

1 **Plasma activation of CO₂ in a dielectric barrier discharge: a**
2 **chemical kinetic model from the microdischarge to the reactor**
3 **scales**

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7 **Abstract**

8 The conversion of CO₂ into value-added chemicals or fuels has attracted much attention over
9 the past years. Plasma technology represents a highly promising alternative due to its non-
10 equilibrium nature, deemed crucial for CO₂ dissociation reactions. Gaining a deep
11 understanding of the reaction mechanisms involved under plasma conditions is essential to
12 improve the performance of such processes. Among other theoretical calculations, plasma
13 chemical kinetic modelling constitutes a very suitable approach to address this challenge. In
14 this work, a zero-dimensional model of a dielectric barrier discharge (DBD) reactor is applied
15 to CO₂ splitting, providing a novel approach for including experimental parameters as
16 discharge power and flow rate based on the analysis of the different scales involved. The
17 model choices is extensively discussed as regards experimental parameters, cross-section
18 data and the chemical reactions considered. The predictions of the model are in good
19 agreement with existing experimental data and therefore the model is considered valid to
20 analyse the CO₂ splitting reaction mechanism based on its results. It is concluded that the
21 electron impact dissociation is the dominant process towards CO₂ conversion, which could
22 explain the low energy efficiency achieved since only ~10% of the electron energy is
23 consumed by mechanism. The remaining energy would be lost towards vibrational excitation
24 not leading to CO₂ dissociation in DBD reactors.

25 **Keywords:** Dielectric barrier discharge; Non-thermal plasma, CO₂ conversion, Plasma
26 chemical kinetic modelling; Reaction pathways.

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28 **1. Introduction**

29 Turning CO₂ into a valuable feedstock by the development of new processes for its
30 conversion to value added chemicals or fuels constitutes a major challenge already being
31 addressed by scientists and engineers all over the world. The large amounts of CO₂ emitted
32 on a daily basis due to the burning of fossil fuels account for the availability of this molecule.
33 In addition, these anthropogenic CO₂ emissions must be reduced due to their effect as a
34 greenhouse gas, as well as their negative impact in terms of global warming [1]. For these
35 reasons, CO₂ splitting has attracted great attention over the past years among scientists within
36 the fields of sustainability, renewable energy and environmental sciences [2–11].

37 Unfortunately, CO₂ is a highly stable molecule ($\Delta G^\circ = -394 \text{ kJ/mol}$) and its dissociation
38 is strongly endothermic ($\Delta H^\circ = +283 \text{ kJ/mol}$) [2]. Hence, high conversions are not easy to
39 achieve without a fairly poor energy efficiency. Many research efforts have aimed to
40 overcome these difficulties, among which plasma processing is presented as a promising
41 alternative due to their non-equilibrium nature [13–25]. Electron impact reactions provide
42 unique mechanisms for CO₂ dissociation that can take place at room temperature and
43 atmospheric pressure, this being a major advantage of non-thermal plasma technologies in
44 comparison with other methods like thermal catalysis [1]. Also, turning a plasma system on
45 and off is relatively straightforward, which makes it the ideal complement to the promising
46 yet fluctuating renewable energy sources [2].

47 Dielectric barrier discharge (DBD) reactors have been extensively studied for CO₂
48 conversion, partially due to their simplicity [13–25]. These types of reactors normally operate
49 at atmospheric pressure and near room temperature. Moreover, they have a simple design
50 suitable for industrial scales and a catalyst can be easily incorporated [14,17–25]. The energy
51 efficiency of CO₂ splitting reactions in DBD reactors (typically below 10% at atmospheric
52 pressure [26,27]) needs further improvement for this technology to be industrially relevant.
53 In terms of syngas production from CO₂ reforming of methane, DBD reactors should reach
54 an energy efficiency of around 60% to be competitive with both existing and emerging
55 technologies. This target can be reduced by a factor of 2 or 3 for direct oxidative pathways
56 towards liquid products, which is closer to the currently achieved energy efficiency [2].

57 In the quest for improving the energy efficiency, understanding the reaction mechanisms of
58 CO₂ conversion is of major importance [2]. Numerical modelling seems to be the best
59 approach for revealing the underlying chemistry of this system. Among these simulations,
60 plasma kinetic modelling provides a great tool to analyse the relevance of various processes
61 leading to CO₂ conversion. Due to the high computational cost of fluid models, non-
62 dimensional models have been developed and applied to DBD reactors, yielding reasonable
63 agreement with experimental data in most cases [28–35].

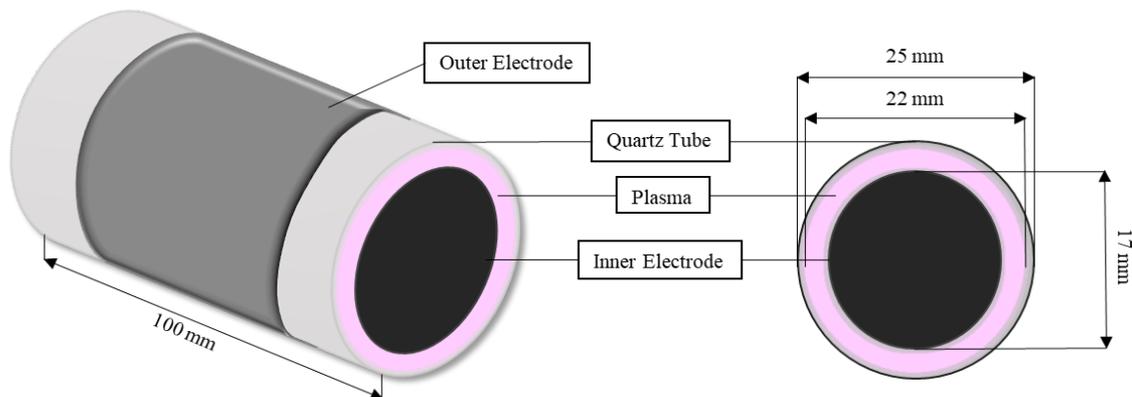
64 In this study, calculations based on a zero-dimensional plasma kinetic model of CO₂ splitting
65 in a tubular DBD reactor are performed and the results are compared with existing
66 experimental data [36]. Once validated, the model is used to understand the reaction
67 mechanisms involved based on its results. A novel approach to the already existing DBD
68 reactor zero-dimensional models is presented in order to incorporate the effect of the main
69 experimental parameters in the CO₂ conversion, namely discharge power and flow rate. To
70 the best of our knowledge, some important considerations and approximations included in
71 the model have never been tested before. A discussion of the most suitable cross sections
72 datasets for the electron impact dissociation is also presented based on results reported
73 elsewhere [32,37]. Polak and Slovetsky's CO₂ dissociation total cross section data [38] was
74 finally selected to calculate the CO₂ electron impact dissociation rate coefficient, being
75 contrasted to experimental results in terms of CO₂ conversion for the first time. A reduced
76 chemistry set reported in [31] is employed for this model, also contributing towards a low
77 computational cost as it only involves 17 reactions and 9 species. A reduced electric field
78 (E/N) well outside the range of figures reported elsewhere for DBD reactors is used. This
79 might have important consequences regarding the main channels for CO₂ dissociation and
80 the energy efficiency achieved in DBD reactors in comparison with that of microwave (MW)
81 discharges. Calculations were performed by means of the ZDPlasKin Fortran module
82 (version 2.0a, Sep 2017) [39]. BOLSIG+ solver (version 03/2016) was employed to calculate
83 the rate coefficients of the electron impact reactions [40]. LXCat project databases were used
84 for retrieving cross section data [41].

85 **2. Description of the model**

86 2.1. Experimental setup to be modeled

87 According to the experiments that the model in this study intends to represent, a co-axial
88 DBD reactor with no packing will be considered (see Figure 1). In every case relevant to this
89 work, the discharge length is 100 mm while there is a 2.5 mm discharge gap (the inner
90 diameter of the quartz tube is 22 mm while the outer diameter of the inner electrode is 17
91 mm). Further details on the experimental setup can be found in our previous work [36].
92 Different values for the discharge power and flow rate are considered (10 to 50 W and 25 to
93 125 mL/min, respectively), corresponding to different experimental measurements. The
94 voltage across the gap has been calculated through Lissajous figures, leading to a reduced
95 electric field of 56 Td. This value will be used as an input parameter throughout all the
96 calculations performed in this work. For further information on the method used to calculate
97 E/N from Lissajous figures, see ref [42].

98



99

100 *Figure 1 – Schematic diagram of DBD plasma reactor*

101

102 2.2. Zero-dimensional DBD reactor model

103 Zero-dimensional models have been previously applied to plasma kinetic modelling of DBD
104 reactors[28–31]. The main simplification of these models relies on neglecting any spatial
105 variations of any property in the radial and angular coordinates of the tubular reactor, i.e.
106 properties only vary along the axial coordinate of the reactor (Z). Like in plug flow models
107 of tubular reactors, a *slice of reactor* with a differential length dZ can be considered as a
108 differential element of volume within which every property is homogeneous. The *slice of*

109 reactor flows through the reactor from $Z=0$ to L (reactor length) with an average velocity
 110 $\langle V \rangle$, considered to be homogeneous in the reactor's flow section for the purpose of this model
 111 (planar velocity profile). In addition, this magnitude is assumed to be constant along the axial
 112 coordinate since density (temperature and pressure) variations between the reactor's inlet and
 113 outlet are neglected. Therefore, the velocity is essentially the ratio between the reactor length
 114 (L) and its residence time (θ). In fact, this model become non-dimensional when the
 115 independent variable Z is translated into the residence time (θ). Each element of volume
 116 flowing through the reactor ($Z = 0$ to L) can be seen as a small batch reactor progressing in
 117 time until reaching the residence time of the reactor ($t = 0$ to θ). Then, as expressed in
 118 equation 1, the j^{th} production or loss process will contribute to the variation of the number
 119 density of the i^{th} species (N_i) with respect to residence time according to the stoichiometric
 120 coefficient of the i^{th} species in the j^{th} reaction (a_{ij}) and its reaction rate (r_{rtj}). See variable
 121 index in Table S3.

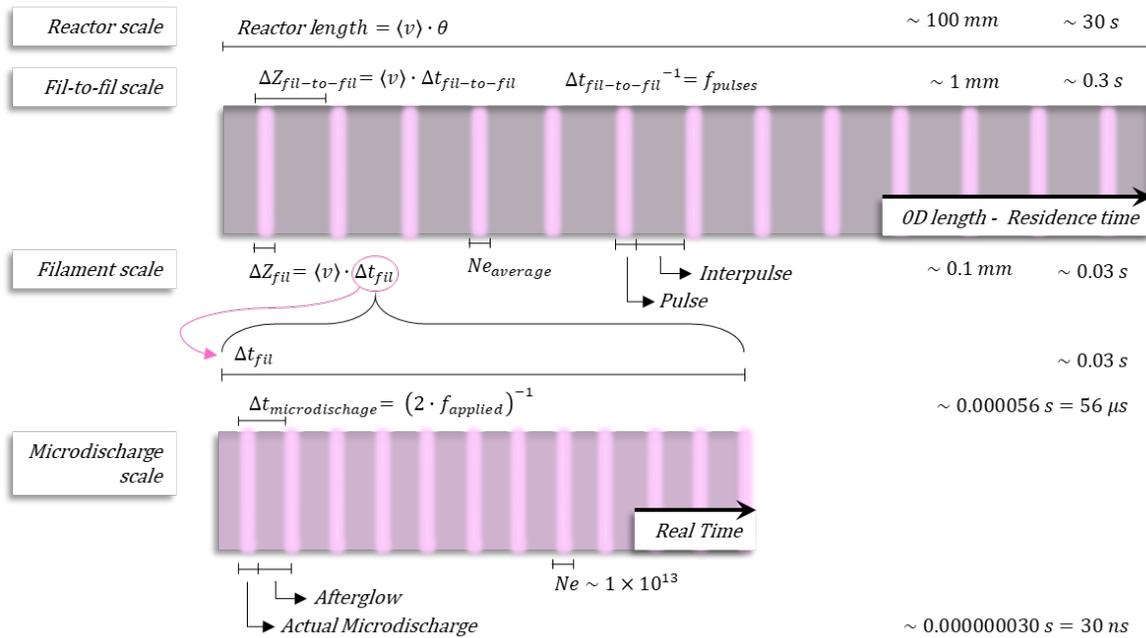
$$122 \quad \frac{dN_i}{d\theta} = \sum_j a_{ij} \times r_{rtj} = \sum_j a_{ij} \times k_j \times \prod_l N_l \quad (1)$$

