

1 **The effect of ocean ventilation on the Transient Climate**

2 **Response to Emissions**

3 Anna Katavouta * and Richard G. Williams

4 *Department of Earth Ocean and Ecological Sciences, School of Environmental Sciences,*

5 *University of Liverpool, Liverpool, UK*

6 Philip Goodwin

7 *School of Ocean and Earth Sciences, University of Southampton, Southampton, UK*

8 **Corresponding author address:* Anna Katavouta, Department of Earth Ocean and Ecological Sci-
9 ences, University of Liverpool, Liverpool, UK

10 E-mail: a.katavouta@liverpool.ac.uk

ABSTRACT

11 The surface warming response to carbon emissions is affected by how the
12 ocean sequesters excess heat and carbon supplied to the climate system. This
13 ocean uptake involves the ventilation mechanism, where heat and carbon are
14 taken up by the mixed layer and transferred to the thermocline and deep ocean.
15 The effect of ocean ventilation on the surface warming response to carbon
16 emissions is explored using simplified conceptual models of the atmosphere-
17 ocean with and without explicit representation of the meridional overturning.
18 Sensitivity experiments are conducted to investigate the effects of (i) mixed-
19 layer thickness, (ii) rate of ventilation of the ocean interior, (iii) strength of the
20 meridional overturning and (iv) extent of subduction in the Southern Ocean.
21 Our diagnostics focus on a climate metric, the Transient Climate Response
22 to carbon Emissions (TCRE), defined by the ratio of surface warming to the
23 cumulative carbon emissions, which may be expressed in terms of separate
24 thermal and carbon contributions. The variability in the thermal contribution
25 due to changes in ocean ventilation dominates the variability in the TCRE
26 on timescales of years to centuries, while that of the carbon contribution
27 dominates on timescales of several centuries to millennia. These ventilated
28 controls are primarily from changes in the mixed-layer thickness on decadal
29 timescales, and in the rate of ventilated transfer from the mixed layer to the
30 thermocline and deep ocean on centennial and millennial timescales, which
31 is itself affected by the strength of the meridional overturning and extent of
32 subduction in the Southern Ocean.

33 **1. Introduction**

34 Climate model projections reveal that the global-mean surface warming increases nearly linearly
35 with cumulative carbon emissions (Allen et al. 2009; Gillet et al. 2013; Matthews et al. 2009; Zick-
36 feld et al. 2009). This proportionality between the global-mean increase in surface air temperature
37 and the cumulative carbon emissions has been used to define a climate metric in Earth system
38 models, referred to as the Transient Climate response to cumulative carbon Emissions (TCRE).

39 The ocean plays a central role in determining this connection between surface warming and
40 carbon emissions through ocean uptake of heat and carbon (Solomon et al. 2009). The ocean
41 uptake of atmospheric CO₂ acts to decrease radiative forcing and so provides a cooling effect,
42 while the proportion of radiative forcing driving ocean heat uptake declines in time and so provides
43 a warming effect (Goodwin et al. 2015; Williams et al. 2016, 2017a).

44 The dependence of surface warming on carbon emissions differs in magnitude between different
45 models, such as with the TCRE varying between 1.20 and 2.45 K (1000 PgC)⁻¹ in a suite of
46 10 CMIP5 models with an annual 1% rise in atmospheric CO₂ (Williams et al. 2017b). Their
47 inter-model differences in the TCRE arise mostly from differences in the thermal response on
48 decadal to multi-decadal timescales, with differences in the carbon response becoming important
49 on multi-decadal to centennial timescales (Williams et al. 2017b). The inter-model spread in
50 climate feedbacks (Andrews et al. 2012; Forster et al. 2013) is the largest driver of uncertainty in
51 the TCRE, but the inter-model spread in ocean heat uptake also contributes (Raper et al. 2002;
52 Geoffroy et al. 2012; MacDougall et al. 2017; Williams et al. 2017b). What is unclear is the
53 effect of different ocean ventilation mechanisms in controlling this surface warming dependence
54 on carbon emissions and in leading to inter-model differences in the TCRE.

55 The ocean uptake of anthropogenic heat and carbon is primarily controlled by the ventilation
56 process involving uptake of heat and carbon by the surface mixed layer and subsequent transfer
57 into the main thermocline and the deep ocean. This ventilated response is affected by the strength
58 of the Atlantic meridional overturning circulation, which in turn alters the surface warming re-
59 sponse to carbon emissions (Xie and Vallis 2012; Rugenstein et al. 2013; Winton et al. 2013).
60 The Atlantic meridional overturning circulation varies significantly amongst Earth system models
61 (Gregory et al. 2005; Cheng et al. 2013) and this variation is partially responsible for the spread
62 in the transient warming due to emissions (Kostov et al. 2014). However, ocean ventilation is not
63 solely controlled by the strength of the meridional overturning circulation, but also affected by the
64 thickness of the mixed layer, and the horizontal gyre, eddy and circumpolar circulations affecting
65 the formation of mode waters and their spreading into the thermocline and ocean interior. Hence,
66 we need to understand how the full range of physical effects contributing to ocean ventilation help
67 determine the climate response of a model.

68 In this study we investigate how the climate metric, the Transient Climate Response to cumu-
69 lative carbon Emissions, is controlled by: (i) the thickness of the mixed layer in contact with the
70 atmosphere; (ii) the rate of ventilation between the mixed layer and the ocean interior; (iii) the
71 strength of the meridional overturning; and (iv) the extent of Southern Ocean mode water for-
72 mation. To address these questions, we take a step back from the complex Earth system models
73 and conduct sensitivity experiment using idealised atmosphere-ocean models, so as to provide a
74 clearer mechanistic connection between the effects of different processes contributing to ventila-
75 tion and the TCRE. Since observational reconstructions reveal enhanced uptake of anthropogenic
76 heat and carbon in the upper thermocline over the global ocean (Sabine et al. 2004; Roemmich
77 et al. 2015), one of our conceptual models include a thermocline with a dynamically-controlled
78 thickness (Gnanadesikan 1999; Marshall and Zanna 2014).

