

1 **Integration of Scheimpflug-based Corneal Tomographic and Biomechanical**
2 **Assessments for Enhancing Ectasia Detection**

3 Renato Ambrósio Jr, MD, PhD^{1,2,3}; Bernardo Lopes, MD^{1,2}; Fernando Faria-Correia,
4 MD^{1,4}; Marcella Q. Salomão, MD^{1,2}; Jens Bühren, MD⁵; Cynthia J. Roberts, PhD⁶;
5 Ahmed Elsheikh, PhD⁷; Riccardo Vinciguerra, MD^{8,9}; Paolo Vinciguerra, MD^{10,11}

6

7 1. Rio de Janeiro Corneal Tomography and Biomechanics Study Group; Rio de Janeiro,
8 Brazil

9 2. Department of Ophthalmology, Federal University of São Paulo; São Paulo, Brazil

10 3. Department of Ophthalmology, Pontific Catholic University of Rio de Janeiro; Rio de
11 Janeiro, Brazil

12 4. School of Health Sciences, University of Minho, Braga, Portugal

13 5. Augenpraxisklinik Triangulum; Hanau, Germany

14 6. Department of Ophthalmology & Visual Science, and Department of Biomedical
15 Engineering, The Ohio State University; Columbus, OH, USA

16 7. School of Engineering, University of Liverpool – Liverpool, United Kingdom

17 8. Department of Surgical Sciences, Division of Ophthalmology, University of Insubria;
18 Varese, Italy

19 9. Department of Corneal and External Eye Diseases, St. Paul's Eye Unit, Royal Liverpool
20 University Hospital, Liverpool, United Kingdom

21 10. Eye Center, Humanitas Clinical and Research Center, Via Manzoni 56, Rozzano (MI);
22 Italy

23 11. Vincieye Clinic; Milan, Italy

24

25 **Corresponding author:** Renato Ambrósio Jr, MD, PhD dr.renatoAmbrósio@gmail.com;

26 phone/fax +5521 2234-4233

27 Rua Conde de Bonfim 211/712 – Rio de Janeiro, RJ – 20.520-050, Brazil

28

29 **Financial Disclosure(s):** Dr. Ambrósio, Dr. P. Vinciguerra, and Dr. Roberts are consultants for
30 OCULUS Optikgeräte GmbH (Wetzlar, Germany). Dr. Bühren has received lecture fees from
31 OCULUS; Dr. Elsheikh has received research funding from OCULUS Optikgeräte GmbH. “None
32 of the remaining authors have any financial disclosures”

33

34 **Running head:** Tomographic/Biomechanical Index (TBI) for Ectasia detection

35

36 **PRECIS**

37 In a multicenter study, the TBI was developed using random forest method with leave-one-out
38 cross-validation (RF/LOOCV) for combining parameters from Scheimpflug-based corneal
39 tomography and biomechanical assessments for enhanced ectasia detection.

40 **Acknowledgments**

41 The authors thank Dr. Sven Reisdorf, PhD and Dr. Andreas Steinmuller, MSc (OCULUS) for the
42 overall support in processing the data along with the helpful discussions and calculations. The
43 Corvis ST instruments used in this study were provided by Oculus.

44

45 **ABSTRACT**

46 **Purpose:** To present the Tomographic/Biomechanical Index (TBI), that combines
47 Scheimpflug-based corneal tomography and biomechanics for enhancing ectasia
48 detection. **Methods:** Patients from different continents were studied. One eye randomly
49 selected from 480 patients with normal corneas and from 204 keratoconus patients
50 comprised groups I and II respectively. Group III included 72 non-operated ectatic eyes
51 from 94 patients with very asymmetric ectasia, whose fellow eyes (group IV) presented
52 with normal topography. Pentacam HR and Corvis ST (OCULUS; Wetzlar, Germany)
53 parameters were analyzed and combined using different artificial intelligence methods
54 (AI). The accuracies for detecting ectasia of BAD-D (Belin/Ambrósio Deviation) and CBI
55 (Corvis Biomechanical Index) were compared to TBI, considering the areas under
56 receiver operating characteristic curves (AUROC). **Results:** The random forest method
57 with leave-one-out cross-validation (RF/LOOCV) provided the best AI model. The
58 AUROC for detecting ectasia (groups II, III and IV) of TBI was 0.996, being statistically
59 higher (DeLong, $p < 0.001$) than BAD-D (0.956) and CBI (0.936). TBI cutoff value of 0.79
60 provided 100% sensitivity for detecting clinical ectasia (groups II and III) with 100%
61 specificity. Considering group IV, AUROC for TBI, BAD-D and CBI were 0.985, 0.839
62 and 0.822 (DeLong, $p < 0.001$). An optimized TBI cutoff value of 0.29 provided 90.4%
63 sensitivity in group IV, with 96% specificity. **Conclusion:** TBI generated by RF/LOOCV
64 provides accuracy for detecting ectasia, exceeding other techniques. TBI is sensitive for
65 detecting sub-clinical (fruste) ectasia among eyes with normal topography in very
66 asymmetric patients. TBI may also confirm unilateral disease, potentially epitomizing the
67 inherent ectasia susceptibility of the cornea.

68

69 INTRODUCTION

70 The detection of mild or sub-clinical forms of ectatic corneal diseases (ECD) has
71 gained momentous relevance because these cases are at very high risk for developing
72 iatrogenic progressive ectasia (keratectasia) after corneal Laser Vision Correction (LVC)
73 procedures.^{1,2} Ectasia progression after LVC occurs due to the biomechanical
74 decompensation of corneal stroma, which is related to two different factors: the
75 preoperative predisposition or biomechanical status of the cornea, and the structural
76 impact from the surgical procedure. The impact from the LVC procedure may be
77 evaluated using different parameters including the residual stromal bed (RSB) and the
78 percent of tissue altered (PTA).³⁻⁶ In fact, the current concept is that when screening for
79 ectasia risk among candidates for LVC, the surgeon should consider the inherent
80 ectasia susceptibility of the cornea, which goes beyond (not over) the detection of mild
81 cases with ECD.² Besides elective Refractive Surgery, augmenting sensitivity for
82 identifying mild forms of ectasia at early clinical stage and monitoring disease
83 progression have become of utmost importance because of the definitive paradigm shift
84 in the management of ECD, which is related to the introduction of novel therapeutic
85 approaches such as corneal crosslinking (CXL) techniques and intrastromal corneal ring
86 segments (ICRS) implantation.^{7,8}

87 The last three decades witnessed a factual revolution in corneal imaging, which
88 includes the development of high resolution technologies capable of detailed
89 characterizations of different aspects of corneal shape and anatomy, and the
90 introduction of scientifically validated methods for representing and interpreting the
91 generated data for improving the clinical decision process.⁹ Placido-disk based corneal

92 topography characterizes the anterior or front corneal surface in detail, which enables
93 the detection of abnormal patterns of corneal shape that accompany mild forms of
94 keratoconus in cases in which routine examination shows no abnormal findings.¹⁰ Such
95 augmentation of sensitivity to detect ectasia among eyes with normal slit-lamp
96 biomicroscopy and normal distance corrected visual acuity (DCVA) has positioned
97 corneal topography as a mandatory exam for screening ectasia risk prior to LVC.^{1,2,10}
98 However, there are still cases that undergo ectasia progression after LVC procedures,
99 even for low to mild corrections, despite relatively normal topography findings prior to
100 LASIK,¹¹⁻¹³ surface ablation,¹⁴ or SMILE (Small-Incision Lenticule Extraction).¹⁵

101 Front surface corneal analysis (topometric or topography) evolved into the three-
102 dimension (3D) tomographic characterization, which typifies elevation of the front and
103 back surfaces along with thickness mapping.¹⁶ Eyes with normal topometric findings
104 from patients with clinical ectasia detected in the fellow eye have been commonly
105 studied to demonstrate the improved ability of corneal tomography to detect ECD.¹⁷⁻¹⁹ In
106 addition, the ability of tomographic data to augment the ability to detect ectasia risk or
107 susceptibility in retrospective analysis of cases that developed keratectasia after
108 LASIK.^{12,20,21} Further advances on corneal imaging allowed for segmental or layered
109 tomographic (3D) characterization with epithelial,^{22,23} and Bowman's layer thickness
110 mapping.²⁴

111 Nevertheless, beyond shape analysis, clinical biomechanical assessment has
112 been considered as an ultimate tool for enhancing the overall accuracy for identifying
113 mild forms of ECD, along with the characterization of the inherent susceptibility of the
114 cornea for ectasia progression.^{12,21} In fact, there is a consensus that the

115 pathophysiology of corneal ectasia is related to altered biomechanical properties.⁸ In
116 addition, the current concept as proposed by Roberts and Dupps²⁵ is that a focal
117 abnormality in corneal biomechanical properties precipitates a cycle of decompensation,
118 leading to secondary localized thinning and steepening (bulging), which generates
119 optical aberrations.²⁵ The Reichert Ocular Response Analyzer (ORA), a non-contact
120 tonometer (NCT) that monitors corneal deformation through an infrared apical reflex,
121 was introduced as the first clinical tool for *in vivo* biomechanical assessment.²⁶ Even
122 though ORA first generation pressure-dependent parameters – corneal hysteresis (CH)
123 and corneal resistance factor (CRF) provided relatively low sensitivity and specificity for
124 discriminating keratoconic from normal corneas,²⁷ parameters derived from the corneal
125 deformation signal were characterized, providing higher accuracy.²⁸ Interestingly, such
126 data were found useful to improve diagnostic accuracy for mild forms of ECD when
127 combined with tomography data.^{21,29}

128 The Corvis ST (OCULUS Optikgeräte GmbH; Wetzlar, Germany) is also an NCT,
129 but utilizes an ultra-high speed (UHS) Scheimpflug camera to monitor the deformation
130 of the cornea in greater detail, with a collimated air pulse and fixed pressure profile.³⁰
131 While the first set of parameters derived from the Corvis ST measurement were found
132 to have a relatively poor discriminant ability to detect ectatic diseases,³¹⁻³³ novel
133 parameters such as the inverse concave radius of curvature during the concave phase
134 of the deformation response, the deformation amplitude ratio between the apex and at
135 2mm from the apex (DA Ratio 2mm) and the stiffness parameter at first applanation
136 (SPA1) were found to improve detection of ECD.^{34,35} As described by Vinciguerra and
137 coworkers,³⁶ the Corvis Biomechanical Index (CBI) was developed using linear

138 regression analysis (LRA) for combining parameters from the deformation corneal
139 response (DCR) and from the horizontal thickness profile,³⁷ leading to high accuracy to
140 detect clinical keratoconus.³⁶ Besides detection of ECD, the characterization of the
141 deformation response has also provided an equation for intraocular pressure (IOP)
142 correction, reducing reliance of IOP measurements on both corneal thickness and
143 age.³⁸ The purpose of the current study was to develop a combined parameter based
144 on Scheimpflug imaging to advance the ability to detect clinical and sub-clinical ectasia,
145 using corneal tomography data from the Pentacam (OCULUS Optikgeräte GmbH;
146 Wetzlar, Germany)¹⁸ and biomechanical assessment from the Corvis ST.

