The geomagnetic jerk of 2003.5-characterisation with regional observatory secular variation data

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Abstract

The 2003.5 geomagnetic jerk was identified in geomagnetic records from satellite data, and a matching feature reported in variations in length-of-day (Δ LOD), but detailed study has been hampered by lack of geomagnetic observatory data where it appears strongest. Here we examine secular variation (annual differences of monthly means) based on a new resource of 43 Chinese observatory records for 1998 until the present, focusing on 10 series of particularly high quality and consistency. To obtain a clean series, we calculate the covariance matrix of residuals between measurements and a state-of-the-art field model, CHAOS-6, and use eigenvalue analysis to remove noisy contributions from the uncorrected data. The magnitude of the most significant eigenvector correlates well with Dcx (corrected, extended Dst), suggesting the noise originates from unmodelled external magnetic field. Removal of this noise eliminates much coherent misfit around 2003—2005; nevertheless, the 2003.5 jerk is seen clearly in the first time derivative of the East component in Chinese data, and is also seen in the first time derivative of the

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vertical component in European data. Estimates of the jerk time are centred on 2003.5, but with some spatial variation; this variation can be eliminated if we allow a discontinuity in the secular variation as well as its temporal gradient. Both regions also provide evidence for a jerk around 2014, although less clearly than 2003.5. We create a new field model based on new data and CHAOS-6 to further examine the regional signals. The new model is close to CHAOS-6, but better fits Chinese data, although modelling also identifies some data features as unphysical.

Keywords: Geomagnetic field, Secular variation, Jerk, CHAOS-6, Length of day

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¹ 1. Background

The observed geomagnetic field originates from field sources both internal 2 and external to the Earth, varying on time scales of milliseconds to billions 3 of years. Largely, short time scales (a year or less) are the result of exter-4 nal variations (changes in the magnetosphere or ionosphere associated with 5 solar field variations), while variations on longer time scales originate from 6 the internal field generated in the Earth's core by the magnetohydrodynamic 7 dynamo. The shortest observed changes that have been attributed to inter-8 nal variations are the so-called geomagnetic jerks, first defined by Courtillot 9 et al. (1978) as a sudden change in the slope of the geomagnetic secular 10 variation (SV, the first time derivative of the Earth's magnetic field), or 11 equivalently an abrupt (step-like) change in the secular acceleration (SA, the 12 second time derivative). The most widely discussed jerk is in 1969 (Malin and 13

Hodder, 1982), but many others have been identified (e.g., 1978, 1991, 1999) 14 and 2003) in time series of geomagnetic observatory data, or geomagnetic 15 models (Mandea et al., 2010), most recently from 2011 (Chulliat and Maus, 16 2014) and 2014 (Torta et al., 2015). A feature of recent interest has been an 17 approximately 6-year cycle in SV linking to jerks (Chulliat and Maus, 2014), 18 and also seen strongly in variations in Earth rotation (length-of-day, LOD) 19 (Gillet et al., 2010; Holme and De Viron, 2013). These observations support 20 an association with possible torsional oscillations in the outer core (Bloxham 21 et al., 2002), linked to either inner-core rotation and coupling (Mound and 22 Buffett, 2003) or an intrinsic flow mode (Gillet et al., 2010). However, there 23 remains considerable debate as to the nature of jerks. Are they a global or 24 localised feature (Mandea et al., 2010; Torta et al., 2015)? Is the discontinu-25 ity in the second derivative the best way to characterise them (Alexandrescu 26 et al., 1996)? Do external field features (Alldredge, 1984; Demetrescu and 27 Dobrica, 2014) cause or contribute to some jerks? Are all jerks similar, or 28 are there a variety of different types, and potentially causes (Mandea et al., 29 2010)?30

Most studies on geomagnetic jerks focus on magnetic observatory data, 31 because of their long-time stability, and high temporal resolution to define the 32 secular variation. However, (Mandea and Olsen, 2006) developed a comple-33 mentary study tool deriving "virtual observatories" using data from magnetic 34 satellites, by stacking the data in time for a limited geographical region. The 35 derived individual secular variation estimates are of lower quality than those 36 from ground based observatories, but provide global data availability rather 37 than depending on the sparse and uneven geomagnetic observatory network. 38