79 The outline of the paper is as follows. The formulation of the idealised models and sensitivity
80 experiments are first presented (Section 2). The climate response in the sensitivity experiments is
81 interpreted by separating the dependence of surface warming on carbon emissions, as given by the
82 TCRE, into a product of thermal and carbon contributions (Williams et al. 2016) and identifying
83 the relative importance of the different processes contributing to ocean ventilation (Section 3).
84 The effect of different ventilation processes on the TCRE is assessed across parameter space by
85 diagnosing the response of a large set of model ensembles (Section 4). Finally, the implications
86 and the caveats to the study are discussed (Section 5).

87 **2. Model formulation and experiments**

88 The effect of different processes contributing to ocean ventilation on the climate metric, the
89 TCRE, are investigated using two idealised box models of the atmosphere-ocean system, either
90 without or with an explicit representation of the ocean meridional overturning circulation.

91 *a. 1D box model of the atmosphere-ocean*

92 The 1D box model consists of three homogeneous layers: a slab atmosphere, an ocean mixed
93 layer and an ocean interior (Fig.1a). The model solves for the heat and carbon exchange due
94 to carbon emissions between these layers, including physical and chemical transfers, but ignor-
95 ing biological transfers, and sediment and weathering interactions; see supplementary material in
96 Katavouta et al. (2018). Ocean ventilation is represented by the ocean interior taking up the tem-
97 perature and carbon anomalies of the mixed layer with a relaxation closure, such that the rates of
98 change in the temperature and the dissolved inorganic carbon of the ocean interior are described
99 by

$$\frac{d}{dt}T_{int}(t) = \frac{1}{\tau_{vent}} (\Delta T_{ml}(t) - \Delta T_{int}(t)), \quad (1a)$$

$$\frac{d}{dt}DIC_{int}(t) = \frac{1}{\tau_{vent}} (\Delta DIC_{ml}(t) - \Delta DIC_{int}(t)), \quad (1b)$$

100 where τ_{vent} is a relaxation timescale referred to as the ventilation timescale, $\Delta T(t)$ is the temper-
 101 ature change in K and $\Delta DIC(t)$ the carbon change in mol kg⁻¹ relative to the pre-industrial, and
 102 subscripts *ml* and *int* refer to the ocean mixed layer and interior values; this model is referred to
 103 as the 1D box model.

104 *b. Box model of the atmosphere-ocean with meridional overturning*

105 Our box model of the atmosphere and ocean with meridional overturning (Fig.1b) follows the
 106 layered model of the global thermocline by Gnanadesikan (1999) and the extensions by Johnson
 107 et al. (2007) and Marshall and Zanna (2014).

108 Light water is transformed to dense water by surface cooling in the northern high latitudes, at
 109 a volume rate of q_{NA} , equivalent to the strength of the meridional overturning. Dense water is
 110 transformed back to light water either by diapycnal transfers in the low latitudes, at a volume
 111 rate of q_v , or by a surface warming conversion into light waters in the southern high latitudes
 112 associated with the residual circulation, at a volume rate of q_{so} , involving a northward Ekman
 113 volume flux partly compensated by a poleward mesoscale eddy flux. The volume of light waters
 114 and overturning strength, q_{NA} , is then controlled in a dynamic manner in terms of the diapycnal
 115 mixing parametrised by a diapycnal mixing coefficient, the wind stress in the Southern Ocean,
 116 the strength of the eddies in the Southern Ocean parametrised by the eddy diffusivity, and the
 117 additional ocean warming and enhancement of stratification due to the anthropogenic emissions
 118 (see Appendix for the closures).

119 To define the extent of ventilation, the light waters in the low latitudes extend over a variable
120 thickness, $h(t)$, which are further separated into two layers: a mixed layer with constant thickness,
121 $h_{ml} = 100$ m, and a thermocline layer with thickness, $h_{therm}(t) = h(t) - h_{ml}$ (Fig.1b).

122 To take into account the extent of communication between the atmosphere and the upper ocean,
123 an isolation fraction, δ , is defined. This isolation fraction δ defines the relative proportion of the
124 subduction occurring in the Southern Ocean and sets the fraction of waters remaining below the
125 mixed layer and spreading northward within the thermocline; instead $(1 - \delta)$ sets how much of the
126 subduction occurs in the low latitudes and the fraction of waters in contact with the atmosphere in
127 the tropics and subtropics. A rough estimate of δ corresponds to the ratio of the volume of waters
128 subducted in the southern high latitudes, consisting of Sub-Antarctic mode water and Antarctic
129 Intermediated Water, and transported northward versus the total volume of waters subducted and
130 transported northward to the northern high latitudes, consisting of subtropical mode water, Sub-
131 Antarctic mode water and Antarctic Intermediate Water. Based on the water-mass diagnostics of
132 Talley (1999) at 24° N, this partitioning implies that the ratio δ is about 0.7, suggesting that most
133 of the subducted waters are from the Southern Ocean and so these waters are shielded from the
134 atmosphere in the low latitudes.

135 A slab atmosphere is used to parametrise the exchange of heat and carbon between the atmo-
136 sphere and the ocean, and two upper ocean boxes are used to represent the southern and northern
137 high latitudes. These high latitude boxes are used to solve for the heat and carbon transfer in
138 the ocean, but do not directly affect the model dynamics and volume transports (see Appendix
139 for model closures). The model solves for the ocean carbon cycle including physical and chemi-
140 cal transfers, but ignores biological transfers, and sediment and weathering interactions involving
141 changes in the cycling of organic carbon or calcium carbonate. The ocean carbonate system is
142 solved using the iterative algorithm of Follows et al. (2006) and assumes that the total alkalinity

143 remains constant: the model solves for the changes in pH and the fraction of carbonate species
144 present in seawater and its effect on the the capacity of the ocean to absorb the changes in atmo-
145 spheric CO_2 . This idealised model is referred to as the box model with overturning.