147

148 **Methods**

149 Eight hundred and fifty eyes from 778 patients were included in this multicenter
150 retrospective study. The patients were enrolled from two clinics located in two different
151 continents: *Instituto de Olhos Renato Ambrósio* in Rio de Janeiro (Brazil), and the
152 Vincieye Clinic in Milan (Italy). Institutional review board (IRB) from Humanitas Clinical
153 and Research Center (Milan, Italy) ruled that approval was not required for the
154 retrospective chart review study. The ethics committee of the Federal University of São
155 Paulo approved this retrospective research study, which was conducted in accordance
156 with the standards set in the 1964 Declaration of Helsinki, and revised in 2000. The
157 eyes were divided into four groups. Group I (N) included one eye randomly selected
158 from 480 patients with normal corneas. Group II (KC) was comprised of one eye
159 randomly selected from 204 keratoconus patients. One eye was randomly included per
160 patient in order to avoid selection bias related to the use of both eyes from the same
161 subject.³⁹ Seventy-two non-operated eyes with clinical ectasia from 94 patients with
162 very or highly asymmetric ectasia (VAE) were included in Group III (E-VAE), whose
163 fellow eyes presented with normal topography (Group IV – NT-VAE). Twenty-two
164 (22/94) very asymmetric ectasia cases had one or more surgical procedures such as
165 CXL and ICRS implantation in the ectatic eye prior to the study, and were not included
166 in Group III because these cases did not have a Corvis ST measurement
167 preoperatively.

168 All patients had a comprehensive ophthalmic examination, including the Corvis
169 ST and Pentacam HR (OCULUS Optikgeräte GmbH; Wetzlar, Germany) exams with

170 acceptable quality for proper analysis. Soft contact lens wear was discontinued for at
171 least three days prior to the exam and rigid or hybrid contact lenses were discontinued
172 for a minimal period of three weeks. The inclusion criteria for being a normal case
173 (Group I) was to have normal corneas on the general eye exam in both eyes, including
174 normal slit-lamp biomicroscopy, DCVA of 20/20 or better, overall subjective normal
175 topography and tomography exams with no previous surgery and no use of topical
176 medications different than artificial tears in both eyes. Keratoconic eyes included in this
177 study were diagnosed with clinical ectasia in both eyes without any previous ocular
178 procedures, such as CXL or ICRS implantation.^{40,41} The criteria for clinical diagnosis of
179 ectasia included topographic characteristics, such as skewed asymmetric bow-tie,
180 inferior steepening and at least one slit lamp finding (Munson's sign, Vogt's striae,
181 Fleischer's ring, apical thinning, Rizutti's sign).⁴¹ Patients were considered as very
182 asymmetric if the diagnosis of ectasia was confirmed in one eye based on the
183 previously described criteria and the fellow had a normal front surface curvature
184 (topometric) map. Objective criteria for considering normal topography was rigorously
185 applied for defining the cases of Group IV, including KISA% lower than 60 and a
186 paracentral inferior–superior (I-S value) asymmetry value at 6mm (3mm radii) less than
187 1.45.⁴² These criteria avoid problems related to the subjectivity and inter and intra-
188 examiner variability of the classifications of topographic maps.⁴³ All cases from each
189 clinic had the tomographic data blindly re-evaluated by an expert on Anterior Segment
190 from the other center (R. Ambrósio and P. Vinciguerra) for confirming inclusion criteria.

191 All measurements from the Corvis ST and Pentacam HR were taken by an
192 experienced technician. Proper exam quality was assured by a manual, frame-by-frame

193 analysis of each exam, made by an independent masked examiner to ensure quality of
194 each acquisition, including good edge detection over the whole deformation response or
195 rotating Scheimpflug images, with the exclusion of severe alignment errors (x-direction),
196 and blinking errors. Data from Pentacam HR and Corvis ST were exported to a custom
197 spreadsheet using special research software.

198

199 **Statistical Analysis**

200 Statistical analyses were performed by different software packages: MedCalc
201 Statistical Software version 16.8.4 (MedCalc, Ostend, Belgium
202 <https://www.medcalc.org>), SPSS version 23 (IBM Corp. in Armonk, NY, USA), the R
203 Core Team version 3.3.1.2016 (R Foundation for Statistical Computing, Vienna, Austria.
204 URL <https://www.R-project.org/>), and a custom-written MATLAB program (R14, The
205 MathWorks, Natick, MA, USA).

206 The data were analyzed and combined using different artificial intelligence
207 methods (AI) including logistic regression analysis (LRA) with forward stepwise
208 inclusion, support vector machine (SVM) and random forest (RF).^{39,44} These methods
209 were employed to optimize the ability to distinguish normal corneas (group I) from
210 ectatic cases (groups II, III and IV) by the combination of parameters from corneal
211 deformation response (CDR) and tomography, including Corvis Biomechanical Index
212 (CBI),³⁶ and BAD-D (Belin/Ambrósio Deviation).^{12,18,21,34,45-48} Considering the combined
213 parameters were programmed to have their output values as a continuous number

214 ranging from zero to one, an LRA function was created only using the BAD-D as the
215 input parameter to calculate BAD-DI in order to facilitate comparisons. The leave-one-
216 out cross-validation (LOOCV) technique was chosen for validation. In this method, a
217 new model is built as many times as the number of cases included in the study. Each
218 different model is built for all cases excluding one subject in which the model is tested.
219 The results of the non-included cases in each of the 850 built models provide the output
220 values of the LOOCV. Thereby, the validation model refers to the different models there
221 were built with the leave-one-out strategy. Considering the number of false positive and
222 false negative cases, the model would be validated or not. Once the model is properly
223 validated for its generalized performance, a definitive algorithm would be built for all
224 cases, which is expected to provide a more optimistic performance, but possibly with
225 some degree of overfitting. However, it is expected that the results from the LOOCV
226 provide a more realistic estimation of the performance when the model is applied in a
227 novel population.

228 The Kolmogorov-Smirnov goodness-of-fit test and D'Agostino-Pearson test were
229 applied for checking normal distributions. Spearman rank correlation test was used to
230 measure the degree of association between age and TBI. ANOVA was used to test
231 differences for age among the groups. Considering all indices in the keratoconus group
232 were non-normally distributed, the analyzed parameters were compared among the
233 groups using the non-parametric Kurskal-Wallis test, followed by the post hoc Dunn's
234 test to compare each pair of groups. The discriminative ability of each parameter was
235 assessed by Receiver operating characteristic (ROC) curves. For each parameter
236 tested, the area under the ROC curve (AUROC) was calculated and the best cutoff

237 value that yielded the highest accuracy is determined along with the sensitivity and
238 specificity. Pairwise comparisons of the AUROC were accomplished with nonparametric
239 approach as described by DeLong and coworkers for comparing the performance of
240 diagnostic tests.⁴⁹ Furthermore, separation curves that display accuracy as a function of
241 shifting the cut off value were plotted as described by Bühren.⁵⁰ This method allows for
242 comparisons among the different metrics by using normalized cut points by a Z
243 transformation with the optimum cutoff set to zero. The area under the separation curve
244 (AUSEP) was calculated between the x limits of -2 and 2 standard deviations and y
245 limits of 50 and 100% accuracy. Thus, higher AUSEP values indicate a high
246 discriminative ability with a high tolerance to shifts of the critical cutoff value.⁵⁰ For ROC
247 analysis a custom-written MATLAB program (R14, The MathWorks, Natick, Mass.) was
248 used to confirm results obtained by MedCalc.

249

250

251

252

253 **Results**

254 A total of three hundred and sixty-four patients (227 healthy, 111 keratoconus
255 and 26 cases with very asymmetric ectasia [VAE]) were enrolled from the Rio de
256 Janeiro Corneal Tomography and Biomechanics Study Group at *Instituto de Olhos*
257 *Renato Ambrósio* in Rio de Janeiro, Brazil. Four hundred and fourteen patients were
258 enrolled from the Vincieye Clinic in Milan, Italy (253 healthy, 93 keratoconus and 68
259 cases with VAE). Table 1 summarizes the demographic characteristics of the groups.
260 Females accounted for 57.5% of normal patients, while there were 64.43% of males
261 among ectasia patients. There were no statistically significant differences for age
262 among the groups (ANOVA, $p=0.273$). However, there was a broader range in the
263 normal group.

264 Table 2 summarizes the descriptive statistics of the most important parameters
265 among the groups. Central and minimal corneal thickness values, and maximal (KMax)
266 keratometric values were normally distributed among normal eyes ($p>0.5$). Central
267 (apex) thickness averaged $558\mu\text{m}$ with $30.1\mu\text{m}$ of standard deviation, ranging from 470
268 to $674\mu\text{m}$. Mean thinnest pachymetry was $552\mu\text{m}$ with $30\mu\text{m}$ of standard deviation,
269 ranging from 467 to $646\mu\text{m}$. The average difference between central and thinnest point
270 values was $5.8\mu\text{m}$ with $4\mu\text{m}$ of standard deviation, ranging from 0 to $24\mu\text{m}$, with 10.4%
271 of cases having over $10\mu\text{m}$ difference and 3.1% having over $15\mu\text{m}$ difference. Mean
272 maximal keratometry (Kmax) was 44.38D with 1.54D of standard deviation, ranging
273 from 40.2 to 48.5D. Eighteen eyes (3.75%) in the normal group had a positive
274 topometric keratoconus classification (TKC).⁵¹ Six cases (1.25%) had an I-S value
275 higher than 1.45 and 1 case (0.21%) had KISA% higher than 60. Mean BAD-D was

276 0.745 with 0.56 standard deviation, ranging from -1.13 to 2.35. Twenty eyes from group
277 I (4.6%) had BAD-D values higher than 1.6 and 82 eyes (17.1%) had BAD-D values
278 higher than 1.26 among normal eyes. CBI³⁶ was higher than 0.5 in 2.5% of normal
279 cases (false positives).

280 All frank ectasia cases (groups II and III) had abnormalities detected by corneal
281 topography that fulfilled criteria for diagnosis.^{41,42} However, forty-eight cases (17.4%)
282 had Kmax lower than 47.5D and 23 cases (8.7%) had Kmax lower than 46D. The
283 Oculus topometric classification for keratoconus (TKC)⁵¹ distribution was negative for 13
284 cases (4.7%). Eighty-nine cases (32.2%) were classified as grade 1, 78 (28.3%) as
285 grade 2, 67 (24.3%) as grade 3 and 29 (10.5%) cases were classified as grade 4
286 ectasia. Four frank ectatic cases (1.4%) had BAD-D lower than 1.6, 14 cases (5.1%)
287 had I-S value lower than 1.45D and 40 cases (14.5%) had KISA% lower than 60. CBI³⁶
288 was higher than 0.5 in 94.2% of frank ectatic eyes.