123 Plasma discharges in DBD reactors present a filamentary regime for most gases and it is
 124 certainly the case for CO_2 [43]. Therefore, the element of volume described above passes
 125 through a number of filaments as it flows through the reactor, facing a high concentration of
 126 plasma electrons which in turn generate short lived plasma species by electron impact
 127 reactions. In terms of the non-dimensional model, these filaments, which are spatially spread
 128 along the axial coordinate of the reactor, can be represented as consecutive pulses over time
 129 with a certain frequency (f_{pulses}) [29]. This parameter has been widely varied among the
 130 different zero-dimensional models published in the past years, ranging from values in the
 131 order of the actual voltage frequency (tens of kHz) [29] to arbitrarily chosen values like 1000
 132 kHz [28] or 0.03 kHz [31]. Interestingly, this frequency of pulses in the model is not strongly
 133 related to the actual frequency of the voltage applied to the plasma system. In fact, it can be
 134 understood in terms of the period resulting from the ratio of the distance between two
 135 consecutive filaments ($\Delta Z_{fil-to-fil}$) and the velocity of the fluid ($\langle v \rangle$). That is to say, the
 136 frequency of the pulses in the zero-dimensional model can be expressed as in equation 2,
 137 where $\langle v \rangle$ is the average velocity of the fluid inside the reactor and $\Delta Z_{fil-to-fil}$ is the space

138 between two consecutive filaments (see Figure 2). Notably, the latter quantity brings
 139 uncertainty into the model. However, this reasoning gives a much narrower range of
 140 reasonable values for the frequency of pulses, within which it is just a fitting parameter.

141
$$f_{pulses} = \frac{1}{\Delta t_{fil-to-fil}} = \frac{\langle v \rangle}{\Delta Z_{fil-to-fil}} \quad (2)$$

142



143

144

Figure 2 – Scales and parameters in the model of a DBD reactor

145

146 2.3. Effect of power in the model's parameters – filament-to-filament scale

147 Mei et al. showed experimentally that the power deposited on the plasma system affects the
 148 conversion of CO₂ [36]. In the referred work, a range of power values from 10 to 50 W was
 149 covered resulting in an increase from 17.4 to 22.4% in the CO₂ conversion. Furthermore, we
 150 consider the electric field must remain constant regardless of the power value, as the
 151 breakdown voltage should as well (56 Td for all calculations in this work, as measured
 152 applying the methodology in [42] to the experimental setup of [36]). However, an increase
 153 in the power does cause a rise in the number of filaments per unit area observed in the system,
 154 as reported in [44]. Model wise, we propose to take this effect into consideration to account

155 for the rise in conversion with power. Ultimately, a greater number of filaments implies a
 156 shorter spacing $\Delta Z_{fil-to-fil}$ and so a higher frequency of pulses f_{pulses} for the same velocity
 157 of the fluid. In other words, this implies more pulses in the same residence time and, hence,
 158 a greater conversion.

159 The spacing between filaments is not known and a reference value of 1 mm was proposed
 160 for this model based on experimental observations. Then, this magnitude should be slightly
 161 above or below that figure for lower or higher power deposition figures, respectively.
 162 Therefore, a dependence between $\Delta Z_{fil-to-fil}$ and the power has been proposed (equation 3)
 163 according to the relationship found experimentally between power and conversion [36].

$$164 \quad \Delta Z_{fil-to-fil} = \frac{1 \text{ mm}}{K_p \times P^a} \quad (3)$$

165 The values of K_p and a are parameters to be found by minimising the difference between
 166 experimental and theoretical conversion values for every power value. In this way,
 167 $\Delta Z_{fil-to-fil}$ and consequently f_{pulses} constitutes the first fitting parameter of this model, as
 168 in other zero-dimensional models [29–31,34].

169

170 2.4. Effect of flow rate in the model's parameter – *one-filament scale*

171 As it has been shown experimentally, the flow rate has an inverse effect on the conversion,
 172 yielding lower CO₂ conversion at higher flow rates [36]. To start with, a higher flow rate
 173 results in both a shorter residence time (θ) and a higher frequency of pulses (f_{pulses}). These
 174 effects cancel out and the resulting number of pulses (num_{pulses}) remains the same
 175 regardless of the flow rate, as can be seen in equation 4, where the residence time of the
 176 reactor can be expressed as $\theta = \frac{\text{Reactor Volume}}{\text{Flowrate}} = \frac{L}{\langle v \rangle}$ (see Figure 2).

$$177 \quad num_{pulses} = f_{pulses} \times \theta = \frac{L}{\Delta Z_{fil-to-fil}} \quad (4)$$

178 Thus, the above described effects cannot explain the drop in conversion on its own and a
 179 closer look at a filament is needed to address the effect of a reduction in the flow rate. In this
 180 model, the space between filaments ($\Delta Z_{fil-to-fil}$) consists of a filament and a non-

181 filamentary region (interpulse), as shown in Figure 2. In the filament, molecules experience
182 collisions with plasma electrons and electron impact reactions occur giving rise to more free
183 electrons and reactive plasma species. On the other hand, ground state chemistry dominates
184 in the interpulse since no plasma electrons are present and the short lived plasma species tend
185 to be rapidly consumed in recombination reactions. Hence, the pulses (where free electrons
186 are available) are what really drives the conversion of CO₂ in our model.

187 Although the number of pulses remains the same for every flow rate, it can be seen intuitively
188 that each pulse is shorter lived at higher flow rates. In fact, the duration of both the pulse and
189 the interpulse decrease at higher flow rates. However, as the CO₂ number density remains
190 steady during the interpulse, a shorter interpulse does not have a noticeable impact in the
191 conversion. By contrast, a lower duration of the pulse has a big impact in the CO₂ number
192 density variation, resulting in a smaller overall CO₂ conversion for the same number of
193 pulses.

194 The time during which an element of volume *sees* the pulse depends on the width of the
195 filament and the velocity of the fluid, i.e., the flow rate. The filament width (ΔZ_{fil}) has been
196 reported to range from 0.1 to 0.2 mm [43], so it should be noted that there is roughly an order
197 of magnitude between that figure and the space between two consecutive filaments
198 $\Delta Z_{fil-to-fil}$. Then, there is also an order of magnitude between the period between filaments
199 ($\Delta t_{fil-to-fil}$, which determines the frequency of pulses f_{pulses} and the number of pulses
200 num_{pulses} given a residence time θ) and the duration of one filament (Δt_{fil} , which drives
201 the CO₂ conversion for a given number of pulses num_{pulses}). Besides, the duration of a
202 filament in the zero-dimensional model could be expressed as $\Delta t_{fil} = \frac{\Delta Z_{fil}}{\langle v \rangle}$.

203 However, the above stated expression for Δt_{fil} predicts much greater conversion drops than
204 those observed experimentally when increasing the flow rate. For this reason, in this study
205 we suggest a balancing effect for this relation, proposing that the filament width depends on
206 the velocity for the reasons exposed as follows.

207 First, let's consider the mechanisms that allow filaments to appear in a DBD reactor.
208 Filaments are actually a group of micro-discharges that occur in the same spot every time the
209 polarity of the electrodes changes. A micro-discharge lasts for tens of nanoseconds (ns)

210 before the electrons reach the positive electrode and the accumulated charge makes the local
211 electric field collapse [43]. A filament duration of 30 ns has been repeatedly reported in the
212 literature [28–34]. After a polarity reversal occurs, the deposited charge facilitates the
213 formation of a new micro-discharge in the same spot. Although electrons dissipate in tens of
214 nanoseconds, it takes tens of micro seconds (μs) for slow-moving heavy ions to reach the
215 negative electrode, resulting in a low but long-lasting falling ion current. Hence, both the
216 accumulated negative charge and the ion current characterises this region in space as a micro-
217 discharge remnant, after a micro-discharge occurred. With a frequency of 9 kHz, a voltage
218 polarity reversal occurs every 56 μs . The fact that the micro-discharge remnant is not fully
219 dissipated before the polarity changes also facilitates the formation of a new micro-discharge
220 in the same spot. This is called *memory effect* and explains why it is actually possible to see
221 filaments in a DBD reactor. If the micro-discharges were formed on a new spot every time
222 the polarity changed, the discharge would appear uniform and no spatially localised single
223 filaments could be observed [43].

224 For the purpose of this model, we will analyse what impact could the flow regime have on
225 the memory effect. As the flow regime changes from laminar to turbulent, velocity profiles
226 inside the reactor tend to become planar. This is a result of more random particle
227 displacements and a higher dispersion that tends to make properties homogeneous inside a
228 *slice of reactor*, including the velocity. Thus, a more turbulent flow regime could slightly
229 disperse the ions in the microdischarge remnant. Also, the velocity in the proximity of the
230 inner walls of the reactor is higher in turbulent flow, as the velocity profile becomes planar.
231 This could have an impact on how electrons are deposited in the positive electrode, enhancing
232 dispersion as they move towards the electrode and giving the deposited electrons a wider
233 spread over the cathode surface. All these dispersion effects could very slightly affect the
234 memory effect of the micro-discharges. This effect might be very small as filaments are
235 indeed observed for every flow rate, but it could be understood as a minimal step towards
236 homogenizing the discharge (which would be the result of having no memory effect at all).
237 Nevertheless, this effect could suffice to slightly disperse the micro-discharge remnant and
238 moderately widen the spot where a next micro-discharge could occur, hence resulting in an
239 enlargement of the filament width.

240 Based on this hypothesis, we propose a dependence between the filament width and the
 241 velocity of the fluid, which has an effect in the time a molecule spends in a filamentary region
 242 (duration of the pulse in terms of the model, Δt_{fil}). As stated above, the duration of the pulse
 243 has a great impact on the CO₂ conversion and it is what really drives the results for a constant
 244 number of pulses, num_{pulses} . Therefore, equations 5 and 6 are proposed, where the values
 245 of K_v and b are parameters to be found by minimizing the difference between experimental
 246 and theoretical conversion figures for every flow rate value.

$$247 \quad \Delta Z_{fil} = K_v \times \langle v \rangle^b \quad (5)$$

$$248 \quad \Delta t_{fil} = \frac{\Delta Z_{fil}}{\langle v \rangle} = \frac{K_v \times \langle v \rangle^b}{\langle v \rangle} \quad (6)$$

249 Hence, as long as b is positive and smaller than 1, this effect could moderate the negative
 250 effect that a higher velocity has on the conversion values predicted by the model. In this way,
 251 the duration of the pulse Δt_{fil} (or the width of the filament, ΔZ_{fil}) works as the second fitting
 252 parameter of this model.

253

254 2.5. Electron density in one filament – *micro-discharge scale*

255 Considering the velocity of the fluid and the width of one filament, the time spent by a
 256 molecule inside the filament (model-wise, the duration of the pulse Δt_{fil}) ranges from around
 257 15000 to 37000 μ s. In that period of time, around 300 to 700 micro-discharges occur, as the
 258 frequency of the applied voltage is 9 kHz. This means, there is one micro-discharge every 56
 259 μ s ($\Delta t_{micro-discharge}$), each of them consisting of 30 ns of an actual micro-discharge
 260 (electron avalanche and plasma channel) plus an afterglow until the next micro-discharge. In
 261 our model, this happens every time the element of volume passes through a filament (that is
 262 num_{pulses} times). See Figure 2 for a comparison between the different scales involved.

