σ_p/p (95%)	0.64×10^{-3}
After 8 s e-cooling + Local IBS	
ϵ_x / ϵ_y (rms) [π mm mrad]	3.45 / 3.4
σ_p/p (rms)	0.39×10^{-3}
ϵ_x / ϵ_y (68%) [π mm mrad]	1.55 / 1.34
σ_p/p (68%)	0.34×10^{-3}
ϵ_x / ϵ_y (95%) [π mm mrad]	46.3 / 43.83
σ_p/p (95%)	0.73×10^{-3}

295 Moreover, in Fig. 11 the momentum spread profile presents an interesting
296 asymmetry. It presents a longer tail for positive $\Delta p/p$ values, likely caused by
297 a slight acceleration of antiprotons in the tails due to e-beam (from the cooler)
298 space charge effects. This point requires further investigation.

299 5. Conclusions and prospects

300 The AD-ELENA complex at CERN will provide cooled, high quality beams
301 of 100 keV kinetic energy antiprotons at intensities exceeding those achieved
302 presently at the AD by a factor of ten to one hundred. This will improve by
303 the same factor the efficiency of antihydrogen production, opening the door to
304 unique antimatter experiments.

305 In order to design and optimise such machines it is important to accurately
306 simulate the beam evolution performance. It will allow us to predict the quality
307 of the beam and its evolution at the different stages of the machine cycle. The
308 main limiting effect during the beam cooling process is IBS. Therefore it is nec-
309 essary to understand and simulate precisely how it affects the beam parameters
310 for realistic beam distributions.

311 Using the reference of beam profile measurements in the AD we have gener-
312 ated input macroparticle distributions for beam tracking simulation studies of
313 ELENA. For these simulations initial beam bi-Gaussian (core-tail) \bar{p} transverse
314 distributions have been considered as an input for the electron cooling simu-
315 lation of coasting beams using the code BETACOOOL. Although replacing the
316 real profile by a bi-Gaussian distribution is a simplification, it constitutes an
317 important improvement compared to a simple Gaussian approximation to get a
318 better understanding of the influence of a halo in the initial contribution.

319 Three different IBS models have been compared during the cooling process
320 for the first cooling plateau of the ELENA cycle: the so-called (standard) Mar-
321 tini model [5], the simplified kinetic model [29] and a local model [30].

322 It has clearly been shown that the cooling simulation results depend strongly
323 on the IBS model applied. Therefore, it is very important to select an adequate

324 model depending on the accuracy level required for the beam evolution pre-
325 dictions. In a cooling process, where the beam can deviate quickly from the
326 Gaussian profile, the use of a shape-independent model is appropriate. For in-
327 stance, the use of a local model, although very demanding in terms of computing
328 time, is useful to avoid unphysical results, such as beam core overcooling.

329 We are planning to complete this study performing a start-to-end simulation
330 for the whole ELENA cycle. This will include realistic assumptions of initial
331 particle distributions, based on real measurements, and also using beam-shape
332 IBS independent models. Of course, following the usual procedure for these
333 kind of studies, the validation of any computation model will be determined
334 by comparison with measurements during the commissioning phase and future
335 operation of the machine.

336 It is also important to mention that whilst done for the ELENA case, the
337 conclusions from this paper are also well suited for other future low energy
338 antiproton and ion machines, for example the Ultra-low energy Storage Ring
339 (USR) [35] in the context of the future Facility for Low-energy Antiproton and
340 Ion Research (FLAIR) at GSI [36].