146 *c. Sensitivity experiments*

147 The climate response is explored in both box models to carbon emissions, emitted to the at-
148 mosphere at a constant rate of 20 PgC y^{-1} for 100 years, and then integrated until equilibrium
149 is reached after several 1000 years. The resulting increase in atmospheric CO_2 drives a radiative
150 forcing: $R(t) = a\Delta\ln CO_2(t)$ (Myhre et al. 1998), where $a = 5.35 \text{ W m}^{-2}$ and the pre-industrial
151 $CO_2(t_o)$ is 280 ppm. This radiative forcing, $R(t)$, is assumed to drive a global-mean radiative re-
152 sponse, $\lambda(t)\Delta T(t)$, plus a planetary heat uptake, $N(t)$, (Gregory et al. 2004; Gregory and Forster
153 2008), such that

$$R(t) = \lambda(t)\Delta T(t) + N(t), \quad (2)$$

154 where $\lambda(t)$ is the climate feedback parameter, which is assumed constant and equal to
155 $1 \text{ W m}^{-2}\text{K}^{-1}$ in all our simulations for simplicity. This λ value is close to the CMIP5 Earth
156 system models mean of $1.13 \text{ W m}^{-2}\text{K}^{-1}$ (Forster et al. 2013). The planetary heat uptake, $N(t)$,
157 is dominated by the ocean heat uptake (Church et al. 2011), and in both models, more than 95%
158 of heat passes into the ocean; henceforth, the planetary and the ocean heat uptakes are taken to
159 be effectively equivalent. The ocean carbon and heat uptakes due to the anthropogenic carbon
160 emissions are approximated to be spatially uniform in these simplified conceptual models.

161 The 1D box model is used to explore the climate response and the sensitivity of the TCRE to
162 two aspects of ocean ventilation: (i) the thickness of the ocean mixed layer setting the proportion
163 of waters in direct contact with the atmosphere, and (ii) the ventilation timescale setting the rate
164 of transfer of heat and carbon from the mixed layer to the ocean interior. Sensitivity experiments

165 include varying the thickness of the mixed layer between a range of 50 to 300 m and the ventilation
166 timescale between a range of 100 and 2000 years, and these changes occurring either separately
167 or simultaneously (Table 1).

168 The box model with overturning is used to explore the climate response and the sensitivity of the
169 TCRE to two further mechanisms that control the rate of ventilation of the ocean interior and extent
170 of communication with the atmosphere: (i) the strength of the meridional overturning that sets the
171 volume transport and transfer of heat and carbon into the deep ocean and (ii) the isolation fraction,
172 δ , that controls the proportion of waters subducted in the Southern Ocean. Sensitivity experiments
173 are conducted varying the Southern Ocean wind stress and the isolation fraction, and these changes
174 are applied either separately or simultaneously (Table 1): the wind stress varies between 0.05 and
175 0.15 N m^{-2} corresponding to a variation of the pre-industrial overturning strength between 13
176 and 35 Sv, this range encapsulates the observed value of about 17 Sv for the Atlantic meridional
177 overturning circulation (McCarthy et al. 2015); and the isolation fraction varies between 0.1 and
178 0.9, encapsulating a data-based estimate of δ of about 0.7 (Talley 1999) .

179 The 1D box model starts by design from a steady state since the model only solves for anoma-
180 lies relative to its initial state. The box model with overturning is initialised with a prescribed
181 atmospheric $\text{CO}_2=280$ ppm, temperature and dissolved inorganic carbon for the mixed layer in
182 the low latitudes and the northern, the southern and deep ocean (Table 2), and a range of choices
183 in the Southern Ocean wind stress that provides the Ekman upwelling in the Southern Ocean and
184 the isolation fraction (Table 1). The model is integrated until the model transports, the thermo-
185 cline thickness and its temperature and dissolved inorganic carbon all adjust to an equilibrium
186 state (Appendix). The box model with overturning is simple enough to experience no significant
187 model drift beyond a negligible truncation error and so the model reaches a real equilibrium state.

188 This pre-industrial equilibrium state differs for each ensemble (Table 2) and then forms the initial
189 conditions for the model integrations with anthropogenic emissions.

190 Including anthropogenic emissions drives increasing radiative forcing and additional ocean heat
191 supply, which in turn alters the volume of light water and the strength of the meridional overturn-
192 ing. The change in the meridional overturning, $\Delta q_{NA}(t)$, involving the volume transport from the
193 upper ocean into the deep ocean in the high latitudes in the northern hemisphere, is related to the
194 total ocean heat uptake averaged over the surface area of light water, $N(t)$ in W m^{-2} , by

$$\Delta q_{NA}(t) = \frac{N(t)A_{low}}{\rho_o C_{p,o}(T_{light}(t) - T_{deep}(t))}, \quad (3)$$

195 where this change in overturning equates to changes in the North Atlantic Deep Water formation;
196 here A_{low} is the model area covered by the low latitudes, ρ_o is a referenced ocean density, $C_{p,o}$ is
197 the specific heat capacity for the ocean, and T_{light} and T_{deep} are the temperatures of light waters in
198 the low latitudes (mixed layer and thermocline) and of dense waters in the deep ocean respectively.

199 These changes in the strength of the meridional overturning, $q_{NA}(t)$ (Fig. 2a), drive subsequent
200 changes in the Southern Ocean residual circulation involving a surface warming conversion into
201 light waters in the southern high latitudes, $q_{so}(t)$ (Fig. 2b), and the diapycnal transfer in the low
202 latitudes, $q_v(t)$ (Fig. 2c), which then collectively alter the thickness of the thermocline, $h_{therm}(t)$
203 (Fig. 2d). The meridional overturning weakens with the additional surface heating during emis-
204 sions, but gradually recovers after emissions cease (Fig. 2). For simplicity, the climate feedback
205 parameter is chosen to remain constant in our sensitivity experiments, and so does not alter with
206 changes in the overturning, as instead explored by Winton et al. (2013) and Garuba et al. (2018).