Using this method, Olsen and Mandea (2007) identified several jerks, includ-39 ing one centred on 2003.5. This feature is of particular interest because it is 40 not aligned with the approximately 6-year variation, but nevertheless corre-41 lates with a jerk-like feature in variations in Earth rotation or length of day 42 Δ LOD (Holme and De Viron, 2013), also separate from the 6-year variation. 43 Inference from the rotational record suggests a possible discontinuity in not just the rate of secular variation, but the secular variation itself, changing the 45 range of possible physical mechanisms that could give rise to it. The similar-46 ity in timing of the two records also constrains other geophysical properties, 47 particularly deep-mantle electrical conductivity (Holme and De Viron, 2013). 48 To better examine this feature in the geomagnetic data, a study of ground 49 observatory data is clearly highly advantageous. Brown et al. (2013) provide 50 such a study, but Olsen and Mandea (2007) localise the event as around the 51 90° E meridian, a geographic region for which easily available data from world 52 geomagnetic data centre holdings are sparse. Here we investigate previously 53 unutilised data from 43 Chinese observatories covering the period 1998 to 54 2016. These data provide a particular tool for studying this jerk, but also a 55 potential homogeneous database for future high resolution regional studies 56 of secular variation, to compare with other densely instrumented areas such 57 as Europe. We compare these data with the European data, focusing partic-58 ularly on the 2003.5 jerk to determine whether there exist linked changes in 59 Asia and Europe, which therefore could provide a global constraint on secular 60 variation, and a direct observational constraint on the rapid variation of the 61 geodynamo. We characterize the short-period variation in the time series as 62 being related to external field, and by subtracting this influence, strengthen 63

the interpretation and better constrain the timing of the 2003.5 jerk. To explore the content of the new data, we create a new global, time-dependent model which is both close to the field predicted by the CHAOS-6 model and also better fits the newly available Chinese data. We will use this tool to better characterize all rapid variations in secular variation.

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70 2. Data

There are currently 43 operational Chinese observatories (Figure 1) pro-71 viding good spatial coverage throughout the Chinese mainland, with records 72 broadly available from 1998 to the present day, and many extending earlier. 73 Available observatories were established and are maintained by the Geo-74 magnetic Network of China, Chinese Earthquake Administration, which has 75 provided hourly mean data; many of these data are not as yet held by the 76 World Data Centers. To compare with and verify our results, 7 European 77 observatories (figure 2) are also studied. The codes of all 43 Chinese obser-78 vatories are listed in the appendix. 79

80

Figure 1

Figure 2

As we are interested primarily in internal field variations, from all available hourly data we calculated monthly means of the three components (northward X, eastward Y and vertically downward Z) of the magnetic field of each observatory, thereby eliminating high-frequency external variations. We estimated SV determining annual differences of monthly means, for example for Y as:

$$\left. \frac{dY}{dt} \right|_t = Y_{(t+6)} - Y_{(t-6)} \tag{1}$$

where t denotes time in months. By taking differences, we eliminate constant 87 crustal field offsets (Bloxham and Jackson, 1992). By taking annual differ-88 ences, we reduce the influence of external noise, e.g. magnetospheric ring 89 currents, particularly those components with annual cycles. This method 90 is equivalent to the approach of Mandea et al. (2000), who took monthly 91 differences, but then applied a 12-month running mean. There are gener-92 ally two problems when dealing with the data: baseline jumps (or erroneous 93 data) and data gaps, resulting from many possible causes (e.g., instrument 94 error, power failure, station relocation, anthropogenic current disturbance, 95 etc). We have applied all documented baseline corrections, and have iden-96 tified and corrected for some additional jumps (see appendix). Data gaps 97 are more difficult, and unfortunately many of the Chinese data series are 98 discontinuous. Brown et al. (2013) treated a gap shorter than 6 months by 99 interpolating, while if longer than 6 months the data were split into separate 100 time series. We choose to use the data "as is", and will consider data gaps 101 by comparison with the CHAOS-6 field model and covariance modelling, de-102 scribed below. Our primary focus is on 10 Chinese observatories with the 103 most continuous records (THJ, JIH, QIX, GLM, TSY, COM, YON, WMQ, 104 DLG and CHL, see figure 1). To compare the results, monthly mean data 105 of 7 European observatories (BEL, CLF, DOU, FUR, HLP, HRB and NGK, 106 see figure 2) are adopted from the Bureau Central de Magntisme Terrestre 107 (BCMT), World Monthly Means Database Project, which provides monthly 108

averages of components dX/dt, dY/dt and dZ/dt at 118 observatories worldwide) calculated from hourly means held by the World Data Centre (WDC) for Geomagnetism at the British Geological Survey, Edinburgh (Chulliat and Telali, 2007).

113 3. Jerk-like features

120

In figures 3-5, we plot the secular variation estimates for both arrays of observatories. For the dZ/dt component, the plot of variation for the Chinese data is dominated by a linear secular trend. To bring out the rapid changes, we provide an subfigure (middle figure of fig 5) in which this trend is removed.

