

Dynamic analysis of a pumped-storage hydropower plant with random power load

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Abstract: This paper analyzes the dynamic response of a pumped-storage hydropower plant in generating mode. Considering the elastic water column effects in the penstock, a linearized reduced order dynamic model of the pumped-storage hydropower plant is used in this paper. As the power load is always random, a set of random generator electric power output is introduced to research the dynamic behaviors of the pumped-storage hydropower plant. Then, the influences of the PI gains on the dynamic characteristics of the pumped-storage hydropower plant with the random power load are analyzed. In addition, the effects of initial power load and PI parameters on the stability of the pumped-storage hydropower plant are studied in depth. All of the above results will provide theoretical guidance for the study and

analysis of the pumped-storage hydropower plant.

Keywords: pumped-storage hydropower plant, dynamic characteristics, random load, mathematical modeling

1. Introduction

Pumped-storage hydropower plants (PSHP) play an important role in the peak regulation and frequency control of a power grid. They pump water with the power consumption at valley hours and generate electricity with the power consumption at peak hours to balance energy production and consumption levels [1-5]. As the PSHP can assume advantageously the power-frequency regulation, they allow power plant owners to improve the power supply quality effectively [6-10]. Therefore, the research on dynamic analysis and stability of the PSHP is of great importance.

Many studies focus on the modeling and dynamic analysis of the PSHP [11-16]. It is worth mentioning the work presented in Ref. [17] where the dynamic characteristics of a pump-turbine were studied. The dynamic method was proposed to simulate the critical transient parameters. In Ref. [18], the authors explored the nonlinear dynamic behaviors of a hydro-turbine governing system in the process of sudden load increase transient. In Ref. [19], a one-dimensional numerical code estimating the performances of centrifugal PATs (pumps used as turbines) was presented. The work of [20] is aimed to analyze the different guide-vane closing schemes for reducing the maximum transient pressures in the S-shaped region. A series of model tests were conducted on a pumped-storage station model and the measured data fully validated the correctness of the analyses.

In practical situations, it is difficult to regulate and control perfectly the dynamic characteristics of the PSHP because of the random power load [21-25]. In addition, the lack of the accurate model of the PSHP and the qualitative analysis of control parameters also make it hard to ensure the stable operation of the PSHP [26-28]. However, few researchers have focused on the dynamic characteristics of the PSHP with random power load. Therefore, to overcome the above situations, this paper tries to investigate the influences of the PI gains on the PSHP with the random load from

the view point of dynamics. In addition, the effects of the initial load on the dynamic characteristic of the PSHP with random power load are analyzed deeply by means of simulations.

The remaining content of this paper is organized as follows. Section 2 introduces the PSHP. Section 3 presents the linear reduced order model of the PSHP. In Section 4, the system dynamic response is analyzed by means of simulations. The effects of the PI gains and initial power load on the dynamic characteristics of PSHP are discussed. Finally, Section 5 condenses the conclusions.

2. Dynamical model of the PSHP

The scheme of the considered system, corresponding to the mechanical and hydraulic components of the hydropower plant, is represented in Fig. 1. The main model blocks are described in the following subsections.

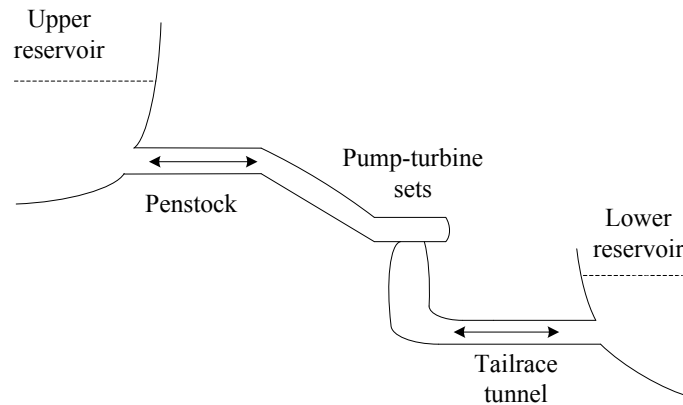


Fig. 1. Scheme of the dynamic model.

