

# Ultrafast laser parallel micro drilling using multiple annular beams generated by a spatial light modulator

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## Abstract

Ultrafast laser parallel micro drilling using diffractive multiple annular beam patterns is demonstrated in this paper. The annular beam was generated by diffractive axicon computer generated holograms (CGHs) using a spatial light modulator (SLM). The diameter of the annular beam can be easily adjusted by varying the radius of the smallest ring in the axicon. Multiple annular beams with arbitrary arrangement and multiple annular beam arrays were generated by superimposing an axicon CGH onto a Grating and Lenses (GL) algorithm calculated multi-beam CGH and a binary Dammann grating CGH, respectively. Micro holes were drilled through a 0.03mm thick stainless steel foil using the multiple annular beams. By avoiding huge laser output attenuation and mechanical annular scanning, the processing is ~ 200 times faster than the normal single beam processing.

## Keywords

Ultrafast laser, Spatial light modulator, Computer generated holograms, Annular beam, Micro drilling

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## 1. Introduction

Ultrafast lasers have been widely used for high precision micro-fabrication. The unwanted thermal defects can be avoided due to the ultrashort timescale in which energy is coupled to the electronic system [1 - 3]. When the input processing fluence,  $F$ , is kept in the low regime, heat diffusion during the temporal ultrashort pulse duration can be reduced to the nanometer scale [4 - 6]. In order to ensure this 'thermal free' processing, huge output attenuation that keeps the fluence sufficiently low is always required [7]. This severely limits the useful throughput.

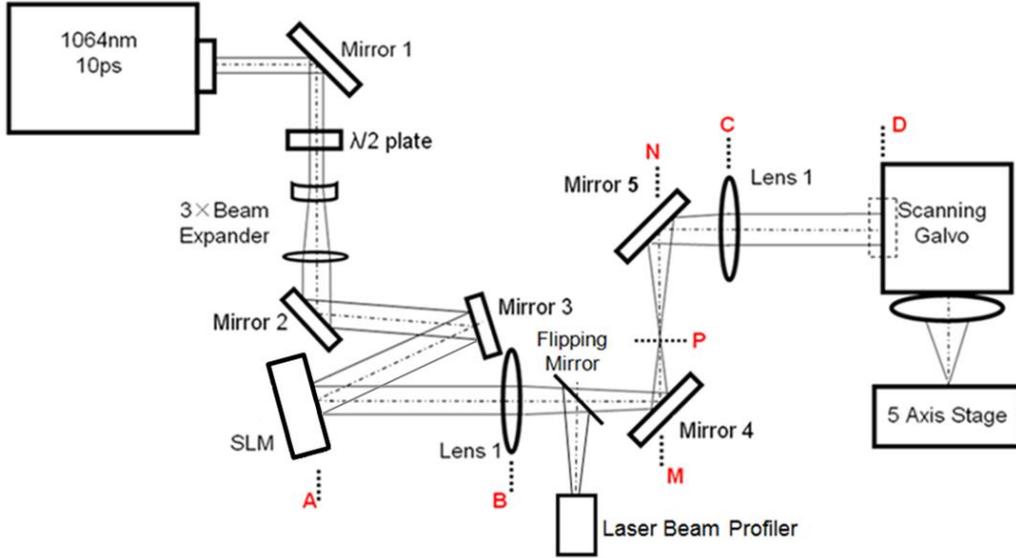
Parallel processing using diffractive multiple beams generated by a spatial light modulator (SLM) is a novel method to increase the throughput and efficiency of ultrafast laser fabrication [8 - 11]. Applications ranging from surface thin film patterning of transparent conducting oxides (TCOs) [12] and internal 3D refractive index modification of poly (methyl methacrylate) (PMMA) [13, 14] have been recently reported with the parallel processing technology. However, in this previous research, the shape of the multiple beams was unmodified, remaining circular. The use of other interesting beam shape can make some specific laser micro fabrication more flexible. For example, the generation of different sized annular beams can be used to obtain optical trepanning drilling, which is more efficient than the traditional mechanical trepanning drilling [15 - 17].

In this paper, ultrafast laser parallel micro drilling using diffractive multiple annular beam patterns is demonstrated. The annular beam was generated by diffractive axicon computer generated holograms (CGHs) using a spatial light modulator (SLM). The diameter of the annular beam can be easily adjusted by varying the radius of the smallest ring in the axicon. Multiple annular beams with

arbitrary arrangement and multiple annular beam arrays were generated by superimposing an axicon CGH onto a Grating and Lenses (GL) algorithm calculated multi-beam CGH and a binary Damman grating CGH, respectively. Micro holes were drilled through a 0.03mm thick stainless steel foil using the multiple annular beams. By avoiding huge laser output attenuation and mechanical annular scanning, the processing is  $\sim 200$  times faster than the normal single beam processing.

