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Sedimentation of inertia-less prolate spheroids in homogenous isotropic turbulence with application to non-motile phytoplankton

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Phytoplankton are the foundation of aquatic food webs. Through photosynthesis, phytoplankton draw down CO_2 at magnitudes equivalent to forests and other terrestrial plants and convert it to organic material that is then consumed by other planktonic organisms in higher trophic levels. Mechanisms that affect local concentrations and velocities are of primary significance to many encounter-based processes in the plankton including prey-predator interactions, fertilization and aggregate formation. We report results from simulations of sinking phytoplankton, considered as elongated spheroids, in homogenous isotropic turbulence to answer the question of whether trajectories and velocities of sinking phytoplankton are altered by turbulence. We show in particular that settling spheroids with physical characteristics similar to those of diatoms weakly cluster and preferentially sample regions of downwelling flow, corresponding to an increase of the mean settling speed with respect to the mean settling speed in quiescent fluid. We explain how different parameters can affect the settling speed and what underlying mechanisms might be involved. Interestingly, we observe that the increase in the aspect ratio of the prolate spheroids can affect the clustering and the average settling speed of particles by two mechanisms: first is the effect of aspect ratio on the rotation rate of the particles, which saturates faster than the second mechanism of increasing drag anisotropy.

Key words: Phytoplankton, prolate spheroids, tracers, settling particles, aspect ratio, homogenous isotropic turbulence

1. Introduction

The behavior of suspended particles in turbulent flows is of considerable interest to a variety of processes including dispersion of aerosols and collisions of water droplets

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in the atmosphere, dispersions of oil spills treated with dispersants, sediment transport and ecological processes in the plankton (see e.g. Guazzelli & Morris 2011). The latter is perhaps the least familiar to fluid dynamicists but is of great importance because of the key roles plankton play in oceanic food webs, sustaining all the world's commercially important fisheries, and in global biogeochemical cycles, particularly the carbon cycle. Our interest here is in the behavior of diatoms in turbulent flows. Diatoms are one of the largest and most significant groups of photosynthetic planktonic organisms in coastal and high latitude environments. They are unicellular but many species form colonies, often in the form of long chains and filaments as shown in figure 1, making them an attractive model for studies on non-spherical particles in environmental turbulent flows. Diatoms are non-motile but they possess a siliceous cell wall that is denser than seawater (Eppley *et al.* 1967), causing cells to be, generally, negatively buoyant. From an ecological perspective, sinking velocities and trajectories of diatoms in the upper mixed layer of the ocean are of a great interest, because of their effect on encounter-based processes in the plankton (e.g., prey predator interactions, aggregate formation) and because the sedimentation of diatoms (as individuals or in aggregates) contributes to the shunting of CO_2 from the atmosphere into the deep ocean where it gets sequestered for thousands of years.

Sinking rates of diatoms have been largely measured in quiescent water (Smayda 1970) while in the surface layer of the ocean, where diatoms reside, shear stresses applied by wind, breaking waves and thermal instabilities induce turbulence (Gerbi *et al.* 2009). Diatoms are typically smaller or of the same size of the Kolmogorov length scale (Karp-Boss & Jumars 1998; Barton *et al.* 2014), hence our interest is in turbulence at the dissipation scale, which is supposedly independent of the production mechanism. Early observations that diatoms thrive in turbulence (Margalef 1978) and that stirring of cultures keeps cells in suspension lead to the notion that turbulence helps keep phytoplankton suspended and increases their residence time in the sun-lit surface layer of the ocean. Intriguing laboratory observations, however, suggest that turbulence enhances sinking velocities of at least some species of phytoplankton, including diatoms, relative to their still-water velocities (Ruiz *et al.* 2004) but mechanisms remain illusive. Ruiz *et al.* (2004) proposed differential concentration as the mechanisms for the observed altered settling velocities but this mechanism invoked results from systems with particles that are drastically different to diatoms (Wang & Stock 1993; Wang & Maxey 1993). [Differential concentration in these studies is induced by particle inertia, leading to particle concentration in regions of downwardly moving fluid, however, diatoms and other phytoplankton are weakly inertial to follow the same physical mechanism.](#)

Here we use a numerical model to examine whether rotation and orientation of diatoms in a turbulent flow can result in biased trajectories, enhanced sinking and preferential concentrations. While diatom morphologies are complex and may include spines and other projections (see figure 1), Nguyen *et al.* (2011) showed that in a simple shear flow the motion of a diatom with spines or projections could be well predicted from the theory of the motion of spheroids in a simple shear flow, providing that the cell is described by the smallest inscribing spheroid that encompasses both the cell and its spines. In a steady shear flow, a prolate spheroid spends most of its time aligned with the velocity vectors and tumbles with a predictable frequency that is a function of its aspect ratio and the magnitude of the shear rate (Jeffery 1922). Observations on the motion of rigid diatom chains in a Couette flow show that they undergo periodic rotation, as predicted by theory (Jeffery 1922), with a period that increases with increasing the chain aspect ratio (Karp-Boss & Jumars 1998). In unsteady shear and fully developed turbulent flows, the motion of axisymmetric particles becomes more complex but a growing number of

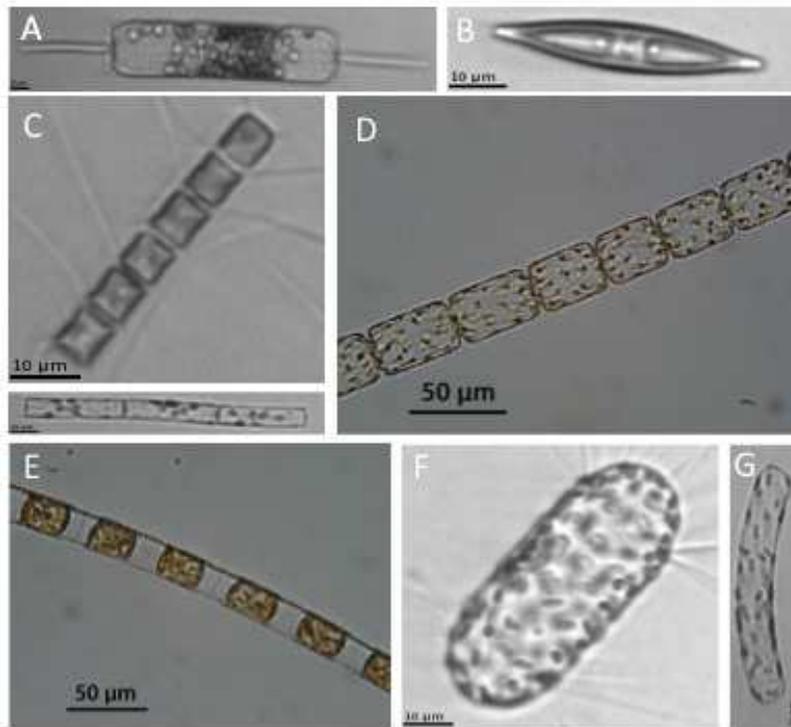


FIGURE 1. A mosaic of images of diatoms taken with a light microscope (*D* & *E*) or an Imaging Flow cytometer (*A*, *B*, *C*, *F* & *G*). *A*. *Ditylum brightwellii* *B*. *Navicula* sp. *C*. *Chaetoceros* sp. (a chain forming diatom), *D*. *Lauderia annulata* (a chain forming diatom), *E*. *Lithodesmium undulatum* (a chain forming diatom), *F*. *Chorethron* sp., and *G*. *Cylindrotheca* sp.