Notation

- b_{11} , b_{12} , partial derivatives of the flow with respect to the head, speed and wicket gate position (p.u.)
- b_{13} gate position (p.u.)
- b_{21} , b_{22} , partial derivatives of the turbine torque with respect to the head, speed and wicket gate position (p.u.)
- b_{23} and wicket gate position (p.u.)
- c turbine mechanical torque (p.u.)

h	net head (p.u.)
h_c	reservoir water level (p.u.)
Δh	relative deviation of the net head (p.u.)
k_{loc}	local head losses coefficient (p.u.)
k_p	proportional adjustment coefficient (p.u.)
k_i	integral adjustment coefficient (s^{-1})
Δn	relative deviation of the unit speed (p.u.)
p_g	generator electric power output (p.u.)
Δp_g	relative deviation of the generator electric power output (p.u.)
p_t	mechanical power (p.u.)
Δp_t	relative deviation of the mechanical power (p.u.)
q	flow through the turbine (p.u.)
Δq	relative deviation of the flow through the turbine (p.u.)
q_t	flow in the penstock (p.u.)
Δq_t	relative deviation of the flow in the penstock (p.u.)
z	wicket gate position (p.u.)
Δz	relative deviation of the wicket gate position (p.u.)
$r / 2$	continuous head losses coefficient (p.u.)
T_m	mechanical starting time (s)
T_w	water starting time in the penstock (s)
T_e	water elastic time (s)
T_r	dashpot time constant (s)
δ	transient speed droop

The speed variations caused by the unbalance between the relative deviation of generator power Δp_g and relative deviation of mechanical power Δp_t are presented as follows [29]:

$$T_m \cdot \frac{d\Delta n}{dt} \cdot n = \Delta p_t - \Delta p_g \quad (1)$$

Where T_m is the mechanical starting time and Δn indicates the relative deviation of unit speed.

A PI controller is used to eliminate the speed deviations. The controller gains are expressed as follows:

$$\frac{1}{\delta} \cdot \left(1 + \frac{1}{T_r} \int dt \right) \cdot \Delta n = \Delta z, \quad k_p = \frac{1}{\delta} \quad \text{and} \quad k_i = \frac{1}{\delta T_r}. \quad (2)$$

where δ and T_r indicates the transient speed droop and dashpot time constant, respectively. k_p and k_i are the proportional adjustment coefficient and integral adjustment coefficient, respectively.

Note that:

$\Delta n = (n - n^0) / n^0$, $\Delta z = (z - z^0) / z^0$ are the relative deviations of unit speed and wicket gate position, respectively. Similarly, $\Delta q_t = (q_t - q_t^0) / q_t^0$, $\Delta q = (q - q^0) / q^0$, $\Delta h = (h - h^0) / h^0$ and $\Delta p_t = (p_t - p_t^0) / p_t^0$ are the relative deviations of corresponding variables. The superscript '0' denotes the initial value.

3. The linear reduced order model of the PSHP

For control design purposes in plants with long penstocks, a reduced order penstock model is applied in this section [31]. The characteristic equations of the PSHP are linearized in the neighborhood of an initial equilibrium operating point in order to use linear methods for adjusting the controller gains [32].

A Π -shaped element having one series branch and two shunt branches is used here (Fig. 2). The total head losses are considered in the series branch and the

elasticity effect is included in the shunt branches. The variations in the relative deviation of the reservoir water level Δh_c are neglected and only the downstream shunt branch is involved in the plant dynamics. The series branch is represented by Eq. (3) and the shunt downstream branch by Eq. (4).

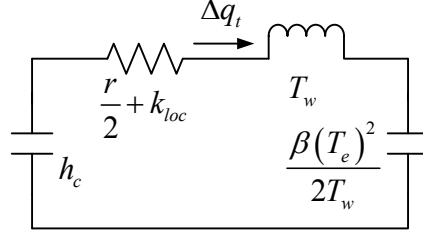


Fig. 2. Scheme of the penstock Π -shaped element model.

$$\frac{d\Delta q_t}{dt} = \frac{1}{T_w} \left(\Delta h_c - \Delta h - 2 \left(\frac{r}{2} + k_{loc} \right) \Delta q_t q_t^0 \right) \quad (3)$$

$$\frac{d\Delta h}{dt} = \frac{2T_w}{\beta T_e^2} (\Delta q_t - \Delta q) \quad (4)$$

where $\beta = \frac{8}{\pi^2} \cdot \frac{r}{2}$ and k_{loc} indicate the continuous head losses coefficient and local head losses coefficient, respectively. T_w and T_e are the water starting time in the penstock and water elastic time, respectively. From Ref. [11], the adequacy of the model has been verified.

The characteristic equations of the PSHP are Eqs. (1), (2), (3) and (4).

The linearized model of a hydro-turbine can be expressed as follows:

$$\Delta q = b_{11}\Delta h + b_{12}\Delta n + b_{13}\Delta z \quad (5)$$

$$\Delta c = b_{21}\Delta h + b_{22}\Delta n + b_{23}\Delta z \quad (6)$$

and

$$\Delta p_t \approx n^0 \Delta c + c^0 \Delta n = n^0 b_{21} \Delta h + (n^0 b_{22} + c^0) \Delta n + n^0 b_{23} \Delta z. \quad (7)$$

The coefficients b_{11} , b_{12} and b_{13} are the partial derivatives of the flow with respect to the head, speed and wicket gate position, respectively; the coefficients b_{21} , b_{22} and b_{23} are the partial derivatives of the turbine torque with respect to the head, speed and wicket gate position, respectively.