289 All eyes included in group IV were objectively determined to have normal
290 topography (NT-VAE), having I-S value lower than 1.45D, KISA% lower than 60 and no
291 positive TKC value.⁴² Figure 1 displays the front surface axial or sagittal curvature
292 (topometric) maps using Smolek-Klyce absolute 1.5D scale from the 94 NT-VAE cases.
293 BAD-D was higher than 1.6 in 40 cases (42.6%) and higher than 1.26 in 64 cases
294 (68.1%). Thirty-five (37.2%) cases in group IV had CBI higher than 0.5 and 42 cases
295 (44.7%) had CBI higher than 0.3.

296 Three different artificial intelligence approaches were applied for combining data
297 from corneal deformation response (Corvis ST) and corneal tomography (Pentacam)

298 data using leave-one-out cross-validation (LOOCV). Indices were determined from the
299 logistic regression analysis (LRAI) with forward stepwise inclusion, support vector
300 machine (SVM) and random forest (RF). The most accurate method was the random
301 forest which is referred to as the TBI. A linear regression formula was applied for
302 normalizing BAD-D into an index, with outputs ranging from zero to one (BAD-DI). The
303 BAD-DI formula included a constant and a coefficient for BAD-D ($y = a + b \cdot x$): 2.85958
304 (constant) + (-4.84877 * BAD-D), so that BAD-D and BAD-DI have a perfect correlation.
305 However, this approach facilitates comparison with other parameters as seen in Figure
306 2, which display the dot-plot graphs for the BAD-D, BAD-DI, CBI, and TBI.

307 Table 2 includes the mean, standard deviation, median and range (minimum –
308 maximum) for the main parameters, including BAD-D, BAD-DI, CBI, LRA, SVM and
309 TBI. Results of Kruskal–Wallis one-way analysis of variance demonstrated differences
310 among the studied groups for all studied parameters ($p < 0.000001$), which was
311 confirmed by Jonckheere–Terpstra trend test ($p < 0.00001$). Post-hoc Dunn’s test results
312 were similar for all parameters, confirming differences among all paired groups
313 ($p < 0.001$), with the exception of the comparison between keratoconus and ectatic eyes
314 from the very asymmetric cases (group II x group III [KC x VAE-E]).

315 Table 3 summarizes the results of receiver-operating characteristic (ROC) curve
316 analysis and the area under the separation curve (AUSEP) calculated between the
317 limits of -2 and +2 standard deviations. The analysis was performed for testing the
318 discriminating abilities to separate normal cases and all diseased cases (Table 3A),

319 normal cases from the cases with frank ectasia (table 3B) and normal cases with the
320 supposed subclinical cases (table 3C). These data correlate to Figure 3 (A-C).

321 The TBI results presented refer to the outputs of the random forest method with
322 leave-one-out cross-validation (RF/LOOCV) strategy, which provided the highest
323 accuracy compared to LRA and SVM. The AUROC of the TBI for detecting ectasia
324 (groups II, III and IV) was 0.996. The cut off value of 0.48 correctly classified 97.5% of
325 the cases, having 98.8% specificity with 96.2% sensitivity. TBI had 100% sensitivity to
326 detect frank ectasia cases (AUROC=1.0; groups II and III) with no false positives among
327 the normal cases with optimal cut off values ranging from 0.75 to 0.81. Considering the
328 ability to detect the eyes with normal topography from patients with clinical ectasia in the
329 fellow eye, optimization of cut off value to 0.29 provided 90.4% sensitivity with 4% false
330 positives (96% specificity; AUROC=0.985). TBI had a statistically higher AUROC
331 (DeLong, $p < 0.001$) than all other parameters for every analysis performed, except for
332 the comparisons with BAD-D for detecting clinical ectasia cases (groups II and III), in
333 which TBI had AUROC of 1.0 and BAD-D (and BAD-DI) had 0.997 (DeLong; $p = 0.1198$).
334 However, the AUSEP for BAD-D and BAD-DI were respectively 64 and 95, while TBI
335 was 112. Such difference in AUSEP potentially confirms the higher discriminating ability
336 of TBI than BAD-D to distinguish normal and clinical ectatic cases despite the non-
337 significant differences found among the AUROC (Table 3). TBI had a significant
338 negative correlation with age ($p < 0,0001$; Spearman's coefficient of rank correlation [ρ]
339 = -0.18).

340 The ‘final’ random forest algorithm that is programmed and included in the
341 commercial Oculus software is based on an optimized algorithm that included all 850
342 cases in the training set. This output provided an effectively perfect accuracy, reaching
343 an AUROC of 1.0 for all subgroup comparisons in the current study. Considering the
344 highest value for normal cases was 0.34 and the lowest values for frank ectatic cases
345 (groups II and III) and for the cases in group IV were respectively 0.91 and 0.37, the cut
346 off value of 0.35 correctly classified 100% of the cases. Interestingly, the correlation of
347 the output of the TBI with LOOCV and the final model was highly significant ($p < 0.0001$;
348 Spearman's coefficient of rank correlation [ρ] = 0.887).

349 Discussion

350 In this study, we introduce the TBI (Tomographic/Biomechanical Index) as a
351 novel parameter based on a robust and innovative combination of data derived from
352 Scheimpflug based corneal tomographic and biomechanical analysis. The TBI is
353 derived from Pentacam HR and Corvis ST exams, resulting in higher accuracy for
354 detecting ECD than all previous analyzed parameters. This was confirmed by analyzing
355 the AUROC and AUSEP curves (Figures 2 and 3). While, it is important to include
356 cases with mild or sub-clinical forms of ECD to facilitate appreciation of the clinical
357 benefit for the novel parameter, the AUROC of TBI was statistically higher than all other
358 analyzed parameters including CBI, when considering the detection of cases with
359 clinical ectasia (groups II and III). As demonstrated by Vinciguerra and coworkers,³⁶ CBI
360 was accurate for detecting clinical ectasia cases, with 16 false negative cases (5.7%)
361 and 97.5% specificity, and AUROC of 0.977 which was statistically lower than TBI. In
362 addition, the analysis of the separation curves (AUSEP) potentially reveals the benefits
363 of TBI over metrics that are indeed highly accurate. For example, the BAD-D^{12,18,21,34,45-}
364 ⁴⁸ had 98.2% sensitivity to detect clinical ectasia with less than 1% false positives
365 (99.2% specificity) among normal eyes in the current study. The AUROC of BAD-D (and
366 BAD-DI) was 0.997 which is not significantly lower than the one for TBI (AUROC=1.0)
367 accordingly to DeLong's test to compare AUROC.⁴⁹ However, the analysis of the
368 separation curves as described by Bühren⁵⁰ discloses a more dichotomous response
369 characteristic of the TBI (Figure 2D), which is more tolerant to shifts on the cut off
370 criterion compared to BAD-D and BAD-DI (Figure 2A).

371 The study included a large cohort of patients with normal corneas and with
372 different levels of ectatic corneal disease (ECD). In order to avoid selection bias related
373 to the use of both eyes from the same subject, we included one eye randomly selected
374 per patient in groups I and II.³⁹ Seventy two patients had one eye in group III and the
375 other eye in group IV. While these patients had both eyes included, these cases were
376 by definition highly asymmetric, which avoids the problems related to enantiomorphism
377 or similarities between right and left eyes. Considering the limitations of subjective
378 interpretation of corneal topography maps,⁴³ we were restricted to applying front surface
379 curvature indices as described by Rabinowitz⁴² for objectively defining the inclusion
380 criteria of group IV. Interestingly, even after twenty-three cases from the preliminary set
381 of group IV were reclassified into group II due to the above criteria, some cases from
382 group IV would still be found with suspicious curvature maps (Figure 1).

383 The current study included 94 eyes that reached objective criteria for normal
384 corneal topography from patients with clinical ectasia in the fellow eye. This constitutes
385 one of the largest cohort studies including such a special group of cases.^{17-19,52} TBI was
386 sensitive to detect abnormalities among 90.4% of cases in Group IV with less than 5%
387 false positives. However, while these cases have been referred to as forme fruste
388 keratoconus by Klyce,⁵³ it is important to consider that some of these cases may be true
389 unilateral ectasia cases.⁵⁴ Remarkably, there is a consensus that true unilateral
390 keratoconus does not exist, but also that secondary, induced ectasia caused by a pure
391 mechanical process, such as eye rubbing, may occur unilaterally.⁸ These ideas are in
392 agreement with the two-hit hypothesis, which put forward the concept of ectasia to
393 result from an underlying genetic predisposition along with external environmental

394 factors, including eye rubbing and atopy.⁷ Our hypothesis is that TBI may reflect the
395 inherent susceptibility of the cornea to ectasia progression.

396 A possible study for assessing ectasia susceptibility involves the analysis of the
397 preoperative state of cases that developed ectasia after LVC along with the surgical
398 parameters which represent the impact from surgery on the cornea.²⁰ Another possible
399 approach is to integrate finite element simulations with the corneal structural and shape
400 analysis. In addition, adding longitudinal analysis for a retrospective evaluation of
401 patients that progressed to clinical ectasia would further improve criteria to define such
402 a group.²¹ Even though we included a relatively large number of cases with mild ECD,
403 50% of the cases from groups II and III had Kmax lower than 52D and 65% had TKC
404 grade 2 or lower.

405 A limitation of the current cohort may be the criteria for inclusion in Group I. Even
406 though this is expected to be relatively rare, it is possible that some eyes with a normal
407 clinical exam, including corneal topography and tomography, have mild or susceptible
408 forms of ectasia such as in cases that progressed to keratectasia after different LVC
409 procedures.¹¹⁻¹⁵ The preoperative state of stable cases with long term follow up after
410 LVC would provide a more robust population for the normal control group.^{17,20,34}

411 The random forest method provided the most efficient strategy for developing
412 TBI. In this advanced compound artificial intelligence based model, analysis starts like
413 an ordinary decision tree. This includes successive nodes defined by independent
414 variables with objective decisions based on cut off values. As in a classic decision tree,
415 the analyzed case is successively split into two mutual subgroups (branches) that

416 subdivide until a final decision of class assignment (leaves). The random forest takes
417 this approach to the next level by combining numerous trees with the concept of an
418 ensemble or cooperative effort. The algorithm grows the trees by sampling the data into
419 random subgroups. Some input variables are also randomly selected to test their
420 capability of splitting the data at each node. The predictor variable that provides the best
421 split, according to an objective function is applied on each node. Each tree gets a "vote"
422 in classifying. The final classification is based on the votes of all trees for providing a
423 combined value that typically varies from zero to one.⁴⁴ The increase in complexity
424 enhances the power of discrimination and reduces the chances of overfitting.