118	Figure 3
119	Figure 4

Figure 5

For dX/dt, the rapid variation shows strong correlation (correlation coeffi-121 cient r=0.77) between China and Europe, with many oscillations in common 122 during 1998-2015. Focusing on 2003.5 and 2014, changes in slope (\lor and \land 123 shapes) are present simultaneously in both data sets. For dY/dt, a longer 124 term \lor shape also can be clearly recognized in 2003.5 in China, but not 125 clearly in 2014. In contrast, European data express clear jerk like shape in 126 2014 but not in 2003.5. For dZ/dt, comparing the detrended Chinese data 127 we find good agreement between two regions around 2003.5 (r=0.91) and 128 2014 (r=0.83). To summarise, 2003.5's jerk could be clearly identified in 129 China among dX/dt, dY/dt and dZ/dt, consistent with Olsen and Mandea 130 (2007), and 2014's jerk can be located as Torta et al. (2015). 2014's jerk can 131 also be distinguished in Australia, central Pacific and Europe through models 132

including CHAOS-6 (Finlay et al., 2016; Brown et al., 2016). To other jerks (Mandea et al., 2010), 1999 and 2011's jerks can be found in dX/dt in two regions. It is easy to find 2009's jerk in dY/dt and dZ/dt in Europe but not in China. Finally, a jerk-like feature may be emerging around 2015.

137 4. External fields

The data contain a strong component that is related to external and 138 induced fields, in particular from the large-scale magnetospheric ring currents 139 and associated induced signals due to ground electrical conductivity. Strong 140 correlation between variations of different components (particularly dX/dt141 and dZ/dt) are particularly indicative of this. Magnetic field models such as 142 CHAOS-6 and CM4 (Finlay et al., 2016; Sabaka et al., 2004) are constructed 143 to co-estimate the external field, with some allowance for the induced field. 144 This external effect is parameterized by an a priori geomagnetic index, e.g. 145 RC or Dst. However, the global model of the ring current does not include 146 the influence of possible local conductivity structure on induced fields. As an 147 alternative, Wardinski and Holme (2006) showed that the residual between 148 observation and model can replace the Dst index in their calculations as a 149 proxy for unmodelled external signals. Removal of such signals substantially 150 reduces the standard deviation of the data, therefore improving the resolution 151 of internal features such as jerks (Brown et al., 2013). 152

We follow Wardinski and Holme (2006) to create the covariance matrix of residuals of observatory monthly mean annual differences and CHAOS-6 model secular variation prediction. We assume that the residuals are zero¹⁵⁶ mean, so we can define the elements of the covariance matrix

$$cov(p,q) = \frac{\sum_{i=1}^{n} P_i Q_i}{n},$$
(2)

where P, Q are residuals of the secular variation estimates of particular components from one or two observatories, with the sum over n observations. For n observatories each with 3 component data dX/dt, dY/dt and dZ/dt, the covariance matrix is of order 3n; the eigenvalues and eigenvectors of the matrix are then determined. We calculate the covariance matrices separately for groups of 10 Chinese and 7 European sites, yielding 30 and 21 eigenvalues, respectively, plotted in figure 6.

Figure 6

In both data sets, there is a clear sharp decrease between the first and second eigenvalues, after which the values decrease gradually. As a result, the first eigenvector makes a dominant contribution to the misfit. In figure 7, we plot the contributions to this eigenvector for the 10 Chinese observatories.

Figure 7

The spatial structure of this eigenvector is indicative of its origin from 168 the ring current, which produces a field dominantly in dX/dt and dZ/dt169 directions, with the relative values depending on the observatory's location. 170 Here, dX/dt dominates because the Chinese observatories are at low mag-171 netic latitude. The quietest component as seen in this figure is dY/dt, which 172 is perpendicular to the ring current field (Pinheiro et al., 2011). Note that 173 we did not initially obtain this result, but instead determined an eigenvector 174 dominated by one particular observatory; this turned out to be an unmod-175 elled baseline shift, and the ring current structure only became clear when 176 such data artefacts were removed. As a result, the method also acts as a 177

¹⁷⁸ sensitive test of data quality.

We examine the spatial structure of this noisiest (largest eigenvalue) 179 eigenvector in more detail in Figure 8. For the 10 observatories already 180 considered, we extracted the (dX/dt, dY/dt, dZ/dt) components for each 181 observatory, and normalized each 3 vector to unit length. The other 33 ob-182 servatories have data of lower quality; to consider these observatories as well, 183 we repeat the covariance/eigenanalysis by adding one of those observato-184 ries to the 10 good observatories sequentially (making each eigenanalysis of 185 11 observatories (33 data series)), and each time calculated the normalized 186 components for the additional observatory. We plot the dX/dt and dY/dt187 components; an observatory with only a dZ/dt component would plot at the 188 origin. 189

Figure 8

The more consistent the data series for different observatories, the closer 190 the points for the different observatories should be. In figure 8, the left 191 hand figure shows broad consistency between the observatories. The right 192 hand figure provides more details, with 8 observatories separated from the 193 majority; examining the series shows that they contain large misfits likely 194 resulting from uncorrected artefacts. For the 35 consistent series, many have 195 large data gaps, leading to our decision to concentrate analysis on only 10 196 good observatories with broadly continuous records. 197

To support our hypothesis that this largest noise source is related to the ring current, we compare the component of this eigenvector in the residuals at each time (the dot product of the residual vector with this unit eigenvector) with an index of ring-current activity. We use an corrected, extended Dst index, Dcx, which is achieved selecting 17 stations and correcting for the quiet-time seasonal variation (Mursula et al., 2008). (The index is provisional from non-definitive data for 14 stations for 2012-2016.) We calculate the annual differences of Dcx and compared to the noisy contributions from Chinese and European observations (figure 9).