Neglecting second order terms in Eq. (1), the following expression can be obtained:

$$\Delta p_t - \Delta p_g = T_m \cdot \frac{d\Delta n}{dt} \cdot (n^0 + \Delta n) \approx T_m \cdot \frac{d\Delta n}{dt} n^0 \quad (8)$$

The following expression can be obtained by neglecting Δh_c in Eq. (3):

$$\frac{d\Delta q_t}{dt} = \frac{1}{T_w} \left(-\Delta h - 2 \left(\frac{r}{2} + k_{loc} \right) q_t^0 \Delta q_t \right) \quad (9)$$

Finally, the plant model results in a 6th order dynamic system. The state equations are

$$\begin{cases} \frac{d\Delta n}{dt} = \frac{\Delta p_t - \Delta p_g}{T_m n^0} \\ \frac{d\Delta q_t}{dt} = -\frac{1}{T_w} \Delta h - \frac{2 \left(\frac{r}{2} + k_{loc} \right)}{T_w} q_t^0 \Delta q_t \\ \frac{d\Delta q}{dt} = b_{11} \left(\frac{\pi^2 T_w}{4T_e^2} (\Delta q_t - \Delta q) \right) + b_{12} \left(\frac{\Delta p_t - \Delta p_g}{T_m n^0} \right) + b_{13} \left(-k_p \left(\frac{\Delta p_t - \Delta p_g}{T_m n^0} \right) + k_i \Delta n \right) \\ \frac{d\Delta h}{dt} = \frac{\pi^2 T_w}{4T_e^2} (\Delta q_t - \Delta q) \\ \frac{d\Delta p_t}{dt} = n^0 b_{21} \left(\frac{\pi^2 T_w}{4T_e^2} (\Delta q_t - \Delta q) \right) + (n^0 b_{22} + c^0) \left(\frac{\Delta p_t - \Delta p_g}{T_m n^0} \right) + n^0 b_{23} \left(-k_p \left(\frac{\Delta p_t - \Delta p_g}{T_m n^0} \right) + k_i \Delta n \right) \\ \frac{d\Delta z}{dt} = -k_p \left(\frac{\Delta p_t - \Delta p_g}{T_m n^0} \right) + k_i \Delta n \end{cases} \quad (10)$$

4. Numerical experiment

In this section, the effects of the PI gains and initial load on the dynamic characteristics of the PSHP are analyzed by means of the qualitative analysis. The numerical experiments are carried out by using the method of Runge-Kutta. More specifically, the fixed step is 0.1. The initial values are (0.001, 0.001, 0.001, 0.001) and the iteration steps are 1000.

In the daily operation of PSHP, the power load is subjected to a variety of random perturbations sustained in time, due to the dynamic behavior of consumption, temperature changes in the wires, errors in the measuring instruments, changes in the network's topology, etc. Therefore, the randomness is present at all times, and it is necessary to describe it as faithfully as possible to analyze the stochastic behavior of

real PSHP [33,34]. Considering the randomness of the power load, a set of Gaussian white noise (average=0, variance=0.001) generated by Matlab software as shown in Fig. 3 is introduced to simulate the random generator electric power.

The values of the plant parameters are included in Table 1.

Table 1

Turbine parameters and initial operation variables

q^0	1.0	n^0	1.0	h^0	1.0	z^0	1.0
b_{11}	0.5	b_{12}	0.0	b_{13}	1.0	T_w	1.203s
b_{21}	1.611	b_{22}	-1.556	b_{23}	1.111	T_e	5.029s

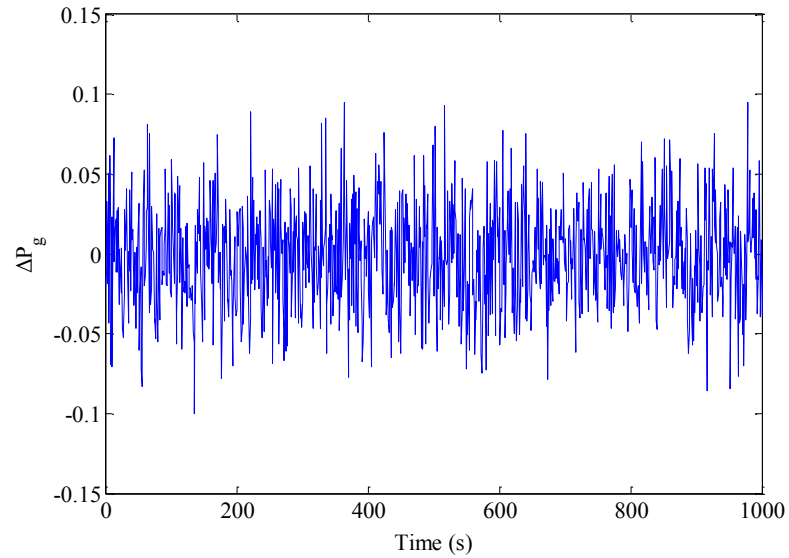


Fig. 3. A set of random generator electric power output.