425 Nevertheless, as for any machine learning method, it is fundamental to include a cross-
426 validation method to infer or presume external validity of the model. In the current study,
427 the leave-one-out cross-validation (LOOCV) was chosen. The LOOCV method
428 increases computational time and complexity, but also significantly increases the
429 reliability or robustness of the model in classifying new data. Interestingly, TBI accuracy,
430 as presented in Figures 2D and 3, refers to the output values from the LOOCV strategy.
431 This is indeed a slightly pessimistic performance compared to the virtually perfect
432 accuracy that would have been found with the 'final' TBI model that is programmed in
433 the commercial Oculus software. Nevertheless, the result from the LOOCV outputs is
434 essentially a more conservative and also a more truthful representation of the
435 generalized performance for the TBI. This is a fundamental consideration that will be
436 addressed in future studies for external validation of TBI, which are already underway.

437 TBI is a combined parameter based on Scheimpflug-based corneal tomography
438 and biomechanical assessments. It provides exceeding accuracy for detecting ectasia

439 comparing to other parameters, with high sensitivity for detecting sub-clinical (fruste)
440 ectasia among eyes with normal topography in very asymmetric patients. TBI may also
441 be considered as an objective index for representing the inherent susceptibility of the
442 cornea to undergo ectasia progression, which is highly relevant when screening
443 refractive surgery candidates.

444

445 **References**

446

447 1. Binder PS, Lindstrom RL, Stulting RD, et al. Keratoconus and corneal ectasia
448 after LASIK. *J Refract Surg* 2005;21:749-52.

449 2. Ambrósio R, Jr., Randleman JB. Screening for ectasia risk: what are we
450 screening for and how should we screen for it? *J Refract Surg* 2013;29:230-2.

451 3. Santhiago MR, Smadja D, Wilson SE, Krueger RR, Monteiro ML, Randleman JB.
452 Role of percent tissue altered on ectasia after LASIK in eyes with suspicious
453 topography. *J Refract Surg* 2015;31:258-65.

454 4. Santhiago MR, Smadja D, Gomes BF, et al. Association between the percent
455 tissue altered and post-laser in situ keratomileusis ectasia in eyes with normal
456 preoperative topography. *Am J Ophthalmol* 2014;158:87-95 e1.

457 5. Ambrósio R, Jr., Dawson DG, Belin MW. Association between the percent tissue
458 altered and post-laser in situ keratomileusis ectasia in eyes with normal preoperative
459 topography. *Am J Ophthalmol* 2014;158:1358-9.

460 6. Ambrósio R, Jr., Wilson SE. Complications of laser in situ keratomileusis:
461 etiology, prevention, and treatment. *J Refract Surg* 2001;17:350-79.

462 7. McGhee CN, Kim BZ, Wilson PJ. Contemporary Treatment Paradigms in
463 Keratoconus. *Cornea* 2015;34 Suppl 10:S16-23.

464 8. Gomes JA, Tan D, Rapuano CJ, et al. Global consensus on keratoconus and
465 ectatic diseases. *Cornea* 2015;34:359-69.

466 9. Salomao MQ, Esposito A, Dupps WJ, Jr. Advances in anterior segment imaging
467 and analysis. *Curr Opin Ophthalmol* 2009;20:324-32.

- 468 10. Ambrósio R, Jr., Klyce SD, Wilson SE. Corneal topographic and pachymetric
469 screening of keratorefractive patients. *J Refract Surg* 2003;19:24-9.
- 470 11. Klein SR, Epstein RJ, Randleman JB, Stulting RD. Corneal ectasia after laser in
471 situ keratomileusis in patients without apparent preoperative risk factors. *Cornea*
472 2006;25:388-403.
- 473 12. Ambrósio R, Jr., Dawson DG, Salomao M, Guerra FP, Caiado AL, Belin MW.
474 Corneal ectasia after LASIK despite low preoperative risk: tomographic and
475 biomechanical findings in the unoperated, stable, fellow eye. *J Refract Surg*
476 2010;26:906-11.
- 477 13. Chan CC, Hodge C, Sutton G. External analysis of the Randleman Ectasia Risk
478 Factor Score System: a review of 36 cases of post LASIK ectasia. *Clin Experiment*
479 *Ophthalmol* 2010;38:335-40.
- 480 14. Malecaze F, Couillet J, Calvas P, Fournie P, Arne JL, Brodaty C. Corneal ectasia
481 after photorefractive keratectomy for low myopia. *Ophthalmology* 2006;113:742-6.
- 482 15. Sachdev G, Sachdev MS, Sachdev R, Gupta H. Unilateral corneal ectasia
483 following small-incision lenticule extraction. *J Cataract Refract Surg* 2015;41:2014-8.
- 484 16. Ambrósio R, Jr., Belin MW. Imaging of the cornea: topography vs tomography. *J*
485 *Refract Surg* 2010;26:847-9.
- 486 17. Saad A, Gatinel D. Topographic and tomographic properties of forme fruste
487 keratoconus corneas. *Invest Ophthalmol Vis Sci* 2010;51:5546-55.
- 488 18. Ambrósio R, Jr., Valbon BF, Faria-Correia F, Ramos I, Luz A. Scheimpflug
489 imaging for laser refractive surgery. *Curr Opin Ophthalmol* 2013;24:310-20.

- 490 19. Smadja D, Touboul D, Cohen A, et al. Detection of subclinical keratoconus using
491 an automated decision tree classification. *Am J Ophthalmol* 2013;156:237-46 e1.
- 492 20. Ambrósio Jr R, Ramos I, Lopes B, et al. Assessing ectasia susceptibility prior to
493 LASIK: the role of age and residual stromal bed (RSB) in conjunction to Belin-Ambrósio
494 deviation index (BAD-D). *Revista Brasileira de Oftalmologia* 2014;73:75-80.
- 495 21. Ambrósio R, Jr., Nogueira LP, Caldas DL, et al. Evaluation of corneal shape and
496 biomechanics before LASIK. *Int Ophthalmol Clin* 2011;51:11-38.
- 497 22. Li Y, Tan O, Brass R, Weiss JL, Huang D. Corneal epithelial thickness mapping
498 by Fourier-domain optical coherence tomography in normal and keratoconic eyes.
499 *Ophthalmology* 2012;119:2425-33.
- 500 23. Reinstein DZ, Gobbe M, Archer TJ, Silverman RH, Coleman DJ. Epithelial,
501 stromal, and total corneal thickness in keratoconus: three-dimensional display with
502 artemis very-high frequency digital ultrasound. *J Refract Surg* 2010;26:259-71.
- 503 24. Pahuja N, Shroff R, Pahanpate P, et al. Application of high resolution OCT to
504 evaluate irregularity of Bowman's layer in asymmetric keratoconus. *J Biophotonics*
505 2016.
- 506 25. Roberts CJ, Dupps WJ, Jr. Biomechanics of corneal ectasia and biomechanical
507 treatments. *J Cataract Refract Surg* 2014;40:991-8.
- 508 26. Luce DA. Determining in vivo biomechanical properties of the cornea with an
509 ocular response analyzer. *J Cataract Refract Surg* 2005;31:156-62.
- 510 27. Fontes BM, Ambrósio R, Jr., Jardim D, Velarde GC, Nose W. Corneal
511 biomechanical metrics and anterior segment parameters in mild keratoconus.
512 *Ophthalmology* 2010;117:673-9.

- 513 28. Luz A, Lopes B, Hallahan KM, et al. Discriminant Value of Custom Ocular
514 Response Analyzer Waveform Derivatives in Forme Fruste Keratoconus. *Am J*
515 *Ophthalmol* 2016;164:14-21.
- 516 29. Luz A, Lopes B, Hallahan KM, et al. Enhanced Combined Tomography and
517 Biomechanics Data for Distinguishing Forme Fruste Keratoconus. *J Refract Surg*
518 2016;32:479-94.
- 519 30. Ambrósio Jr R, Ramos I, Luz A, et al. Dynamic ultra high speed Scheimpflug
520 imaging for assessing corneal biomechanical properties. *Revista Brasileira de*
521 *Oftalmologia* 2013;72:99-102.
- 522 31. Ali NQ, Patel DV, McGhee CN. Biomechanical responses of healthy and
523 keratoconic corneas measured using a noncontact scheimpflug-based tonometer.
524 *Invest Ophthalmol Vis Sci* 2014;55:3651-9.
- 525 32. Bak-Nielsen S, Pedersen IB, Ivarsen A, Hjortdal J. Dynamic Scheimpflug-based
526 assessment of keratoconus and the effects of corneal cross-linking. *J Refract Surg*
527 2014;30:408-14.
- 528 33. Steinberg J, Katz T, Lucke K, Frings A, Druchkiv V, Linke SJ. Screening for
529 Keratoconus With New Dynamic Biomechanical In Vivo Scheimpflug Analyses. *Cornea*
530 2015;34:1404-12.
- 531 34. Ambrósio R, Jr., Lopes B, Faria-Correia F, et al. Ectasia Detection by the
532 Assessment of Corneal Biomechanics. *Cornea* 2016;35:e18-20.
- 533 35. Vinciguerra R, Elsheikh A, Roberts CJ, et al. Influence of Pachymetry and
534 Intraocular Pressure on Dynamic Corneal Response Parameters in Healthy Patients. *J*
535 *Refract Surg* 2016;32:550-61.

- 536 36. Vicniguerra R, Ambrósio Jr R, Elsheikh A, Roberts CR, Lopes BT, Vinciguerra P.
537 Detection of Keratoconus with the new Corvis ST Biomechanical Index. Journal of
538 Refractive Surgery 2016;in press.
- 539 37. Lopes BT, Ramos IdC, Salomão MQ, Canedo ALC, Ambrósio Jr. R. Perfil
540 paquimétrico horizontal para a detecção do ceratocone. Revista Brasileira de
541 Oftalmologia 2015;74:382-5.
- 542 38. Joda AA, Shervin MM, Kook D, Elsheikh A. Development and validation of a
543 correction equation for Corvis tonometry. Comput Methods Biomech Biomed Engin
544 2016;19:943-53.
- 545 39. Lopes B, Ramos ICdO, Ribeiro G, et al. Bioestatísticas: conceitos fundamentais
546 e aplicações práticas. Revista Brasileira de Oftalmologia 2014;73:16-22.
- 547 40. Gomes JA, Tan D, Rapuano CJ, et al. Global consensus on keratoconus and
548 ectatic diseases. Cornea 2015;34:359-69.
- 549 41. Rabinowitz YS. Keratoconus. Surv Ophthalmol 1998;42:297-319.
- 550 42. Rabinowitz YS, Rasheed K. KISA% index: a quantitative videokeratography
551 algorithm embodying minimal topographic criteria for diagnosing keratoconus. J
552 Cataract Refract Surg 1999;25:1327-35.
- 553 43. Ramos IC, Correa R, Guerra FP, et al. Variability of subjective classifications of
554 corneal topography maps from LASIK candidates. J Refract Surg 2013;29:770-5.
- 555 44. Breiman L. Random Forests. Machine Learning 2001;45:5-32.
- 556 45. Ambrósio R, Jr., Luz A, Lopes B, Ramos I, Belin MW. Enhanced ectasia
557 screening: the need for advanced and objective data. J Refract Surg 2014;30:151-2.