207 3. Ocean mechanisms affecting the climate metric, the TCRE

208 The transient climate response to emissions, TCRE, defined by the ratio of the changes in global
209 mean surface air temperature since the pre-industrial era, $\Delta T(t)$, to the cumulative carbon emis-
210 sions, $I_{em}(t)$, may be interpreted as the product of a thermal contribution, $\Delta T(t)/R(t)$, and a car-
211 bon contribution, $R(t)/I_{em}(t)$ (Goodwin et al. 2015; Williams et al. 2016, 2017a; Katavouta et al.
212 2018):

$$\text{TCRE} = \frac{\Delta T(t)}{I_{em}(t)} = \frac{\Delta T(t)}{R(t)} \frac{R(t)}{I_{em}(t)}, \quad (4)$$

213 where $R(t)$ is the radiative forcing.

214 The carbon contribution, $R(t)/I_{em}(t)$, is affected by the ocean carbon uptake as the radiative
215 forcing, $R(t)$, is proportional to the logarithmic change in the atmospheric CO_2 relative to the
216 pre-industrial, $R(t) = a\Delta \ln \text{CO}_2(t)$.

217 In both our models, during emissions (black solid lines in Fig.3a, c), there is an increase in both
218 the atmosphere carbon inventory, ΔI_{atm} , (black dashed lines in Fig.3a, c) and the ocean carbon
219 inventory, ΔI_{ocean} , (black dashed-dotted lines in Fig.3a, c), where Δ represents changes relative to
220 the pre-industrial era. After emissions cease, the ocean carbon inventory increases at the expense
221 of the atmospheric carbon inventory, as carbon is transferred into the ocean until a new global
222 equilibrium is attained after typically 5000 years for a ventilation timescale of $\tau_{vent} = 1000$ y. This
223 transfer of carbon from the atmosphere into the ocean corresponds to a general decrease in the
224 carbon contribution, $R(t)/I_{em}(t)$, (red lines in Fig.3a, c) in time from the onset of emissions until
225 a new equilibrium is reached.

226 The thermal contribution, $\Delta T(t)/R(t)$, may be understood in terms of the empirical global heat
227 budget (2). The thermal contribution is controlled by the fraction of the radiative forcing, $R(t)$,

228 directed towards surface warming and providing a radiative response, $\lambda\Delta T(t)$, rather than an in-
229 crease in ocean heat content, $N(t)$.

230 In both our models, the radiative forcing increases during emissions and decreases after emis-
231 sions cease (black solid lines in Fig.3b, d) following the changes in atmospheric CO_2 . Initially
232 most of the radiative forcing is directed towards warming the ocean and increasing ocean heat
233 content, $N(t)$, (black dashed-dotted lines in Fig.3b, d). As the ocean interior warms, a larger frac-
234 tion of the radiative forcing is instead directed towards surface warming (black dashed lines in
235 Fig.3b, d). After emissions cease, ocean heat uptake gradually declines until the system reaches
236 equilibrium when there is no further ocean heat uptake and all the radiative forcing is directed
237 towards surface warming and providing a radiative response. This gradual decline in the fraction
238 of the radiative forcing directed towards ocean heat uptake corresponds to a general increase in the
239 thermal contribution, $\Delta T(t)/R(t)$ (red lines in Fig.3b, d), until a new equilibrium is attained.

240 For an atmosphere-ocean system at equilibrium, the climate response, $\Delta T(t_{eq})/I_{em}(t_{eq})$, is in-
241 dependent of the ocean ventilation and equal to $a/(\lambda I_B)$ (Williams et al. 2012), where I_B is the
242 buffered atmosphere and ocean carbon inventory at the pre-industrial (Goodwin et al. 2007). How-
243 ever, during the transient period, the thermal and carbon contributions to the TCRE are controlled
244 by how the ocean sequesters heat and carbon, and so the TCRE is a function of ocean ventilation.
245 The effect of different ventilation processes altering the TCRE is investigated next.

246 *a. Role of the thickness of the mixed layer*

247 In our 1D box model, the mixed layer responds relatively rapidly to any forcing applied at the
248 air-sea interface, compared with the response of the ocean interior. This fast response to emissions
249 dominates the climate response during the beginning of the twentieth century (Held et al. 2010).
250 A thick mixed layer leads to less atmospheric CO_2 and a smaller rise in surface air temperature,

251 so that the TCRE and its carbon, $R(t)/I_{em}(t)$, and thermal, $\Delta T(t)/R(t)$, contributions are smaller
252 (Fig. 4a, b and c).

253 The sensitivity of the TCRE (together with its thermal and carbon contributions) to the mixed-
254 layer thickness is largest during the first decade after the start of emissions and then declines in time
255 (Figs. 4a and 5a). After about a century, the TCRE dependence on the mixed-layer thickness is
256 small and eventually, after 500 years, the TCRE becomes independent of the mixed-layer thickness
257 (Fig. 5a middle and right panels).

258 The sensitivity of the thermal contribution for the TCRE to the mixed-layer thickness is gen-
259 erally larger than that of the carbon contribution (Figs. 4b,c, and 5b,c) as the ocean heat uptake
260 is enhanced by its specific heat capacity, while the carbon uptake is inhibited by ocean buffering
261 from carbonate chemistry.

262 *b. Role of the ventilation timescale*

263 In our 1D box model, the ventilation timescale controls the response of the ocean interior to
264 atmospheric changes. A shorter ventilation timescale corresponds to a more rapid ventilation rate
265 and an enhanced transfer of carbon and heat into the ocean interior. Hence, a shorter ventilation
266 timescale leads to a smaller TCRE, and a smaller carbon, $R(t)/I_{em}(t)$, and thermal, $\Delta T(t)/R(t)$,
267 contributions during the transient period before equilibrium (Fig. 4d, e and f).