Figure 9

Figure 9 shows a good agreement between the annual differences in vari-207 ations of Dcx and noisy contributions from both China and Europe, par-208 ticularly in the active periods 2003-2006 and 2014 onwards, when Dcx sig-209 nificantly oscillates and their trends look highly consistent. This situation 210 implies that the jerk signature around 2003.5 and 2014 could be seriously 211 influenced by external fields. The correlation coefficient between Chinese 212 magnetic observatories and Dcx is 0.70, and that between European obser-213 vatories and Dcx is 0.68. Note also that the eigenvectors for the separate 214 analyses for China and Europe have correlation coefficient 0.96, confirming 215 the conjecture of Wardinski and Holme (2011) that the dominant eigenvector 216 and its magnitude may be a better correction method than scaling with Dcx. 217

²¹⁸ 5. Cleaned data

We have shown that the largest eigenvalue/eigenvector of the misfit of the data to the field model is not random, but arises from a specific source, likely dominated by variations in the magnetospheric ring current. Therefore, to clean the data for better analysis of possible internal signals, we remove the contribution of the highest (noisiest) eigenvalue, which we believe strongly reduces the influence of magnetospheric ring-current variation. We subtract the noisy contributions corresponding to the largest eigenvalue/eigenvectoras follows:

$$\mathbf{r}' = \mathbf{r} - (\mathbf{r} \cdot \mathbf{v})\mathbf{v},\tag{3}$$

where \mathbf{r} is residual vectors at a particular time, \mathbf{v} is the unit normalized eigenvectors corresponding to the largest eigenvalue. The clean (denoised) data have the influence of the largest eigenvalue removed, plotted in Figures 10-12.

Figure 10

Figure 11

Figure 12

Much of the apparent jerk signal is eliminated, suggesting that much 231 of the sharp change in dX/dt and dZ/dt around 2003.5 is of external ori-232 gin, especially from the magnetospheric ring current. This is of particular 233 significance, as the original identification of the jerk by Olsen and Mandea 234 (2007) was from analysis of the dZ/dt, which might therefore also have been 235 contaminated by external field structure. The similar timings also support 236 and explain earlier discussions of jerk signals from in part external sources 237 (Alldredge, 1984; Demetrescu and Dobrica, 2014). Comparing with figure 7, 238 dX/dt is most changed with dZ/dt less; dY/dt is little changed. In figure 239 10, dX/dt is much changed with fewer oscillations both in China and Europe 240 compared with uncorrected variation. The 2014 jerk can be roughly distin-241 guished while 2003.5 is not clear. Figure 11 shows little change in dY/dt242 due to this direction being perpendicular to the magnetic field of the ring 243 current; the 2003.5 jerk can still be clearly identified in China. For dZ/dt, 244 we again linearly detrend the Chinese data for clarity. No clear jerk is seen 245

²⁴⁶ in the Chinese data, but a jerk signal remains in the European data.

To highlight the suggested jerks, we replot the figures for dY/dt for China (Figure 13) and dZ/dt for Europe (Figure 14).

Figure 13

Figure 14

A jerk is present in both regions at around 2003.5, both records show 249 some evidence of a jerk in 2014, and overall the two signals show broad anti-250 correlation throughout the interval. Therefore the two jerks are global sig-251 nals, albeit seen most clearly in different components in different geographic 252 regions, and therefore in a field model will be dominated by spherical har-253 monic field components of low degree. We further examined the SV of the 254 33 less good Chinese observatories in 2003.5 and 2014 in the same way; these 255 two jerks are reflected particularly cleanly at 18 and 6 of these observatories 256 respectively, where the limited numbers are due to lack of data rather than 257 evidence that the jerk is *not* present. 258

Finally, we estimate the time of the 2003.5 jerk in the Chinese data. We determine best fit lines for the data before and after the jerk, and calculate the time of their intersection, as a classical measure of jerk timing. The results are presented in Table 1.

Table 1

The mean timing is close to 2003.5, although it is not possible to state that the jerk is simultaneous at all locations. However, this time also assumes that SV is continuous. Evidence from both Δ LOD and wavelet analysis of secular variation data (Alexandrescu et al., 1996) suggests that a jerk might involve a change not only in secular variation gradient, but also in its value.