- 558 46. Ambrósio R, Jr., Ramos I, Lopes B, et al. Ectasia susceptibility before laser
559 vision correction. *J Cataract Refract Surg* 2015;41:1335-6.
- 560 47. Belin MW, Ambrósio R. Scheimpflug imaging for keratoconus and ectatic
561 disease. *Indian J Ophthalmol* 2013;61:401-6.
- 562 48. Belin MW, Villavicencio OF, Ambrósio RR, Jr. Tomographic parameters for the
563 detection of keratoconus: suggestions for screening and treatment parameters. *Eye*
564 *Contact Lens* 2014;40:326-30.
- 565 49. DeLong ER, DeLong DM, Clarke-Pearson DL. Comparing the areas under two or
566 more correlated receiver operating characteristic curves: a nonparametric approach.
567 *Biometrics* 1988;44:837-45.
- 568 50. Bühren J, Kuhne C, Kohnen T. Defining subclinical keratoconus using corneal
569 first-surface higher-order aberrations. *Am J Ophthalmol* 2007;143:381-9.
- 570 51. Salomao MQ, Ramos IC, Jordao LF, Canedo ALC, Valbon BF, Luz A, Correa R,
571 Lopes BT, Ambrósio Jr R. Accuracy of Topometric Indices for Distinguishing between
572 Keratoconic and Normal Corneas. *Int J Keratoconus and Ectatic Corneal Diseases*
573 2013;2:108-12.
- 574 52. Arbelaez MC, Versaci F, Vestri G, Barboni P, Savini G. Use of a support vector
575 machine for keratoconus and subclinical keratoconus detection by topographic and
576 tomographic data. *Ophthalmology* 2012;119:2231-8.
- 577 53. Klyce SD. Chasing the suspect: keratoconus. *Br J Ophthalmol* 2009;93:845-7.
- 578 54. Ramos IC, Reinstein DZ, Archer T, Gobbe M, Salomão MQ, Lopes BT, Luz A,
579 Faria-Correia F, Gatinel D, Belin MW, Ambrósio Jr R. Unilateral Ectasia characterized

580 by Advanced Diagnostic Tests. International Journal of Keratoconus and Ectatic

581 Corneal Diseases 2016;5:51-56.

582

583 **Figure legends**

584 **Figure 1:** Front surface axial or sagittal curvature (topometric) maps using Smolek-
585 Klyce absolute 1.5D scale from the 94 cases included in Group IV (VAE-NT).

586 **Figure 2:** box and dot plots showing the distribution of metric values across the groups.
587 **A, BADD B, BADDI C, CBI D, LRI E, SVMI F, TBI.** The box spans the 1st and 3rd
588 quartile. the whiskers indicate the 1.5-fold interquartile range. Colored markers
589 representing each value and their mean are superimposed.

590 **Figure 3:** receiver-operating characteristic and separation curves for the different
591 metrics. **A,** group I (normals) vs. groups II (keratoconus), III (very asymmetric ectasia)
592 and IV (topographically normal fellow eyes of very asymmetric ectasia eyes) **B,** group I
593 vs. groups II and III **C,** group I vs. groups IV.

Tables

Table 1. Demographic Characteristics of the Groups

	RIO				Milano			
	n	Male	Female	Ave Age (min - max)	n	Male	Female	Ave Age (min - max)
group I <i>(normals)</i>	227	96	131	37.71 (7 - 90)	253	108	145	43.20 (7 - 88)
group II <i>(KC eyes)</i>	111	72	39	32.90 (12 - 64)	93	66	27	38.10 (16 - 72)
group III <i>(E-VAE eyes)</i>	19	10	9	32.89 (14 - 74)	53	30	23	36.96 (13 - 83)
group IV <i>(NT-VAE eyes)</i>	26	15	11	35.02 (14 - 74)	68	39	29	37.66 (13 - 83)

Table 2: Descriptive statistics. Mean \pm standard deviation; median (minimum – maximum)

	<i>group I (normals)</i>	<i>group II (KC eyes)</i>	<i>group III (E-VAE eyes)</i>	<i>group IV (NT-VAE)</i>
I-S Value	0.16 \pm 0.55	5.79 \pm 4.32	5.17 \pm 3.63	0.53 \pm 0.51
	0.16 (-1.46 - 1.91)	4.80 (-2.60 - 33.69)	4.34 (-2.07 - 16.07)	0.61 (-0.76 - 1.42)
KISA	10.73 \pm 13.95	2699.29 \pm 12870.32	1579.36 \pm 4666.63	13.81 \pm 14.88
	5.24 (0.33 - 82.62)	369.72 (2.30 - 173021)	285.03 (2.79 - 35153)	7.51 (0.33 - 59.20)
Pachy Min	552.56 \pm 29.99	466.86 \pm 47.84	480.11 \pm 42.14	517.66 \pm 30.95
	553 (467 - 646)	468.50 (173 - 596)	479.50 (351 - 581)	521 (449 - 599)
Pachy Apex	558.45 \pm 30.10	488.60 \pm 123.24	493.85 \pm 43.37	525.98 \pm 29.68
	559 (470 - 647)	485 (209 - 213)	492.50 (356 - 583)	529 (451 - 606)
ART Max	469.84 \pm 76.56	177.63 \pm 76.08	197.58 \pm 88.84	369.89 \pm 77.23
	463 (247 - 744)	166.50 (0.00 - 460)	174 (66.00 - 442)	365 (190 - 546)
ART Avg	601.90 \pm 93.58	261.34 \pm 104.37	292.61 \pm 110.97	491.43 \pm 78.47
	591.50 (359 - 985)	259.50 (0.00 - 653)	270.50 (101 - 609)	487.5 (298 - 667)
EleF BFS8mm Thinnest	1.90 \pm 1.63	19.60 \pm 19.33	19.00 \pm 10.46	2.83 \pm 1.74
	2.00 (-4.00 - 8.00)	16.50 (-50.00 - 72.00)	16.50 (0.00 - 49.00)	3.00 (-2.00 - 9.00)
EleB BFS 8mmThinnest	6.04 \pm 4.40	56.04 \pm 125.78	44.47 \pm 20.86	9.39 \pm 5.21
	6.00 (-5.00 - 19.00)	42.00 (2.00 - 1805.00)	43.00 (12.00 - 95.00)	9.00 (1.00 - 27.00)
SP_A1	106.30 \pm 17.65	66.84 \pm 24.11	67.25 \pm 24.90	85.19 \pm 26.04
	104.81 (60.69 - 165.00)	66.72 (2.91 - 150.11)	65.66 (32.33 - 116.74)	89.29 (35.22 - 142.45)
DARatioMax 2mm	4.30 \pm 0.50	5.86 \pm 1.56	5.53 \pm 1.21	4.83 \pm 0.64
	4.30 (3.19 - 5.60)	5.58 (3.20 - 15.36)	5.33 (3.55 - 8.77)	4.71 (3.68 - 6.52)
MaxInverse Radius Gauss5Fmm1	0.16 \pm 0.02	0.21 \pm 0.05	0.20 \pm 0.04	0.17 \pm 0.02
	0.15 (0.08 - 0.24)	0.20 (0.12 - 0.51)	0.19 (0.12 - 0.31)	0.17 (0.12 - 0.28)
BAD-D	0.75 \pm 0.56	7.97 \pm 4.66	6.97 \pm 3.64	1.61 \pm 0.68
	0.8 (1.13 - 2.35)	6.93 (0.76 - 25.94)	6.37 (1.82 - 18.79)	1.53 (0.18 - 3.22)
BAD-DI	0.12 \pm 0.14	0.98 \pm 0.11	0.99 \pm 0.06	0.44 \pm 0.31
	0 (0.070 - 0.87)	1 (0.06 - 1)	1 (0.59 - 1)	0.38 (0.01 - 0.99)
CBI	0.06 \pm 0.14	0.92 \pm 0.22	0.91 \pm 0.24	0.41 \pm 0.4
	0 (0 - 0.88)	1 (0 - 1)	1 (0 - 1)	0.24 (0 - 1)
LRAI	0.11 \pm 0.15	0.88 \pm 0.26	0.81 \pm 0.33	0.87 \pm 0.28
	0 (0.050 - 0.79)	1 (0.03 - 1)	1 (0.02 - 1)	1 (0.02 - 1)
SVMI	0.1 \pm 0.11	0.88 \pm 0.28	0.81 \pm 0.35	0.88 \pm 0.3
	0.08 (0.04 - 0.95)	1 (0.07 - 1)	1 (0.05 - 1)	1 (0.04 - 1)
TBI	0.07 \pm 0.1	0.97 \pm 0.04	0.97 \pm 0.04	0.76 \pm 0.28
	0 (0.070 - 0.75)	0.97 (0.83 - 1)	0.97 (0.87 - 1)	0.76 (0.08 - 1)

KC: keratoconus, VAE-E: ectatic eye from patients with very asymmetric ectasia, VAE-NT: normal topography fellow eye from patients with very asymmetric ectasia. BAD-D: Belin/Ambrósio Deviation value; BAD-DI: Belin/Ambrósio Deviation normalized index; CBI: Corvis Biomechanical Index; DA Ratio 2mm: deformation amplitude ratio between the apex and at 2mm from the apex; I-S: paracentral inferior–superior asymmetry value at 6mm (3mm radii); KISA: keratoconus percentage index; LRAI: linear regression analysis index; **MaxInverse Radius: inverse of maximal inverse radius at highest concavity**; Pachy Apex: pachymetric

value at the corneal apex: Pachy Min: pachymetric value at the corneal apex; SPA1: stiffness parameter at first applanation; SVM: support vector machine; TBI: tomographic & biomechanical index.

Table 3: Results of receiver-operating characteristic (ROC) curve analysis.