268 The sensitivities of the carbon and thermal contributions to the ventilation rate operate on dif-
269 ferent timescales (Fig. 5b,c). On timescales of a decade to a century, the thermal contribution
270 dominates the sensitivity of the TCRE, while on timescales of 500 years, the carbon contribution
271 becomes more important. This difference in the sensitivities of the carbon and thermal contri-
272 butions to the TCRE is due to the ocean heat and carbon uptake being controlled by different

273 mechanisms operating on different timescales, such as involving the effects of heat storage and
274 climate feedback versus carbon storage and ocean carbonate chemistry.

275 The TCRE sensitivity to the ventilation timescale is relatively small compared to the TCRE
276 sensitivity to the thickness of the mixed layer during the first decade since the onset of emissions
277 (Fig 5a left panel). After the first decade, the TCRE becomes more sensitive to the ventilation
278 timescale and is further modified by the thickness of the mixed layer (Fig. 5a middle panel). On a
279 timescale of 500 years, the TCRE only depends on the ventilation timescale (Fig. 5a right panel).

280 *c. Role of the meridional overturning and isolation fraction*

281 In the box model with overturning, the ventilation is affected by two mechanisms: the strength
282 of overturning circulation and the extent of subduction in the Southern Ocean. The overturning
283 circulation controls the exchange of water between the upper ocean and the deep ocean, and so
284 alters the transfer of heat and carbon to the deep ocean. A stronger overturning is associated with
285 an enhanced transfer of heat and carbon into the deep ocean, and so leads to a smaller TCRE and
286 its carbon and thermal contributions (Fig. 6a, b and c), represented by $R(t)/I_{em}(t)$ and $\Delta T(t)/R(t)$,
287 respectively.

288 The isolation fraction, δ , sets the proportion of waters subducted in the Southern Ocean relative
289 to the total subduction rate. As δ increases, the proportion of waters subducted in the Southern
290 Ocean increases, which reduces the communication with the atmosphere in the low latitudes and
291 so reduces the uptake of heat and carbon there. In turn this reduced ocean heat and carbon uptake
292 leads to a larger TCRE and carbon, $R(t)/I_{em}(t)$, and thermal, $\Delta T(t)/R(t)$, contributions (Fig. 6d,
293 e and f). In addition, as δ increases, the thermocline waters become more isolated from the
294 atmosphere and so the TCRE becomes less sensitive to the overturning strength (Fig. 7a).

295 The sensitivities of the carbon, $R(t)/I_{em}(t)$, and thermal, $\Delta T(t)/R(t)$, contributions to the
296 strength of the overturning and the isolation fraction (Fig. 7b, c) operate in a similar manner
297 to the sensitivities to the rate of ventilation in the 1D box model (Fig. 5b, c): the thermal contribu-
298 tion again dominates the sensitivity of the TCRE on timescales of decades to a century, while the
299 carbon contribution becomes more important on timescales of 500 years.

300 **4. Controls of the variability in the climate metric, the TCRE**

301 The relative importance of the different ventilation mechanisms and emission scenarios in con-
302 trolling the TCRE are now examined using ensemble experiments covering a wide parameter space
303 (Table 1). The variability in the TCRE is quantified using the coefficient of variation, defined by
304 the ratio of the standard deviation and mean for a given ensemble of model experiment with per-
305 turbed parameters at a particular time (Hawkins and Sutton 2009; Williams et al. 2017b).

306 A coefficient of variation is estimated for each of the four sets of ensembles with perturbation
307 in either (i) the mixed-layer thickness, h_{ml} , (ii) the ventilation timescale, τ_{vent} , (iii) the strength of
308 the overturning circulation altering with variations in the zonal wind stress in the Southern Ocean,
309 τ_{wind} , or (iv) the proportion of water subducted in the Southern Ocean altering with the isolation
310 fraction, δ (Table 1). This statistical measure is also evaluated for ensembles with several thousand
311 members with combined perturbations in the input parameters for the 1D box model and the box
312 model with overturning.

313 *a. Effect of ocean ventilation on the TCRE variability*

314 In the 1D box model, the variability of the TCRE due to the combined variability of the mixed-
315 layer thickness and ventilation timescale is initially large, reduces over the next century, and subse-
316 quently increases over a couple of centuries before decreasing towards zero over several millennia

317 (black line in Fig. 8a). On decadal timescales, the thickness of the mixed layer controls the vari-
318 ability of the TCRE, while on timescales of several decades to a century, there is a decreasing
319 effect of mixed-layer thickness and an increasing importance of the ventilation timescale. Even-
320 tually after a couple of centuries, the ventilation timescale solely controls the variability of the
321 TCRE (black lines in Fig. 8a, b and c).

322 The variability in the TCRE is dominated by the thermal contribution, $\Delta T(t)/R(t)$, on timescales
323 from years to centuries, but is then dominated by the carbon contribution, $R(t)/I_{em}(t)$ (Fig. 8a,c).
324 Over the first century, the variability in the thermal contribution generally decreases in time, while
325 the variability in the carbon contribution slightly increases in time (red and blue lines in Fig. 8a).
326 This trend in the variability of the TCRE and its thermal contribution is generally consistent with
327 CMIP5 model diagnostics forced by a 1% increase in atmospheric CO₂ (Williams et al. 2017b).
328 However, in the CMIP5 diagnostics, there is an initial large variability in the carbon contribution
329 with a slight decreasing trend over the first 30 years since the pre-industrial, which is possibly due
330 to effects of the terrestrial carbon uptake or from the pre-industrial conditions in CMIP5 models
331 not being in equilibrium at the onset of emissions.