Such a jump would be smoothed by the analysis: an annual first difference (as 268 used to estimate the secular variation) is equivalent to a 12-month running 269 average of secular variation, smoothing any such jump. To investigate this, 270 we define the jerk time to be 2003.5, allowing a discontinuity in SV, and 271 take a running average. Figure 15 provides an example for the observatory 272 GLM. In all cases, the prediction provides an equally good fit to the data as 273 allowing a difference in calculation of the jerk time, and as here the running 274 averages are almost indistinguishable. We therefore claim that the data are 275 consistent with both a variation in jerk timing over China, but also with a 276 jerk at a common time but allowing an offset in secular variation, and may 277 not allow these two hypotheses to be distinguished. 278

Figure 15

279 6. A perturbed field model

To this point, we have taken the CHAOS-6 model as a true representation 280 of the field for the Chinese region, despite that model not being constrained 281 by the new secular variation data. Some features in SV not predicted by 282 CHAOS-6 seem coherent between several (although by no means all) of the 283 different data series. To investigate the possible implications of these data, 284 we seek a new global, time-dependent model which is both close to the field 285 predicted by the CHAOS-6 model (and so assumed to match well the satellite 286 data from which it is constructed) and also better fits the newly available 287 Chinese data. Our methodology follows that of Lodge and Holme (2009). We 288 expand in a spherical harmonic basis in latitude and longitude, truncated at 289 spherical harmonic degree $l_{max} = 14$, with each coefficient further expanded 290

on a basis of cubic B-splines, with temporarly dense knots at spacing 0.1 291 years. The CHAOS6 model is expanded on order 6 B-splines with half-year 292 knot spacing; we obtain a reference model from a least-squares fit to each set 293 of spline coefficients for each Gauss coefficient; the lower degree of the splines 294 is countered by the higher knot density. We seek a model between times t_0 295 and t_1 (1997.1 and 2018.1 to match the limits of the CHAOS6 model) min-296 imizing three properties: 1) the mean square misfit to the secular variation 297 estimates derived from the 43 Chinese observatories; 2) the time integrated 298 square vector misfit at Earth's surface to the CHAOS-6 model; and 3) the 299 time integrated squared secular acceleration at the core-mantle boundary 300 (CMB). Condition 1 requires a fit to the new data presented here, condition 301 2 provides a proxy to the fit to the satellite and observatory data from which 302 CHAOS-6 was constructed (defined at Earth's surface), and condition 3 pre-303 vents unreasonably large temporal variation. Condition 1 is implemented 304 as a fit to data, while conditions 2 and 3 are both "damping", giving the 305 objective function Γ to be minimized as 306

$$\Gamma = \sum_{i=1}^{n} \left(\dot{\mathbf{B}}(\mathbf{x}_{i}) - \dot{\mathbf{B}}_{i} \right)^{2} \\
+ \lambda \int_{t_{0}}^{t_{1}} \sum_{l=1}^{l_{max}} (l+1) \sum_{m=0}^{l} \left((g_{l}^{m} - g_{l}^{m}_{\text{CHAOS}})^{2} + (h_{l}^{m} - h_{l}^{m}_{\text{CHAOS}})^{2} \right) dt \\
+ \mu \int_{t_{0}}^{t_{1}} \sum_{l=1}^{l_{max}} (l+1) \left(\frac{a}{c} \right)^{(2l+4)} \sum_{m=0}^{l} \left((\ddot{g}_{l}^{m})^{2} + (\ddot{h}_{l}^{m})^{2} \right) dt \tag{4}$$

The first term is the mean square fit to the secular variation data by the model. $\dot{\mathbf{B}}_i$ is a vector of SV data, with the difference taken to the model prediction at observatory location \mathbf{x}_i . The second term minimizes the mean

square misfit mean field integrated over Earth's surface, radius a, given by 310 the squared difference between the model Gauss coefficients g_l^m, h_l^m of degree 311 l and order m and those of the CHAOS-6 model. The third term minimises 312 the mean square secular acceleration at the core-mantle boundary, radius c. 313 The two damping parameters λ and μ allow a range of possible solutions; 314 we present three representative possible models, which we designate as low, 315 medium and high damping. The low damping allows comparatively large 316 secular acceleration, while the high damping provides a model closely con-317 strained to match the field prediction of CHAOS-6. To illustrate the fit to 318 the data, we plot the fit for each component to the station YON. 319

Figure 16

Figure 17

Figure 18

The high damping model provides little departure from CHAOS-6; to 320 obtain a closer fit to the data, more time variation is required see for example 321 Figure 16 (dX/dt). That this variation may be unreasonably high is shown 322 by a more detailed plot of the dZ/dt for 2010–2012 (see more details in 323 figure 19). The high damped model shows little change to CHAOS-6, while 324 the intermediate and low damping models have changed to fit sharp changes 325 in the data in 2011.3 which may well be an artifact. Only with low damping 326 is the data fit substantially improved; compared to CHAOS-6, the misfit is 327 reduced by 22.0%, 18.7% and 22.1% for dX/dt, dY/dt, dZ/dt components 328 respectively. Even with this weakly damped model, some strong features in 329 the data coherent between different observatories are not fit, even when the 330 error estimate for a short period (e.g., 2002–2005) is artificially reduced. 331

This implies that such features cannot be represented by the components of a potential field are not likely to be a result of unmodelled internal field structure, suggesting further cleaning or selection of data to be necessary.