A. groups I vs. [II,III,IV]: normal vs. ‘diseased’ (KC, E-VAE and NT-VAE fellow eyes; Figure 2A)

<i>Parameter</i>	<i>AUROC</i>	<i>Sensitivity</i>	<i>Specificity</i>	<i>correctly classified [%]</i>	<i>cutoff</i>	<i>specificity @ 100% sensitivity</i>	<i>AUSEP</i>
BAD-D	0.956	0.841	0.965	90.3	1.62	14	51
BAD-DI	0.956	0.841	0.965	90.3	0.45	14	83
CBI	0.937	0.808	0.971	88.9	0.46	0	82
LRAI	0.967	0.884	0.960	92.2	0.44	31	95
SVM	0.964	0.868	0.975	92.1	0.34	1	105
TBI	0.996	0.962	0.988	97.5	0.48	72	110

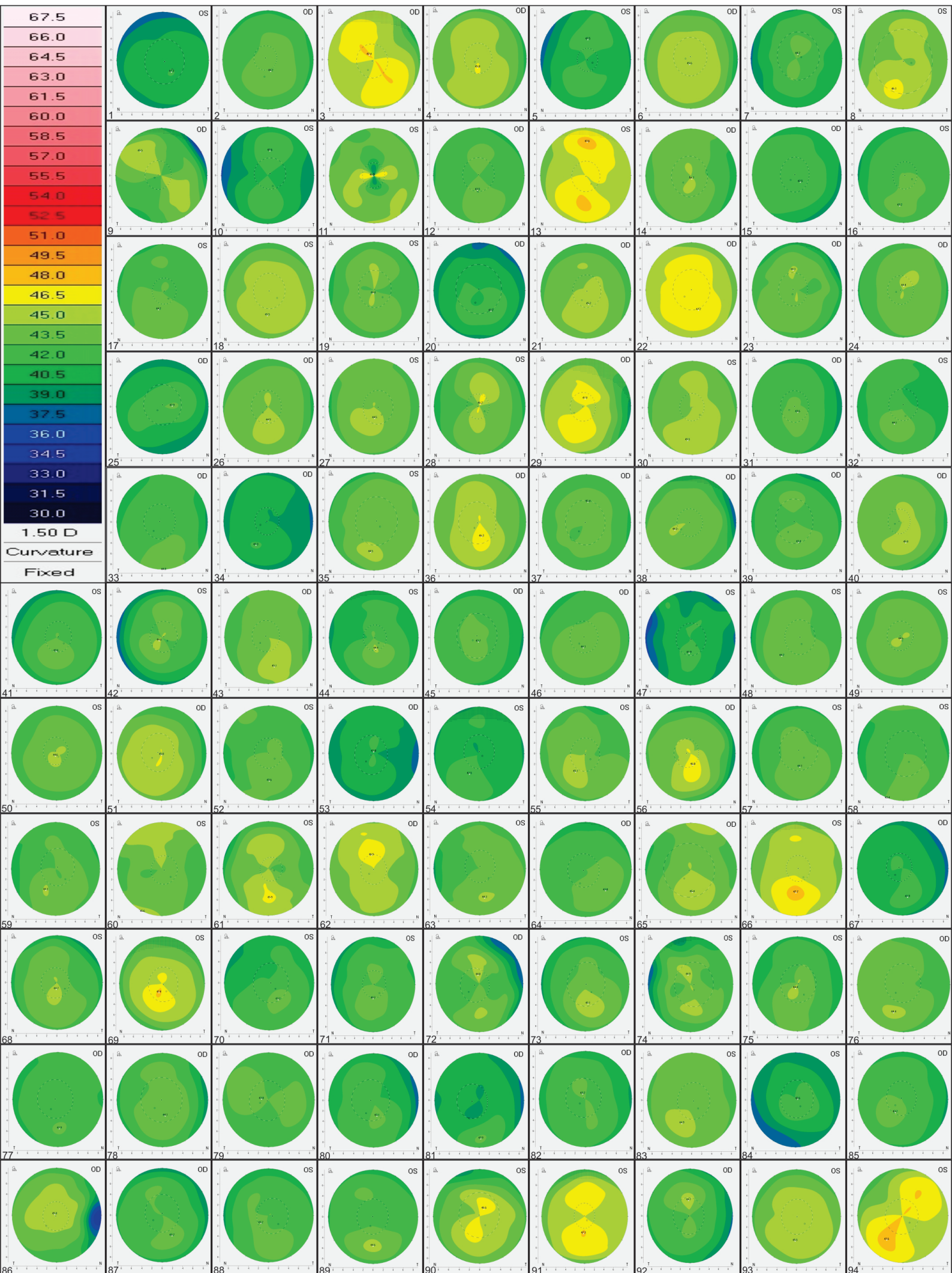
B. groups I vs. [II,III]: normal vs. frank ectasia (KC and E-VAE eyes; Figure 2B)

<i>parameter</i>	<i>AUROC</i>	<i>sensitivity</i>	<i>specificity</i>	<i>correctly classified [%]</i>	<i>cutoff</i>	<i>specificity @ 100% sensitivity</i>	<i>AUSEP</i>
BAD-D	0.997	0.982	0.992	98.7	1.97	47.3	64
BAD-DI	0.997	0.982	0.992	98.7	0.69	47.3	95
CBI	0.977	0.946	0.975	96.0	0.49	12.9	95
LRAI	0.967	0.888	0.960	92.4	0.44	32	99
SVM	0.964	0.877	0.967	92.2	0.30	1	109
TBI	1.000	1.000	1.000	100.0	0.79	100	112

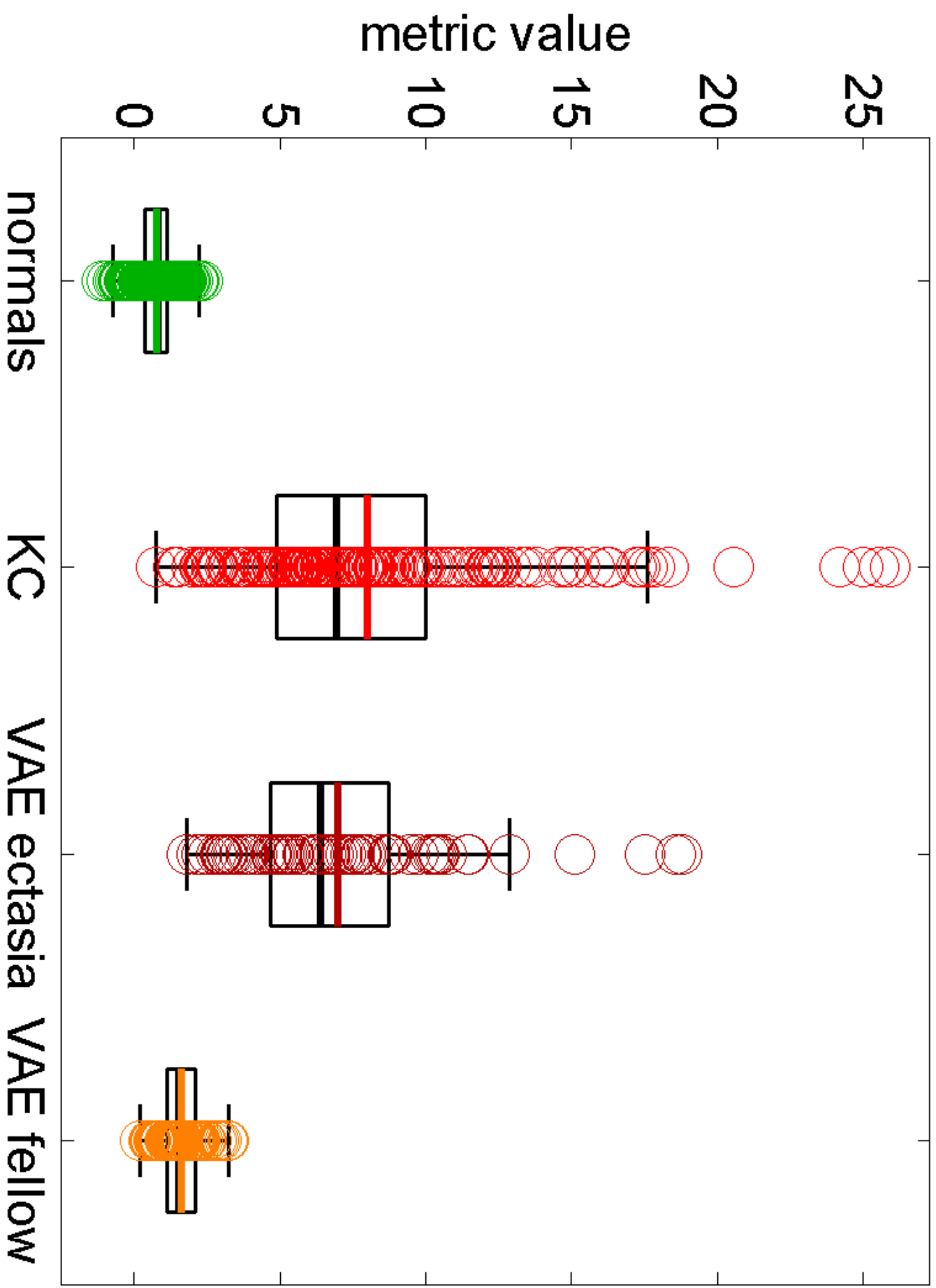
C. groups I vs. IV: normal vs. NT-VAE fellow eyes (Figure 2C)

<i>parameter</i>	<i>AUROC</i>	<i>sensitivity</i>	<i>specificity</i>	<i>correctly classified [%]</i>	<i>cutoff</i>	<i>specificity @ 100% sensitivity</i>	<i>AUSEP</i>
BAD-D	0.838	0.809	0.717	76.3	1.08	14	49
BAD-DI	0.838	0.809	0.717	76.3	0.14	14	47
CBI	0.822	0.681	0.823	75.2	0.07	0	46
LRAI	0.968	0.872	0.969	92.1	0.51	31	125
SVM	0.965	0.851	1.000	92.6	0.96	1	79
TBI	0.985	0.904	0.960	93.2	0.29	71.9	99