studies have advanced our understanding of the translation, rotation and orientation of dilute suspensions of small spheroids and fibers in turbulence, highlighting the rich dynamics of interactions (see the recent review by Voth & Soldati 2017). Important insights about the motion of neutrally buoyant rigid fibers in turbulence came from a study by Olson & Kerekes (1998). These authors used analytical approximations to derive translational and rotational dispersion coefficients for fibers in an isotropic stochastic flow field and showed a strong dependence of these coefficients on the fiber length. Using direct numerical simulations, Shin & Koch (2005) studied the translational and rotational motions of neutrally buoyant slender fibers in fully developed isotropic turbulence. Particles in their simulations ranged in size from tracer-like particles to fibers that are larger than the Kolmogorov scale. Their results show that fibers that are much smaller than the Kolmogorov length scale act as flow tracers and rotate like material lines. **With increasing length the fiber rotation rate attenuates as it becomes insensitive to the eddies that are smaller than the fiber length.** The assuagement of the rotation rate was shown later to be associated with the tendency of rod-like particle to align more strongly with the vorticity vector than with the principle axis of strain (Pumir & Wilkinson 2011). Experimental measurements of rotation rates along the trajectories of short nylon threads in a turbulent flow are in agreement with model results (Parsa *et al.* 2012). Several studies have followed since, expanding the parameter space of this problem (e.g. Andersson *et al.* 2012; Parsa & Voth 2014; Ni *et al.* 2015; Byron *et al.* 2015). A common observation of these studies is the strong preferential alignment of anisotropic

particles, either with the direction of the mean flow near a wall in turbulent channel flows (Zhang *et al.* 2001; Marchioli *et al.* 2010) or with the local velocity gradient tensor in isotropic turbulence, subsequently affecting rotational and translational motions.

The studies described above considered neutrally buoyant particles. For particles denser than the carrying fluid the presence of gravity adds further complication to the dynamics. The case of slender fibres sedimenting in a quiescent fluid has been the subject of many studies, see the review by Guazzelli & Hinch (2011). Most of these studies investigate the dilute regime, numerically (Mackaplow & Shaqfeh 1998; Butler & Shaqfeh 2002; Gustavsson & Tornberg 2009), whereas both dilute and semi-dilute regimes have been examined experimentally (e.g. Herzhaft *et al.* 1996; Herzhaft & Guazzelli 1999). The results show that in the dilute regime, a suspension loses its homogeneity forming packets that are separated by sparse regions. In this regime the mean sedimentation velocity increases compared to the maximum velocity of an isolated fibre. In the semi-dilute regime, however, hindrance effect reduces mean velocity and the effect is stronger for a suspension of fibers than for a suspension of spheres. In both regimes the fibres are observed to orient in the direction of gravity (Herzhaft & Guazzelli 1999). Fewer studies have examined the problem of anisotropic particles settling in an external flow (i.e. not induced by the motion of the particles). Earlier studies have considered a cellular flow field and showed enhanced sedimentation of spheroids compared to spheres, and that at large aspect ratios tumbling become chaotic (Mallier & Maxey 1991; Shin & Maxey 1997). Siewert *et al.* (2014) used direct numerical simulations to study settling velocities of heavy ellipsoids in decaying isotropic turbulence. They found a preferential orientation with respect to the direction of gravity for prolate and oblate ellipsoids and a higher sedimentation velocity than that calculated from the orientation probabilities. Their study demonstrated that non-spherical, inertial particles experience a preferential sweeping mechanism as was previously demonstrated for spheres (Wang & Maxey 1993; Toschi & Bodenschatz 2009; Gustavsson *et al.* 2014; Bec *et al.* 2014). The effect of turbulence on the settling of spheroids was found to be dependent on the turbulence level and the aspect ratio of the spheroid (see Siewert *et al.* 2014). In that study, all parameters were chosen to match ice particles in turbulent clouds where the inertia of the particles is high. Diatoms and other phytoplankton represent the other extreme, anisotropic particles that are weakly inertial. Here we expand modelling efforts to the parameter space at which phytoplankton operate (see appendix A).

We model diatom chains as prolate spheroids, using analytical and direct numerical simulations to examine if mean settling velocities of inertia-less diatoms are altered by turbulence. We begin by introducing the flow solver and the one-way coupling model used in this study to describe the particle motion in homogenous isotropic turbulence §2. Next, we examine whether turbulence affects sinking velocities and clustering of weakly inertial prolate spheroids and how this may vary as a function of different particle parameters (§3). Alteration of sinking velocities is explained further in this section, considering a simple shear flow. The main conclusions and final remarks are drawn in §4.

2. Governing equations and numerical method

2.1. Fluid phase

The incompressible turbulent velocity field, \mathbf{u} , obeys the Navier-Stokes and continuity equations:

$$\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} = -\nabla p + \frac{1}{Re} \nabla^2 \mathbf{u} + \mathbf{f}, \quad (2.1)$$

$$\nabla \cdot \mathbf{u} = 0. \quad (2.2)$$

Here t denotes the time, p the pressure, Re the Reynolds number and \mathbf{f} the random forcing field necessary to maintain the turbulent velocity in a statistically steady state. The equations are discretized in a cubic domain with periodic conditions at the boundaries. We employ Direct Numerical Simulation (DNS) to solve all the relevant flow scales without any artificial model at the smallest scales. Since we evolve the equations in a three-periodic domain, it is natural to do so in Fourier space with a pseudo-spectral method. In this numerical scheme the nonlinear terms are evaluated in physical space using the classic 2/3 rule to minimize aliasing error. Time integration is performed with a third-order low-storage Runge-Kutta method where the diffusive terms are analytically calculated (note that in Fourier space the Laplacian operator is proportional to the square of the modulus of the wave vector k^2) while an Adam-Bashforth-like approximation is employed for the nonlinear terms (Rogallo 1981). The stochastic forcing is evaluated in Fourier space and acts isotropically on the first shell of wave vectors. The forcing amplitude is constant in time and the field is delta-correlated in time and uniformly distributed in phase and directions (Vincent & Meneguzzi 1994). We employed a resolution of 128^3 grid points with a Taylor Reynolds number $Re_\lambda = 100$ and 64^3 grid points with a Taylor Reynolds number $Re_\lambda = 60$. The turbulence is characterized by the Taylor Reynolds number $Re_\lambda \equiv u'\lambda/\nu$, where u' is the root-mean-square of velocity fluctuations, ν is the kinematic viscosity and λ is the Taylor microscale, $\lambda \equiv \sqrt{\epsilon/15\nu u'^2}$, with ϵ the kinetic energy dissipation rate. The resolution was chosen so that the velocity gradients are well resolved since they drive the the equation of motion of the particles. Particle statistics are computed from independent samples separated by 1.6 turbulent Kolmogorov time scales, $\tau_f \equiv \sqrt{\nu/\epsilon}$, corresponding to about 300 configurations per particle. The numerical code has been already employed to study gyrotactic micro-organisms in homogeneous turbulence (Zhan *et al.* 2014) and rain droplet evaporation in clouds (Sardina *et al.* 2015).