263 For this behaviour to be computationally represented, a time step in the order of a fraction of
 264 a nanosecond would be needed. Then, it would require around 10^{10} time-steps numerically
 265 integrated to build up to a residence time of around tens of seconds. For this reason, the
 266 hundreds of micro-discharges taking place when the element of volume passes through a

267 filament will be averaged over the period of time inside that filament Δt_{fil} . The purpose of
 268 this simplification is to obtain an average electron density Ne_{av} valid for the whole period
 269 inside the filament, Δt_{fil} . Then, the number of micro-discharges in one filament can be
 270 expressed as in equation 7, leading to equation 8 for Ne_{av} .

$$271 \quad num_{micro-discharges} = \Delta t_{fil} \times 9 \text{ kHz} \times 2_{half-cycles} = \frac{\Delta t_{fil}}{\Delta t_{micro-discharge}} \quad (7)$$

$$272 \quad \int_0^{\Delta t_{fil}} Ne_{av} dt = num_{micro-discharges} \times \int_0^{\Delta t_{micro-discharge}} Ne(t) dt \quad (8)$$

273 As stated above, the plasma electrons during a micro-discharge are considered to last for
 274 around 30 ns [43], peaking somewhere in that interval and becoming zero from 30 ns onwards
 275 until the next micro-discharge (until $\Delta t_{micro-discharge}$ is reached). According to the
 276 literature, the electron density Ne can reach values around 10^{12} - 10^{14} cm^{-3} [43]. Thus, the
 277 electron density in one micro-discharge will be modeled as a function of time standing at 0
 278 cm^{-3} at 0 ns, promptly reaching a maximum of $1 \times 10^{13} \text{ cm}^{-3}$ at 3 ns and subsequently falling
 279 steadily to 0 cm^{-3} at 30 ns ($Ne(t)$). Then, the right hand side of equation 8 would modify as
 280 in equation 9.

$$281 \quad \int_0^{\Delta t_{fil}} Ne_{av} dt = num_{micro-discharges} \times \left[\int_0^{30 \text{ ns}} Ne(t) dt + \int_{30 \text{ ns}}^{\Delta t_{micro-disc.}} 0 dt \right] \quad (9)$$

282 From then on, an average electron density that is valid for the duration of one filament in our
 283 model (Δt_{fil}) can be obtained as expressed in equations 10 and 11.

$$284 \quad Ne_{av} \cdot \Delta t_{fil} = num_{micro-discharges} \times \left[\int_0^{30 \text{ ns}} Ne_{micro-disc.}(t) dt \right] \quad (10)$$

$$285 \quad Ne_{av} = \frac{1}{\Delta t_{micro-discharge}} \times \left[\int_0^{30 \text{ ns}} Ne_{micro-disc.}(t) dt \right] \quad (11)$$

286 In this way, an average electronic density of $4 \times 10^9 \text{ cm}^{-3}$ is obtained, which will be considered
 287 constant for the duration of the pulse in our model (Δt_{fil} , which as it has been said, involves
 288 thousands of micro-discharges). This value will be used for all calculations over the range of
 289 power and flow rate values covered in this study. It should be noted that this value depends

290 on the duration of the pulse (30 ns) and $\Delta t_{micro-discharge}$ (which depends on the frequency
291 of the applied voltage, 9 kHz) rather than on Δt_{fil} .

292 To the best of our knowledge, an electron density of $1 \times 10^{13} \text{ cm}^{-3}$ is a reasonable value to base
293 our approximation on as it is within the range of values reported for DBD reactors 10^{12} - 10^{14}
294 cm^{-3} . Furthermore, values in this region have been used in several published modelling works
295 [28–34]. However, our calculated conversion is very sensible with respect to the electron
296 density. Hence, the latter is acting as a third fitting parameter of our model, even though it is
297 not intended to. This leads to a discussion about what a relatively arbitrarily chosen electron
298 density means for the simulation. Several plasma phenomena lie under this umbrella over
299 which we do not have control and cannot model accurately. Moreover, even if we could
300 measure the electron density precisely, the only way we could account for those phenomena
301 is to have an average electron density that yields good agreement with the experiments in
302 terms of CO_2 conversion.

303 For these reasons, we consider this approach acceptable as long as the electron density fits
304 within the reported values for DBD reactors. From a maximum electron density of 1×10^{13}
305 cm^{-3} , the average electron density of $4 \times 10^9 \text{ cm}^{-3}$ arises. It should be mentioned that the exact
306 same figure has been used for all calculations in this work.

307

308 2.6. Summary of the reactor model

309 For the reasons exposed above, our model consists of a number of pulses (num_{pulses}) that
310 occur every $\Delta t_{fil-to-fil}$ seconds. Each pulse will have a constant electronic density
311 $Ne_{average}$ held for Δt_{fil} and an interpulse of around $(\Delta t_{fil-to-fil} - \Delta t_{fil})$ seconds with no
312 plasma electrons, until the element of volume reaches the next filament or pulse (see Figure
313 2). This new approach implies a very low computational cost, which allows us to perform
314 calculations effectively (typically in the order of hours of computational time). Table S1
315 summarises the parameters of each calculation performed in this work.

316 As described above, the unknown physical aspects of a DBD discharge lead to the three
317 fitting parameters of this model, namely, the frequency of pulses (f_{pulses}), the duration of the

318 pulse (Δt_{fil}) and the average electron density (Ne_{av}). The former is related to the spacing
319 between filaments $\Delta t_{fil-to-fil}$ and represents the effect of the discharge power in the
320 conversion of CO₂. The second fitting parameter represents the time spent by a molecule
321 inside a filament and depends on the fluid velocity or flow rate. Notably, the ratio between
322 Δt_{fil} and $\Delta t_{fil-to-fil}$ is equal to that between the plasma volume and the total reactor
323 volume. At this point, it should be highlighted that this selection of fitting parameters is
324 equivalent to that of other zero-dimensional models [29–34]. However, the way in which
325 these fitting parameters are derived in our model results in a narrower range of reasonable
326 values for them (no more than one order of magnitude in both cases).

327 Finally, the electron density is not intended as a fitting parameter, however it should be
328 regarded as such since the conversion predicted by the model is very sensitive to it. Although
329 this limits the reliability on our model, there is no further improvement we could do at the
330 moment. The average electron density is calculated considering a maximum electron density
331 of $1 \times 10^{13} \text{ cm}^{-3}$ and a micro-discharge duration of 30 ns. Both values agree with the state of
332 the art of plasma kinetic modelling of DBD reactors [29–35].

333 2.7. Chemical model

334 For the chemical model, a reduced set of reactions developed and reported in [31] was
335 employed. This reduced set consists of 9 species (see Table S2) and 17 reactions, which
336 implies a much lower computational cost than the complete set (around 42 species and 500
337 reactions) [28,31,33]. The reactions considered, shown in Table 1, involve 7 electron impact
338 reactions (R1 to R7), as well as 5 reactions among ions (R8 to R12) and 5 between neutral
339 species (R13 to R16). As regards CO₂ conversion by electron impact reactions, the main
340 mechanisms identified in [28] are taken into account, i.e., electron attachment (R1), electron
341 impact dissociation (R2) and total ionisation (R3). Vibrationally excited states of CO₂ were
342 not taken into account in this model for the reasons presented in Section 0.

343 In addition, Electron impact dissociation reactions were considered for O₃ and O₂ (R4 and
344 R5, respectively), while for the latter two electron attachment reactions were also included
345 in the model (R6 and R7). The significance of these reactions for the simplified model relies
346 partially on the fact that they compete with CO₂ decomposition reactions for the plasma

347 electrons, causing the CO₂ conversion to flatten as the O₂ and O₃ densities increase. Among
 348 the ionic and neutral reactions, recombination processes of O atoms (or anions) with CO to
 349 form CO₂ are also part of the reaction set. Likewise, these reactions contribute to flatten the
 350 conversion of CO₂ at long residence times [31]. For further details on this model and its
 351 validity, refer to [31].

352 *Table 1 - Reduced reactions set. All rate constants in cm³s⁻¹ unless indicated otherwise.*

No.	Reaction	Rate constant	Reference	Note
R1	e + CO ₂ → e + e + CO ₂ ⁺	f(σ)	[45]	1
R2	e + CO ₂ → CO + O + e	f(σ)	[45]	1
R3	e + CO ₂ → CO + O ⁻	f(σ)	[45]	1
R4	e + O ₃ → O + O ₂ + e	f(σ)	[46]	1
R5	e + O ₂ → e + O + O	f(σ)	[45]	1
R6	e + O ₂ → O + O ⁻	f(σ)	[45]	1
R7	e + O ₂ + M → O ₂ ⁻ + M	f(σ)	[46]	1,2
R8	O ⁻ + CO → e + CO ₂	6.50×10 ⁻¹⁰	[31]	-
R9	O ⁻ + O ₂ → e + O ₃	1.00×10 ⁻¹²	[31]	-
R10	O ⁻ + O ₃ → e + O ₂ + O ₂	3.00×10 ⁻¹⁰	[31]	-
R11	e + CO ₂ ⁺ → CO + O	6.50×10 ⁻⁰⁷	[31]	-
R12	O ₂ ⁻ + CO ₂ ⁺ → CO + O ₂ + O	6.00×10 ⁻⁰⁷	[31]	-
R13	O + O + M → O ₂ + M	5.2×10 ⁻³⁵ e ^(900/T[K])	[31]	2
R14	O + O ₂ + M → O ₃ + M	4.5×10 ⁻³⁴ (T[K]/298) ^{-2.70}	[31]	2
R15	O + O ₃ → O ₂ + O ₂	8.0×10 ⁻¹² e ^(-17.13/T[K])	[31]	-
R16	O + CO + M → CO ₂ + M	1.7×10 ⁻³³ e ^(-1510/T[K])	[31]	2
R17	O ₃ + M → O ₂ + O + M	4.1×10 ⁻¹⁰ e ^(-11430/T[K])	[31]	2

1. Rate coefficient calculated by BOLSIG+ solver for a given EEDF.
2. Three-body process, rate coefficients in cm⁶s⁻¹

353

354 2.8. Vibrationally excited states of CO₂

355 The role of vibrationally excited states of CO₂ in its dissociation and the decision to exclude
 356 them from the chemistry set is addressed in this section. A fluid model for CO₂ dissociation

357 reactions in a parallel DBD reactor including an extensive description of the vibrational
358 kinetics can be found in [47]. Treanor *et al.* [48] showed that under conditions characterised
359 by a vibrational temperature well greater than the translational temperature, a population
360 inversion in the energy levels can be achieved. Therefore, as discussed in [33,43], these
361 largely populated highly excited anharmonic vibrational levels are deemed crucial for the
362 dissociation of the CO₂ molecule. In this regard, a study of the vibrational distribution
363 function for CO₂ comparing MW and DBD discharges (at 20 Torr and atmospheric pressure,
364 respectively) can be found in [33]. According to their results, the population of high
365 vibrational states is a result of the rates of (or the competition between) the different processes
366 involved, namely, electron impact vibrational excitation (exciting CO₂ molecules),
367 vibrational-vibrational exchange collisions (which favour highly excited states) and
368 vibrational-translational relaxations (which de-excite vibrationally excited CO₂ molecules as
369 it thermalises the gas). In addition, there are factors that favour or impede the different
370 mechanisms involved. For instance, a long duration of a plasma pulse will favour vibrational
371 excitations as it implies availability of free energetic electrons. On the other hand, a high
372 pressure will contribute to the de-excitation of CO₂ molecules back to their ground state.
373 Indeed, it is concluded that the pressure enhances the reaction rate of vibrational-translational
374 (VT) transitions as collisions with ground state CO₂ molecules are more likely [33].