Figure 19

The increased temporal structure of the new models is demonstrated by considering the secular variation spectrum

$$W'(l,c) = (l+1)(\frac{a}{c})^{(2l+4)} \sum_{m=0}^{l} (\dot{g}_l^m)^2 + (\dot{h}_l^m)^2,$$
(5)

Here \dot{g}_l^m , \dot{h}_l^m are time derivatives of the Gauss coefficients. In Figure 20, we show the power spectra at 2004.0 for our three differently damped models, also plotting W(l,c)/(l(l+1)), which following Mcleod (1996) and Holme et al. (2011), we might expect to be broadly independent of degree l.

Figure 20

Both the medium and low damping models show a strong rise in secular variation power above degree 10, which is unlikely to be physical. In Figure 21 we compare contour maps of SV at Earth's surface for CHAOS-6 and the weakly damped new model; the broad structure is unchanged, but the contours show small scale variations that are probably not justified.

Figure 21

A change in SV near China (better matching the data) is achieved, but only at the expense of considerably increased detail over the whole globe, which is not consistent with the original data. If plotted at the CMB, the map of the new model shows excessive small scale structure. We conclude that there is no strong evidence in the new data requiring substantial adjustment to the CHAOS-6 model – substantially improved fit to data requires ³⁵² unreasonably large small-scale secular variation.

353 7. Discussion and Conclusions

We have examined collections of spatially close geomagnetic observatory 354 records, focusing on a new set of data from Chinese observatories, and for 355 comparison, a set of well-studied European observatories. The Chinese data 356 are of slightly lower quality than the European data: the data are more 357 gappy, and require correction of undocumented baseline jumps. Neverthe-358 less, after such corrections, the data are of high quality, and provide a close 359 to homogenous data set for study of regional intra-decadal and longer secu-360 lar variation. We have focused on one period in particular, centered around 361 2003.5, for which a rapid SV change (a geomagnetic jerk) had previously been 362 reported (Olsen and Mandea, 2007). This previous identification had been 363 based on a model constructed from satellite data using virtual observatories 364 (averages of satellite data over a limited region); secular variation studies 365 with observatory data will be more robust. Our data show strong features 366 around 2003.5, particularly in the dX/dt and dZ/dt components for both 367 the Chinese and European observatory arrays. However, further analysis 368 suggests that these features result from external field variation, probably a 369 jump in the strength of the ring current (reflected in Dcx). Removing these 370 external fields removes much of the sharp signal in dX/dt and dZ/dt, but 371 a clear jerk remains in the dY/dt component at Chinese observatories. The 372 jerk is also seen in dZ/dt at European observatories, although some contam-373 ination from external sources may remain. Nevertheless, as the features form 374 part of the long term trends in secular variation, we argue that there is a 375

³⁷⁶ component of internal origin.

Using CHAOS-6, we plot the evolution of dY/dt, and estimates of its first (SV) and second (SA) derivatives. The broad structure is similar for all Chinese observatories; we plot QIX, located in the middle of the observatory grouping, along with its CHAOS-6 predictions.

Figure 22

Figure 22 shows clearly the jerk in the SV around 2003.5, and allowing for the averaging of the data the SA record is consistent with a jump, perhaps overly smoothed in the CHAOS-6 model prediction. This figure does not illustrate evidence in the Chinese data of the most recently identified geomagnetic jerk in 2014 (Torta et al., 2015), this feature is only seen strongly in 6 Chinese observatories (THJ, GLM, WMQ, CDP, QGZ and HZC).

The exact timing of the jerk is of great interest (e.g. Pinheiro et al. 387 (2011)); time delays have been used to propose higher electrical conductivity 388 of the deep mantle under certain geographic regions, particularly in the Pa-389 cific. Taking the usual definition of a jerk implying continuous SV, both data 390 and model suggest that even in the limited region covered by the Chinese 391 data, there is some offset of jerk times with locations. All observatories show 392 the jerk at around 2003.5, but varying between 2003 (at WMQ, the most 393 westerly located of our 10 selected observatories) and close to 2004 (DLG, 394 the most easterly of our observatories). The shift in jerk timing may instead 395 result from different SV time gradients before and after 2003.5; the jerk is 396 apparently shifted towards the less steep trending time. This is consistent 397 with the observations above for WMQ and DLG. However, this simple anal-398 ysis is complicated by the possibility of a jump in the secular variation itself, 399