2.2. Solution of the particle motion

The prolate spheroids studied here are small compared to the Kolmogorov length scale of the turbulence and have densities close to that of the carrier fluid. The translational relaxation time, τ_p , for prolate spheroids, assuming an isotropic particle orientation distribution is given by

$$\tau_p = \frac{2\rho_p a^2}{9\mu_f} \frac{\mathcal{AR} \ln(\mathcal{AR} + \sqrt{\mathcal{AR}^2 - 1})}{\sqrt{\mathcal{AR}^2 - 1}}, \quad (2.3)$$

with a the semi-minor axis of the prolate spheroid and \mathcal{AR} the aspect ratio (the ratio of polar over equatorial radii of the spheroid) (Shapiro & Goldenberg 1993). The time scale for the particles studied here is around three to four orders of magnitude smaller than the relaxation time of the turbulence flow around the particles. Furthermore, rotational relaxation times, concerning spinning and tumbling motions, are reported in the literature to be typically shorter than the translational relaxation time (Zhao *et al.* 2015; Marchioli *et al.* 2016). With these operating parameters a tracer model for the particle motion is a suitable assumption (Shin & Koch 2005; Voth & Soldati 2017) and we, therefore, assume that the cells behave like passive tracers with a correction given by their Stokes settling velocity.

The particle translational motion obeys

$$\frac{d\mathbf{x}}{dt} = \mathbf{u}|_{\mathbf{x}} + \mathbf{v}_s(\mathbf{p}), \quad (2.4)$$

$$\mathbf{v}_s(\mathbf{p}) = v_s^{min} \hat{\mathbf{e}}_g + (v_s^{max} - v_s^{min}) (\hat{\mathbf{e}}_g \cdot \mathbf{p}) \mathbf{p}, \quad (2.5)$$

\mathcal{AR}	1	2	3	5	10	15	20
v_s^{max}	3.03	3.17	3.11	2.90	2.46	2.18	1.97
v_s^{min}	3.03	2.77	2.53	2.18	1.71	1.46	1.29
v_s^{max}/v_s^{min}	1.00	1.14	1.23	1.33	1.44	1.49	1.53
v_s^{iso}	3.03	2.90	2.72	2.42	1.96	1.70	1.52

TABLE 1. Maximum, minimum and average of settling velocities in quiescent flow, scaled with the Kolmogorov velocity for the investigated cases versus different aspect ratios. $\rho_p/\rho_f = 1.05$ and $D_{eq} = \eta/6$.

with \mathbf{x} denoting spheroid position, $\mathbf{u}|_{\mathbf{x}}$ the fluid velocity at spheroid position, \mathbf{p} the spheroid orientation vector, \mathbf{v}_s the Stokes settling velocity and $\hat{\mathbf{e}}_g$ a unit vector in the direction of gravity. v_s^{min} and v_s^{max} are the minimum and maximum settling speeds in quiescent flow, corresponding to the particles falling with their major axis perpendicular or parallel to the gravity direction. These velocities can be written as

$$v_s^{max} = \frac{(\rho_p - \rho_f) gl^2}{\mu_f} \gamma_0(\mathcal{AR}) \quad ; \quad v_s^{min} = \frac{(\rho_p - \rho_f) gl^2}{\mu_f} \gamma_1(\mathcal{AR}) \quad , \quad (2.6)$$

with g the gravitational acceleration, l the length of the spheroid's major axis, μ_f the dynamic viscosity of the fluid, ρ_p and ρ_f the densities of the particle and the fluid. γ_0 and γ_1 are functions of the aspect ratio \mathcal{AR} , whose full expression can be found in Dahlkild (2011) among others.

The spheroid rotation follows the inertialess Jeffery equation

$$\frac{d\mathbf{p}}{dt} = \frac{1}{2} \boldsymbol{\omega}|_{\mathbf{x}} \times \mathbf{p} + \alpha [\mathbf{I} - \mathbf{p}\mathbf{p}] \cdot \mathbf{E}|_{\mathbf{x}} \cdot \mathbf{p} \quad , \quad (2.7)$$

with $\boldsymbol{\omega}|_{\mathbf{x}}$ the flow vorticity at the particle's position, \mathbf{I} the second order identity tensor, $\mathbf{E}|_{\mathbf{x}}$ the symmetric part of the velocity deformation tensor and α a function of the spheroid aspect ratio \mathcal{AR} , defined as

$$\alpha = \frac{\mathcal{AR}^2 - 1}{\mathcal{AR}^2 + 1} \quad . \quad (2.8)$$

To solve the equations above, the flow velocity, vorticity and velocity gradients at the particle positions are calculated with a second-order interpolation scheme and a high enough resolution to capture the flow velocity gradients. The same Runge-Kutta scheme used for the carrier phase is employed to perform the time integration of equations (2.4) and (2.7) with a small enough time step ($\approx 0.001\tau_f$) to capture the time evolution of particle orientations via a formulation based on quaternions. We evolve a total of 200000 spheroids for each simulation.

3. Results

We first investigate the settling of prolate spheroidal particles of constant volume, focusing on the effect of the particle aspect ratio. The parameters used are $Re_\lambda = 100$, $\frac{\rho_p}{\rho_f} = 1.05$ and $D_{eq} = \eta/6$ where D_{eq} is the diameter of a sphere having the same volume as the prolate spheroid and η is the Kolmogorov length scale. Fixing the volume, the settling speed varies with the aspect ratio. It should be noted that for the higher aspect ratio

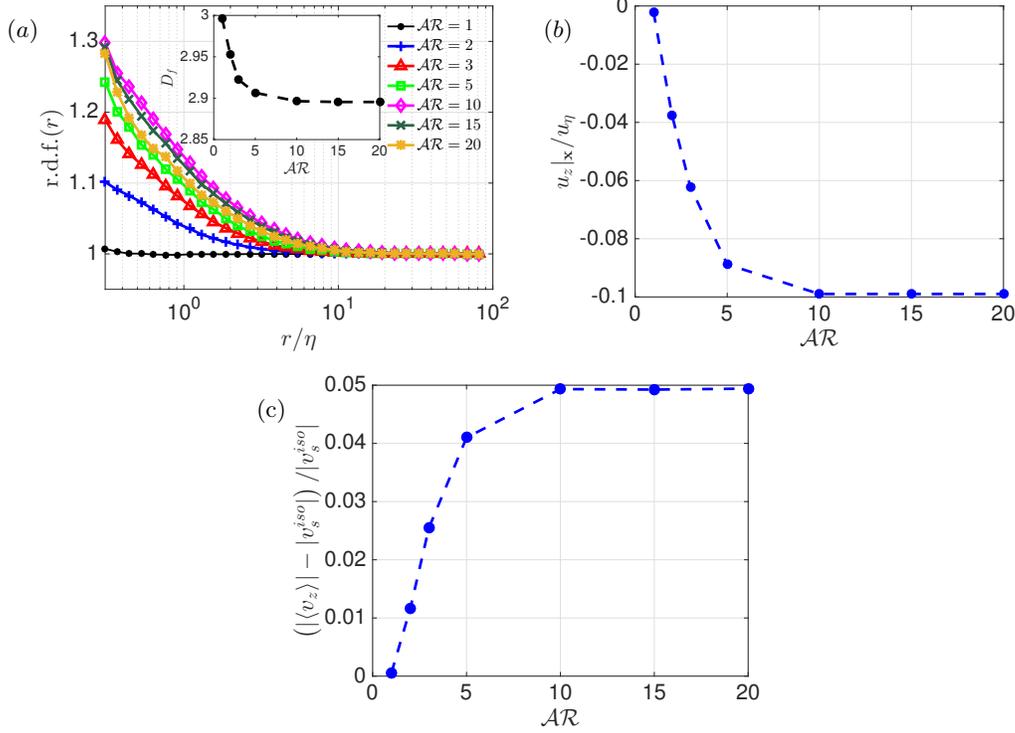


FIGURE 2. (a) Radial distribution function of particle positions; the inset in this panel reports the fractal dimension of the clustering, estimated by fitting r.d.f. with a power-law in the range $r/\eta = [0.2 : 2]$, (b) average of fluid vertical velocity at the particle position and (c) increase in the settling velocity (difference in the settling rate with respect to the quiescent settling average v_s^{iso} , normalized by v_s^{iso}).