332 In the box model with overturning, the variability in the strength of the overturning and the
333 isolation fraction contribute equally to the variability of the TCRE on timescales of some cen-
334 turies (Fig. 8d, e, f), but the strength of overturning dominates on longer timescales. The thermal
335 contribution again dominates the variability in the TCRE on timescales up to some centuries (red
336 and blue lines in Fig.8d-f), but the carbon contribution becomes important on several centuries to
337 millennia.

338 From this sensitivity analysis, the implications for understanding inter-model variability in the
339 TCRE from Earth system models are that (i) on decadal timescales, inter-model differences in
340 the thickness of the mixed layer are likely to be a major source of variability through their effect

341 on ocean heat uptake, (ii) on timescales of decades to centuries, inter-model differences in the
342 ventilation of heat are likely to be a major source of uncertainty from inter-model differences in the
343 strength of overturning and mode water formation, and (iii) on centuries to millennia, inter-model
344 differences in the carbon contribution become important due to differences in the overturning.

345 *b. Effect of the carbon emissions on the TCRE variability*

346 The sensitivity analysis is repeated for different rates and duration of carbon emissions to explore
347 their interplay with the ventilated control of the TCRE (Fig. 9). The coefficient of variation for
348 changes in the mixed-layer thickness is generally similar for these experiments with different
349 carbon forcing (Fig. 9a).

350 The variability of the thermal contribution, $\Delta T(t)/R(t)$, due to changes in the ventilation
351 timescale is effectively independent of the rate of carbon emissions and when emissions cease
352 (red lines in Fig. 9b). However, the variability of the carbon contribution, $R(t)/I_{em}(t)$, due to
353 changes in the ventilation timescale does alter with the rate of carbon emissions and the time when
354 emissions cease. When there is more cumulative carbon emission, either from a larger emission
355 rate or emissions ceasing later, the variability of the carbon contribution is smaller in the centuries
356 after emissions ceasing (blue lines in Fig. 9b), which accordingly leads to the variability in the
357 TCRE also being smaller (black lines in Fig. 9b).

358 This dependence of the variability in the carbon contribution to the rate and duration of carbon
359 emissions is associated with the carbonate chemistry and changes in the buffering capacity of the
360 ocean. A greater cumulative carbon emission from a larger emission rate or prolonged carbon
361 emissions leads to a more acidic ocean surface during emissions, which alters the buffering ca-
362 pacity of the ocean. The ocean carbon uptake is then more controlled by these larger changes in
363 buffering capacity, rather than by the variability from the physical changes in ventilation, such as

364 from the ventilation timescale, the overturning strength and the isolation fraction (Fig. 9b, c and
365 d).

366 The timescale of variability of different ocean ventilation processes for the TCRE and its thermal
367 and carbon contribution are generally robust to changes in the strength of the emissions (Fig. 9),
368 despite the strength of the carbon contribution varying with the cumulative carbon emission.

369 **5. Discussion and summary**

370 Sensitivity experiments are conducted using conceptual atmosphere-ocean models to understand
371 how different aspects of ocean ventilation influence the climate metric, the Transient Climate
372 Response to cumulative carbon emissions (TCRE), and its thermal and carbon contributions. In
373 our experiments, the variability in the TCRE from ocean ventilation is dominated on timescales
374 of years to centuries by the thermal response and on timescales of centuries to millennia by the
375 carbon response. The effect of the ventilation is primarily controlled by the thickness of the mixed
376 layer on timescales of years to decades and then gradually switches to being controlled by the
377 rate of ventilation of the ocean thermocline and deep ocean on timescales of several decades and
378 longer. This rate of ventilation of the ocean interior is itself affected by both the variability in the
379 Atlantic meridional overturning circulation and the extent of subduction in the Southern Ocean,
380 with the variability in the meridional overturning circulation dominating on timescales of several
381 centuries and longer.

382 Idealised one-dimensional box models have been extensively used to understand the thermal
383 contribution of the ocean to the climate response to carbon emissions (Wigley and Schlesinger
384 1985; Gregory 2000; Held et al. 2010; Geoffroy et al. 2012; Kostov et al. 2014), together with a
385 more limited use of conceptual models including a physical representation of overturning (Mar-
386 shall and Zanna 2014). However, unlike previous studies, our models solve for changes in the

387 ocean heat and carbon budgets due to carbon emissions and hence allow the sensitivity of the
388 climate metric, the TCRE, to be assessed. Similarly to previous studies, the thermal response to
389 changes in radiative forcing undertakes a fast adjustment associated with the ocean mixed layer
390 on timescales of years to decades and a slow adjustment associated with the ventilation of the
391 ocean interior on timescales of decades to many centuries (Gregory 2000; Held et al. 2010). How-
392 ever, unlike previous studies, we demonstrate that the carbon response to carbon emissions also
393 undertakes a fast adjustment associated with the response of the ocean mixed layer and a slow
394 adjustment associated with the ventilation of the ocean interior. This slow adjustment of the car-
395 bon response becomes important in controlling variability in the TCRE on timescales of several
396 centuries to millennia. For the slow and fast responses, the timescales for the thermal and carbon
397 adjustment are not the same as they involve different effects for the thermal response from ocean
398 heat uptake and climate feedback and for the carbon response from ocean carbon uptake and ocean
399 carbonate chemistry.

400 Our sensitivity experiments suggest that the inter-model variability in the TCRE for Earth sys-
401 tem models is partly controlled by differences in ocean ventilation, associated with the thickness
402 of the mixed layer and the rate of ventilation of the ocean interior. Changes in the ocean circula-
403 tion redistribute the heat in the ocean and modify the pattern of sea surface warming (Banks and
404 Gregory 2006; Xie and Vallis 2012; Garuba and Klinger 2016). This dynamic effect from the evo-
405 lution of the overturning circulation with warming is captured in our box model with overturning
406 and so our experiments include this effect on the TCRE. However, our model omits any connection
407 between the pattern of sea surface warming and the cloud cover and climate feedbacks (Rose et al.
408 2014; Rugenstein et al. 2016; Trossman et al. 2016; Ceppi and Gregory 2017; Andrews and Webb
409 2018). Our model also ignores the time evolution of the climate feedbacks (Andrews et al. 2012)
410 associated with the changes in the pattern of surface warming (Armour et al. 2013; Andrews et al.

