

Real-Space Observation of Quantum Tunneling by Carbon Atom: Flipping Reaction of Formaldehyde on Cu(110)

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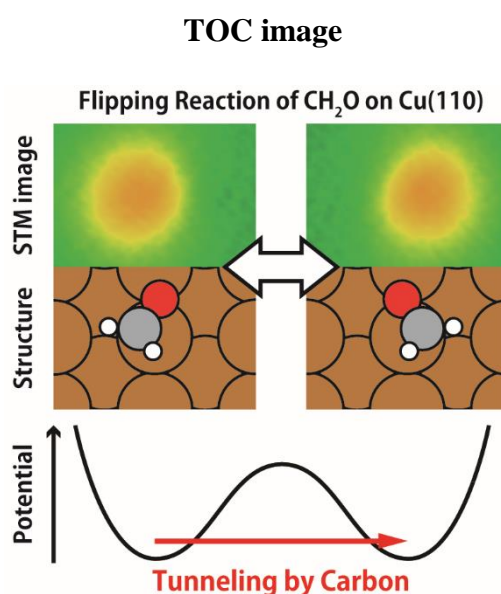
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We present a direct observation of carbon-atom tunneling in the flipping reaction of formaldehyde between its two mirror states on a Cu(110) surface using low-temperature scanning tunneling microscopy (STM). The flipping reaction was monitored in real time and the reaction rate was found to be temperature independent below 10 K. This indicates that this reaction is governed by quantum mechanical tunneling, albeit involving a substantial motion of the carbon atom ($\sim 1 \text{ \AA}$). In addition, deuteration of the formaldehyde molecule resulted in a significant kinetic isotope effect ($R_{\text{CH}_2\text{O}}/R_{\text{CD}_2\text{O}} \approx 10$). The adsorption structure, reaction pathway, and tunneling probability were examined by density functional theory calculations, which corroborate the experimental observations.



Keywords: Carbon tunneling, Single-molecule chemistry, Formaldehyde, Metal surface, Low-temperature scanning tunneling microscopy

Tunneling is a pure quantum-mechanical effect resulting from the wave-like property of a particle, which makes it possible to pass through a classically insurmountable barrier. Hydrogen tunneling was recognized already in the early days of quantum chemistry¹ and plays a crucial role in chemical and biological reactions.^{2, 3, 4, 5} The contribution of tunneling in chemical reactions strongly depends on the particle mass and decreases rapidly with increasing mass of the atom. Therefore, heavy-atom tunneling such as carbon and oxygen had been ignored for a long time. However, experimental evidence of carbon tunneling was reported for the tautomerization of cyclobutadiene in the late 20th century.^{6, 7, 8} Since then, several different reactions involving carbon tunneling have been found,^{9, 10, 11, 12, 13, 14} even at elevated reaction temperatures.^{15, 16} These findings suggest carbon tunneling may be broadly involved in organic reactions.

Tunneling in chemical reactions has been conventionally investigated by spectroscopic methods such as nuclear magnetic resonance and vibrational-rotational spectroscopy. In experiments, the mechanism of carbon tunneling is elusive compared to hydrogen. In the latter case, deuteration of molecules can provide solid evidence through the significant kinetic isotope effects (KIEs), which is rather subtle for $^{12}\text{C}/^{13}\text{C}$, as well as through the temperature dependence of a reaction rate. In the last two decades, low-temperature scanning tunneling microscopy (STM) has emerged as a unique tool to investigate reactions occurring via tunneling. Hydrogen tunneling was examined in diffusion of hydrogen atom,¹⁷ hydrogen-bond exchange reactions in small water clusters,^{18, 19} and in single-molecule tautomerization.^{20, 21} Remarkably, heavy-atom tunneling was observed for CO,²² Cu,²³ Co,²⁴ and cyclooctadiene.²⁵ These studies show the capability of STM not only to visualize tunneling dynamics *in real space*, but also to perturb it through a modification of the potential energy surface using the STM tip.^{20, 26}

So far, the example of heavy-atom tunneling is scarce and a quantitative description remains a challenging task in theoretical simulations. Here we report a new type of reaction involving carbon tunneling, namely flipping of a formaldehyde molecule on a Cu(110) surface.