cases examined here ($\mathcal{AR} \geq 15$), the larger diameter of the spheroid exceeds Kolmogorov length scale η (≈ 1.24 for $\mathcal{AR} = 24$). This does not violate our assumption of a tracer particle since rods act as tracers when their length is less than 5η and deviations from the tracer behavior are very small until about 15η (Parsa & Voth 2014). For the simulations presented here, the average settling speed of a uniformly distributed suspension, v_s^{iso} , varies in the range $1.5 - 3u_\eta$. Table 1 shows the settling velocities for the investigated cases. The reported values are all normalized by the Kolmogorov velocity. Note that the average settling speed v_s^{iso} for spheroids in a quiescent flow is calculated as:

$$v_s^{iso} = \frac{(v_s^{max} + 2v_s^{min})}{3}, \quad (3.1)$$

based on the assumption that the orientation of spheroids (cosine of the angle between spheroid's symmetric axis and the gravity direction) is uniformly distributed.

The results of the simulations are shown in figure 2. The main observation is that within the parameter space relevant to diatom chains, settling spheroids weakly cluster (figure 2 panel a) and preferentially sample regions of downwelling flow, leading to downward velocity biases of up to 10% of the Kolmogorov velocity u_η (figure 2 panel b). This corresponds to an increase of the mean settling speed of about 5% compared to the mean settling speed in quiescent fluid (panel c in figure 2). These effects increase with the aspect ratio, \mathcal{AR} , and saturate for $\mathcal{AR} \geq 10$. In studies regarding unstable settling

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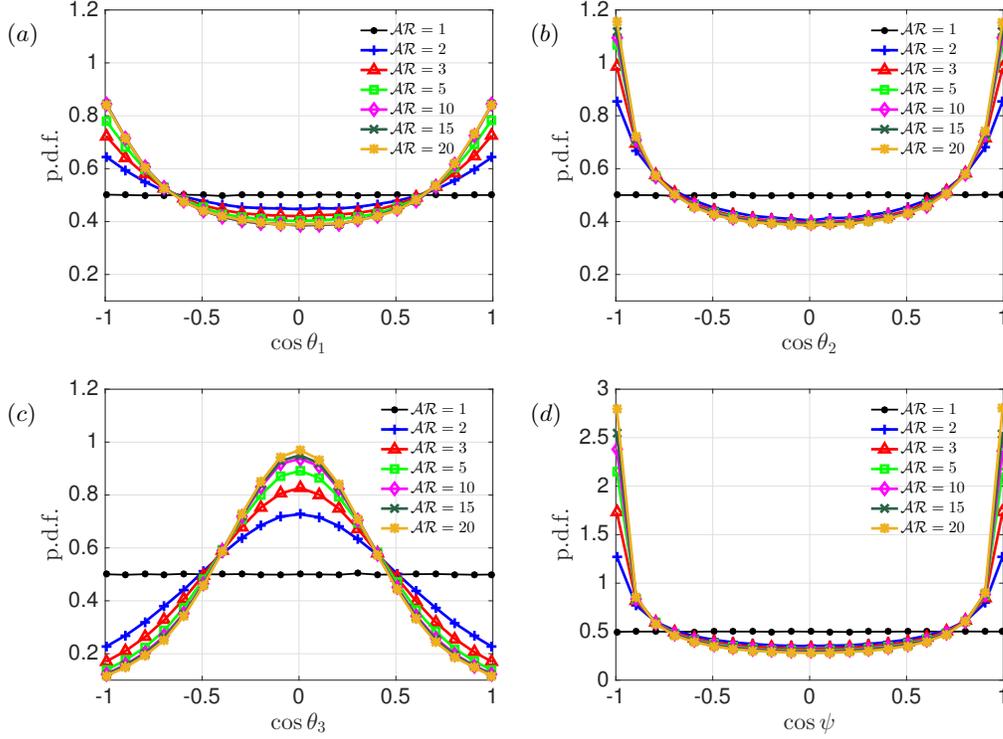
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FIGURE 3. p.d.f of orientation of particles with different aspect ratios with respect to the three eigenvectors of the deformation tensor (a – c) and (d) the local vorticity vector.

suspensions (Koch & Shaqfeh 1989; Herzhaft *et al.* 1996; Mackaplow & Shaqfeh 1998; Herzhaft & Guazzelli 1999), the enhanced sedimentation velocity is explained by two mechanisms. First, the preferential concentration in downwelling flow (as also observed in this study) and, second, the preferred orientation parallel to the gravity direction that causes fibres to settle faster. In these studies, the velocity disturbances due to the settling particles produce vertical shearing motion, which causes the preferential orientation. In the present study, however, the turbulent flow remains isotropic due to the one way coupling assumption and the second effect cannot be observed. Therefore, the increase in the settling speed can be only attributed to preferential sampling of regions with downwelling flow.

To quantify patchiness (clustering) in fully three-dimensional isotropic turbulent flows, we use the radial pair distribution function (RDF), sometimes also called the correlation function. The RDF measures the probability of finding a particle pair separated by a given radial distance, normalized by the value expected from a uniform distribution. This is defined as

$$g(r) = \frac{1}{4\pi r^2} \frac{dN_r}{dr} \frac{1}{n_0}, \quad (3.2)$$

where, $n_0 = 0.5N_p(N_p - 1)/V_0$ is the density of pairs in the whole volume V_0 . N_p is the total number of particles in the domain and N_r is the number of pairs at distance r . The small volume fraction, used here, removes the exclusion effects, and thus an RDF for a random distribution results in a flat value of 1. The radial distribution function (RDF) is reported in figure 2(a). In the inset of the same figure, we report the scaling exponent

of RDF at small separations, also often used as an indicator of patchiness (Durham *et al.* 2013). This exponent denotes the fractal dimension of the set where particles are found. Patchiness is seen to increase with the particle aspect ratio and saturate at the largest values considered. However, a fractal dimension 2.9 shows weak clustering. Increasing the aspect ratio, while keeping the volume and the density ratio constant, changes the average settling speed, v_s^{iso} , and the ratio between maximum and minimum settling speed, v_s^{max}/v_s^{min} , simultaneously. Therefore the saturation in the patchiness and the preferential sampling of regions of downwelling flow can be explained by the change in v_s^{iso} and v_s^{max}/v_s^{min} . A detailed study of each effect is given in the next subsection.