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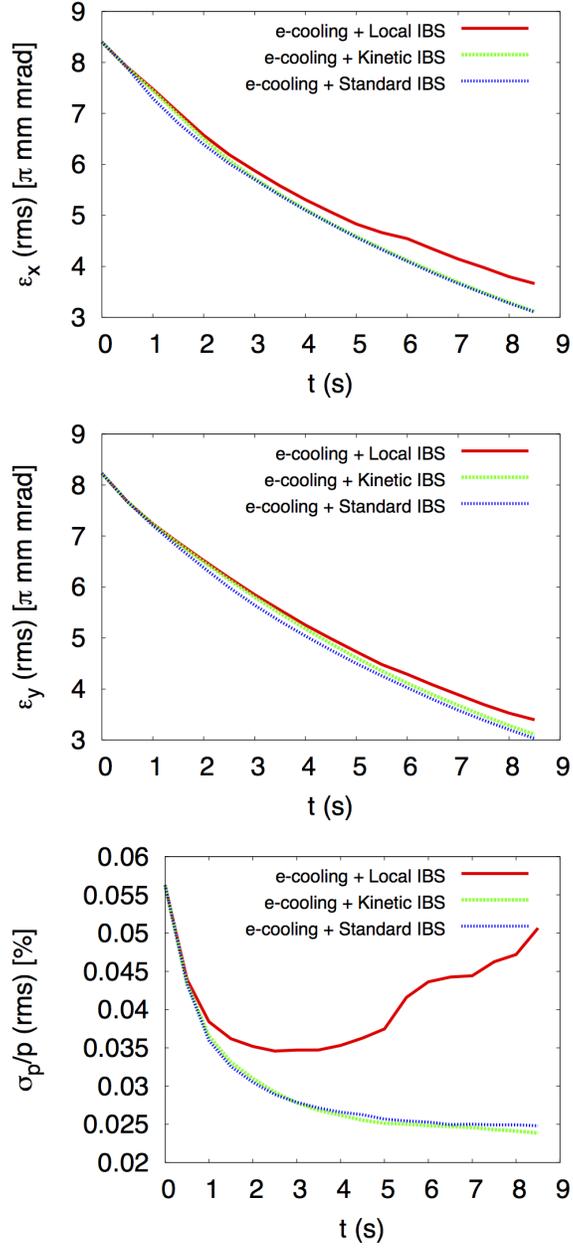


Figure 8: Beam parameter time evolution over the e-cooling process at 35 MeV/ c momentum: rms horizontal (top) and vertical (middle) rms emittances, and relative rms momentum spread (bottom). The action of different IBS models is compared.

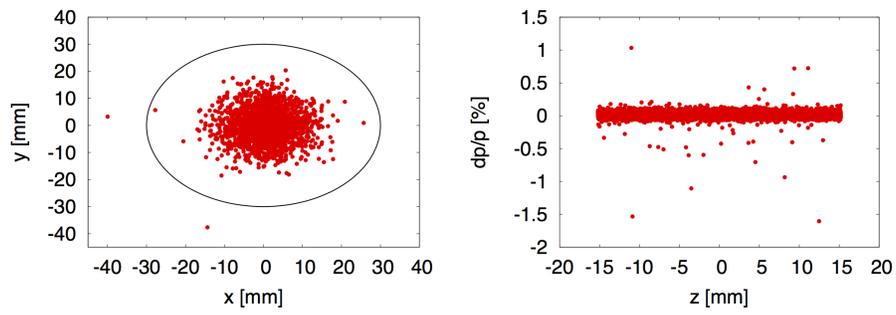


Figure 9: Transverse (left) and longitudinal (right) particle distribution after 8 s cooling at 35 MeV/c momentum for the case e-cooling + local IBS. The solid black circle represents the effective physical transverse aperture of the beam pipe.