From Table 1, the plant is operating in rated conditions. When the random generator electric power output is introduced into the PSHP, Figs. 4-6 show the actual three-dimensional dynamic responses of the system.

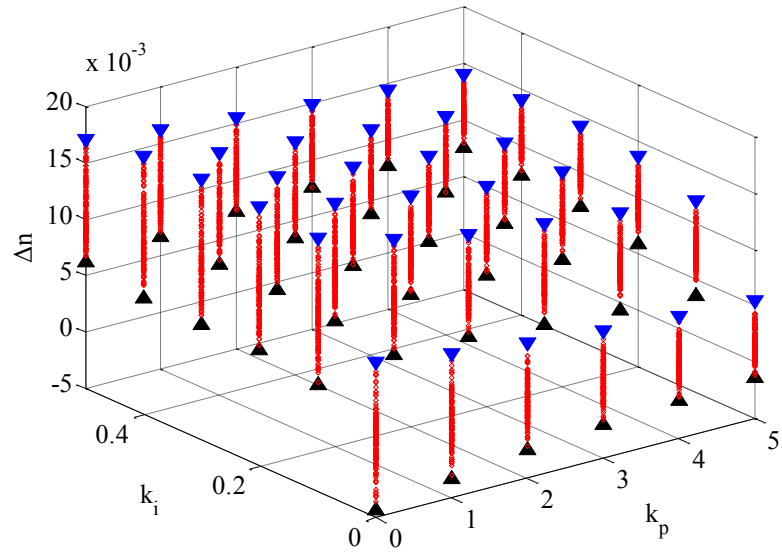


Fig. 4. Three-dimensional bifurcation diagram of the relative deviation of the speed.

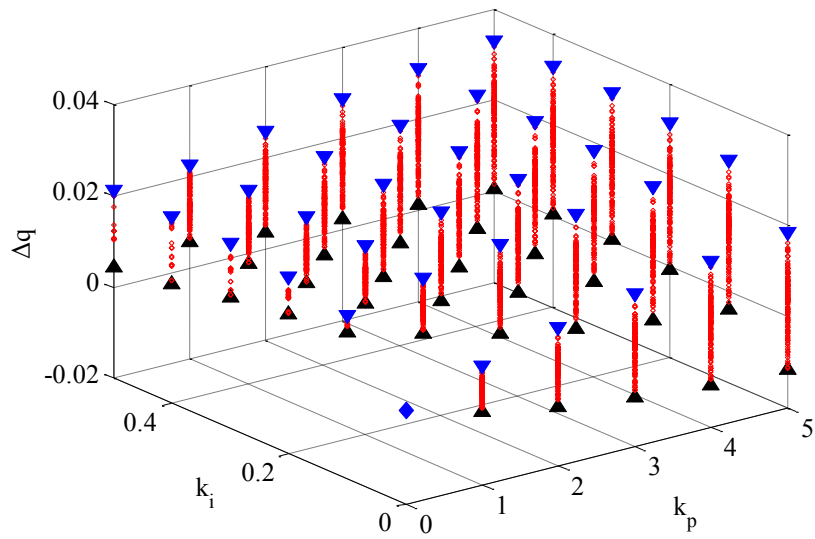


Fig. 5. Three-dimensional bifurcation diagram of the relative deviation of the flow through the turbine.

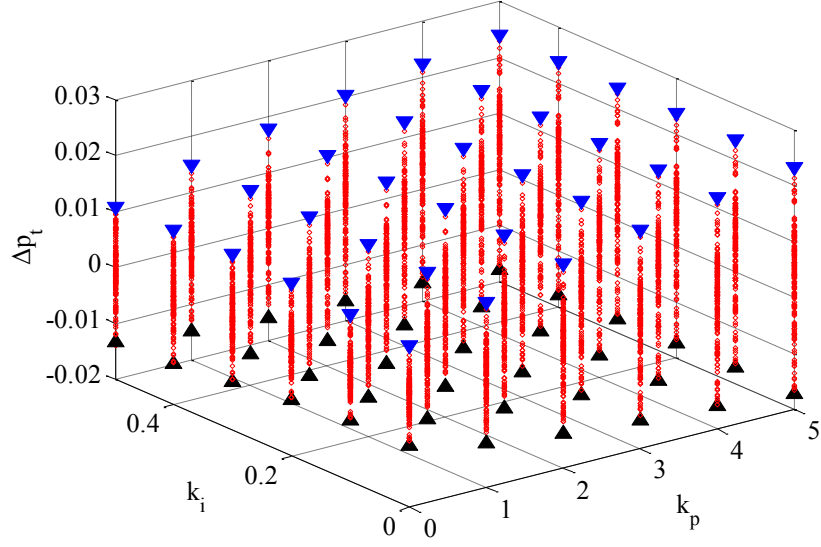


Fig. 6. Three-dimensional bifurcation diagram of the relative deviation of the mechanical power.