In figure 3, we study the relation between particle orientation and the underlying flow field when varying the particle shape. In figure 3(a), (b) and (c), we show the orientation of the particle with respect to the three eigendirections of the strain tensor, defined such that $\lambda_1 > \lambda_2 > \lambda_3$ so that the first eigendirection is extensional and the third eigendirection is compressional. The angles between the eigendirections and the spheroid orientation are denoted as θ_1 , θ_2 and θ_3 . In figure 3d, we show ψ , the angle between the orientation and the local vorticity vector. While spherical particles, $\mathcal{AR} = 1$, are isotropic in nature, elongated spheroids tend to align with the local flow strain, more frequently with the second eigendirection, and with the local flow vorticity. Indeed, the pdfs peak when prolate particles are parallel to the eigendirections associated with λ_2 and λ_1 . An increasing probability of parallel alignment with the first two eigendirections of the strain is seen with increased aspect ratio. The spheroid is most likely to be normal to the third eigendirection of the strain as shown in figure 3(c). The strongest tendency to align with the local vorticity vector is consistent with previous observations for neutrally buoyant spheroids (Chevillard & Meneveau 2013; Ni *et al.* 2015). The alignment with the vorticity vector increases with the aspect ratio \mathcal{AR} .

3.1. Numerical experiments

The parameters that define the behaviour of the particles in this regime are the ratio of the amplitude of the sedimenting velocity and the Kolmogorov velocity scale of the turbulence, v_s^{iso}/u_η and the aspect ratio \mathcal{AR} . However increasing the aspect ratio, while maintaining the mass constant, simultaneously changes the the average settling speed, v_s^{iso} , and the ratio between maximum and minimum settling speed, v_s^{max}/v_s^{min} . In other words, changing the aspect ratio can affect the results by affecting the rotational motion and also by changing sedimentation trajectories. To disentangle these different effects, we perform a series of numerical experiments to investigate separately the effect of the aspect ratio, \mathcal{AR} , the amplitude of the sedimenting velocity v_s^{iso} and the ratio between the maximum (spheroid aligned with the gravity direction) and minimum (normal to gravity) settling speed v_s^{max}/v_s^{min} . In each series of simulations we fix all the parameters except for one to focus on a single parameter effect. While varying only one parameter can result in unrealistic conditions occasionally, it sheds light on the isolated effect of the parameter of interest on particles' collective behavior. Since phytoplankton exhibits a striking diversity of cell shapes and characteristics, their kinematics can be influenced in important ways, i.e. their characteristics might change their kinematics in a way that these effects get disentangled from each other. For example, an organism that resists falling in a certain direction can increase the drag anisotropy independently of the aspect ratio.

3.1.1. Effect of sedimenting velocity magnitude

First we examine how particle clustering varies with the amplitude of the settling speed. To this end, we keep the aspect ratio $\mathcal{AR} = 5$, corresponding to a ratio between

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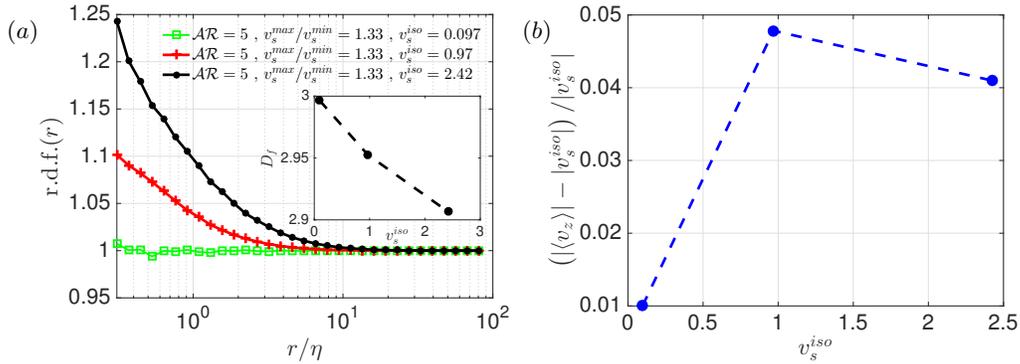


FIGURE 4. (a) Radial distribution function of particle positions and (b) increase in the settling velocity for $\mathcal{AR} = 5$ and the indicated values of v_s^{iso} . v_s^{iso} is normalized by the Kolmogorov velocity u_η .

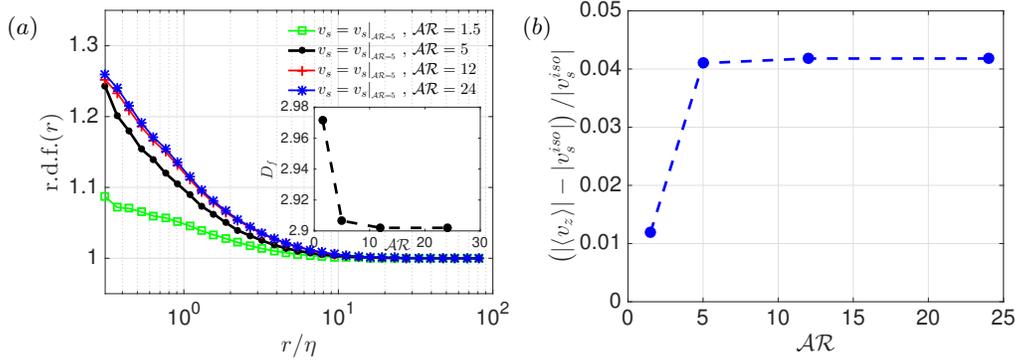


FIGURE 5. (a) Radial distribution function of particle positions and (b) increase in the settling velocity for the different aspect ratios indicated, while keeping the same maximum and minimum settling speed.

maximum and minimum settling speed, $v_s^{max}/v_s^{min} = 1.33$, and change v_s^{iso} from 0.1 to about 2.5 Kolmogorov velocities (this may correspond to a change in the particle size with respect to the turbulence Kolmogorov scale or a change in particle density). Results in figure 4(a) show that patchiness increases with the average settling speed, as measured by the RDF or by the fractal dimension (inset in figure 4a). The increased clustering, however, does not correspond to an increase of the relative average settling speed when v_s^{iso} is greater than the Kolmogorov velocity.

3.1.2. Effect of aspect ratio

To elucidate the role of the particle rotation rate on the observed preferential sampling, we vary \mathcal{AR} , while artificially keeping the settling speed fixed, both the components parallel and normal to gravity, at the values corresponding to $AR = 5$ in table 1. The solution of Jeffery's equation (2.7) reveals that the time spent aligned with the local shear increases with increasing aspect ratio. The results, displayed in figure 5, show that the RDF and the relative increase of sedimenting velocity saturate for $\mathcal{AR} \geq 5$. Interestingly, rotation rates of oblate and prolate particles are seen to saturate for $\mathcal{AR} > 5$ and for $\mathcal{AR} < 1/5$ in the study of Byron *et al.* (2015). We have also observed, not shown here, that the alignment with the local vorticity increases with the aspect ratio and saturates

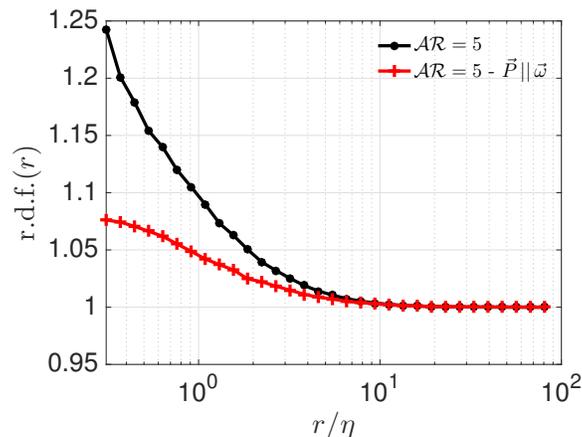


FIGURE 6. Radial distribution function of particle positions for particles with $\mathcal{AR} = 5$ and particles with the same sedimenting velocity but with their orientation forced to be always aligned with the local vorticity vector.

when $\mathcal{AR} \geq 5$ unlike the cases in figure 3, where it continues to increase; this suggests that the alignment with vorticity is influenced by the difference between settling parallel and normal to gravity, which is fixed here.