375 Interestingly, MW discharges represent a plasma duration in the order of the milliseconds
376 (far greater than DBD in the order of nanoseconds) and are usually performed at low
377 pressures, which favours largely populated high vibrational states that can certainly lead to
378 dissociation. On the other hand, DBD discharges are often performed at atmospheric pressure
379 so the vibrational-translational relaxations are orders of magnitude faster than in a low
380 pressure MW discharge (in a DBD reactor, vibrationally excited states can thermalise in a
381 few microseconds). Moreover, DBD microdischarges last for a very short time (in the order
382 of nanoseconds), which is detrimental for the electron impact vibrational excitations. The
383 vibrational excitation gained in a microdischarge (lasting for nanoseconds) is then
384 thermalised (lost) before the next microdischarge takes place (after several microseconds).
385 These factors explain why long-lasting large populations of high vibrational states are not
386 achieved in DBD discharges, thus CO₂ dissociation must proceed through other mechanisms
387 such as electronic excitations [33].

388 2.9. Plasma kinetic model – cross sections data

389 The rate coefficients for electron impact reactions were calculated by the Boltzmann solver
390 BOLSIG+ [40] implemented in the ZDPlasKin Fortran module as a function of the
391 corresponding cross sections. Cross section data was retrieved from different databases
392 within the LXCat project [41]. It should be highlighted that the Electron Energy Distribution
393 Function (EEDF) was calculated based on complete and consistent (whenever possible) sets
394 of cross sections for each involved species. The complete and consistent IST-Lisbon
395 Database reported in [37] and available in LXCat ([41]) was used for CO₂ and O₂ processes.
396 Importantly, this cross section data has been validated against measured swarm data [37].
397 For CO, O₃ and O species, complete cross section data sets from Morgan database were
398 adopted [46]. The cross sections for the three body recombination R7 were also taken from
399 the latter database. With all this data, the EEDF was calculated and then used to integrate the
400 corresponding cross sections in order to obtain the rate coefficients of the electron impact
401 reactions included in the model (R1 to R7). Specific references to the databases can be found
402 in Table 1 and a list of the collisional processes considered for the calculation of the EEDF
403 is included in the Supporting Information (Table S4).

404 Regarding the completeness of the IST-Lisbon database for CO₂ processes, it should be noted
405 that only one superelastic collisional process is included, namely, de-excitation from $v_1 \equiv$
406 (010) to the ground level, v_0 . This is the dominant de-excitation process while a second
407 superelastic process would be required for a better accuracy of the calculated swarm
408 parameters at reduced electric fields below ~ 1 Td [37], which is not the case in this study. In
409 addition, the effect of the superelastic process $v_1 \rightarrow v_0$ is particularly important at low
410 electric fields but barely noticeable above 10 Td [37], while our work considers 56 Td.

411 Although the superelastic collision $v_1 \rightarrow v_0$ is included in the set, the number density of
412 CO₂(v_1) will always be zero since vibrationally excited states of CO₂ were not considered in
413 this model (see Section 0). Thus, this superelastic collision will never account for an energy
414 gain towards the EEDF. To assess the impact of this approximation, the EEDF calculated
415 with BOLSIG+ for the case of this study (no CO₂(v_1)) was compared with that obtained for
416 a relative CO₂(v_1) population of 0.076 at 300K, according to [37]. The results indicate that
417 EEDFs considering superelastic collisions tend to be slightly shifted towards higher electron

418 energies (as these processes can effectively transfer energy back to the electrons). Then, our
419 approximation could result in a minor underestimation of the electron impact rate
420 coefficients. However, the effect of superelastic collisions in the EEDF vanishes for reduced
421 electric fields beyond 10 Td and this approximation is considered suitable for our work. A
422 comparison of the calculated EEDFs, electron energies and rate coefficient for both cases at
423 different electric fields can be found in the Supporting Information (Figures S1-S5 and Table
424 S4).

425 The rate coefficient for CO₂ dissociation through electron impact excitation deserves a
426 special mention as this process has been reported to be the dominant mechanism for CO₂
427 conversion in DBD reactors [32]. Hence, the cross section data employed for its calculation
428 is a crucial factor for the validity of the model and the results obtained. Numerous cross
429 section data sources are available for the CO₂ electron impact excitation and the direct
430 association of these processes with CO₂ dissociation has been extensively studied in [32] and
431 [37]. To start with, the IST-Lisbon dataset is based on the excitation processes described by
432 Phelps [49], with thresholds of 7 and 10.5 eV. These cross sections have been extended to a
433 wider range of electron energy as described in [45]. However, these cross sections are likely
434 to involve more processes than only dissociation, as explained in [37]. Then, assigning
435 Phelps's 7 and 10.5 eV cross sections to CO₂ dissociation is not straightforward and may
436 result in an overestimation of the dissociation rate coefficients, as proved in [32] and [37].
437 On the other hand, Itikawa's Database ([50]), also available in LXCat, has been widely used
438 in studies involving zero-dimensional plasma kinetic models [28–31]. However, this dataset
439 has been recently reported to underestimate the CO₂ dissociation reaction rate coefficients
440 [32,37]. Besides, Polak and Slovetsky's cross sections [38] have been reported to
441 satisfactorily represent CO₂ dissociation. In this theoretical study, the authors described a
442 total dissociation cross section showing two energy thresholds, in a similar fashion as
443 Phelps's 7 and 10.5 eV datasets. Regardless of the shape, Polak's cross sections are much
444 smaller in magnitude than those of Phelps, which could contribute to compensate the
445 overestimation reported for the latter dataset [32,37]. Among these and other excitation cross
446 sections, Phelps's 7 eV and Polak's datasets appear to be the most suitable to model CO₂
447 dissociation, according to results in [32] and [37], respectively.

448 In this work, the recommendation given by the authors of the IST-Lisbon Database was
449 followed [37]. Therefore, Polak and Slovetsky's CO₂ dissociation total cross section data was
450 used to calculate the CO₂ dissociation rate coefficient (R2). Nevertheless, these cross sections
451 were integrated over the EEDF calculated with the IST-Lisbon Database complete and
452 consistent set of cross sections (excluding Polak's cross sections).

453 **3. Results and Discussion**

454 3.1. Validation of the model – average electron density

455 The averaging procedure described in section 2.5 has been verified with the calculation
456 described below. A simulation of one single filament has been performed, involving 662
457 micro-discharges (modelled as 30 ns-long pulses) repeated every 55.6 μs
458 ($\Delta t_{micro-discharge}$). Then, each micro-discharges has an afterglow of (55.6 μs - 30 ns)
459 seconds. This $\Delta t_{micro-discharge}$ corresponds to a frequency of 9 kHz (that of the applied
460 voltage) and covers a reaction time of 3.67×10^{-2} seconds, i.e. Δt_{fil} in this verification
461 ($\Delta t_{micro-discharge} \times num_{microdischarges}$). This $num_{microdischarges}$ and Δt_{fil} corresponds
462 to the calculations with a flow rate of 25 mL/min. The electron density in this case was a
463 function of time peaking at 1×10^{13} cm⁻³ in an interval of 30 ns, as described in section 2.5.
464 Then, the conversion computed by such calculation was compared with that of a calculation
465 consisting of an average electron density of 4×10^9 cm⁻³ (as found in section 2.5) kept constant
466 for 3.67×10^{-2} seconds. The results are 0.3029 % and 0.3028 %, respectively. The absolute
467 error is 0.0001 % while the relative error equals 0.0003 (0.03%). Therefore, it can be
468 concluded that this approximation is reliable for the conditions being addressed in this paper.
469 This involves low temperatures (300 K) and low conversion values, where the chemistry of
470 the system is not too complex and the contribution of reactions between heavy particles in
471 the afterglow is orders of magnitude smaller than that of electron impact processes during
472 the pulse.

473 The computational time saved through this approximation outweighs any concern about the
474 already negligible error introduced by it. The first calculation (662 pulses) ran for 7.5 hours,
475 that is, 450 minutes. By contrast, it took less than a minute to complete the averaged

476 calculation, therefore resulting in a time saving of more than 99%. Thus, we consider this
477 approximation not only reliable but also necessary within this particular framework.

478 3.2. Validation of the model – matching experimental data

479 The validity of the model is only achieved once its results are contrasted with the
480 experimental measurements it intends to represent. Selectivity towards CO varies around 96-
481 98 % for every case, making it useless to compare laboratory measurements with the model
482 results. Therefore, only CO₂ conversion will be used to match the experimental and
483 calculated values. Overall, for the model proposed in this work, the calculated conversion
484 figures are in very good agreement with the experimental data, with only one measurement
485 having a relative error above 5%. The complete set of results including every calculation is
486 presented in Table 2. Table 2 - Results. In addition, results are displayed graphically in Figure
487 3 and Figure 4 for variable power and flow rate figures, respectively. Combined results in
488 terms of SEI (specific energy input, defined as the ratio between the power and the flow rate)
489 are presented in Figure 5. The definitions of the variables used to process the data are as
490 follows.

$$491 \quad \text{Conversion (\%)} = \frac{\text{CO}_2 \text{ Converted } \left(\frac{\text{Mol}}{\text{s}}\right)}{\text{CO}_2 \text{ Input } \left(\frac{\text{Mol}}{\text{s}}\right)} \quad (12)$$

$$492 \quad \text{SEI (J/mL)} = \frac{\text{Power (W)} \times \frac{60 \text{ s}}{1 \text{ min}}}{\text{Flow rate } \left(\frac{\text{mL}}{\text{min}}\right)} \quad (13)$$

$$493 \quad \text{Energy Efficiency (\%)} = \frac{\text{CO}_2 \text{ Converted } \left(\frac{\text{Mol}}{\text{s}}\right) \times \Delta H^\circ_{\text{CO}_2 \text{ Splitting}} \left(\frac{\text{J}}{\text{mol}}\right)}{\text{Power (W)}} \quad (14)$$

494 Where the reaction enthalpy of the CO₂ decomposition reaction is $\Delta H^\circ_{\text{CO}_2 \text{ Splitting}} = 280 \frac{\text{kJ}}{\text{mol}}$

495

496 3.2.1 Effect of discharge power

497 As can be seen graphically in Figure 3, the calculated conversion curve over power variations
498 seems to satisfactorily represent the experimental data. The major deviation is found at 50 W
499 (SEI = 120 kJ/L, see Figure 3), where the calculated conversion is 0.3% greater (a relative
500 error of 1.3%). It is expected that higher power values lead to inaccuracies in the model as it

501 is not able to predict saturation. In fact, a similar behaviour has been reported previously for
 502 SEI figures above 100 kJ/L [31]. However, the system becomes inefficient beyond that SEI
 503 value. The model has been optimized for the range of parameters that yield relatively high
 504 efficiencies, while deviations are expected to occur outside those ranges. Indeed, the range
 505 of applicability of this model covers the most relevant operating conditions in terms of energy
 506 efficiency. As regards conversion, it is noticeable that values up to around 20% can be
 507 modelled accurately with the current reduced chemistry set, as opposed to the reported limit
 508 of 15% [31]. This difference may be related to the chosen Polak's cross sections for the
 509 electron impact CO₂ dissociation reaction as it affects the relative contribution of the different
 510 processes leading to CO₂ splitting.