411 2015). These changes in the climate feedbacks with the evolving pattern of sea surface warming
412 contribute further to inter-model variability in Earth system models.

413 Our box model with overturning only provides a crude representation of the Southern Ocean, a
414 region of enhanced anthropogenic ocean heat and carbon uptake that is highly variable amongst
415 the Earth system models (Frölicher et al. 2015). The fraction of isolation in our conceptual model
416 is meant to represent the variability in intermediate and sub-Antarctic mode water formation, but
417 omits changes in Antarctic bottom water formation. Our conceptual models only include the at-
418 mosphere and ocean, so omit the effect of the terrestrial system, which strongly varies within Earth
419 system models (Arora et al. 2013; Friedlingstein et al. 2014) and drives much of the variability in
420 the carbon contribution to the TCRE (Williams et al. 2017b). However, after emissions cease, the
421 terrestrial uptake of carbon will decline (e.g. Williams et al. 2017a) and the variability in the ocean
422 carbon uptake is expected instead to dominate on timescales of many centuries and longer. Our
423 conceptual models also omit ocean biology and calcium carbonate cycling. While inter-model
424 differences in the representation of ocean biology affect the regional ocean carbon response, their
425 global contribution turns out to be minor on centennial timescales. Likewise inter-model variabil-
426 ity in calcium carbonate cycling and sediment changes only becomes important in affecting the
427 amount of atmospheric CO₂ and modifying the climate response on timescales of several millennia
428 (Archer 2005; Goodwin et al. 2009).

429 While our conceptual study makes simplifying assumptions, our aim is to reveal the importance
430 of the separate physical processes contributing to ocean ventilation and their effect on the climate
431 response to carbon emissions on timescales of years to many centuries. In a realistic Earth system
432 model, the different contributions to ocean ventilation from mixed-layer thickness and circulation
433 changes all occur in an inter-connected manner. However, in our conceptual model, the different
434 ventilation contributions are imposed in a separate manner to reveal the relative importance of

435 changes in mixed-layer thickness and ventilation rate of the ocean interior including the effects of
436 the strength of the meridional overturning and the extent of Southern Ocean mode water formation.
437 By adopting a conceptual model, our ventilation study is also able to span a wide parameter space
438 using a large number of ensembles. Our ensemble analysis suggests that inter-model differences
439 in the TCRE from ocean ventilation are dominated by thermal processes on timescales of years
440 to several centuries and by differences in ocean carbon uptake on timescales of several centuries
441 and longer. Hence, the study provides mechanistic insight into how ocean ventilation affects the
442 climate response during emissions and after emissions cease, as well as providing a well-posed
443 reference point to interpret inter-model variability in the response of complex Earth systems to
444 climate forcing.

445 *Acknowledgments.* This work was supported by a UK Natural Environmental Research Council
446 grant NE/N009789/1. This manuscript benefited from constructive comments from three referees.

447 APPENDIX

448 **Appendix: Box model with overturning**

449 *Volume budget*

450 The dynamics of the box model with overturning is based on the model by Gnanadesikan (1999)
451 (black solid lines and black arrows in Fig. 1b). The thickness of the light water, $h(t)$, is set
452 by the volume balance between the volume transports associated with sinking in the northern
453 high latitudes, $q_{NA}(t)$, diapycnal upwelling in the low latitudes, $q_v(t)$, and the residual circulation
454 involving the Ekman upwelling in the southern high latitudes driven by winds and the return flow

455 due to baroclinic eddies, $q_{so}(t) = q_{Ekman} + q_{eddy}(t)$, such that

$$A_{low} \frac{dh(t)}{dt} = q_{NA}(t) + q_v(t) + q_{so}(t), \quad (A1)$$

456 where $A_{low} = 2 \times 10^{14} \text{ m}^2$ is the area covered by the low latitudes.

457 The volume transport associated with the Ekman upwelling, q_{Ekman} , is specified as

$$q_{Ekman} = \frac{\tau_{wind} L_x}{\rho_o f}, \quad (A2)$$

458 where $L_x = 30000 \text{ km}$ is the zonal extent of Southern Ocean, $\rho_o = 1025 \text{ kg m}^{-3}$ is a referenced
 459 ocean density, f is the Coriolis parameter and τ_{wind} is the zonal wind stress varying in the sensi-
 460 tivity experiments from 0.05 to 0.15 N m^{-2} encapsulating the typical value of 0.1 N m^{-2} for the
 461 wind stress; this typical value of the wind stress is expected to be somewhat larger in the Southern
 462 Ocean.

463 The volume transport associated with the baroclinic eddies in the Southern Ocean, $q_{eddy}(t)$, is
 464 parametrised as

$$q_{eddy}(t) = -\frac{k_{eddy} L_x h(t)}{L_y}, \quad (A3)$$

465 where $k_{eddy} = 10^3 \text{ m}^2 \text{ s}^{-1}$ is the eddy diffusion coefficient, and $L_y = 1500 \text{ km}$ is the meridional
 466 extent of the Southern Ocean.

467 The volume transport associated with the diapycnal upwelling, $q_v(t)$, is parametrised as

$$q_v(t) = \frac{A_{low} k_v}{h(t)}, \quad (A4)$$

468 where $k_v = 10^{-5} \text{ m}^2 \text{ s}^{-1}$ is the diapycnal mixing coefficient.