3.1.3. Effect of local alignment

As the alignment with the vorticity vector increases with the aspect ratio \mathcal{AR} , see figure 3(d), it is interesting to further explore if preferential alignment contributes to biased sampling and clustering of particles. To show the isolated effect of particle alignment with the local vorticity vector we performed a simulation forcing the elongated spheroid to be always aligned with the local vorticity (figure 6): we observe that clustering decreases in comparison to the case in which the particle was free to rotate. We therefore conclude that clustering cannot be explained by the alignment with the local flow vorticity alone.

3.1.4. Effect of drag anisotropy

One important feature of non-spherical particles in inertialess flows is their drag anisotropy, which can also be exploited by micro-organisms for locomotion. In the case of settling prolate spheroids, this anisotropy is seen in the oblique settling of inclined particles and in the difference between settling speed when oriented parallel or normal to gravity. For the results presented so far we followed the analytical expression for the settling speed derived for prolate spheroids. Shapes in nature are, however, more complicated. Flexibility and non-uniformly distributed mass are likely to cause deviation from the idealized case. To understand more the relevance of drag anisotropy we perform simulations of spheroids with aspect ratio $\mathcal{AR} = 5$ and fixed average settling speed $v_s^{iso} = 2.42$, while varying the ratio between settling speed in the direction normal and parallel to gravity, v_s^{max}/v_s^{min} . As seen in figure 7(a) clustering increases significantly with drag anisotropy, or v_s^{max}/v_s^{min} . More interestingly, the relative settling speed increases by up to about 20% when $v_s^{max}/v_s^{min} = 3.3$. The value 3.3 is chosen to artificially emphasize the drag anisotropy effect; note that the ratio between maximum and minimum settling speed of spheroidal particles increases with the aspect ratio and saturates at about 1.75 (figure 8).

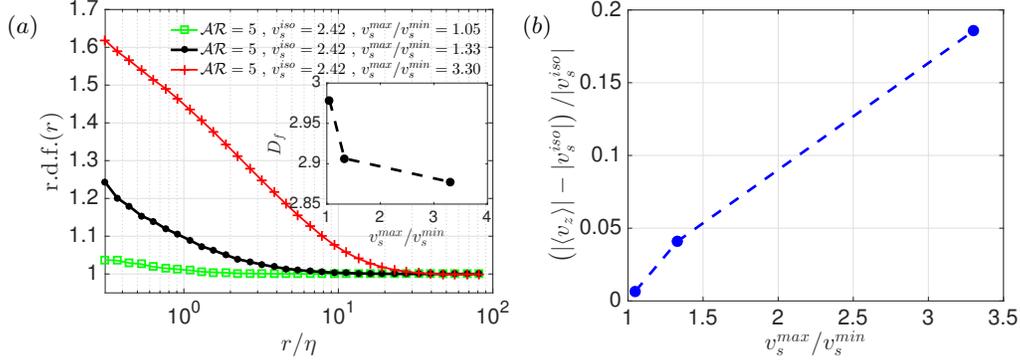


FIGURE 7. (a) Radial distribution function of particle positions and (b) increase in the settling velocity for settling spheroids with aspect ratio $\mathcal{AR} = 5$, fixed average settling speed $v_s^{iso} = 2.42$ and different ratios between settling speed in the direction normal and parallel to gravity, v_s^{max}/v_s^{min} , as indicated in the legend. v_s^{iso} is normalized by the Kolmogorov velocity u_η .

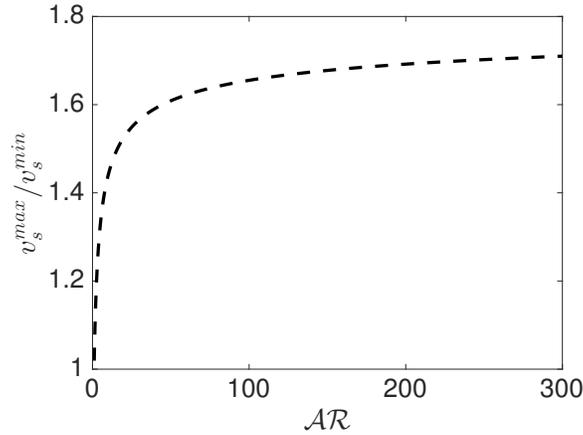


FIGURE 8. v_s^{max}/v_s^{min} versus \mathcal{AR} for prolate particles, see e.g. analytical expressions reported in Dahkild (2011).

3.2. Mechanism for increased settling speed

To understand why ellipsoidal particles preferentially locate in regions of downwelling flow and thus have an enhanced settling speed, we consider a vertical linear shear, $\mathbf{u} = -\gamma x \hat{\mathbf{e}}_y$ with motion constrained to the $x-z$ plane. We define θ to be the angle the particle symmetry axis makes with the vertical, so that in $x-z$ co-ordinates the orientation vector is given by $\mathbf{p} = (\sin \theta, \cos \theta)^T$.

From Jeffery's equation (2.7) the time evolution of particle orientation is given by

$$\dot{\theta} = \frac{\gamma}{2} (-1 + \alpha \cos 2\theta). \quad (3.3)$$

Note that the particle rotates most slowly when $\theta = 0$ or π , and thus spends more time in these states, i.e. aligned with the local shear. From equation (2.5), the vertical velocity of a particle is given by