From Figs. 4-6, the settings of the governor PI have great impacts on the dynamic characteristics of the PSHP with the random power load. In addition, it is clear from the above three-dimensional bifurcation diagrams that the PI gains have different effects on different system parameters.

As shown in Fig. 4, the relative deviation of the speed varies from -0.005 to 0.018 when $0 \leq k_i \leq 0.5$ and $0 \leq k_p \leq 5$. In this region, the value of k_i has little effect on the variation range of the relative deviation of the speed, while the increase of k_p can reduce the variation range. It is worth noting that when k_i is near 0, compared with other groups, the variation range suddenly decreases by 0.01. This means that the dynamic characteristics of the speed can be improved effectively, if $k_i = 0$ and $k_p = 5$.

The Fig. 5 shows the responses of the relative deviation of the flow through the turbine. For different PI gains, the relative deviation of the flow through the turbine varies from -0.018 to 0.035. And the changing rule of the relative deviation of the flow is different from that of the speed. In Fig. 4, the relative deviation of the speed drops with the increase of the k_p . By contrast, the relative deviation of the flow through the turbine shows an upward trend with the k_p increasing (Fig. 5). In addition, the relative deviation of the flow through the turbine falls steadily with the

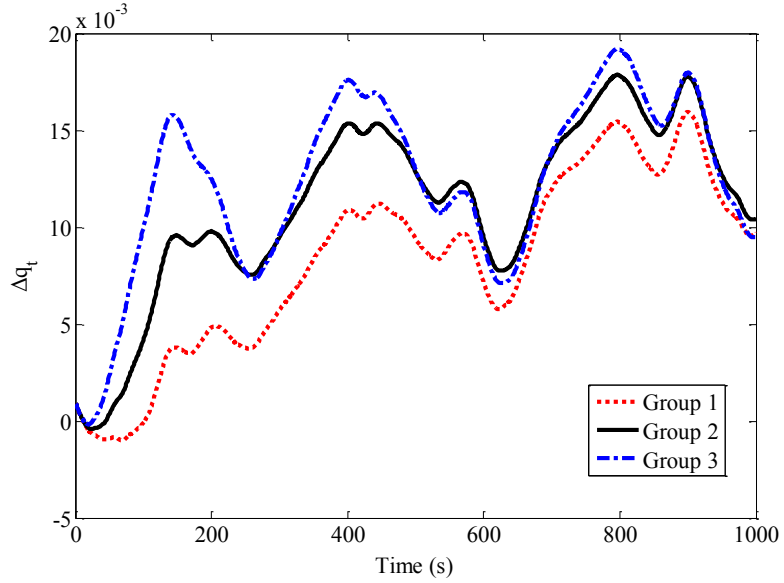
decrease of k_i . The relative deviation of the flow through the turbine has the minimum variation range when $k_i = 0$ and $k_p = 0$.

From Fig. 6, the effects of PI gains on the relative deviation of the mechanical power are similar to that on the relative deviation of the flow through the turbine. The fluctuation range of the relative deviation of the mechanical power experiences a dramatic decrease with the decreases of k_i and k_p .

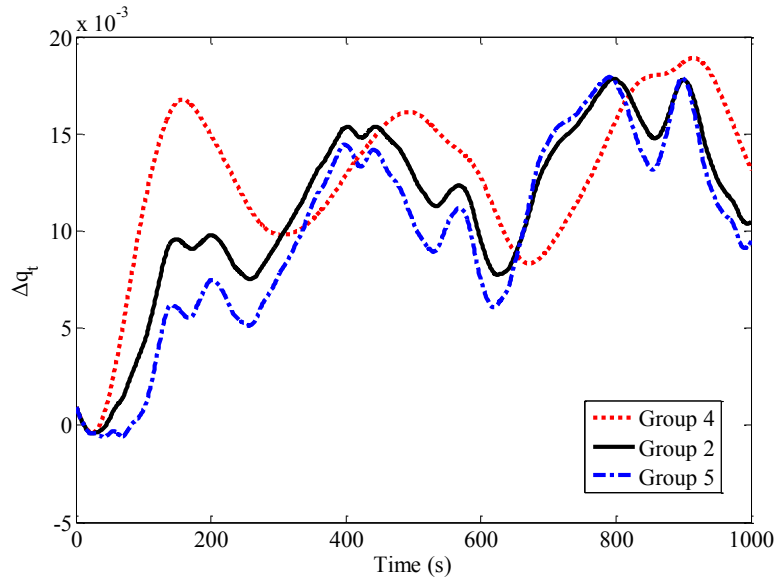
The responses of the relative deviation of the speed, flow through the turbine and mechanical power demonstrate that the PI gains are able to adjust the dynamic characteristic of the PSHP with the random power load. Furthermore, the optimal PI gains for the flow through the turbine and the mechanical power are different from that for the speed. The decrease of k_i can improve the dynamic characteristics of the speed, the flow through the turbine and the mechanical power. The decrease of k_p can also improve the dynamic quality of the flow through the turbine and the mechanical power, while it makes the speed unstable. The three-dimensional bifurcation diagrams of the relative deviation of the system parameters, as the method of qualitative research, present the different regulation laws of the PI gains for different system parameters. In order to further verify the regulation effect of the PI gains, simulation experiments are conducted with five representative groups of the PI gains, respectively. The five groups of the PI gains are