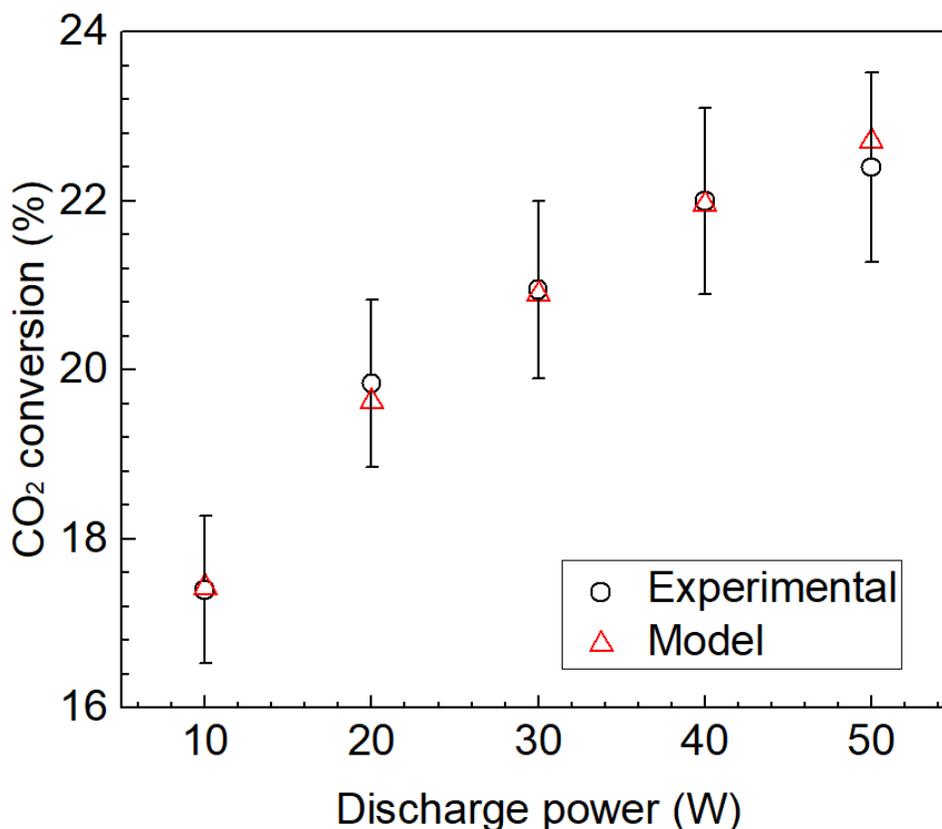
511 *Table 2 - Results. All calculations with i.d. (quartz tube) = 22 mm, o.d. (high voltage*
 512 *electrode) = 17 mm, gap = 2.5 mm, length = 100 mm.*

Flow rate	Power	SEI	EXP. CO₂ Conversion	MODEL CO₂ Conversion	Relative error ¹	EXP. Efficiency	MODEL Efficiency
mL/min	W	kJ/L	%	%	%	%	%
25.0	10	24	17.4	17.4	0.2	8.3	8.3
25.0	20	48	19.8	19.6	1.1	4.7	4.7
25.0	30	72	21.0	20.9	0.3	3.3	3.3
25.0	40	96	22.0	22.0	0.2	2.6	2.6
25.0	50	120	22.4	22.7	1.3	2.1	2.2
25.0	50	120	22.4	22.7	1.3	2.1	2.2
31.2	50	96	20.8	20.9	0.3	2.5	2.5
41.2	50	73	18.0	18.8	4.7	2.8	2.9
62.5	50	48	15.8	16.0	1.5	3.7	3.8
125.0	50	24	12.6	12.0	5.5	6.0	5.7

1. The relative error is defined as the difference between the experimental and model conversions divided by the average of both.

513 3.2.2 Effect of flow rate

514 On the other hand, the model provides acceptable yet less satisfactory results for the
 515 calculations involving variable flow rate. In most cases, the calculated results seem to
 516 overestimate the CO₂ conversion. It can be seen in Figure 4 that this positive error is balanced
 517 by a negative error as the flow rate grows. In fact, the conversion for 125 mL/min is indeed
 518 underestimated by 0.6 % (relatively, 5.5 %). Overall, these results are deemed to be
 519 acceptable in terms of variable flow rate.



521

522

Figure 3 – CO₂ conversion at different discharge powers and 25 ml/min.

523

3.2.3 Overall results

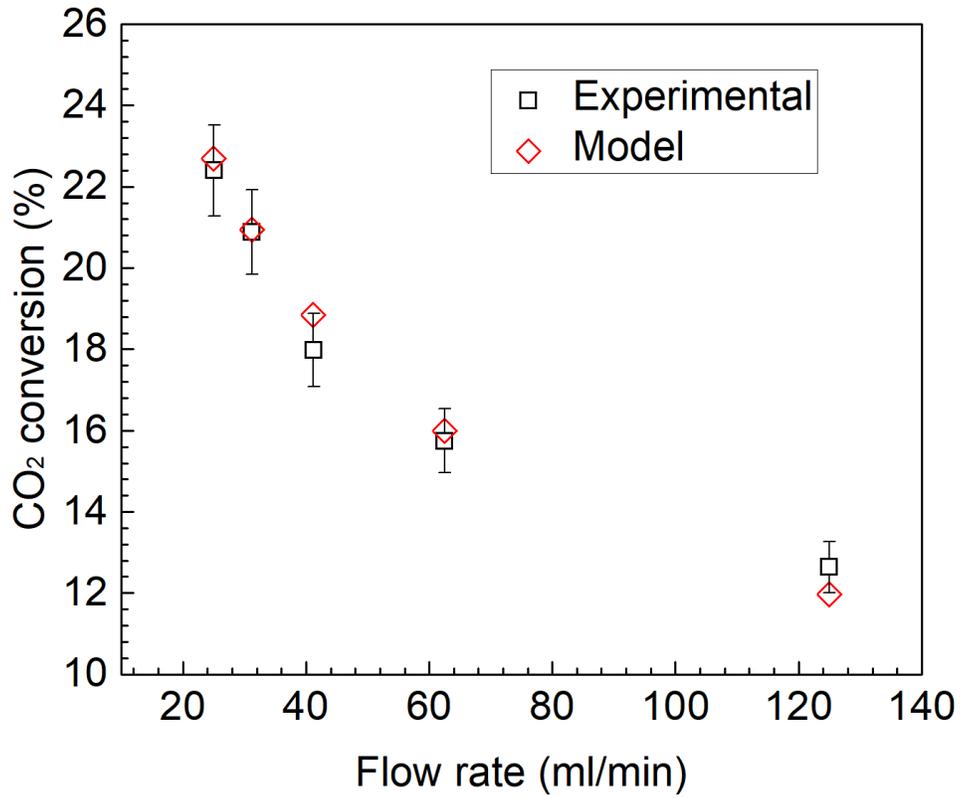
524

According to our results, this model has proved to accurately represent the chemistry of the system up to conversion values of around 20%, with power values ranging from 10 up to 40 W. However, the remaining calculation with variable power (50 W) results in a conversion figure that is slightly higher than the experimental one. In addition, almost every calculation with variable flow rate shows discrepancies with the laboratory measurements, regardless of the conversion value (all of them considering 50 W).

530

Overall, the proposed model presents a reasonable agreement with the experimental measurements in terms of CO₂ conversion for the full range of experimental measurements taken into account. Thus, this validates the model and indicates it is reliable enough so as to analyse the reaction mechanism based on its results (see Section 3.3).

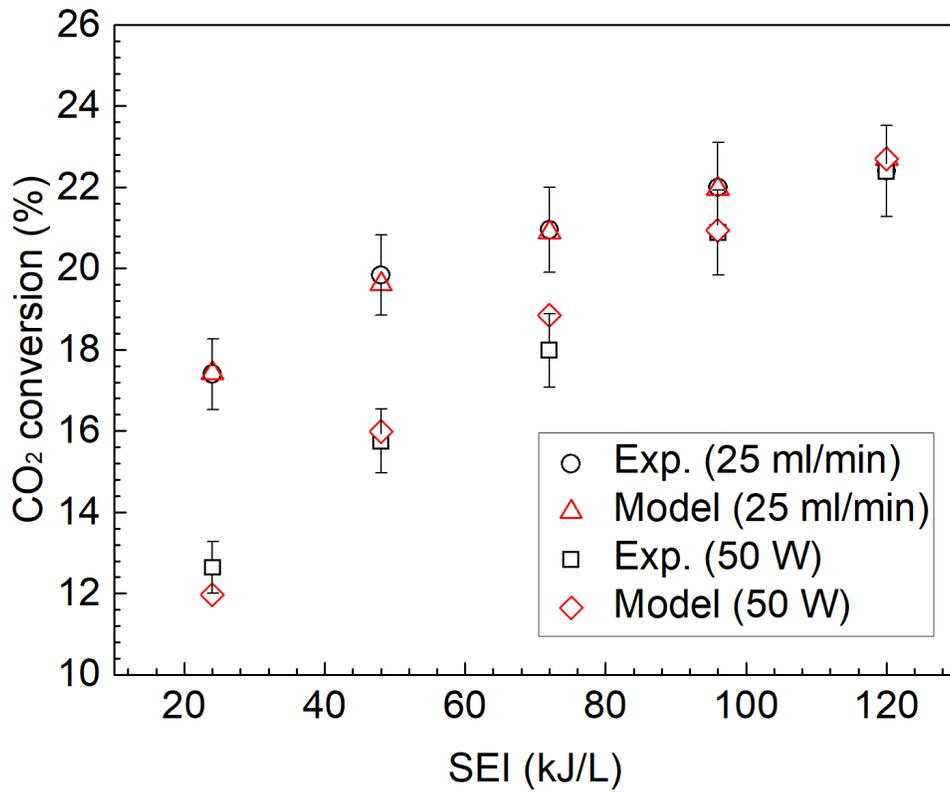
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536

Figure 4 – CO₂ conversion at different flow rates and 50 W.



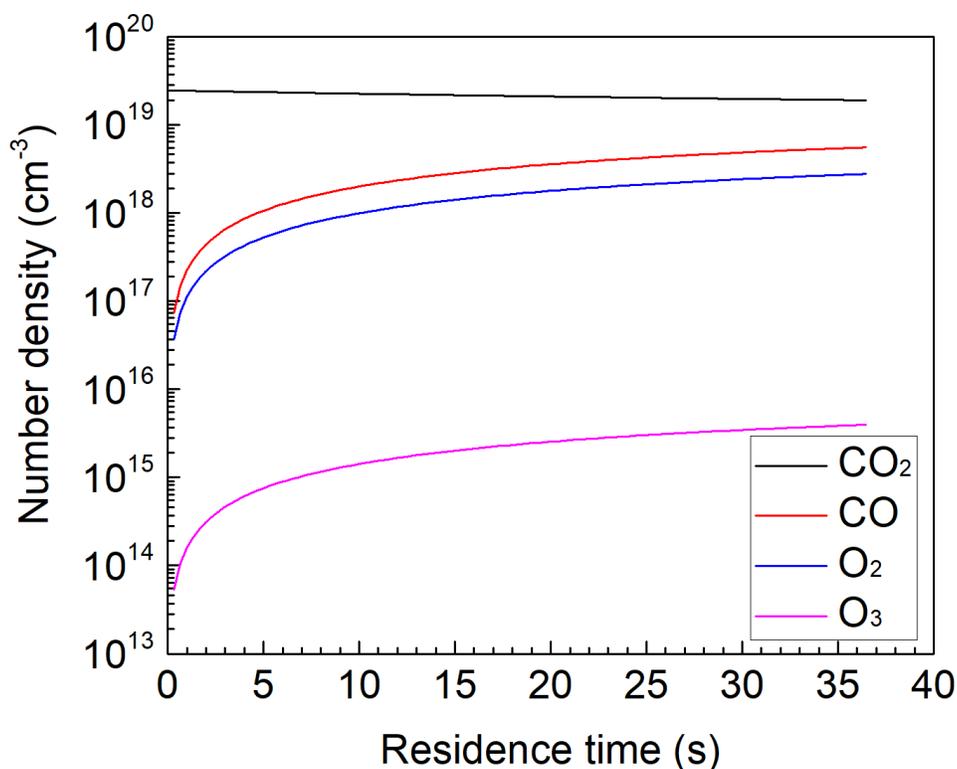
537

538 *Figure 5 – CO₂ conversion at different SEI values by changing discharge power or CO₂*
539 *flow rate.*

540

541 3.3. Reaction pathways analysis

542 As mentioned above, in this study we employed a reduced chemistry set for the conversion
543 of CO₂ developed and reported in [31], consisting of 9 species and 17 reactions (see Table
544 1). Such simplification may lose reliability at higher conversion values as the chemistry of
545 the system becomes more complex and neglected reactions become relevant. However, it
546 seems that point has not been reached in this study. According to our results, the entire range
547 of conversion covered by the experiments in [36] is well reproduced by the calculations
548 yielding a reasonable agreement in every case.