$$v_z = \gamma x - v_s^{min} - (v_s^{max} - v_s^{min}) \cos^2 \theta.$$

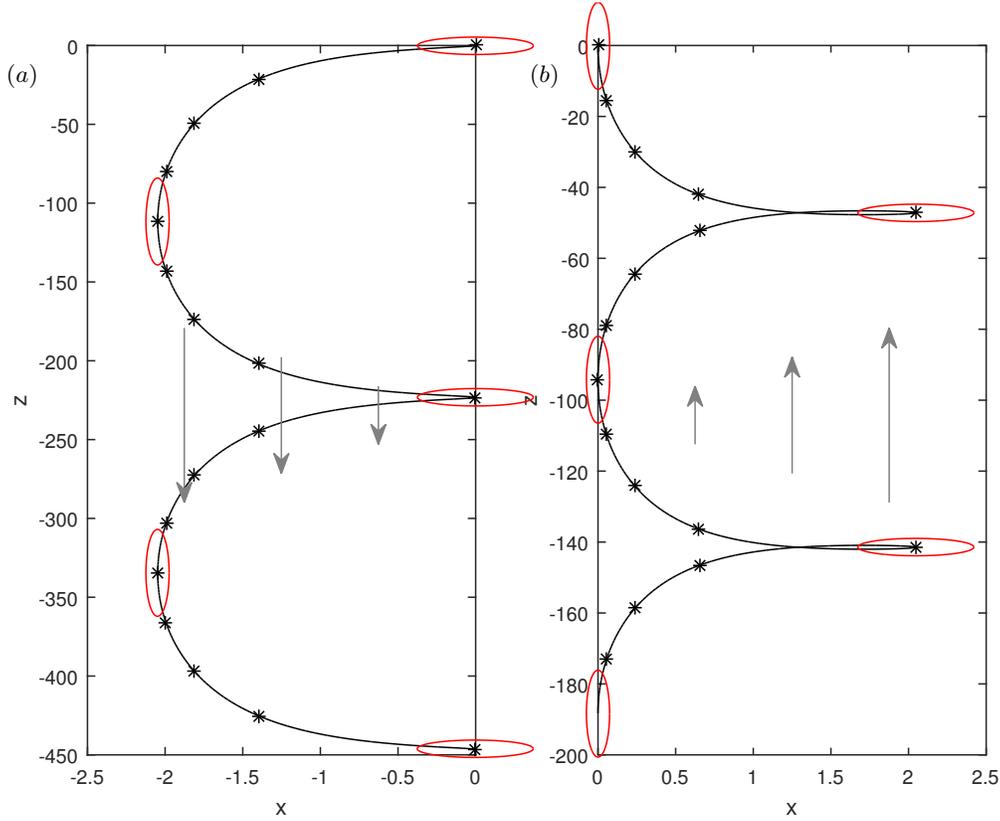


FIGURE 9. Trajectory of single particle in vertical laminar shear over a Jeffery orbit. Particle initially at the origin with orientation (a) $\theta = \pi/2$, (b) $\theta = 0$. Stars indicate position at equally spaced time intervals, red ellipses indicate particle orientation. Grey arrows indicate flow velocity $\mathbf{u} = -\gamma x \hat{\mathbf{e}}_g$.

The time-averaged vertical velocity over a Jeffery orbit (of duration $T = 4\pi/\gamma\sqrt{1-\alpha^2}$) is given by

$$\begin{aligned} \bar{v}_z &= \frac{1}{T} \int_0^T (\gamma x - v_s^{min} - (v_s^{max} - v_s^{min}) \cos^2 \theta) dt \\ &= \gamma \bar{x} - v_s^{min} - \frac{(v_s^{max} - v_s^{min}) \sqrt{1-\alpha^2}}{2\pi} \int_0^{2\pi} \frac{\cos^2 \theta}{-1 + \alpha \cos 2\theta} d\theta, \end{aligned}$$

where \bar{x} is the time-averaged horizontal position. The effect of the shear strength, γ , only appears through the term $\gamma \bar{x}$, and so the effect of the shear on the total vertical velocity of particles can be determined if we know the time-averaged horizontal position. In particular, the only way cells are predicted to exhibit enhanced settling is if they spend more time in downwelling regions.

To demonstrate how the time-averaged horizontal position is biased towards downwelling regions, yielding enhanced settling, we numerically compute particle trajectories for a complete Jeffery orbit for an example set of parameters taken from table 1: $\gamma = 1$, $\mathcal{AR} = 20$ ($\alpha = 0.995$), $v_s^{min} = 1.29$ and $v_s^{max} = 1.97$ (see figure 9). Particles are initially located at the origin, and the initial orientation is taken as $\theta = 0$ or $\theta = \pi/2$. Particles initially horizontal ($\theta = \pi/2$, figure 9a) have a negative horizontal (parallel to

the direction of the flow) component due to shear-induced lift, causing them to translate into downwelling flow. As the particle rotates, it reaches a minimum horizontal position at the point when $\theta = 0$ and then reverses its horizontal component of motion back towards $x = 0$ which is attained when $\theta = 3\pi/2$. The particle has a slowest rotation rate when $\theta = 0$ or π corresponding to the minimum horizontal position, and thus the time-averaged horizontal position is less than the midpoint of the horizontal limits of the trajectory. This bias represents a tendency to cluster in downwelling flow. Particles initially vertical ($\theta = 0$, figure 9b) sediment with a positive horizontal component into upwelling flow. As the particle rotates, it reaches a maximum horizontal position at the point when $\theta = 3\pi/2$ and then reverses its horizontal component of motion back towards $x = 0$ which is attained when $\theta = \pi$. Again, the particle has a slowest rotation rate at the minimum horizontal position (horizontal distance from origin), and thus the time-averaged horizontal position is less than the midpoint of the horizontal limits of the trajectory (horizontal distance from origin is larger). This simple example shows how shear, rotation, lift, and drag-anisotropy couple to bias particle trajectories towards downward flow. These simpler model shows that drag anisotropy can increase the bias towards regions of negative fluid velocity and therefore explains the sensitivity of the results to the ratio between maximum and minimum sedimentation velocity v_s^{max}/v_s^{min} . (see 3.1.4).

Note finally that this mechanism for preferential sampling of downwelling flows is similar to the one reported by Koch & Shaqfeh (1989) when studying the instability of a dispersion of sedimenting spheroids. In their study, however, the vertical shearing motion was induced by the velocity disturbance of a neighbouring spheroid while we assume here a constant background shear.

4. Final remarks

We report results from simulations of elongated, rigid particles (prolate spheroids) with different aspect ratios sinking in homogenous, isotropic turbulence. The parameters used in this study represent marine or freshwater diatoms that are characterized by very small relaxation times compared to that of the fluid but with settling velocities on the order of Kolmogorov velocities characteristics of the mixed layer in the ocean. Given the small size of diatoms relative to the Kolmogorov length-scale and their short relaxation time, cells are assumed to behave like passive tracers with a correction given by their Stokes settling velocity. We show that turbulence does increase the settling velocities of inertia-less elongated particles, compared to their Stokes settling velocities, and that the effect increases as the aspect ratio of the particle increases, but saturates at $\mathcal{AR} \geq 10$. The magnitude of this effect, however, is small ($\sim 5\%$, figure 2c). It should be noted that despite the enhanced mean settling velocity for diatoms reported in this study, there could be dispersion of particles in turbulent flow that increase the residence time of some individuals.

Further, we study homogenous isotropic turbulence at the dissipation scale, and thus neglect large scale turbulence that might play a role in suspending diatoms. Indeed the question ‘‘How local enhancement is related to residence time in the mixed layer of the ocean?’’ is still unanswered and might be very well related to the large scale turbulence that is not captured in the current model. In our model, turbulence dissipation rate, ϵ , was set to $10^{-6}m^2s^{-3}$. This choice is within the range observed in the ocean’s surface boundary layer in a coastal environment (Gerbi *et al.* 2009). For this turbulence level, settling is slightly enhanced. Ruiz *et al.* (2004) used a Couette device to generate turbulence and showed that sinking speeds of different species of phytoplankton increased

significantly (by an order of magnitude for some species) as ϵ increased from $\epsilon < 10^{-6}m^2s^{-3}$ to $\epsilon > 10^{-4}m^2s^{-3}$. They also showed that downward velocities increased as the ratio between the size of the cell (described as equivalent spherical diameter in their study) and the Kolmogorov length-scale increased (Ruiz *et al.* 2004).

Here we show that non-random distributions can arise within the parameter space relevant to diatoms, with weak clustering occurring only for non-spherical cells. Preferential sampling of downwelling flow is due to the interactions between shear, particle rotation, drag, and lift. Elongated spheroids tend to align with the local flow strain (more frequently with the second eigen direction) and with the local flow vorticity, in agreement with previous studies on neutrally buoyant spheroids in homogenous isotropic turbulence (e.g., Ni *et al.* (2015); Voth & Soldati (2017) and references therein). By considering the simple case of one particle sedimenting in linear shear flow we demonstrate that the time-averaged horizontal position of a particle in the flow (over a complete Jeffery orbit) is biased towards downwelling regions. Spheroids with higher average Stokes settling speeds (v_s^{iso}) show greater tendency to cluster (see figure 4a). However, when v_s^{iso} is greater than the Kolmogorov velocity, the increase in clustering does not correspond to an increase in relative average settling speed. We also show that clustering increases significantly with drag anisotropy (i.e., the ratio v_s^{max}/v_s^{min}) in a way that does not appear to saturate. Drag anisotropy increases with increasing \mathcal{AR} and forces particles to sample regions of downwelling flow to a further extent, even when the isolated effect of aspect ratio on the rotational motion is saturated.