Experiments were carried out under ultrahigh vacuum conditions ($<2 \times 10^{-10}$ mbar) with a low-temperature STM from Omicron Nanotechnology GmbH and operated with a Nanonis Controller System. An electrochemically etched tungsten tip was used as a STM probe. The bias voltage (V_{bias}) was applied to the sample, and the tip was grounded. The tunneling current (I_t) was collected from the tip. A single-crystalline Cu(110) surface was cleaned by repeated cycles of argon ion sputtering and annealing to 700 K. Formaldehyde molecules were obtained by sequential dehydrogenation of methanol molecules on the Cu(110) surface. The clean surface was first exposed to CH₃OH or CD₃OD (Aldrich 99 %) gas at 10 K. Adsorbed methanol molecules were then dehydrogenated by applying a voltage pulse of 0.7–1.0 V to yield formaldehyde, as described in Ref. 27.

The equilibrium structures and the minimum energy paths (MEPs) of the adsorbed formaldehyde on the Cu(110) surface were obtained from periodic, plane-wave DFT calculations using the Vienna *ab-initio* simulation program (VASP).²⁸ The electron–ion core interactions and the exchange–correlation effects were treated using the Projector Augmented Wave (PAW) method²⁹ and the vdW-DF-cx version of the van der Waals density functional,^{30, 31, 32} respectively. The Cu(110) surface was represented in a supercell by a five layer slab with a 2×3 and 4×6 surface unit cells and a 25 Å vacuum region. The MEPs were computed using the nudged elastic band method.^{33, 34} Further details of the calculations can be found in the Supporting Information.

Figures 1a–c display topographic STM images of three different products yielded by dissociation of methoxy on Cu(110) at 4.5 K, which could be assigned to formaldehyde: An oval protrusion (O_{pa} : **Fig. 1a**), a pair of protrusion and depression (P_{pd} : **Fig. 1b**), and an oval protrusion but with a lower apparent height (O_{pb} : **Fig. 1c**). The appearance of O_{pa} and O_{pb} looks similar but O_{pb} flips between two mirror-symmetry states spontaneously even at 4.5 K and a low V_{bias} like 10 mV (**Fig. 1c**), whereas no flipping was observed for O_{pa} and P_{pd} at very low V_{bias} . O_{pb} and P_{pd} have also been reported previously, and are identified as formaldehyde.²⁷ However, the previous study did not show the flipping of O_{pb} below V_{bias} of 30 mV. Here we focus on the flipping of O_{pb} at $V_{bias}=10$ mV, where vibrational excitation by tunneling electrons is almost negligible.

The flipping can be monitored over the molecule with the lateral tip position fixed at the highest position in the STM image (as indicated by the dots in **Fig. 1c**). The flipping under the tip causes a change in the tip height (Z) through the feedback loop. In the Z trace (as a function of time, t), a random telegraph signal between two states is observed (**Fig. 1d**), where the “high” and “low” states correspond to the formaldehyde under and away from the tip, respectively. In **Fig. 1d**, the Z trace measured for normal and deuterated formaldehyde (CD_2O) is shown. It is clear that CH_2O flips much more frequently than CD_2O , indicating a significant KIE. In order to discuss the reaction in a quantitative manner, the flipping rate from the “high” to “low” state ($R_{H\rightarrow L}$) and the opposite process ($R_{L\rightarrow H}$) was extracted from the Z trace. Two different methods were used to obtain the rate; by fitting the histogram of the time intervals of the reaction to an exponential decay function or by dividing the total number of reaction events by the total measurement time (both methods are statistically equal). We used the latter method for a very low reaction

rate ($<1 \times 10^{-3} \text{ s}^{-1}$) since the sampling number of the total reaction events was too limited to apply the histogram analysis.

Figure 2a shows the current dependence of the flipping rate (R_{Flip}) for CH_2O obtained at $V_{\text{bias}}=10 \text{ mV}$. We found that the rate depends very weakly on the current. The reaction rate of an adsorbate follows a power law ($R \propto I_t^N$) when induced by tunneling electrons.³⁵ Hence, our result indicates that the flipping cannot be ascribed to an electron-induced process. The population ratio of the “high” and “low” states (P_{H} and P_{L}) is almost unity (top part of **Fig. 2a**), indicating that the potential energy surface (PES) of the flipping reaction was not significantly distorted by any tip–molecule interaction. The deviation of $P_{\text{H}}/P_{\text{L}}$ from unity at a higher current can be explained by a tip-induced modification of the PES.²⁶ It was also found that R_{Flip} is somewhat affected by the tip conditions (see Supporting Information).