Group	1	2	3	4	5
(k_p, k_i)	(2.5,0.1)	(2.5,0.25)	(2.5,0.5)	(0.1,0.25)	(5,0.25)

In the numerical simulation, the effects of k_i on the system parameters are studied through Groups 1, 2 and 3. For Groups 4, 2 and 5, they are selected to research the effect of k_p .



(a) Time waveforms with different k_i .

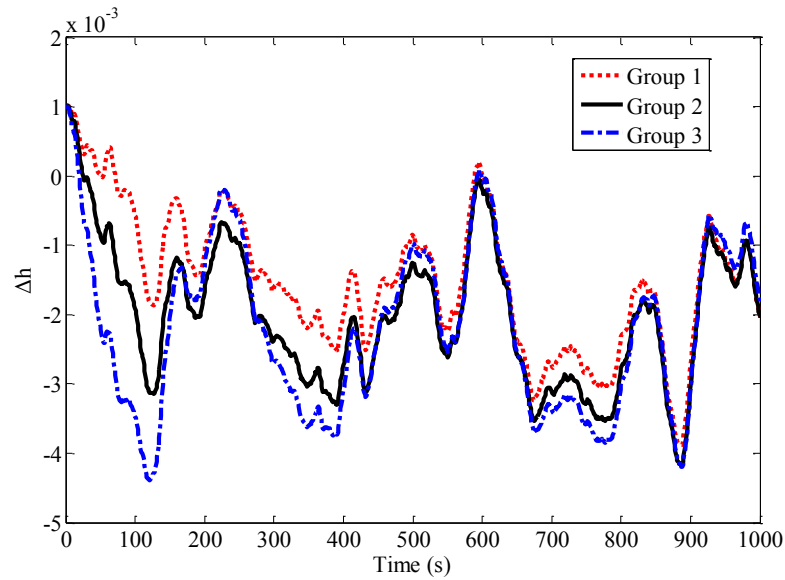


(b) Time waveforms with different k_p .

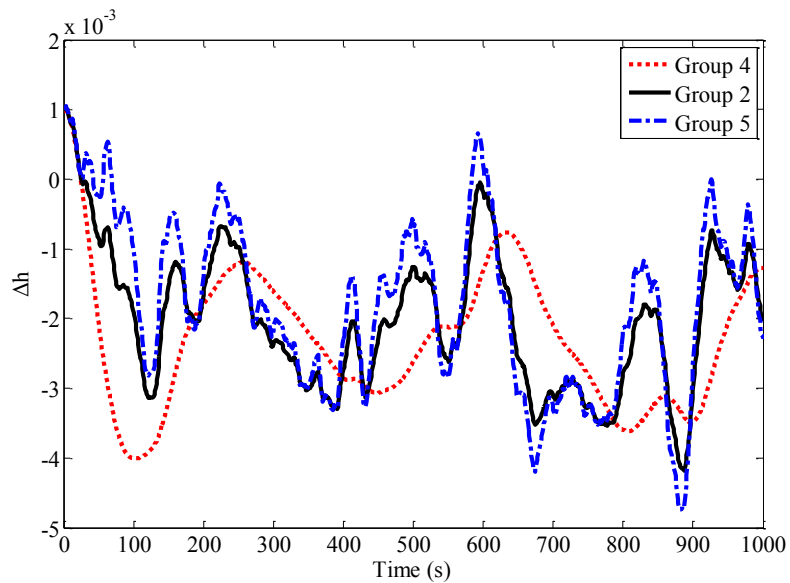
Fig. 7. Time waveforms of the relative deviation of the flow in the penstock with random power load.