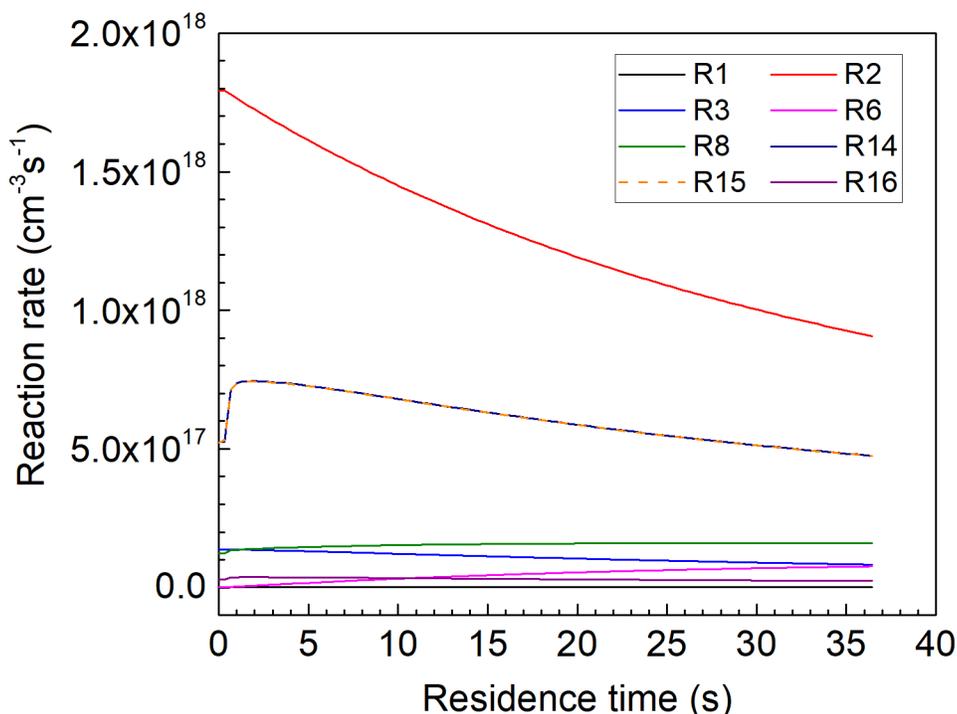
549

550 *Figure 6 – Number density of CO₂, CO and O₂ and O₃ (25 mL/min and 50 W)*

551

552 As the experiments intended to model were performed at atmospheric pressure and ambient
553 temperature, the initial CO₂ number density is set to $2.45 \times 10^{19} \text{ cm}^{-3}$ in all cases. This figures

554 drops to $1.89 \times 10^{19} \text{ cm}^{-3}$ for the highest conversion achieved (22.7%). The main products of
 555 these reactions are CO and O₂, with final number densities of about $5.56 \times 10^{18} \text{ cm}^{-3}$ and
 556 $2.77 \times 10^{18} \text{ cm}^{-3}$, respectively (also for a conversion of 22.7%). The major by-product is O₃,
 557 several orders of magnitude below the final density of O₂ ($3.96 \times 10^{15} \text{ cm}^{-3}$). These results are
 558 illustrated in Figure 6.



559

560 *Figure 7 - Reaction rate of main reactions (25 mL/min and 50 W)*

561

562

Mechanisms for CO₂ splitting and recombination

563 As stated above, the reduced reactions set considered for this study includes three possible
 564 mechanisms for CO₂ decomposition, namely, electron attachment (R1), electron impact
 565 dissociation (R2) and electron impact total ionisation (R3). Their relative contributions to the
 566 observed conversion figures will be determined by their rate coefficients which in turn
 567 depend heavily on the cross sections used for each process. As it has been mentioned, Polak
 568 and Slovetsky's cross sections were used for the electron impact dissociation [38] while the
 569 IST-Lisbon database available in LXCat were used for the remaining two reactions [45].
 570 With these cross sections, the BOLSIG+ solver predicts that the highest rate coefficient is

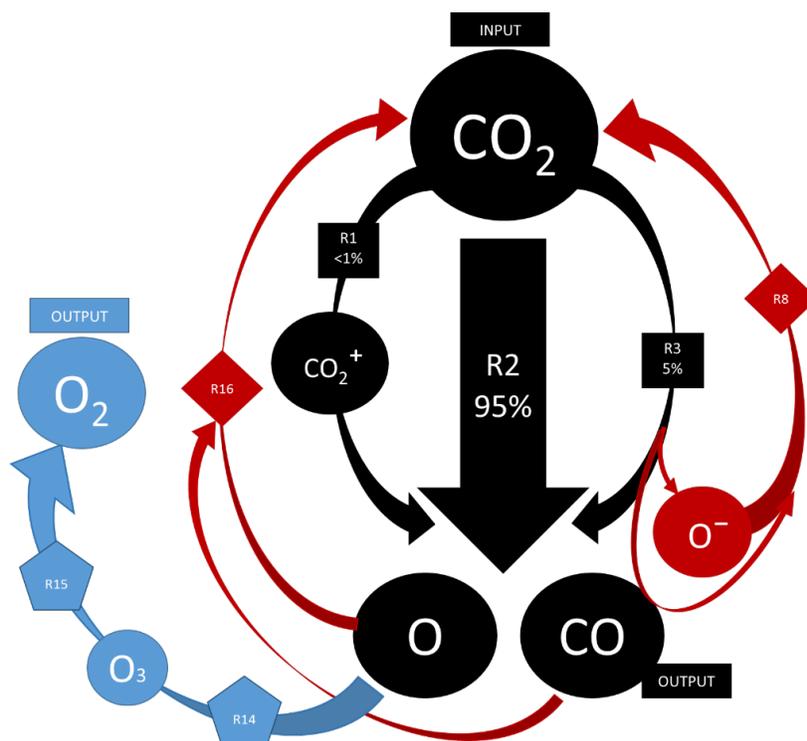
571 that of the electron impact dissociation, R2 (around $1.9 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$ for initial conditions).
572 The electron attachment reaction (R3) has a rate coefficient of around $9.1 \times 10^{-13} \text{ cm}^3 \text{ s}^{-1}$ at
573 initial conditions while that of the total ionisation (R1) is even an order of magnitude lower
574 ($2.9 \times 10^{-14} \text{ cm}^3 \text{ s}^{-1}$). With these results, it can be concluded that the electron impact
575 dissociation is the dominant mechanism for CO_2 splitting accounting for around 95% of the
576 conversion. The electron attachment represents the remaining 5% while the contribution of
577 the total ionisation to the CO_2 conversion is negligible (see Figure 7 for a comparison
578 between reaction rate values). This is in qualitative agreement with the results reported by
579 Ponduri *et al.* [47], while the relative contribution of each dissociation channel changes
580 quantitatively. The latter study consists of a DBD time- and space-dependent fluid model
581 including an exhaustive description of the vibrational kinetics of CO_2 . The authors also
582 conclude that the electron impact dissociation represents the main channel for CO_2
583 dissociation, accounting for approximately 80% of the CO production. In addition, our results
584 qualitatively agree with [32,37]. These DBD models predicted a more balanced contribution
585 of these processes as a result of the cross sections used [28–31]. It should be mentioned that
586 the study from where the reduced set of reactions was taken ([31]) used Itikawa's dataset, as
587 stated in [32]. As described in Section 2.9, this database has been proven to underestimate
588 the electron impact dissociation rate coefficient (compared to the Polak's dataset to be used
589 in this study), making its contribution comparable to that of the total ionisation reaction.

590 It should be highlighted that the reduced electric field in all these calculations is 56 Td
591 according to the experimental measurements (Lissajous figures) [36,42]. This yields an
592 average electron energy of around 2.21 eV. According to the literature, the contribution of
593 the total ionisation overtakes that of the electron attachment by several orders of magnitude
594 at higher E/N values, which are out of the scope of this work [32].

595 The CO produced is rather stable in the plasma and therefore it is the major product of this
596 reaction. Nevertheless, this molecule does take part in some recombination reactions (R8 and
597 R16). The recombination with oxygen anions (O^- , R8) accounts for 73% of the CO loss
598 processes, whereas the three-body recombination with O radicals represents the remaining
599 27%. See Figure S5 for a comparison between the reaction rates of minor contributing
600 reactions (excluding R2, R14 and R15).

601 Regarding O radicals, the recombination with CO molecules (R16) is not their main
 602 consumption mechanism as its rate coefficient is one order or magnitude lower than that of
 603 other processes involving these species. After an initial prevalence of reaction R13 which
 604 builds up an initial O₂ density, reactions R14 and R15 take over. These reactions require an
 605 initial concentration of O₂ and O₃ to occur and became preponderant once achieved. Their
 606 reaction rates are almost indistinguishable from one another, both being in and around ~
 607 $6 \times 10^{17} \text{ cm}^{-3} \text{ s}^{-1}$ (see Figure 7). These two reactions with high rates explain the formation of
 608 O₂ in this chemistry set. The main reaction mechanisms within this chemistry set are depicted
 609 in Figure 8, where black arrows represent CO production while blue ones denote O₂
 610 production. Recombination reactions are indicated with red arrows.

611



612

613

Figure 8 - Scheme of the proposed reaction mechanism

614

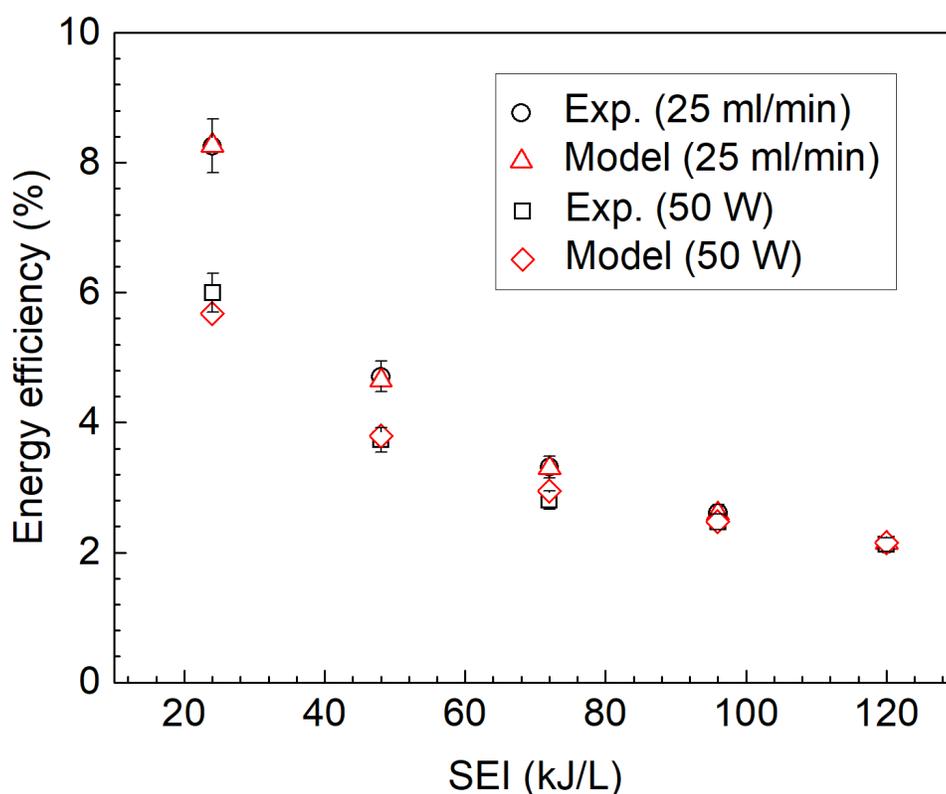
615 3.4. Energy efficiency

616

A discussion on the energy efficiency of this system is presented in this section. The values
 617 obtained for these experiments and calculations are presented in Table 2 and shown in Figure

618 9. An analysis of the agreement between the model and the experimental results will not be
619 included as it is essentially the same as that of the conversion, already addressed above. By
620 contrast, it is relevant to compare the efficiency values obtained with what has been
621 previously reported for CO₂ splitting in DBD reactors, as well as to discuss the potential
622 reasons for the efficiency achieved.