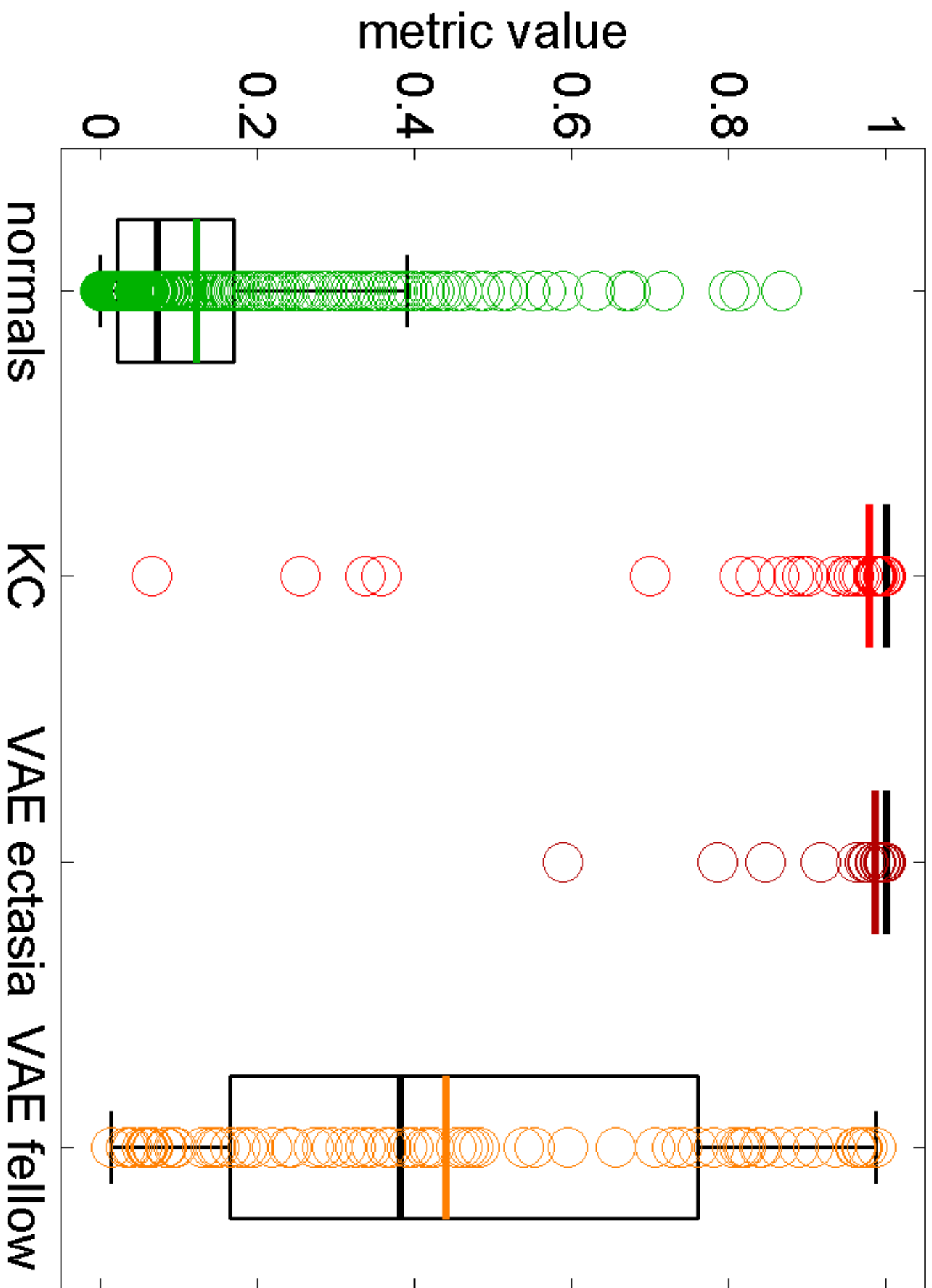
KC: keratoconus, E-VAE: ectatic eye from patients with very asymmetric ectasia, NT-VAE: normal topography fellow eye from patients with very asymmetric ectasia, AUROC area under the ROC curve, AUSEP: area under the separation curve