## 2. Experimental and methodology

### 2.1 Experimental



**Figure 1.** Experimental Setup

The ultrafast laser system used for this research was a custom made Nd: VAN seeded regenerative amplifier laser system (High-Q IC-355-800ps, Photonic Solutions). Schematic of the experimental setup is shown in figure 1. The laser output ( $t_p = 10$  ps,  $\lambda = 1064$  nm,  $R = 5$  kHz) passed through a half wave plate used for adjusting the linear polarization direction, a beam expander ( $M \approx \times 3$ ), and after reflection on mirrors 1, 2 and 3, illuminated a reflective phase only SLM, a Hamamatsu X10468-03 liquid crystal on silicon (LCoS) device with  $800 \times 600$  pixels and dielectric coating for 1064 nm wavelength (reflectivity  $\eta > 95\%$ ), oriented at  $< 10$  degree angle of incidence. A flipping mirror, placed after lens 1, reflected the beam to a charge-coupled device (CCD) camera-based laser profiler (Spiricon) to observe the reconstructed annular beam patterns when it was flipped into beam line. A 4f-optical system was formed from A to D to remove the unwanted 0-th order beam [11]. The beam then entered a scanning galvanometer with  $f = 100$  mm flat field f-theta lens (Nutfield) producing an agile focusing system. Substrates were mounted on a precision 5-axis (x, y, z, p, q) motion control system (Aerotech) allowing accurate positioning of the substrate surface at the laser focus. The spectral bandwidth,  $\Delta\lambda < 0.3$  nm, was relatively narrow and important in eliminating chromatic dispersion of the SLM [11, 18].

### 2.2 Methodology

#### 2.2.1 The generation of single annular focus

Diffraction axicon computer generated holograms (CGH), also described as circular blazed gratings, were used to create annular beams. As shown in figure 2, the radius of the smallest ring in the axicon

is equal to the spatial period of the blazed grating,  $d$ . The blazed grating creates a +1 order beam with a diffraction angle of  $\beta$ , while the axicon generates a diffractive +1 order conical wave. According to the grating equation below,

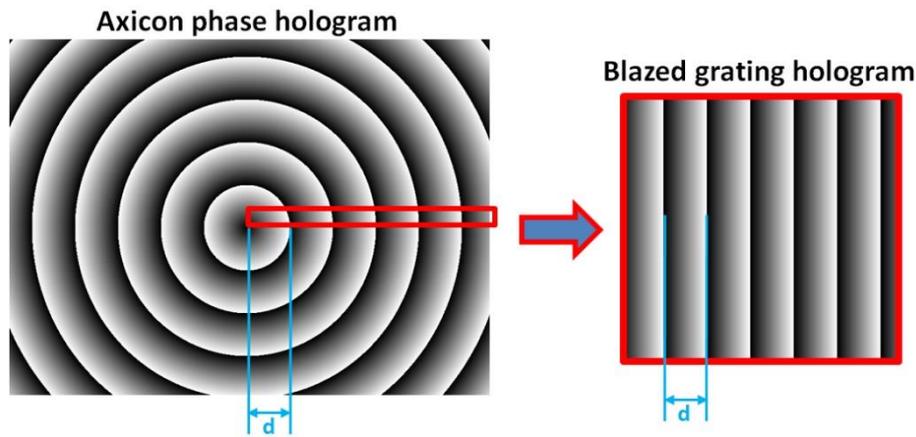
$$d (\sin\alpha + \sin\beta) = m\lambda \quad (1)$$

where  $d$  is the grating period or the radius of smallest ring in the axicon phase,  $\alpha$  is the input beam incidence angle,  $m$  is the diffraction order and  $\lambda$  is the input beam wavelength, the +1 order diffraction angle:

$$\beta \approx \sin\beta = (\lambda/d) - \sin\alpha \quad (2)$$

In our experimental setup,  $\sin\alpha \approx 0.17$  ( $\alpha \approx 10$  degree) is very small and can be neglected. So,

$$\beta \approx (\lambda/d) \quad (3)$$



**Figure 2.** Diffractive axicon CGH (left) and blazed grating CGH (right)

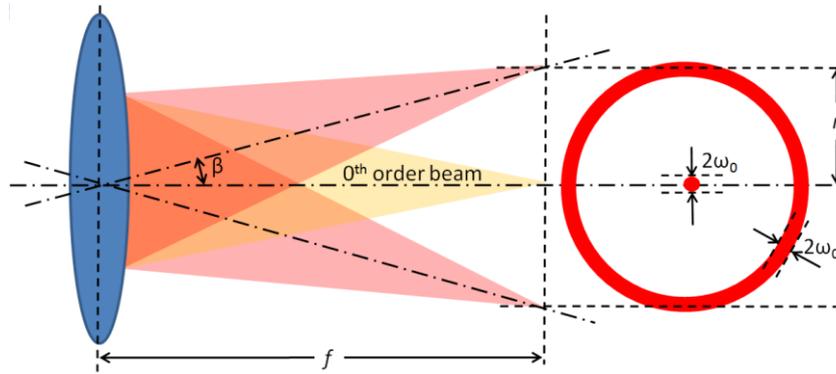
When the diffracted conical wave is focused by the  $f$ -theta lens ( $f = 100\text{mm}$ ), an annular focus is created at the focal plane. As shown in figure 3, the diameter ( $D$ ) of the annular focus can be calculated by:

$$D = 2r = 2f \tan\beta \approx 2f\beta \approx 2f\lambda/d \quad (4)$$

Since the width of the annular focus is comparable to the 0<sup>th</sup> order beam waist ( $2\omega_0$ ), the area of the annular ( $S$ ) focus can be calculated by:

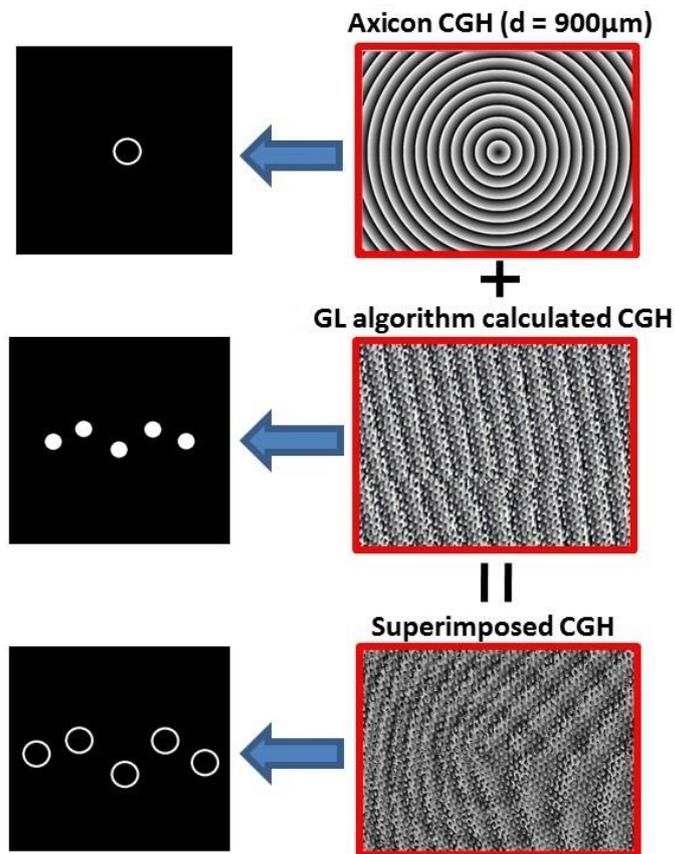
$$S \approx 2\omega_0 c = 2\omega_0 \pi D = 4\omega_0 \pi f \lambda/d \quad (5)$$

where  $c$  is the circumference of the annular focus.



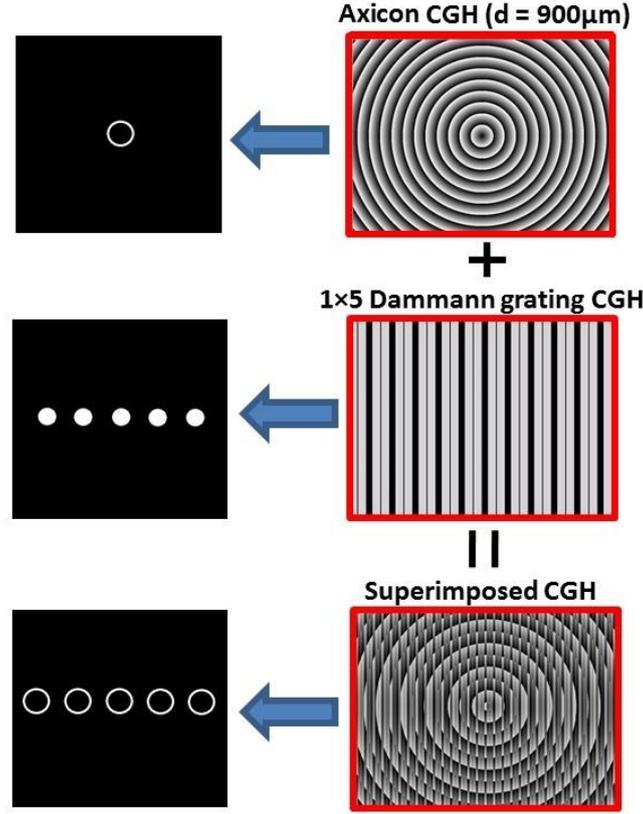
**Figure 3.** Annular focus created at the focal plane of the f-theta lens

### 2.2.2 The generation of multiple annular focuses



**Figure 4(a).** Multiple annular beams with arbitrary arrangement generated by the superimposing an axicon CGH onto a GL algorithm calculated CGH – right column: CGHs, left column: reconstructions

Multiple annular beams with arbitrary arrangement were generated by superimposing an axicon CGH onto a multi-beam CGH calculated by the Grating and Lenses (GL) algorithm [19, 20], as shown in figure 4(a). The GL algorithm has been previously used to calculate CGHs which produced arbitrary multiple diffractive beams for ultrafast laser processing [10 - 12, 18].