Figure 2b shows the temperature dependence of R_{Flip} . If the reaction is thermally activated, a linear relationship with a negative slope is expected between $\log R$ and $1/T$. However, R_{Flip} weakly depends on the temperature below 10 K, indicating that the reaction is governed by tunneling and no thermally-assisted process (coupling with different vibrational modes) is involved.³⁶ In addition, R_{Flip} of CD_2O reveals the KIE of about one order of magnitude.

The possible adsorption structures of the formaldehyde and reaction pathways were examined using DFT calculations. **Figures 3a–3c** summarize the various calculated adsorption geometries of CH_2O on the Cu(110) surface. The η^1 - and η^2 -configuration are consistent with the structures reported in the previous calculation.³⁷ Our simulations found an additional adsorption geometry, denoted as η^3 , which breaks all the symmetries of the Cu(110) surface. Among three adsorption states, η^2 is most stable with an

adsorption energy of 0.87 eV. The other two adsorption geometries are local minimum structures which should also be considered here because they could be kinetically stabilized at cryogenic temperatures. Comparing the calculated STM image in **Fig. 3e** with the experimental image in **Fig. 1a**, η^2 can be assigned to P_{pd} . The relatively large adsorption energy of η^2 is also consistent with the fact that no flipping occurs in P_{pd} . However, O_{pa} and O_{pb} cannot be straightforwardly assigned from the STM images, but we were able to identify these two species from the analysis of the flipping mechanism of the η^1 - and η^3 -configuration as detailed below.

We examined the minimum energy path (MEP) of the flipping reaction using the nudged elastic band method. **Figure 4** shows the MEP for η^1 - and η^3 -configuration between the two mirror-reflected structures. The MEP for η^1 (**Fig. 4a**) was constrained to be in the symmetry plane spanned by the surface normal and the [001] direction and the reaction occurs by a vertical wagging motion. The saddle point of this MEP has two imaginary frequencies. The MEP for η^3 corresponds to an azimuthal rotation of the CH_2 group around the surface normal (**Fig. 4b**). The saddle point of this MEP has a single imaginary frequency and corresponds to a transition structure. The potential energy barrier for η^3 is only ~24 meV and is ~10 times smaller than the one for η^1 . The effective barrier becomes ~20 and ~21 meV for CH_2O and CD_2O , respectively, when the contribution of the zero-point energy of the vibration along the reaction coordinate is included (see Supporting Information for the details). This very small barrier allows for carbon tunneling in the flipping reaction. At the experimental temperature of 4.5 K, no vibrational modes are thermally populated, since all vibrational modes have energies larger than ~7 meV. As shown in **Table 1**, a simple but rough estimate of the tunneling probability based on the calculated MEPs with the WKB approximation (see Supporting

Information for the details) shows that η^3 can be flipped by tunneling through the small barrier, whereas the tunneling process is completely negligible for η^1 . Based on the above findings, we assign our tunneling species O_{pb} to η^3 and O_{pa} to η^1 . In the previously observed carbon tunneling reactions, the displacement of the carbon atom was extremely small (~ 0.1 Å),³⁸ thus resulting in a very narrow barrier that allows tunneling. In the flipping of formaldehyde, the carbon displacement of ~ 1.1 Å between the two mirror-reflected configurations is substantially longer but has a very small potential barrier, representing another condition for carbon tunneling. The difference in the tunneling rates between CH_2O and CD_2O is caused predominantly by the mass difference, since the differences in the effective barrier heights are small. In the WKB approximation, the estimated tunneling rates for CH_2O and CD_2O give a KIE of ~ 40 , which is in reasonable agreement considering the simplicity of this approximation and the limited accuracy of DFT calculation to describe potential energy barriers.

In summary, we identified three different adsorption configurations of formaldehyde on the Cu(110) surface by combined STM experiments and DFT calculations. Remarkably, it was found that the flipping reaction of the η_3 -configuration occurs by tunneling including the carbon atom, which is evident from the temperature-independent reaction rate below 10 K. The MEP analysis revealed that the η_3 -configuration exhibits a very small barrier of ~ 20 (~ 21) meV for the flipping reaction of CH_2O (CD_2O), which allows for carbon tunneling between the vibrational ground states of the mirror-reflected configuration.