as suggested by the ΔLOD data (Holme and De Viron, 2013), but also by 400 wavelet studies suggesting that the jerks are not exact jumps in the second 401 derivative (Alexandrescu et al., 1996). When the effective 12 month averag-402 ing from taking annual differences of the data is allowed for, the predictions 403 assuming continuous SV but varying jerk times, or a common time but dis-404 continuous SV are indistinguishable. Furthermore, the data are still noisy, 405 with features that cannot be well-fit by a model of the internal geomagnetic 406 field, even after the removal of the largest noise eigenvector, making direct 407 analysis of the data difficult. Further study is necessary, particularly focus-408 ing on the sources of the data, but we may conclude at least that the newly 409 available Chinese data are consistent with a common time for the jerk of 410 around 2003.5. 411

We believe our analysis shows evidence of the 2003.5 jerk appearing at 412 widely spaced locations on the Earth, and so that the jerk is of global sig-413 nificance. The timing of the jerk (from the dY/dt in the Chinese data) is 414 also consistent with the feature at 2003.5 reported in the variation in LOD 415 (Holme and De Viron, 2013). LOD variation established rotational jerks, 416 particularly of an approximately 6-year variation, which correlate well with 417 6 year variations in magnetic signals (Gillet et al., 2010; Chulliat and Maus, 418 2014). However, the 2003.5 signal is not linked with the 6 year variation; this 419 is not surprising given its appearance in the long-term secular variation in 420 dY/dt at the Chinese observatories. There may be two kinds of jerks, one as-421 sociated with the 6-year oscillation, and one, such as the one presented here, 422 of different origin, relating to longer term changes in the secular variation, 423 shown particularly clearly by the dY/dt of the Chinese data. Demetrescu 424

and Dobrica (2014) pointed out that jerk arises from the combination of the
internal 22yr and 80 yr signals accoring the decomposition of the geomagnetic SV.

Perturbing the CHAOS-6 model to better fit the new data does not show 428 evidence of missing structure in the model; large features in the data remain 429 unfit. As they cannot be explained by a potential field of internal origin, they 430 probably do not reflect the underlying secular variation. Our results therefore 431 imply that CHAOS-6 model fits the reliable features in rapid field variation. 432 To go further, careful treatment of the data, probably requiring analysis of 433 very noisy monthly mean first differences (rather than annual differences as 434 here) will be necessary to further constrain the origin of geomagnetic jerks. 435 However, the new availability (and hopefully extension) of the Chinese data 436 will provide a powerful tool for further study of this issue. 437

438 Abbreviations

439 SV: secular variation; SA: secular acceleration; CMB: core-mantle bound-440 ary; LOD: length of day.

441 Author's contributions

YF and RH initiated the study, designed the numerical experiments and
wrote the manuscript. YJ provided the related calculating results, GAC supplied some beneficial suggestions. YF finalized the manuscript. All authors
read and approved the final manuscript.

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453 Competing interests

The authors declare that they have no competing interests. This study does not involve humans/animals.

456 Appendix

The brief description of the treatment to the observatory records. Observatory data are either presented in a geographic (X, Y, Z) or geomagnetic (D, H, Z) coordinate system.

- BJI-No records for 2007, 2015 and 2016, to get rid of the questionable D in 2002.
- 462 CDP-No records for 1997, Baseline correction to Z in 2003, to reduce the 463 misfit by subtracting the difference.
- ⁴⁶⁴ CHL-No records for 2011, Baseline correction to D, H and Z in 2008, to ⁴⁶⁵ reduce the misfit by subtracting the difference.
- ⁴⁶⁶ CNH-Baseline correction to D and H in 2007 and 2008, to reduce the misfit ⁴⁶⁷ by subtracting the difference.
- $_{468}$ COM-Baseline correction to D in the first month in 2000, to reduce the misfit

- ⁴⁶⁹ by subtracting the difference.
- 470 COQ-No records before 1998 and period 2011—2014, location had been
- ⁴⁷¹ changed since 2014.
- ⁴⁷² DED-No records for 2006, 2007, 2014 and 2015.
- 473 DLG-No records for 1998, Baseline correction to D, H and Z in 2000 and
- 474 2001, to reduce the misfit by subtracting the difference.
- 475 ESH-Only has records for 2008—2016.
- 476 GLM-Baseline correction to component H in 2008, to get rid of 1 day's ques-
- 477 tionable data.
- 478 GYX-No records for 2006, 2006 and 2013 onwards.
- 479 GZH-No records for 1996—2001.
- 480 HHH-No records for 2001, 2002, 2004, 2006 and 2007, baseline correction to
- $_{481}$ D in 2003, to reduce the misfit by subtracting the difference.
- 482 HZC-No records for the March, 2007.
- 483 JIH-No records for 2001. Baseline correction to D and H in 1996 and 2000,
- ⁴⁸⁴ to reduce the misfit by subtracting the difference.
- ⁴⁸⁵ JYG-No records for 1995—1997.
- 486 KSH-Baseline correction to three components in 2000, 2002 and 2006, to re-
- 487 duce the misfit by subtracting the difference.
- 488 LSA-No records for 1995.
- 489 LYH-No records for 1996—1998.
- ⁴⁹⁰ LZH-No records for 1996, 2007 and 2009.
- ⁴⁹¹ MCH-No records for 1997, 2005—2007.
- ⁴⁹² MCH-Only has records for 2009—2016.
- ⁴⁹³ MZL-No records for 2006.