As shown in Fig. 7, the relative deviation of the flow has the similar varying tendency in Groups 1-5. From Fig. 7(a), the relative deviation of the flow in the penstock in Group 3 is the highest throughout the period, reaching its peak at 19×10^{-3} at 800s. Moreover, the relative deviations of the flow in the penstock in Group 2 and 3 are consistently higher than that in Group 1. These results illustrate that the decrease of k_i can improve the dynamic characteristics of the flow in the

penstock. From Fig. 7(b), the relative deviation of the flow in Group 4 has the highest peak levels. The figures for Groups 2 and 5 are lower than that for Group 4 most of the time. The above results suggest that the flow in the penstock is becoming more stable with the increase of k_p .



(a) Time waveforms with different k_i .

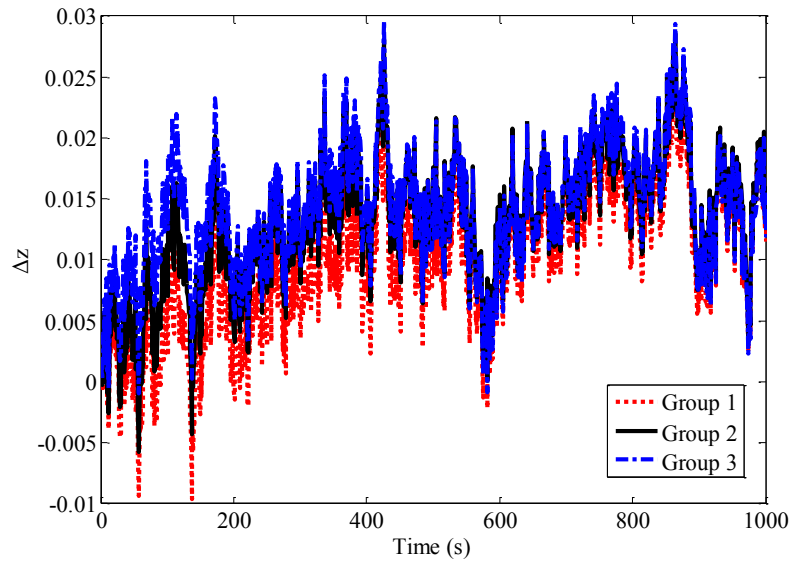


(b) Time waveforms with different k_p .

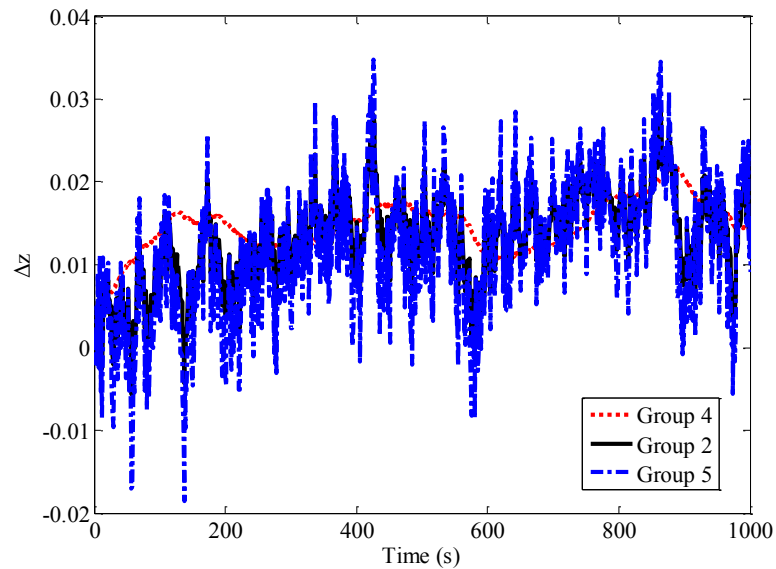
Fig. 8. Time waveforms of the relative deviation of the net head with random power load.

It can be seen from the Fig. 8 that the relative deviations of the net head experience dramatic fluctuations in Groups 1-5. It is worth noting that most of the net head is below zero over the period. From Fig. 8(a), the varying range of the net head is becoming more narrow with the decrease of k_i . In Fig. 8(b), the dynamic

characteristics of the net head is improved with the decrease of k_p because the figure for Group 4 is relative stable compared with that for Groups 2 and 5.



(a) Time waveforms with different k_i .



(b) Time waveforms with different k_p .