623 DBD reactors are known for their low efficiency in CO₂ splitting reactions, rarely exceeding
624 10%. An exhaustive collection of data on DBD energy efficiency can be found in [26,27].
625 The values presented in this work fit within that description and also the decrease in the
626 efficiency as the SEI grows is also consistent with the literature. A maximum efficiency of
627 8.3% was found in this work for a rather low conversion of 17.4%. For higher conversion
628 values, the efficiency drops down to, for instance, 2.2% at a conversion of 22.7%. The
629 dependence of the efficiency with the power seems to be somewhat stronger than with the
630 flow rate. A further analysis of these values can be found in the study from where the
631 experimental data has been taken [36]. In the next section, a discussion about the role of the
632 different factors that are believed to affect the energy efficiency of the CO₂ splitting process
633 is presented (a necessary comparison between MW and DBD discharges is also included).



635 *Figure 9 - Energy Efficiency at different SEI by changing discharge power or CO₂ flow*
636 *rate.*

637

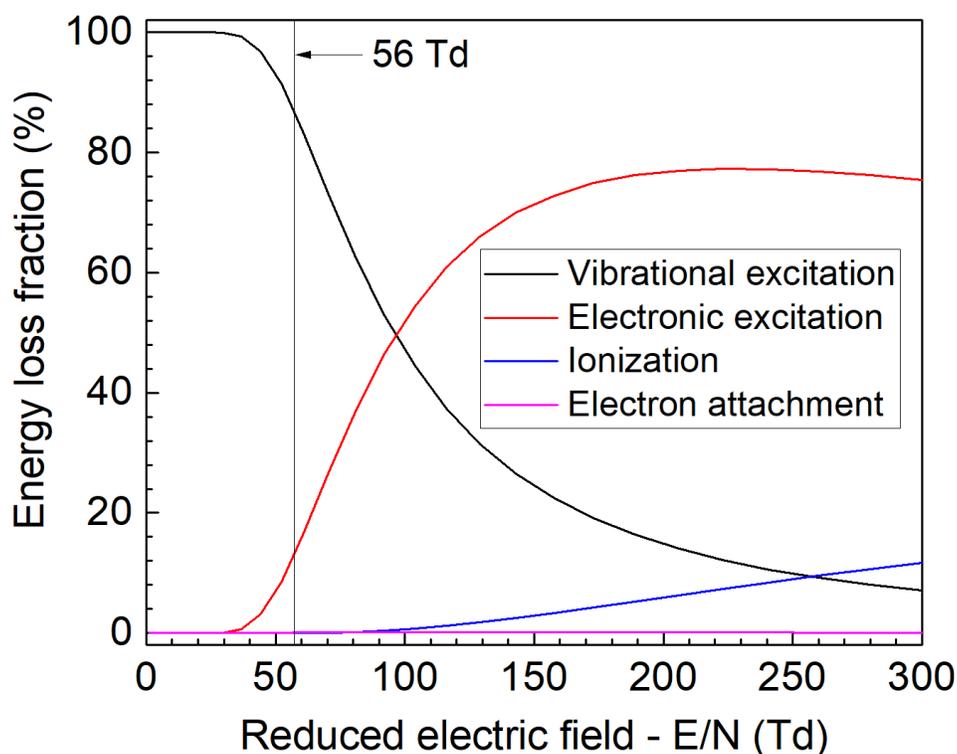
638 3.5.Reduced electric field and vibrationally excited states

639 As opposed to DBD reactors, MW normally show a greater energy efficiency, varying from
640 around 10% up to even 90% [26,27] (see the effect of the operating pressure below). It is
641 often claimed that the reason for the difference in their efficiencies is the range of reduced
642 electric fields they work on, placing vibrationally excited states of CO₂ as the main channel
643 for dissociation in MW discharges. While DBD reactors have been reported to operate at
644 high reduced electric fields (E/N), in the order of 200 Td; MW discharges exhibit a smaller
645 E/N, around 50 Td [31,33]. Indeed, it can be seen in Figure 10 that most of the electron
646 energy is consumed towards electronic vibrational excitation processes at 50 Td, while the
647 relevance of these processes is negligible at higher E/N. At around 200 Td, the vast majority
648 of the electron energy is directed to electron impact excitations (see Figure 10, calculated by
649 BOLSIG+ with the cross-section data sets used in this work). Then, the high efficiency of
650 the MW discharges has been associated with the low E/N figures while the low efficiency in
651 DBD reactors has been linked to the lack of vibrational excitation due to the higher E/N
652 [28,31,33,34].

653 However, the latter argument about the lack of vibrational states at ~200 Td cannot explain
654 the low efficiency of, at least, this DBD reactor. As mentioned above, the reduced electric
655 field used in this work is 56 Td, calculated from experimental measurements obtained
656 through Lissajous Figures (method described in [42] applied to our previous work [36]). The
657 method employed allows measurement of the voltage across the gap, importantly excluding
658 the voltage drop through the dielectric barrier. It is important to notice that this value is in
659 the order of those associated with MW discharges and differs considerably from 200 Td,
660 reported elsewhere and thought to characterise DBD discharges [31,33].

661 At this point it is important to notice that the high efficiencies achieved by MW discharges
662 require this reactor to be operated at low pressure. Moreover, when these discharges are
663 performed at atmospheric pressure, their efficiency drops significantly to values slightly

664 greater than those of DBD discharges (for a collection of data from different experimental
 665 works, see [26,27]). Then, it is apparent that the pressure plays a role in the efficiency of the
 666 CO₂ splitting reaction. In this regard, it has been theoretically shown in [51] that the highest
 667 conversions and energy efficiencies of CO₂ splitting reactions performed on MW discharges
 668 are achieved at 300 mbar, which is in agreement experimental results. Moreover, as stated in
 669 Section 0, long-lasting large populations of high vibrational states are not achieved in DBD
 670 reactors as the vibrationally excited molecules thermalise before the next micro-discharge
 671 occurs, as a result of the combination of high pressure and low duration of plasma that
 672 characterises these types of discharges [33].



673

674 *Figure 10 - Energy loss fractions towards different electron impact processes as a function*
 675 *of E/N, calculated by BOLSIG+ with the cross-sections used in this study.*

676 The present work can now be regarded with these very important results in mind. According
 677 to Figure 10, at 56 Td, most of the energy imparted to the electrons by the plasma is directed
 678 towards vibrational excitation. For that reason, we believe that vibrational excitation does
 679 indeed take place in DBD reactors, although leading to de-excitation rather than dissociation,
 680 due to the characteristic pressure and plasma duration of these discharges. Then, the low
 681 energy efficiency achieved in this work (and other DBD discharges) seems reasonable as

682 vibrational excitation consumes $\sim 90\%$ of the energy imparted by the plasma and is not
683 translated into CO_2 conversion. In other words, $\sim 90\%$ of the energy given to the system is
684 lost in a vibrational excitation – de-excitation sequence. Moreover, very little energy (just
685 above 10%) is transferred to electronic excitation of CO_2 , which has been shown in this work
686 (section 3.3) to be the main contributor to the dissociation process.

687 Finally, through this discussion, we can validate our approach of considering vibrational
688 excitations for the calculations of the EEDF, but not including reactions between
689 vibrationally excited states in the chemistry set as a channel for CO_2 dissociation.

690 **4. Conclusions**

691 In this work, we proposed a novel approach to the already existing zero-dimensional DBD
692 plasma kinetic models in order to include the effect of experimental parameters as discharge
693 power and flow rate. In addition, an average electron density calculated over hundreds of
694 microdischarges was used as an approximation, resulting in a great reduction of the
695 computational cost implied within this particular framework. Our DBD model was applied
696 to CO_2 splitting reactions and contrasted with readily available experimental data covering a
697 range of power and flow rate figures. A reduced chemistry set for CO_2 dissociation reactions
698 was employed [31], together with Polak and Slovetsky's cross section data for the CO_2
699 electron impact dissociation rate coefficient [38].

700 Overall, the results of this model represent the experimental measurements accurately within
701 the whole range of operational parameters tested, with a maximum relative error of around
702 5.5%. Upon this validation of the model, the underlying chemistry and reaction mechanisms
703 involved in the CO_2 conversion were analysed. Our results indicate that, under the operational
704 conditions considered in this work, the electron impact dissociation constitutes the dominant
705 mechanism for the CO_2 splitting, accounting for 95% of the CO_2 conversion. Finally, some
706 insights on the underlying reasons of the low energy efficiency shown by DBD reactors are
707 given. Our results, coupled with important findings published elsewhere [33], suggest that
708 most of the energy input is wasted towards vibrational excitations that have already been
709 proven not to lead to CO_2 dissociation under conditions of short exposure to plasma electrons
710 and atmospheric pressure, which characterise DBD reactors.

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714 **References**

- 715 [1] C. Liu, G. Xu, T. Wang, Non-thermal plasma approaches in CO₂ utilization, *Fuel Process.*
716 *Technol.* 58 (1999) 119–134. doi:10.1016/S0378-3820(98)00091-5.
- 717 [2] R. Snoeckx, A. Bogaerts, Plasma technology – a novel solution for CO₂ conversion?, *Chem.*
718 *Soc. Rev.* 46 (2017) 5805–5863. doi:10.1039/C6CS00066E.
- 719 [3] R. Bennett, S. Clifford, K. Anderson, G. Puxty, Carbon Capture Powered by Solar Energy,
720 *Energy Procedia.* 114 (2017) 1–6. doi:10.1016/j.egypro.2017.03.1139.
- 721 [4] Y. Tan, W. Nookuea, H. Li, E. Thorin, J. Yan, Property impacts on Carbon Capture and
722 Storage (CCS) processes: A review, *Energy Convers. Manag.* 118 (2016) 204–222.
723 doi:10.1016/j.enconman.2016.03.079.
- 724 [5] A. Alonso, J. Moral-Vico, A. Abo Markeb, M. Busquets-Fité, D. Komilis, V. Puentes, A.
725 Sánchez, X. Font, Critical review of existing nanomaterial adsorbents to capture carbon
726 dioxide and methane, *Sci. Total Environ.* 595 (2017) 51–62.
727 doi:10.1016/j.scitotenv.2017.03.229.
- 728 [6] I. Sreedhar, T. Nahar, A. Venugopal, B. Srinivas, Carbon capture by absorption – Path covered
729 and ahead, *Renew. Sustain. Energy Rev.* 76 (2017) 1080–1107.
730 doi:10.1016/j.rser.2017.03.109.
- 731 [7] M. Kumar, S. Sundaram, E. Gnansounou, C. Larroche, I.S. Thakur, Carbon dioxide capture,
732 storage and production of biofuel and biomaterials by bacteria: A review, *Bioresour. Technol.*
733 247 (2018) 1059–1068. doi:10.1016/j.biortech.2017.09.050.
- 734 [8] M.S. Duyar, S. Wang, M.A. Arellano-Treviño, R.J. Farrauto, CO₂utilization with a novel dual
735 function material (DFM) for capture and catalytic conversion to synthetic natural gas: An
736 update, *J. CO₂ Util.* 15 (2016) 65–71. doi:10.1016/j.jcou.2016.05.003.
- 737 [9] N.A. Rashidi, S. Yusup, An overview of activated carbons utilization for the post-combustion
738 carbon dioxide capture, *J. CO₂ Util.* 13 (2016) 1–16. doi:10.1016/j.jcou.2015.11.002.
- 739 [10] S. Saeidi, N.A.S. Amin, M.R. Rahimpour, Hydrogenation of CO₂to value-added products - A
740 review and potential future developments, *J. CO₂ Util.* 5 (2014) 66–81.
741 doi:10.1016/j.jcou.2013.12.005.
- 742 [11] H. Abdullah, M.M.R. Khan, H.R. Ong, Z. Yaakob, Modified TiO₂photocatalyst for
743 CO₂photocatalytic reduction: An overview, *J. CO₂ Util.* 22 (2017) 15–32.
744 doi:10.1016/j.jcou.2017.08.004.
- 745 [12] S. Paulussen, B. Verheyde, X. Tu, C. De Bie, T. Martens, D. Petrovic, A. Bogaerts, B. Sels,
746 Conversion of carbon dioxide to value-added chemicals in atmospheric pressure dielectric
747 barrier discharges, *Plasma Sources Sci. Technol.* 19 (2010). doi:10.1088/0963-
748 0252/19/3/034015.