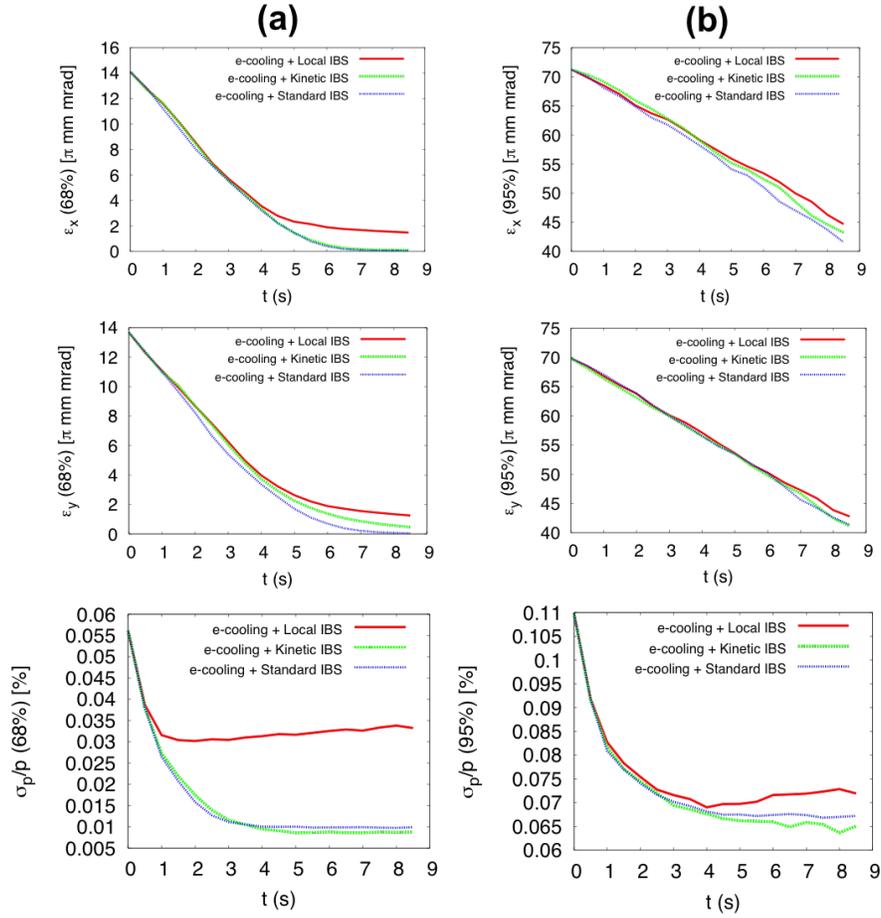


Figure 10: Transverse emittances and relative momentum spread for half beam widths containing 68% of the particles (a), and 95% of the particles (b).

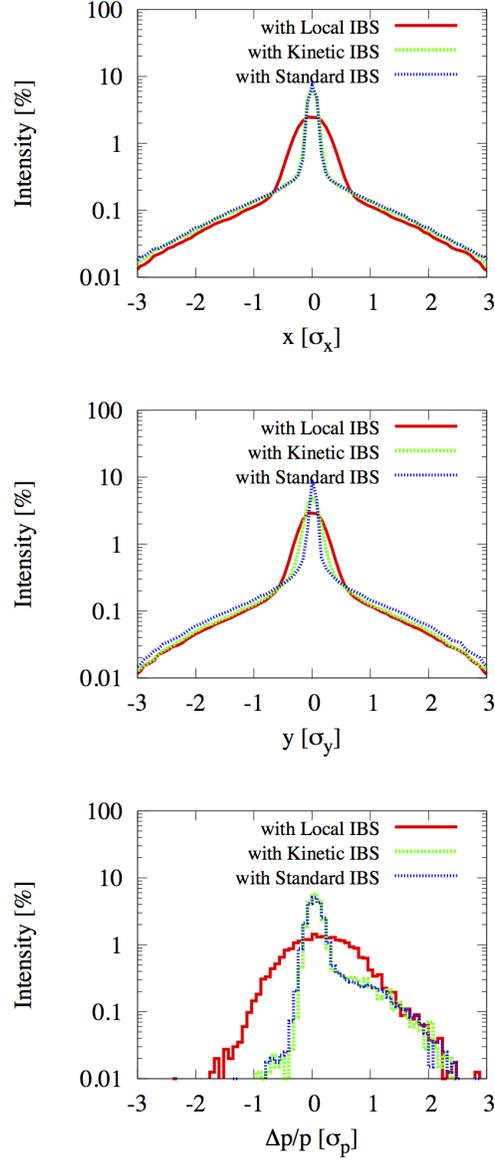


Figure 11: Horizontal (top), vertical (middle) and momentum spread (bottom) distributions after 8 s cooling at 35 MeV/c momentum, comparing the performance under the action of different IBS models. The horizontal axis is written in units of initial rms widths. The intensity is normalised over the corresponding initial rms parameter and the total number of macroparticles.