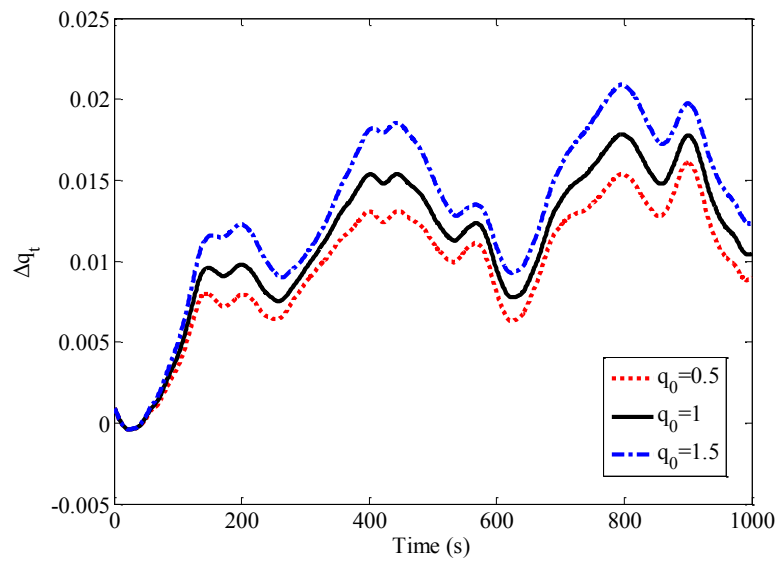
Fig. 9. Time waveforms of the relative deviation of the wicket gate position with random power load.

It is clear from the Fig. 9 that the relative deviation of the wicket gate position fluctuates significantly over the period. This means that the effect of the random power load is more remarkable for wicket gate position than that for other system parameters. The wicket gate position presents stochastic fluctuation with different values of k_i . The quantity of Group 3 has the widest fluctuation range in Fig. 9(a). In

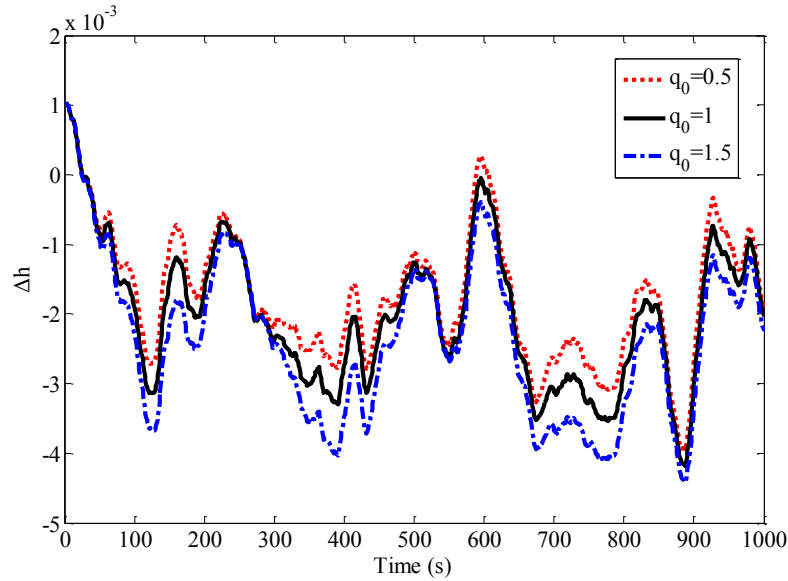
addition, the figure for Group 2 fluctuates more violently than that for Group 1. The results illustrate that the wicket gate position tends to fluctuate more widely with the k_i increasing. It is clear from the Fig. 9(b) that the decrease of the k_p is able to improve the dynamic characteristics of the wicket gate position.

The initial load can be denoted by the initial flow. In order to study the effect of the initial load on the dynamic characteristics of the PSHP, three groups of the initial flow are selected as follows:

Initial flow	Initial load
$q_0 = 0.5$	Partial load
$q_0 = 1$	Full load
$q_0 = 1.5$	Over load



(a) Time waveforms of the flow in the penstock.



(b) Time waveforms of the net head.

Fig. 10. Time waveforms of the relative deviation of the flow in the penstock and the net head with different initial flows.

As shown in Fig. 10, the initial flow q_0 can regulate the fluctuation range of the flow in the penstock and net head. From Fig. 10(a), the relative deviation of the flow in the penstock for $q_0 = 1.5$ is consistently higher than for $q_0 = 1$ and $q_0 = 0.5$. When $q_0 = 0.5$, the flow in the penstock has the minimum range in Fig. 10(a). From Fig. 10(b), the dynamic characteristics of the net head can be improved with the decrease of the initial flow. For different initial flows, the fluctuations of the flow in the penstock are more violent than that of the net head.

Finally, the simulation results demonstrate that the PI gains contribute significantly to regulating the dynamic characteristics of the PSHP with random power load. In addition, the initial load can also influence the stability of the PSHP during the process.

5. Conclusions

In this paper, the effects of PI gains and initial load on the dynamic characteristics of the PSHP with random power load have been analyzed from the point of view of dynamics.

The simulation results show that the PI gains have different influences on

different system parameters. In generating mode, the PI gains are able to improve the dynamic characteristics of the PSHP with random power load. It is important to note that the decrease of k_i is able to increase the stability of the system, while the decrease of k_p has the opposite effect on the speed of the PSHP. Additionally, the simulation results demonstrate that the dynamic characteristics of the PSHP can be improved with smaller initial load.

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