- 749 [13] S. Wang, Y. Zhang, X. Liu, X. Wang, Enhancement of CO₂ Conversion Rate and Conversion
750 Efficiency by Homogeneous Discharges, *Plasma Chem. Plasma Process.* 32 (2012) 979–989.
751 doi:10.1007/s11090-012-9386-8.
- 752 [14] Q. Yu, M. Kong, T. Liu, J. Fei, X. Zheng, Characteristics of the decomposition of CO₂ in a
753 dielectric packed-bed plasma reactor, *Plasma Chem. Plasma Process.* 32 (2012) 153–163.
754 doi:10.1007/s11090-011-9335-y.
- 755 [15] F. Brehmer, S. Welzel, M.C.M. van de Sanden, R. Engeln, CO and byproduct formation
756 during CO₂ reduction in dielectric barrier discharges, *J. Appl. Phys.* 116 (2014) 123303.
757 doi:10.1063/1.4896132.
- 758 [16] D. Yap, J.M. Tatibouët, C. Batiot-Dupeyrat, Carbon dioxide dissociation to carbon monoxide
759 by non-thermal plasma, *J. CO₂ Util.* 12 (2015) 54–61. doi:10.1016/j.jcou.2015.07.002.
- 760 [17] K. Van Laer, A. Bogaerts, Improving the Conversion and Energy Efficiency of Carbon
761 Dioxide Splitting in a Zirconia-Packed Dielectric Barrier Discharge Reactor, *Energy Technol.*
762 3 (2015) 1038–1044. doi:10.1002/ente.201500127.
- 763 [18] D. Mei, X. Zhu, C. Wu, B. Ashford, P.T. Williams, X. Tu, Plasma-photocatalytic conversion
764 of CO₂ at low temperatures: Understanding the synergistic effect of plasma-catalysis, *Appl.*
765 *Catal. B Environ.* 182 (2016) 525–532. doi:10.1016/j.apcatb.2015.09.052.
- 766 [19] T. Butterworth, R. Elder, R. Allen, Effects of particle size on CO₂ reduction and discharge
767 characteristics in a packed bed plasma reactor, *Chem. Eng. J.* 293 (2016) 55–67.
768 doi:10.1016/j.cej.2016.02.047.
- 769 [20] D. Ray, C. Subrahmanyam, CO₂ decomposition in a packed DBD plasma reactor: influence
770 of packing materials, *RSC Adv.* 6 (2016) 39492–39499. doi:10.1039/C5RA27085E.
- 771 [21] D. Mei, Y.-L. He, S. Liu, J. Yan, X. Tu, Optimization of CO₂ Conversion in a Cylindrical
772 Dielectric Barrier Discharge Reactor Using Design of Experiments, *Plasma Process. Polym.*
773 13 (2016) 544–556. doi:10.1002/ppap.201500159.
- 774 [22] S. Xu, J.C. Whitehead, P.A. Martin, CO₂ conversion in a non-thermal, barium titanate packed
775 bed plasma reactor: The effect of dilution by Ar and N₂, *Chem. Eng. J.* 327 (2017) 764–773.
776 doi:10.1016/j.cej.2017.06.090.
- 777 [23] B. Ashford, X. Tu, Non-thermal plasma technology for the conversion of CO₂, *Curr. Opin.*
778 *Green Sustain. Chem.* 3 (2017) 45–49. doi:10.1016/j.cogsc.2016.12.001.
- 779 [24] Y. Uytdenhouten, S. Van Alphen, I. Michielsens, V. Meynen, P. Cool, A. Bogaerts, A packed-
780 bed DBD micro plasma reactor for CO₂ splitting: Does size matter?, *Chem. Eng. J.* 348
781 (2018) 557–568. doi:10.1016/j.cej.2018.04.210.
- 782 [25] J.C. Whitehead, Plasma Catalysis: Known knowns... known unknowns... and unknown
783 unknowns: Processing the research journey, *J. Phys. D. Appl. Phys.* 49 (2016) 243001.
784 doi:10.1088/0022-3727/49/24/243001.
- 785 [26] M. Ramakers, G. Trenchev, S. Heijkers, W. Wang, A. Bogaerts, Gliding Arc Plasmatron:
786 Providing an Alternative Method for Carbon Dioxide Conversion, *ChemSusChem.* 10 (2017)
787 2642–2652. doi:10.1002/cssc.201700589.
- 788 [27] W. Wang, D. Mei, X. Tu, A. Bogaerts, Gliding arc plasma for CO₂ conversion: Better insights
789 by a combined experimental and modelling approach, *Chem. Eng. J.* 330 (2017) 11–25.
790 doi:10.1016/j.cej.2017.07.133.

- 791 [28] R. Aerts, T. Martens, A. Bogaerts, Influence of Vibrational States on CO₂ Splitting by
792 Dielectric Barrier Discharges, *J. Phys. Chem. C.* 116 (2012) 23257–23273.
793 doi:10.1021/jp307525t.
- 794 [29] R. Snoeckx, R. Aerts, X. Tu, A. Bogaerts, Plasma-based dry reforming: A computational study
795 ranging from the nanoseconds to seconds time scale, *J. Phys. Chem. C.* 117 (2013) 4957–
796 4970. doi:10.1021/jp311912b.
- 797 [30] R. Snoeckx, M. Setareh, R. Aerts, P. Simon, A. Maghari, A. Bogaerts, Influence of
798 N₂ concentration in a CH₄/N₂ dielectric barrier discharge used for CH₄ conversion into H₂,
799 *Int. J. Hydrogen Energy.* 38 (2013) 16098–16120. doi:10.1016/j.ijhydene.2013.09.136.
- 800 [31] R. Aerts, W. Somers, A. Bogaerts, Carbon Dioxide Splitting in a Dielectric Barrier Discharge
801 Plasma: A Combined Experimental and Computational Study, *ChemSusChem.* 8 (2015) 702–
802 716. doi:10.1002/cssc.201402818.
- 803 [32] A. Bogaerts, W. Wang, A. Berthelot, V. Guerra, Modeling plasma-based CO₂ conversion:
804 Crucial role of the dissociation cross section, *Plasma Sources Sci. Technol.* 25 (2016).
805 doi:10.1088/0963-0252/25/5/055016.
- 806 [33] T. Kozak, A. Bogaerts, Splitting of CO₂ by vibrational excitation in non-equilibrium plasmas:
807 A reaction kinetics model, *Plasma Sources Sci. Technol.* 23 (2014). doi:10.1088/0963-
808 0252/23/4/045004.
- 809 [34] R. Snoeckx, A. Ozkan, F. Reniers, A. Bogaerts, The Quest for Value-Added Products from
810 Carbon Dioxide and Water in a Dielectric Barrier Discharge: A Chemical Kinetics Study,
811 *ChemSusChem.* 10 (2017) 409–424. doi:10.1002/cssc.201601234.
- 812 [35] A. Hurlbatt, A.R. Gibson, S. Schröter, J. Bredin, A.P.S. Foote, P. Grondein, D. O’Connell, T.
813 Gans, Concepts, Capabilities, and Limitations of Global Models: A Review, *Plasma Process.*
814 *Polym.* 14 (2016) 1–21. doi:10.1002/ppap.201600138.
- 815 [36] D. Mei, X. Tu, Conversion of CO₂ in a cylindrical dielectric barrier discharge reactor: Effects
816 of plasma processing parameters and reactor design, *J. CO₂ Util.* 19 (2017) 68–78.
817 doi:10.1016/j.jcou.2017.02.015.
- 818 [37] M. Grofulović, L.L. Alves, V. Guerra, Electron-neutral scattering cross sections for CO₂: A
819 complete and consistent set and an assessment of dissociation, *J. Phys. D. Appl. Phys.* 49
820 (2016). doi:10.1088/0022-3727/49/39/395207.
- 821 [38] L.S. Polak, D.I.Y. Slovetsky, Excitation and Molecular Dissociation, *Int. J. Radiat. Phys.*
822 *Chem.* 8 (1976) 257–282.
- 823 [39] S. Pancheshnyi, B. Eismann, G.J.M. Hagelaar, L.C. Pitchford, Computer code ZDPlasKin,
824 <http://www.zdplaskin.laplace.univ-tlse.fr> (University of Toulouse, LAPLACE, CNRS-UPS-
825 INP, Toulouse, France), (2008).
- 826 [40] G.J.M. Hagelaar, L.C. Pitchford, Solving the Boltzmann equation to obtain electron transport
827 coefficients and rate coefficients for fluid models, *Plasma Sources Sci. Technol.* 14 (2005)
828 722–733. doi:10.1088/0963-0252/14/4/011.
- 829 [41] S. Pancheshnyi, S. Biagi, M.C. Bordage, G.J.M. Hagelaar, W.L. Morgan, A. V. Phelps, L.C.
830 Pitchford, The LXCat project: Electron scattering cross sections and swarm parameters for
831 low temperature plasma modeling, *Chem. Phys.* 398 (2012) 148–153.
832 doi:10.1016/j.chemphys.2011.04.020.

- 833 [42] D. Mei, X. Zhu, Y.-L. He, J.D. Yan, X. Tu, Plasma-assisted conversion of CO₂ in a dielectric
834 barrier discharge reactor: understanding the effect of packing materials, *Plasma Sources Sci.*
835 *Technol.* 24 (2014) 015011. doi:10.1088/0963-0252/24/1/015011.
- 836 [43] A. Fridman, *Plasma Chemistry*, Cambridge University Press, 2008.
- 837 [44] L.-F. Dong, X.-C. Li, Z.-Q. Yin, S.-F. Qian, J.-T. Ouyang, L. Wang, Self-Organized Filaments
838 in Dielectric Barrier Discharge in Air at Atmospheric Pressure, *Chinese Phys. Lett.* (2001)
839 1380.
- 840 [45] L.L. Alves, The IST-LISBON database on LXCat, *J. Phys. Conf. Ser.* 565 (2014).
841 doi:10.1088/1742-6596/565/1/012007.
- 842 [46] Morgan database, www.lxcat.net, retrieved on January 2, 2018.
- 843 [47] S. Ponduri, M.M. Becker, S. Welzel, M.C.M. van de Sanden, D. Loffhagen, R. Engeln, Fluid
844 modelling of CO₂ dissociation in a dielectric barrier discharge, *J. Appl. Phys.* 119 (2016)
845 093301. doi:10.1063/1.4941530.
- 846 [48] C.E. Treanor, J.W. Rich, R.G. Rehm, Vibrational Relaxation of Anharmonic Oscillators with
847 Exchange-Dominated Collisions, *J. Chem. Phys.* 48 (1968) 1798–1807.
848 doi:10.1063/1.1668914.
- 849 [49] J.J. Lowke, A. V Phelps, B.W. Irwin, Predicted electron transport coefficients and operating
850 characteristics of CO₂–N₂–He laser mixtures, *J. Appl. Phys.* 44 (1973) 4664.
- 851 [50] Itikawa database, www.lxcat.net.
- 852 [51] A. Berthelot, A. Bogaerts, Modeling of CO₂ Splitting in a Microwave Plasma: How to
853 Improve the Conversion and Energy Efficiency, *J. Phys. Chem. C.* 121 (2017) 8236–8251.
854 doi:10.1021/acs.jpcc.6b12840.
- 855