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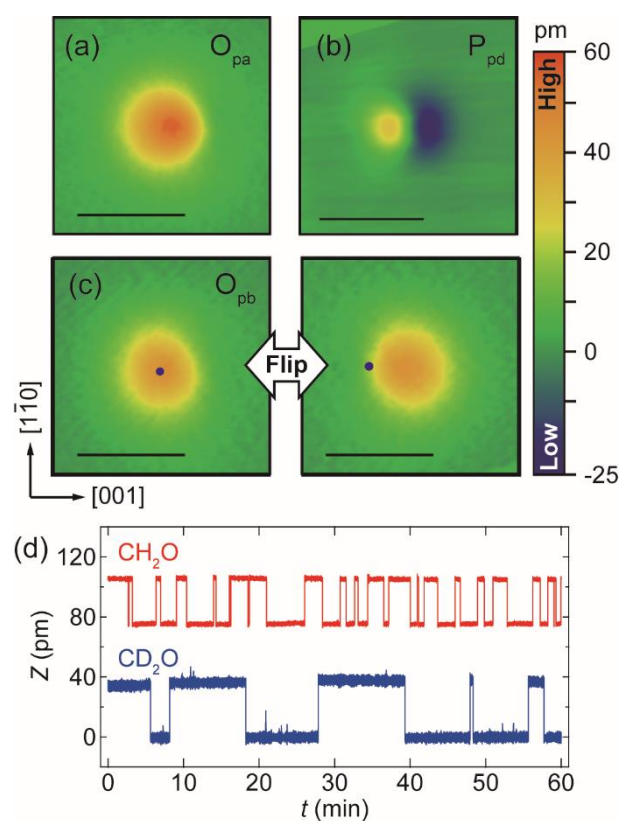


Figure 1. (a–c) STM images of three different products after injecting tunneling electrons of 1 V to methoxy, (a) O_{pa} , (b) P_{pd} , (c) O_{pb} with two mirror-reflected configurations. (4.5 K, $V_{bias}=10$ mV, $I_t=10$ pA). P and O_b has been identified as formaldehyde.²⁷ The scale bar in each figure is 1 nm. (d) Traces of the tip height (Z) measured for CH_2O (red) and CD_2O (blue). The lateral tip position during the measurement is indicated in (c) with blue dots. The data for CH_2O is vertically shifted for clarity. The Z traces were acquired at $V_{bias}=10$ mV and $I_t=10$ pA.

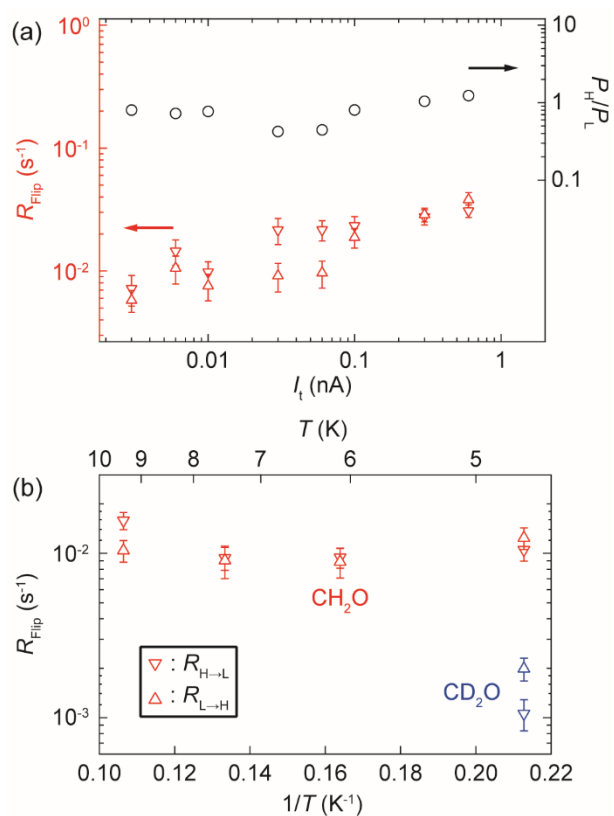


Figure 2. (a) Current dependence of R_{Flip} for the “high” to “low” transition ($R_{\text{H} \rightarrow \text{L}}$, inverted triangle) and the reverse process ($R_{\text{L} \rightarrow \text{H}}$, triangle) for CH₂O acquired at 4.5 K. V_{bias} was fixed at 10 mV during the measurement. The black circles in the top part show the current dependence of the fractional population ratio ($P_{\text{H}}/P_{\text{L}}$). (b) Temperature dependence of R_{Flip} for CH₂O (red). The rate for CD₂O (blue) at 4.5 K is plotted for comparison.