**Figure 4(b).** 1×5 annular beam array created by superimposing the axicon CGH onto a 1×5 Dammann grating CGH - right column: CGHs, left column: reconstructions

When using GL algorithm, periodic and symmetrical geometry designs (e.g. N×M beam array) of the multi-beam pattern must be avoided to ensure a good uniformity [12, 21, 23]. Therefore, to create a highly symmetrical annular multiple beam array, Dammann grating [22] CGHs can be used instead of the CGHs calculated by GL algorithm [23]. As shown in figure 4(b), a 1×5 annular beam array can be created by superimposing the axicon CGH onto a 1×5 Dammann grating CGH.

### 2.2.3 The calculation of processing fluence

During experiments, pulse energies ( $E_p$ ) were directly measured by an energy meter. Peak fluences ( $F$ ) can be calculated by

$$F = 2 E_p / S \quad (6)$$

where  $S$  is the area of the focus. When processing with a single circular Gaussian beam, the fluence is:

$$F = 2 E_p / (\pi \omega_0^2) \quad (7)$$

where  $\omega_0$  is the radius of the Gaussian beam waist. In this case,  $\omega_0 \approx 11.9\mu\text{m}$  has been calculated by:

$$2\omega_0 = 4 \lambda f M^2 / (\pi \Phi) \quad (8)$$

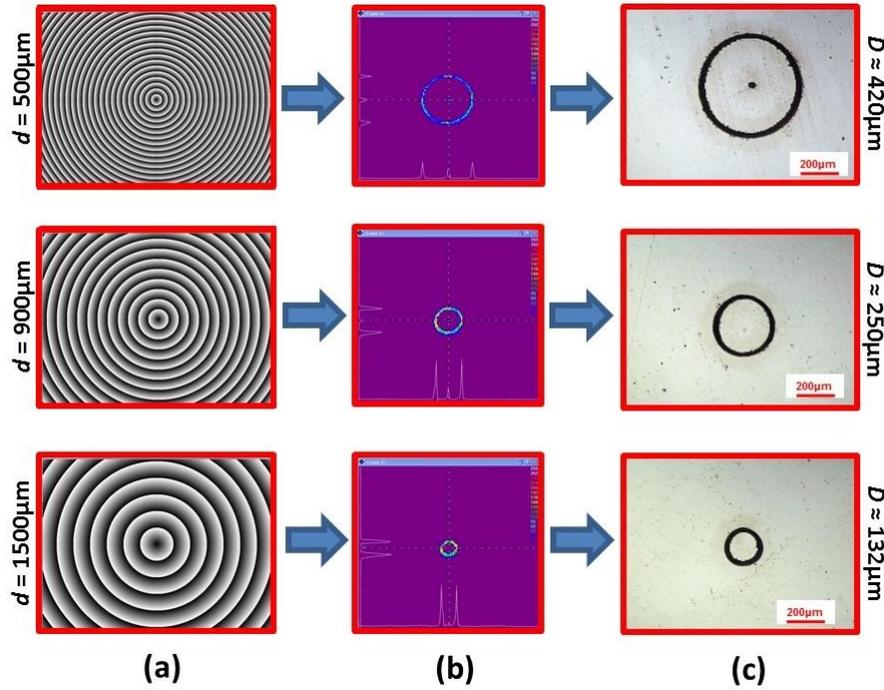
where  $f = 100\text{mm}$  is the focal length of the f-theta lens,  $\Phi = 6.3\text{mm}$  is the diameter of expanded laser beam and  $M^2 = 1.1$  is the beam quality factor. From equation (5) and (6), when processing with single or multiple annular beams, the fluence is:

$$F = E_p d / (2n\omega_0 \pi f \lambda) \quad (9)$$

where  $n$  is the number of annular focuses.