Mechanisms that affect sinking and dispersion of phytoplankton hold significant implications to carbon and energy fluxes in aquatic systems. Underlying distributions of phytoplankton at the micro-scale are not well understood as we still lack the tools to measure them in the field. Few available observations suggest that at scales of centimeters, the seascape is more heterogeneous than previously thought (Malkiel *et al.* 1999; Seuront *et al.* 2001; Mitchell *et al.* 2008) but mechanisms remain poorly understood. This study provides insights into one mechanism by which weak clustering of chains and elongated cells of diatoms can occur at the *mm* – *cm* scale. A typical fractal dimension of 2.8 – 2.9 shows a weak clustering and it might be that other mechanisms exist behind the clustering that our model cannot capture.

Cell shape is an important morphological trait affecting many aspects in the ecology of phytoplankton (Smayda 1970; Lewis 1976; Sournia 1982; Reynolds 1989; Reynolds & Irish 1997; Karp-Boss & Boss 2016) and results from our numerical model further highlight the complex interactions of cell shape with ambient flows. Interestingly, the observed increase in settling speeds does not increase indefinitely, and saturates for $\mathcal{AR} > 10$. Increasing the aspect ratio, while keeping the particle volume and density ratio constant, varies other characteristics of the particle simultaneously. For example, the mean settling speed in quiescent flow decreases as the ratio between maximum (when particle is oriented parallel to the gravity direction) and minimum (when particle is oriented normal to the gravity direction) settling speed increases. We have therefore performed a series of numerical experiments to isolate the effect of the aspect ratio \mathcal{AR} , the magnitude of settling velocity v_s^{iso} and the ratio between the maximum and minimum settling speed v_s^{max}/v_s^{min} in quiescent flow. When v_s^{iso} and v_s^{max}/v_s^{min} are held constant, the increase in clustering and settling speed begins to saturates at $\mathcal{AR} = 5$. This indicates that the relative enhancement that we observe for ellipsoids with aspect ratios larger than 5 is due to an increase in the ratio between the maximum and minimum settling speed (v_s^{max}/v_s^{min}) that is associated with a change in particle shape (\mathcal{AR} at constant volume). Interestingly, an analysis of typical aspect ratios among phytoplankton shows a peak in distribution at $\mathcal{AR} \sim 5$ (Clavano *et al.* 2007; Karp-Boss & Boss 2016), but this may be a

coincidence because in nature multiple processes (grazing, diffusion, mechanical breakage by shear) act simultaneously as selective pressures on shape and size in phytoplankton (Karp-Boss & Boss 2016).

The model presented here is an idealized case of turbulence and phytoplankton in the ocean. Direct numerical simulations are computationally expensive and cannot be used to capture the full range of scales characteristics of oceanic turbulence and are limited to low Reynolds numbers. We consider homogeneous isotropic turbulence but in the ocean most turbulent mixing occurs near boundaries and is subjected to stratification and vertical shear. It was found, however, that in stratified regions of the ocean, isotropic motions do exist over some range of scale bounded at the lower end by the Kolmogorov length scale, providing that the non-dimensional isotropy parameter $I = \epsilon/\nu N^2$ exceed ~ 200 , where ϵ is the local mean kinetic energy dissipation, ν the kinematic viscosity and N the local mean value of the buoyancy frequency (Thorpe 2007).

Modelling phytoplankton as rigid prolate spheroids with an even distribution of mass is another simplification of the model. Diatoms exhibit complex morphologies (see figure 1) and often bear spines and other cell projections that can alter dynamics in the flow. Another attribute of chain forming diatoms that is dynamically important is flexural stiffness, as it spans 4 orders of magnitudes between different species (Young 2011). Variations in rotation rates between rigid and flexible particles were observed in a laboratory setting (Karp-Boss & Jumars 1998) and it is likely that rigid and flexible chains will also exhibit different dynamics in turbulence, a subject that requires more investigations in the future.

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Appendix A. Parameter space for phytoplankton

Dissipation rates of turbulent kinetic energy ϵ in the ocean vary greatly in space and time. In the open ocean, typical values range from 10^{-10} to $10^{-7} m^2 s^{-3}$, while coastal regions, especially those influenced by tidal fronts, experience higher dissipation rates, on the order of 10^{-7} to $10^{-4} m^2 s^{-3}$ (Smyth & Moum 2000; Barton *et al.* 2014). Within the water column, turbulence kinetic energy dissipation rate are higher at the surface and decrease with depth (Smyth & Moum 2000). Given the kinematic viscosity of seawater $\nu \sim 10^{-6} m^2 s^{-1}$, characteristic Kolmogorov length scale η in the ocean ranges from $\sim 300 \mu m$ to a few mm . Generally speaking, diatoms are smaller than characteristic Kolmogorov length scales in the ocean, and range in size from a few μm for small solitary cells to 100s of μm in length for chain forming species (Karp-Boss & Jumars 1998). This size ratio may become order 1 for very long chains in strong turbulence but this would represent an extreme case. Sinking velocities of diatoms have been measured in quiescent water by measuring the temporal change in concentration of diatoms at the top and

Parameter	Values
Kinetic energy dissipation rate (ϵ)	$10^{-10} - 10^{-4} m^2 s^{-3}$
Taylor Reynolds number (Re_λ)	50 – 200
Sinking velocity of diatoms (v_s^{iso})	$2 \mu m s^{-1} - 1 mm s^{-1}$
Velocity ratio (v_s^{iso}/u_η)	0.02 - 11
Size ratio (L/η)	0.003 - 2
Density ratio (ρ_p/ρ_f)	1 - 1.3
Relaxation time of a cell (τ_p)	$\sim 10^{-4} s$
Relaxation time of fluid (τ_f)	$\sim 1 s$
Stokes number (τ_p/τ_f)	$\sim 10^{-4}$

TABLE 2. A summary of the parameter values relevant to marine diatoms. The value of ϵ is considered $10^{-6} m^2 s^{-3}$ for calculating τ_f and Re_λ .

bottom of a water column with a known height and calculating average (community) settling velocities. Using this approach, settling velocities (v_s^{iso}) were found to range between $2 \mu m s^{-1}$ to $\sim 1 mm s^{-1}$ (reviewed in Smayda 1970).

Characteristic velocities at dissipation scale in the ocean ($u_\eta = (\nu\epsilon)^{1/4}$) are in the order of 0.01 - 0.1 $mm s^{-1}$, resulting in velocity ratio $v_s^{iso}/u_\eta \approx 1 - 4$ (assuming maximum v_s^{iso} of 1 $mm s^{-1}$). Densities of marine diatoms ρ_p have not been measured directly but estimated from Stokes equation for settling spheres, based on measured sinking velocities. Densities were found to be in the range of 1.03 - 1.15 $g cm^{-3}$ for actively growing cells with higher values for cells in senescence (1.059-1.33 $g cm^{-3}$; Eppley *et al.* 1967). Average density of surface seawater ρ_f is 1.025 $g cm^{-3}$ and thus the density ratio relevant to the parameter space of phytoplankton is in the range of 1 - 1.3. Table 2 summarizes the parameter values relevant to marine diatoms.

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