- ⁴⁹⁴ NAJ-No records for 1998, 2002 and 2006 onwards.
- ⁴⁹⁵ QGZ-No records for 2005 and part of 2012, 2015.
- ⁴⁹⁶ QIM-Only has records for 2013—2016.
- $_{497}$ QIX-No records for part of 2007, baseline correction to D in 2015 and 2016,
- ⁴⁹⁸ to reduce the misfit by subtracting the difference.
- ⁴⁹⁹ QZH-No records for 1999, 2002—2006.
- ⁵⁰⁰ SQH-Only has records for 2009—2014.
- ⁵⁰¹ SSH-No records for 2006—2011.
- ⁵⁰² SYG-No records for 1997, 2004–2007.
- ⁵⁰³ TAA-No records for 1995, 1996, 1998 and 2003.
- TAY-No records for 1996 and 1997, to get rid of the questionable D in 2005.
- ⁵⁰⁵ THJ- Complete records.
- TSY-Baseline correction to H in 2000, to reduce the misfit by subtracting the difference.
- ⁵⁰⁸ WHN-No records for 1995, and 2007.
- ⁵⁰⁹ WJH-Only has records for 2013—2016.
- $_{510}$ WMQ- No records for 1999, Baseline correction to H in 2000, to reduce the
- ⁵¹¹ misfit by subtracting the difference.
- $_{512}$ XIC- No records for 1997, Baseline correction to H in 2007, to reduce the
- ⁵¹³ misfit by subtracting the difference.
- 514 YCB- No records for 1999 and 2000.
- ⁵¹⁵ YON- No records for 1995.
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Figure 1: Locations of 43 Chinese observatories. (red squares: 10 principally investigated observatories –THJ, JIH, QIX, GLM, TSY, COM, YON, WMQ, DLG and CHL). Lambert Conformal Projection.

Figure 2: Locations of 7 European observatories (BEL, CLF, DOU, FUR, HLP, HRB and NGK). Lambert Conformal Projection.

Figure 3: Comparison of uncorrected annual differences of monthly means of X, dX/dt, between China (top) and Europe (buttom). Vertical black dash lines correspond to possible jerk times in 2003.5 and 2014.

Figure 4: Comparison of uncorrected annual differences of monthly means of Y, dY/dt, between China (top) and Europe (buttom).

Figure 5: Comparison of uncorrected annual differences of monthly means of Z, dZ/dt, between China (top) and Europe (buttom). The Chinese dZ/dt data are additionally linearly detrended (middle).



Figure 6: Eigenvalues of components dX/dt, dY/dt and dZ/dt of 10 Chinese (red line) and 7 European (black line) observatories.

Figure 7: The components of the eigenvectors corresponding to the largest eigenvalue for the 10 Chinese observatories. Squares: dX/dt; diamonds: dY/dt; stars: dZ/dt.

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Figure 8: Normalization of the largest eigenvalue eigenvector for all 43 Chinese observatories, on full (left) and expanded (right) axes. Red squares: good observatories; black circles: less good observatories.

Figure 9: The comparison between the noisy contributions from China and Europe with annual differences of monthly means of Dcx index. Black line: Noisy contributions from China; blue line: Noisy contributions from Europe; red line: Annual differences of Dcx.

Figure 10: Comparison of denoised annual differences of monthly means of X, dX/dt, between 10 Chinese and 7 European observatories.

Figure 11: Comparison of denoised annual differences of monthly means of Y, dY/dt, between 10 Chinese and 7 European observatories.

Figure 12: Comparison of denoised annual differences of monthly means of Z, dZ/dt, between 10 Chinese and 7 European observatories.

Figure 13: Denoised annual differences of monthly means of Y, dY/dt, of 10 Chinese observatories.

Figure 14: Denoised annual differences of monthly means of Z, dZ/dt, of 7 European observatories.

Figure 15: The variation of $\mathrm{d}\,Y/\mathrm{d}\,t$ of GLM.

Figure 16: The variation of $\mathrm{d}X/\mathrm{d}t$ of YON under different damping parameters.

Figure 17: The variation of $\mathrm{d}\,Y/\mathrm{d}t$ of YON under different damping parameters.

Figure 18: The variation of $\mathrm{d}Z/\mathrm{d}t$ of YON under different damping parameters.