### 3. Results and discussions

#### 3.1 Processing with single annular beam

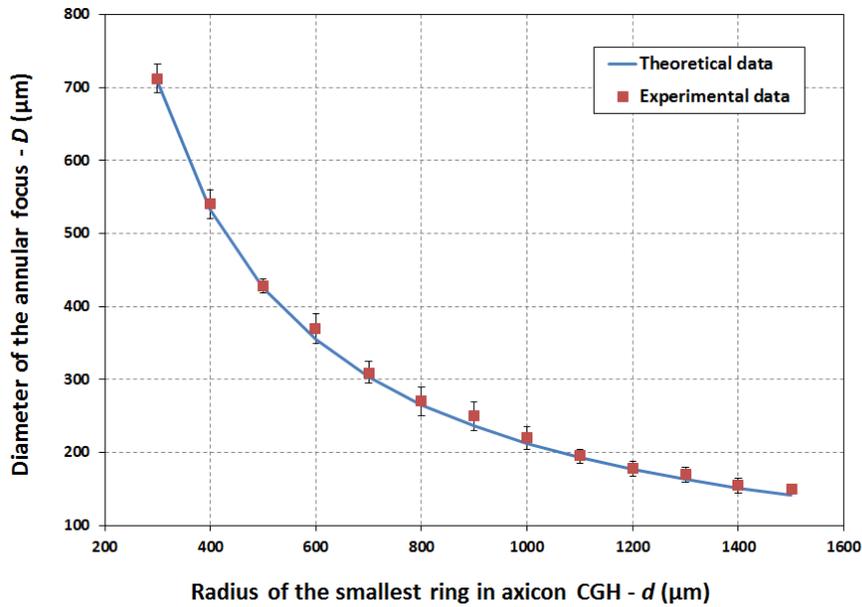


**Figure 5.** Single annular beam processing – column (a): diffractive axicon CGHs with different radius of smallest ring,  $d$ ; column (b): annular beams observed by the Spiricon beam profiler; column (c): optical micrographs showing the annular ablation footprints on a stainless steel sample

Surface ablation of a stainless steel sample using different sized annular beams created by diffractive axicon CGHs is demonstrated in figure 5. The laser intensity distributions measured by the Spiricon beam profiler are presented in column (b). As demonstrated, the irradiance is confined only in the central dot ( $0^{\text{th}}$  order) and the surrounding ring as depicted in figure 3. Each ablation annular footprint shown in the column (c) was fabricated by 1000 pulses at fluence  $F \approx 0.3\text{J}/\text{cm}^2$  (approximate  $1.5\times$  ablation threshold). As shown, a small circular hole machined by the undiffracted  $0^{\text{th}}$  order beam was found in the centre of the  $D \approx 420\mu\text{m}$  annular footprint, but no such holes were observed when  $D \approx 250\mu\text{m}$  and  $132\mu\text{m}$ . This is because higher pulse energy ( $E_p$ ) was applied to reach the fluence level ( $F \approx 0.3\text{J}/\text{cm}^2$ ) when  $D$  is larger (i.e.  $S$  is larger) and the corresponding  $0^{\text{th}}$  order is hence stronger. In this case, for  $D \approx 420\mu\text{m}$ ,  $250\mu\text{m}$  and  $152\mu\text{m}$  annular beam, the total input  $E_p$  were  $\approx 48\mu\text{J}$ ,  $28\mu\text{J}$  and  $15\mu\text{J}$  and the  $0^{\text{th}}$  order energy were measured to be  $\approx 0.5\mu\text{J}$ ,  $0.3\mu\text{J}$  and  $0.15\mu\text{J}$ , respectively. Using equation (7), the corresponding fluence of the  $0^{\text{th}}$  orders are  $0.22\text{J}/\text{cm}^2$ ,  $0.13\text{J}/\text{cm}^2$  and  $0.07\text{J}/\text{cm}^2$ . Only the  $0^{\text{th}}$  order in  $D \approx 420\mu\text{m}$  annular beam has the fluence higher than the sample's ablation threshold that was measured to be  $\approx 0.2\text{J}/\text{cm}^2$ .

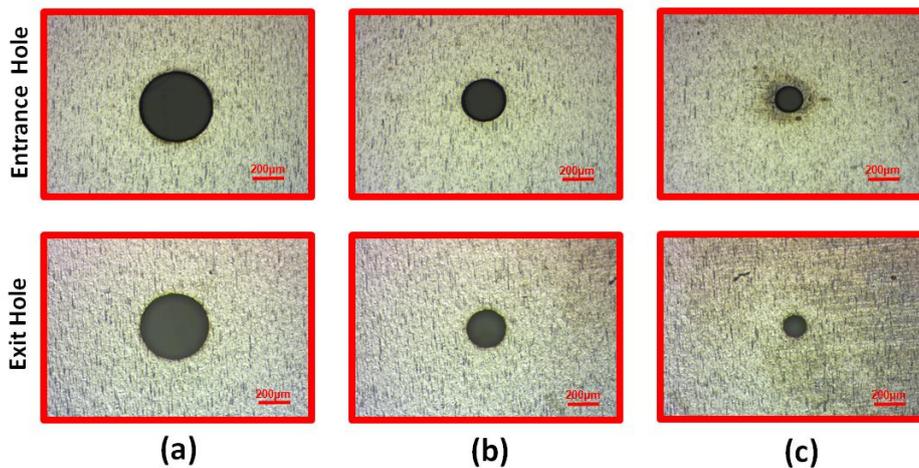
A graph showing the diameter of the annular beam ( $D$ ) against the radius of the smallest ring in the axicon CGH ( $d$ ) is demonstrated in figure 6. As shown, the experimental data acquired from

measuring the annular ablation footprint on the stainless steel sample perfectly matches the theoretical data calculated using equation (4). This indicates an excellent accuracy of the theoretical derivation in 2.2.