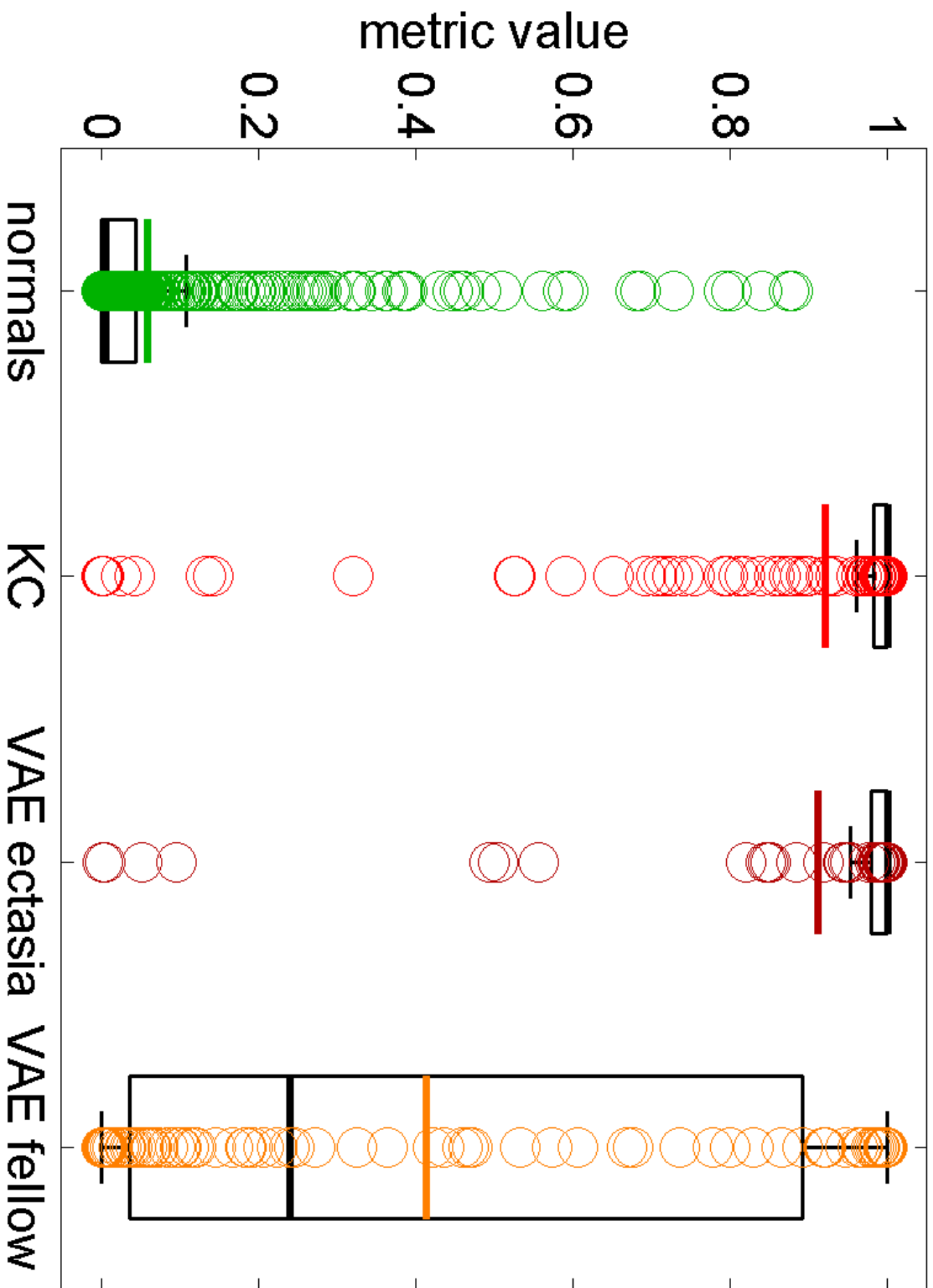
BADD



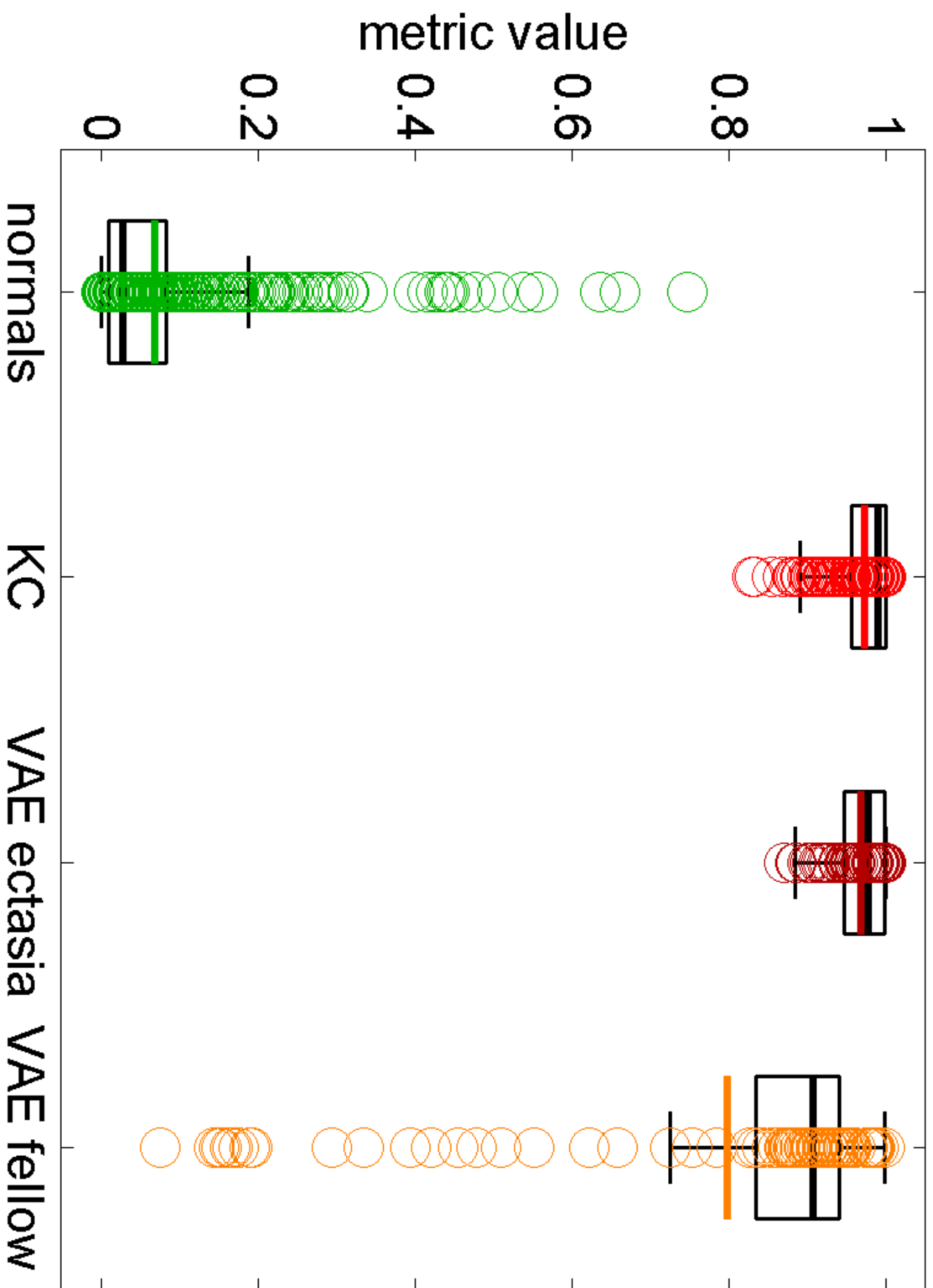
BADDI



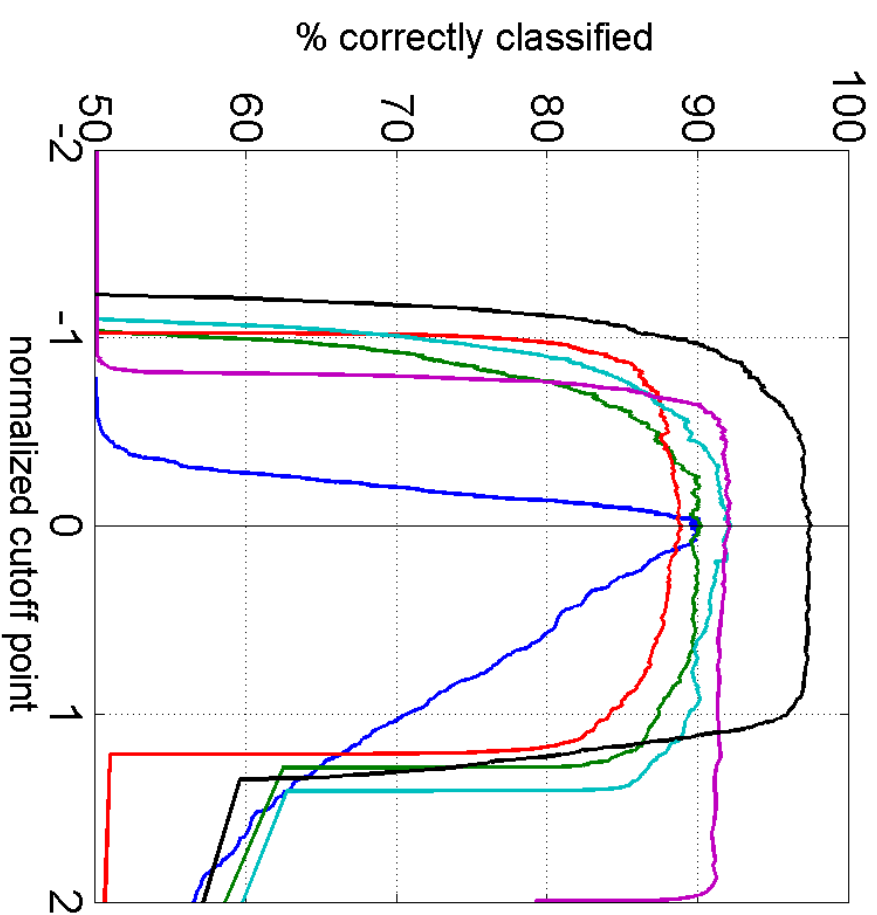
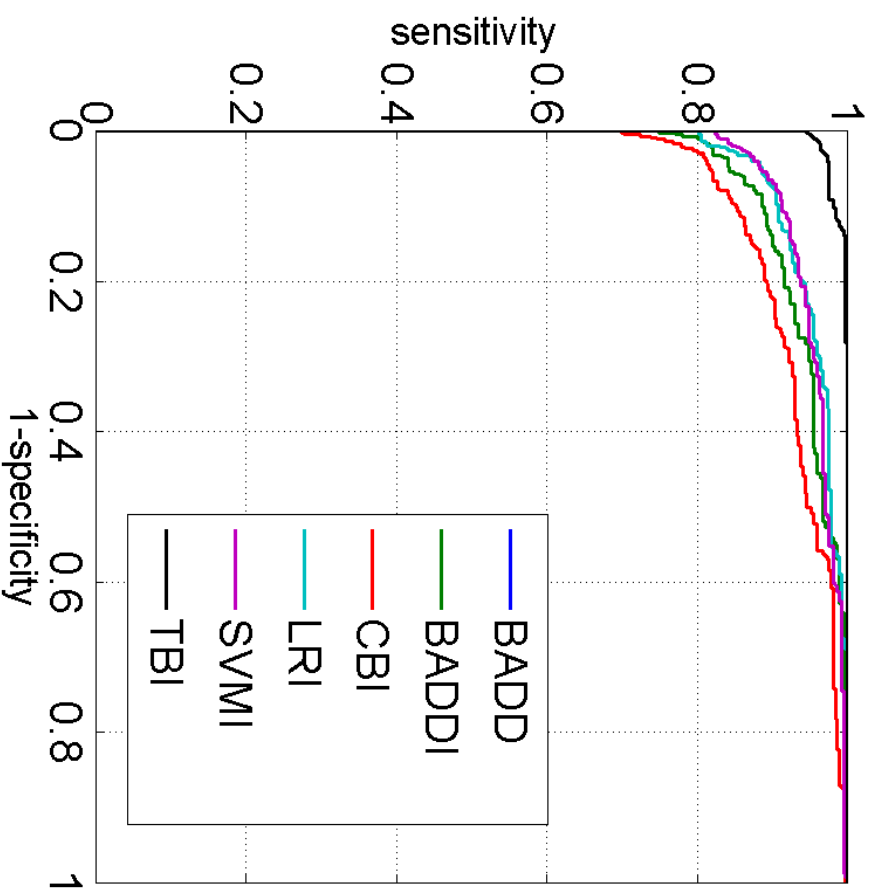
CBI

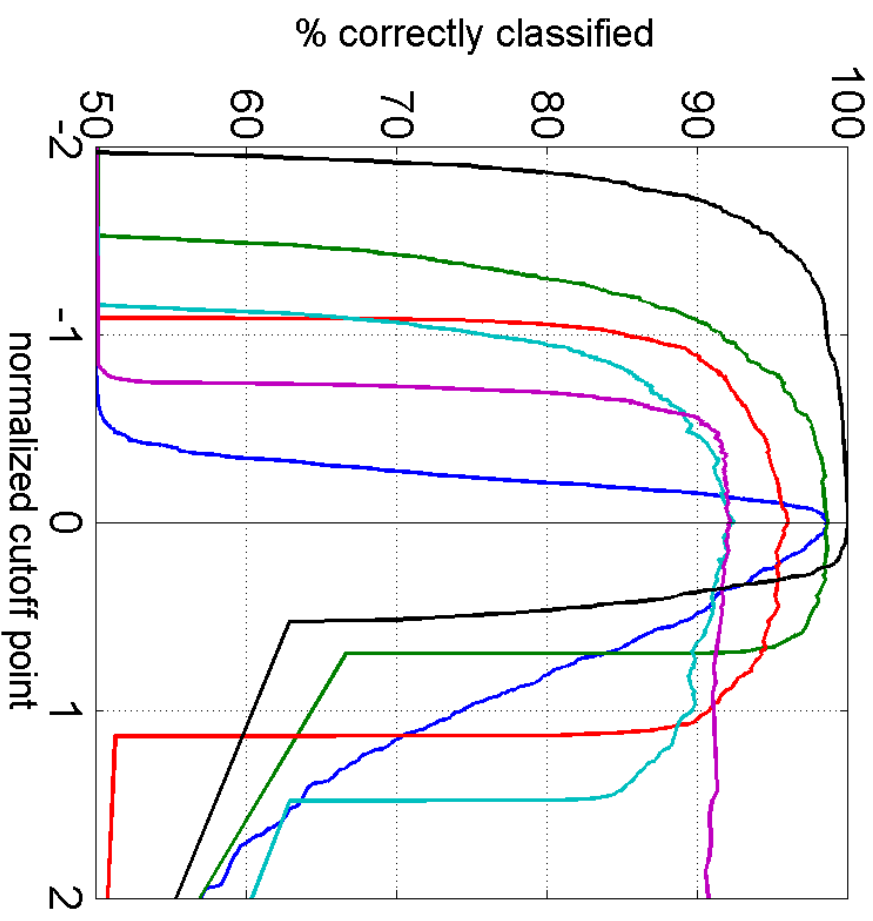
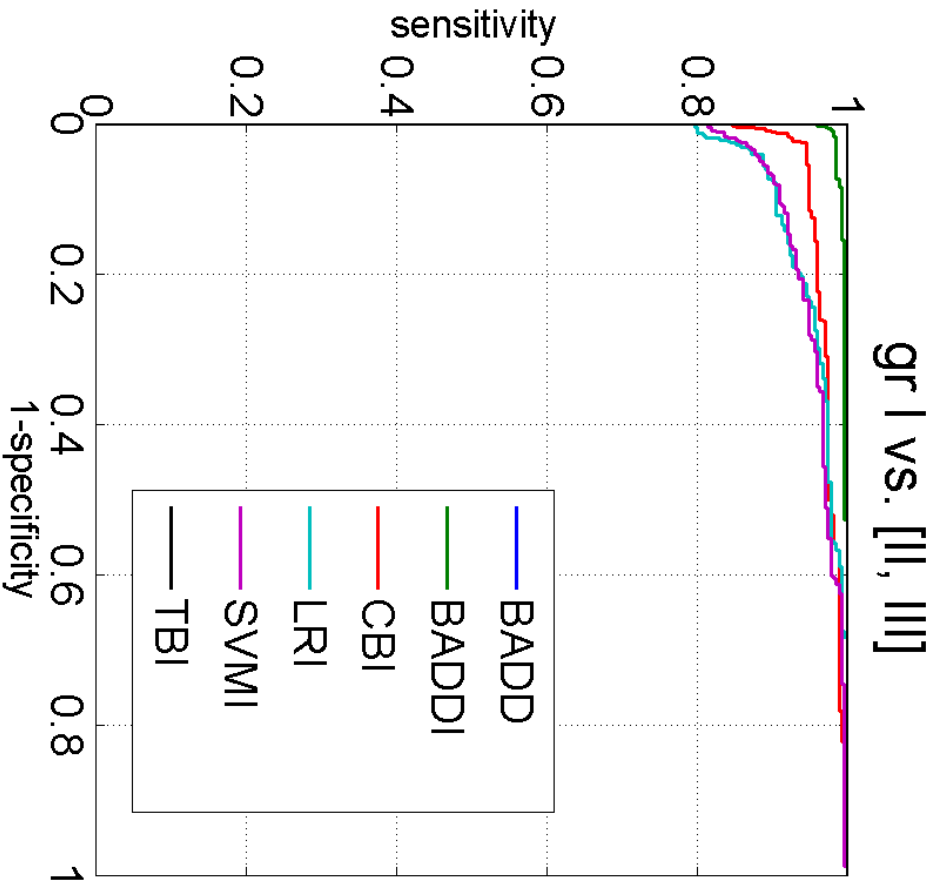


TBI



group I vs. [II, III, IV]





group I vs. IV