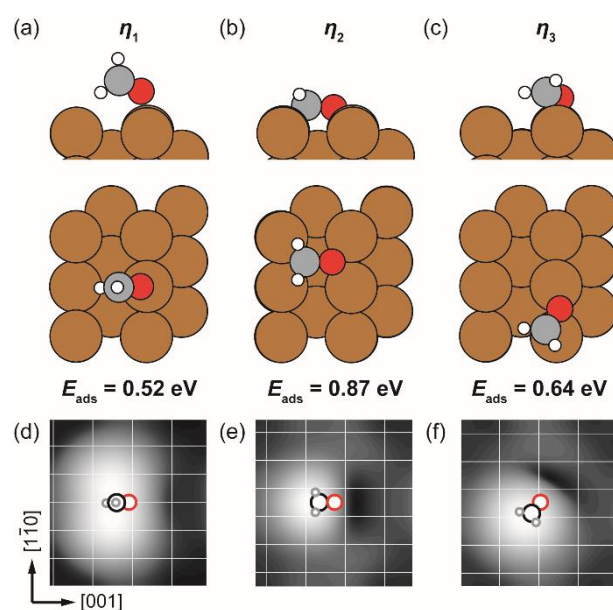


Figure 3. Calculated structures of (a) η^1 -, (b) η^2 - and (c) η^3 -configuration of the formaldehyde on the Cu(110) surface. The adsorption energies (E_{ads}) are given in the figure. (d–f) Simulated topographical STM images at an average tip-surface distances of (a) 10.0, (b) 7.5 and (c) 8.7 Å and at the Fermi level with a broadening of 0.1 eV. The white grid lines represent the surface lattice of Cu(110). The structure of the adsorbed formaldehyde is superimposed for each structure.

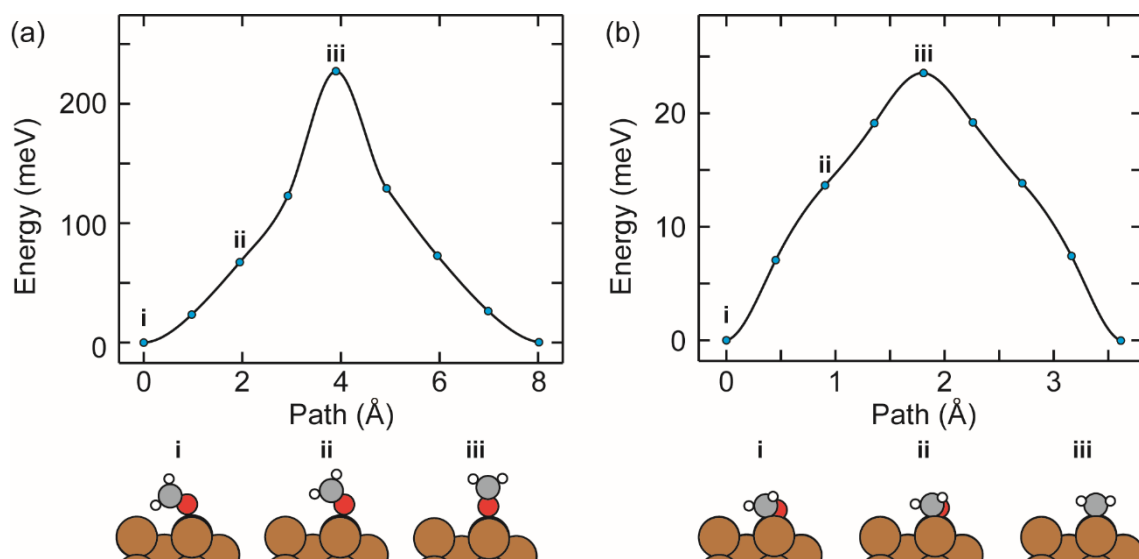


Figure 4. MEP of the flipping reactions of η^1 - and η^3 -configuration on the Cu(110) surface. The path lengths were obtained from the distances between the images in configuration space. The structures along each path are shown in the bottom panel.

Table 1. MEP effective barriers heights (D_{eff}) and lengths (Δs) between the two mirror-reflected configurations, estimated tunneling rates (R_t) and probabilities (P_0) of the flipping reactions of η^1 - and η^3 -configuration on the Cu(110) surface. The values in the parenthesis correspond to the ones for the deuterated species (CD_2O). The calculations are detailed in Supporting Information.

	D_{eff} (meV)	Δs (Å)	R_t (s^{-1})	P_0
η^1	214 (215)	7.8	2×10^{-56} (2×10^{-63})	6×10^{-70} (5×10^{-77})
η^3	20 (21)	3.62	6×10^{-2} (1.5×10^{-3})	3×10^{-14} (8×10^{-16})

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