**Figure 6.** Diameter of the annular focus versus radius of the smallest ring in axicon CGH

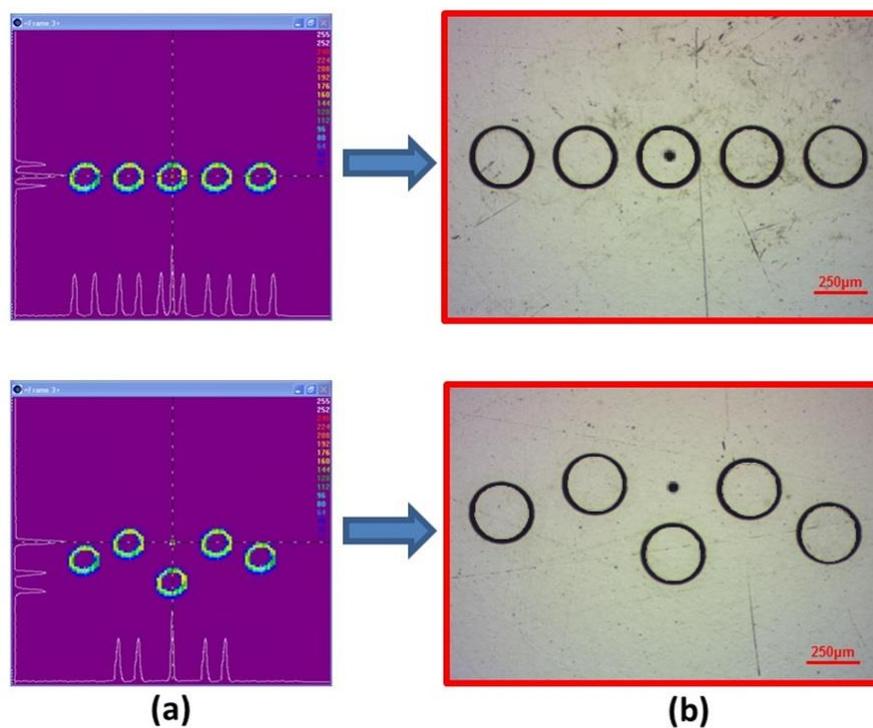
The annular beams were used to drill holes with different diameters through a 0.03mm thick stainless steel foil, known as optical trepanning drilling [14, 15]. The laser beam was focused on the upper surface of the stainless steel foil. Since the thickness of the stainless steel foil ( $\sim 30\mu\text{m}$ ) is comparable to the depth of focus of the f-theta lens, there is no need to adjust the focal position when the laser is drilling through the foil. No processing gases were used during the experiment. As shown in figure 7, the drilled holes with different size are demonstrated in column (a), (b) and (c), generated by annular beams using diffractive axicon CGHs with  $d = 500\mu\text{m}$ ,  $900\mu\text{m}$  and  $1500\mu\text{m}$ , respectively. 5000 pulses at a fluence of  $F \approx 0.3\text{J}/\text{cm}^2$  were applied to drill through the foil sample. The entrance hole diameters are  $\approx 426\mu\text{m}$ ,  $255\mu\text{m}$ , and  $160\mu\text{m}$ , while the exit hole diameters are  $\approx 420\mu\text{m}$ ,  $250\mu\text{m}$ , and  $153\mu\text{m}$ . The darker area that appears around the entrance hole (c column) is not a heat-affected zone. It was formed by micro/nano sized particles generated during the processing and can be easily cleaned up by ultrasonic cleaning.



**Figure 7.** Optical micrographs showing the annular beam drilled holes through a stainless steel foil

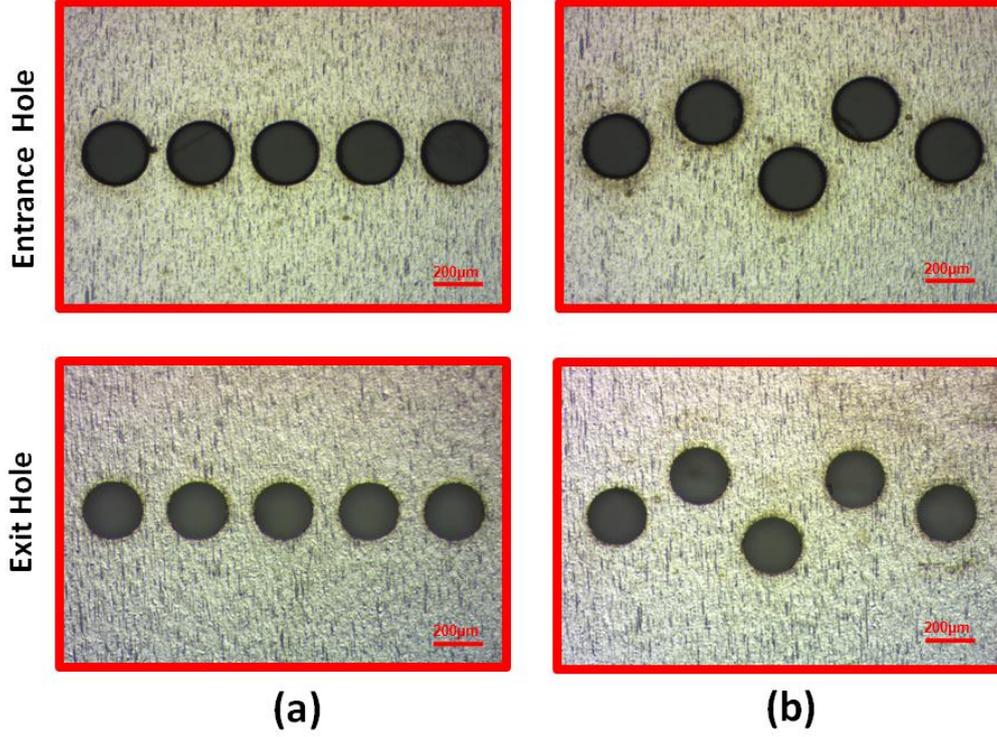
### 3.2 Processing with multiple annular beam patterns

Multiple(five) annular beam patterns with excellent uniformity were generated using the superimposed CGHs which has been discussed in 2.2.2. As shown in figure 8, pattern profiles observed by the laser profiler (Spiricon) are shown in column (a), while optical micrographs showing surface ablation footprints on a stainless steel sample are demonstrated in column (b). The footprints were fabricated by 1000 pulses at fluence ( $F$ )  $\approx 0.3\text{J}/\text{cm}^2$ , calculated using equation (9). Since five annular beams ( $D \approx 250\mu\text{m}$ ) were generated simultaneously, the focal area ( $S$ ) and the pulse energy ( $E_p$ ) required to reach the fluence level are five times larger than the single annular beam. In this case, the measured total input  $E_p$  was  $\approx 150\mu\text{J}$ , where huge attenuation of the laser output was avoided. As shown in column (b), a small unwanted micro hole corresponding to the 0th order is present. There are two methods to prevent the 0th ordering from damaging the sample. One is to physically block the 0th order at the Fourier plane of the 4f optical system using a small target [11], and the other is to defocus the 0th order at the processing plane by adding a Fresnel phase onto the CGH[18].



**Figure 8.** Multiple(five) annular beam patterns generated using the superimposed CGHs - column (a): pattern profiles observed by the laser profiler (Spiricon); column (b): optical micrographs showing surface ablation footprints on a stainless steel sample

The multiple annular beam patterns were used to drill holes through a 0.03mm thick stainless steel foil. The optical micrographs in figure 9 demonstrate the entrance and the exit holes. For the  $1 \times 5$  ring array pattern (fig.9, column (a)), the entrance and the exit hole diameters are:  $262.0 \pm 7.0\mu\text{m}$ ,  $247.0 \pm 6.0\mu\text{m}$ , respectively. For the random 5 rings pattern (fig.9, column (b)), the entrance and the exit hole diameters are:  $268.0 \pm 11.0\mu\text{m}$ ,  $248.0 \pm 9.0\mu\text{m}$ , respectively. 0th order was blocked at the Fourier plane of the 4f optical system to avoid unwanted damages on the sample. 5000 pulses at a fluence of  $\approx 0.3\text{J}/\text{cm}^2$  were applied to drill through the foil sample. As demonstrated, with efficient usage of the laser output, the drilling process was completed within 1s. This is approximate 200 times faster than the normal single circular beam processing which requires huge laser output attenuation and complicated mechanical scanning, as shown in table 1.



**Figure 9.** Optical micrographs showing the entrance and the exit holes of a stainless steel foil sample drilled by multiple (five) annular beam patterns

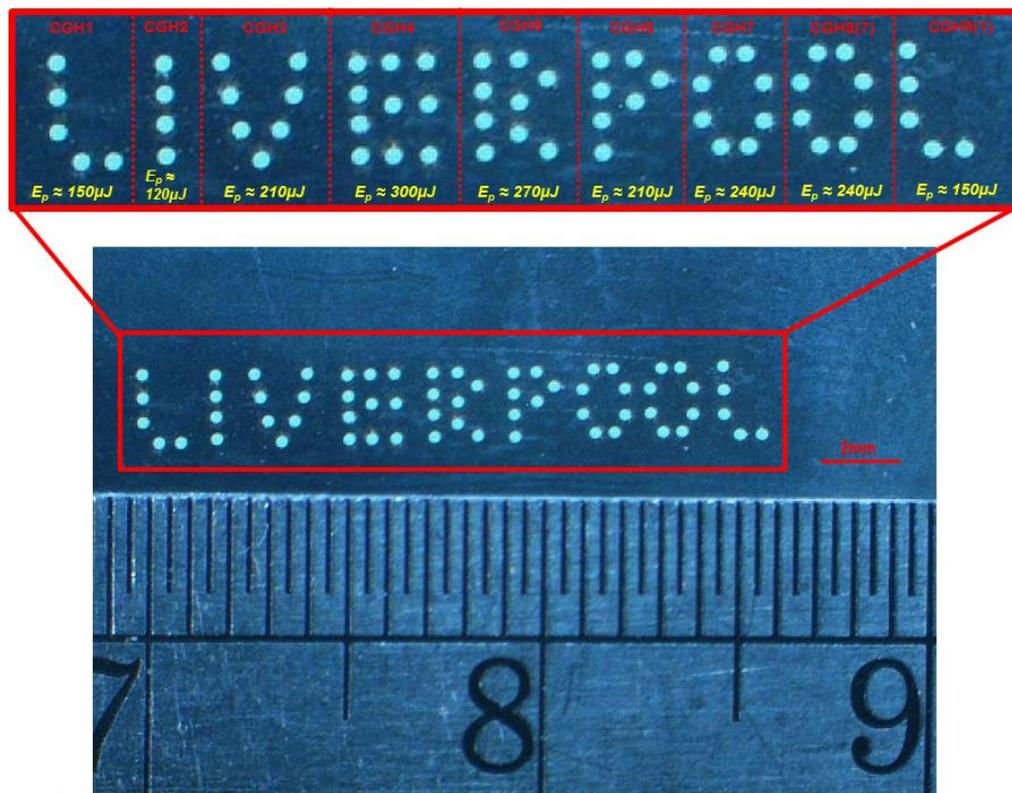
**Table 1.** Comparison of drilling five holes through a 0.03mm thick stainless steel foil between single circular beam mechanical trepanning<sup>a</sup> and five annular beam pattern optical trepanning

	Single circular beam	five annular beam
Area of focus - $S$ ( $\mu\text{m}^2$ )	$\sim 445$ <sup>b</sup>	$\sim 88350$ <sup>c</sup>
Pulse energy - $E_p$ ( $\mu\text{J}$ )	$\sim 0.7$	$\sim 150$
Peak fluence - $F$ ( $\text{J}/\text{cm}^2$ )	$\sim 0.3$	$\sim 0.3$
Ent. hole diameter - $D_{\text{ent}}$ ( $\mu\text{m}$ )	$264.0 \pm 5.0$	$262.0 \pm 7.0$ (array pattern) $268.0 \pm 11.0$ (random pattern)
Exi. hole diameter - $D_{\text{exi}}$ ( $\mu\text{m}$ )	$246.0 \pm 4.0$	$247.0 \pm 6.0$ (array pattern) $248.0 \pm 9.0$ (random pattern)
Drill time - $t$ (s)	$\sim 200$	$\sim 1$

- The circular beam was mechanically scanned around a circle (dia.  $\approx 250\mu\text{m}$ ) by the scanning galvanometer at a speed of  $v = 2\text{mm/s}$  and 100 times overscan to drill through the sample
- Calculated by  $S = \pi \omega_0^2$ , where  $\omega_0 \approx 11.9\mu\text{m}$  is the radius of the beam waist
- Calculated by equation (5) multiplied by  $n = 5$ , i.e:  $S \approx 4 n \omega_0 \pi f \lambda / d = 20 \omega_0 \pi f \lambda / d$ , where  $d = 900\mu\text{m}$

By combining real time control of the CGHs with scanning, the processing has significant potential to produce complicated arbitrary micro-drilling patterns. Figure 10 shows a micro-drilling result of a ‘Liverpool’ pattern, which comprises 63 holes drilled through a 0.03mm thick stainless steel foil with entrance diameter  $\approx 264.0 \pm 10.0\mu\text{m}$  and exit diameter  $\approx 245.0 \pm 9.0\mu\text{m}$ . The pattern was generated by applying 9 CGHs in turn, each of which generated multiple annular beams and formed one letter. The scanning galvanometer scanned the beam to a correct position when switching the CGH. During the processing, each CGH was given 1 second dwelling time, allowing 5000 pulses applied to drill through the sample. Since different CGH created different number of annular beams, the applied pulse energy  $E_p$  varied when changing the CGH to ensure a constant fluence ( $F \approx 0.3\text{J}/\text{cm}^2$ ), as shown in figure 10. We are still trying to complete the whole pattern by playing the CGHs in real time,

synchronized with the scanning galvanometer positioning and the pulse energy adjustment. If the synchronization is achieved, the whole pattern should be completed in about 9 seconds.



**Figure 10.** 'Liverpool' pattern generated by applying 9 CGHs in turn

#### 4. Conclusions

Ultrafast laser parallel micro drilling using diffractive multiple annular beam patterns is demonstrated in this paper. The annular beam was generated by diffractive axicon computer generate holograms (CGHs) using a spatial light modulator (SLM). The diameter of the annular beam can be easily adjusted by varying the radius of the smallest ring in the axicon. Multiple annular beams with arbitrary arrangement and multiple annular beam arrays were generated by superimposing an axicon CGH onto a Grating and Lenses (GL) algorithm calculated multi-beam CGH and a binary Dammann grating CGH, respectively. Micro holes were drilled through a 0.03mm thick stainless steel foil using the multiple annular beams. By avoiding huge laser output attenuation and mechanical annular scanning, the processing is  $\sim 200$  times faster than the normal single beam processing.

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