469 The volume transport associated with the sinking in the northern high latitudes, $q_{NA}(t)$ is
 470 parametrised as

$$q_{NA}(t) = -\frac{g'}{2f} h(t_o)^2 + \Delta q_{NA}(t), \quad (A5)$$

471 where $g' = 0.02 \text{ m s}^{-2}$ is the reduced gravity, t_o is the pre-industrial era and Δ is the change rela-
 472 tive to the pre-industrial. The changes in the volume transport associated with the sinking in the
 473 northern latitudes, $\Delta q_{NA}(t)$, are controlled by the ocean heat uptake due to anthropogenic emis-
 474 sions, $N(t)$, and the temperature contrast between the light and dense waters in the low latitudes,
 475 $T_{light}(t) - T_{deep}(t)$, as described by (3) and so (A5) becomes

$$q_{NA}(t) = -\frac{g'}{2f}h(t_o)^2 + \frac{N(t)A_{low}}{\rho_o C_{p,o}(T_{light}(t) - T_{deep}(t))}. \quad (\text{A6})$$

476 The model is initialised with a random thickness of light waters, h , and integrated to a steady
 477 state, which provides the volume transports and the thickness of the thermocline in low latitudes in
 478 the pre-industrial era, $h(t_o)$ (Table 2). The volume transports and the upper ocean thickness, $h(t)$,
 479 evolve with warming due to emissions according to (A1) to (A6) (Fig. 2). The total ocean depth
 480 is assumed constant and equal to 4000 m. The deep ocean thickness in the low latitudes evolves
 481 following the changes in the upper ocean thickness.

482 *Thermal and carbon budgets*

483 There is air-sea exchange of heat and carbon between the slab atmosphere and the upper ocean.
 484 In the low latitudes, the upper ocean consists of a layer of light water separated into two layers
 485 (Fig.1b): a mixed layer with fixed thickness, $h_{ml} = 100 \text{ m}$, and a thermocline layer with varying
 486 thickness set by the volume transports, $h_{therm}(t) = h(t) - h_{ml}$. In the high latitudes, the upper
 487 ocean is represented by boxes for the Southern Ocean and the northern high latitudes, both with
 488 fixed thicknesses of $h_{high} = 1000 \text{ m}$.

489 The model is initialised and run to thermal and carbon equilibrium where there is no net ocean
 490 heat and carbon uptake and the heat and carbon divergence at each of the ocean boxes in con-
 491 tact with the atmosphere are balanced by heat and carbon fluxes from the atmosphere. This pre-

492 industrial state has (i) higher dissolved inorganic carbon in the high latitudes and the deep ocean,
 493 and ocean carbon uptake in the northern high latitudes and ocean carbon release in the low lati-
 494 tudes, and (ii) higher temperature in the upper ocean in the low latitudes, and ocean heat uptake at
 495 the low latitudes and ocean heat release at the northern high latitudes. An example of the model
 496 pre-industrial ocean heat and carbon distribution is shown in Table 2.

497 The discrete form of the divergence theorem is used to express the heat and carbon budgets. The
 498 budget for a scalar C such as temperature or dissolved inorganic carbon of a box/layer is expressed
 499 as

$$\frac{d}{dt} (C_{box}(t)V_{box}(t)) = - \int_{box} \nabla \cdot (C(t)\vec{v}(t)) dV + S_C(t), \quad (A7)$$

500 where $\vec{v}(t)$ is the velocity of the flow into the box, V is the volume and S_C is a source/sink of C ,
 501 for example representing the supply of C from the atmosphere into the ocean. The discrete form
 502 of the divergence theorem for this box is expressed as

$$\int_{box} \nabla \cdot (C\vec{v}) dV = \oint_{box} C\vec{v} \cdot d\vec{S} = - \Delta_{box} (Cq), \quad (A8)$$

503 where S is the boundary surface of the volume V with $d\vec{S}$ being outward pointing, q is a volume
 504 transport through the boundary surface of the box and is positive into the box, and Δ_{box} notes the
 505 transports of C into the box minus the transports of C out of the box. The change in the sign when
 506 using Δ_{box} is due to the transport being defined positive into the box. As an example for the deep
 507 ocean, $\Delta_{deep} (C(t)q(t)) = -(q_{NA}(t)C_N(t) + q_{SO}(t)C_{deep}(t) + q_v(t)C_{deep}(t))$, which represents that
 508 the total convergence of C in the deep ocean box is equal to the amount of the scalar C sinking in
 509 the northern high latitudes into the deeper ocean (with q_{NA} being negative) minus the amount of
 510 the tracer C returning from the deep ocean into the upper ocean either in the Southern Ocean or in
 511 the low latitudes by diapycnal transfer.

512 Using (A7) and (A8), the budget for a scalar C becomes

$$\frac{d}{dt} (C_{box}(t)V_{box}(t)) = \Delta_{box} (C(t)q(t)) + S_C(t). \quad (\text{A9})$$

513 This discrete form of the budget given by (A9) is used to express the heat and carbon budgets in
514 the model.

515 The changes in the heat budget for the global model driven by the radiative forcing, R , are
516 described by

$$\rho_a C_{p,a} A h_{atm} \frac{d}{dt} (T_{atm}(t)) + \rho_o C_{p,o} \sum_{box}^{ocean} \frac{d}{dt} (T_{box}(t)V_{box}(t)) = AN_{TOA}(t), \quad (\text{A10a})$$

$$\rho_a C_{p,a} A h_{atm} \frac{d}{dt} (T_{atm}(t)) = A (N_{TOA}(t) - N(t)), \quad (\text{A10b})$$

$$\rho_o C_{p,o} \sum_{box}^{ocean} \frac{d}{dt} (T_{box}(t)V_{box}(t)) = AN(t), \quad (\text{A10c})$$

$$N(t) = \frac{1}{A} \sum_{box}^{ocean} (A_{box} N_{box}(t)), \quad (\text{A10d})$$

517 with the changes in the heat budget of each individual box being described by

$$\rho_o C_{p,o} \frac{d}{dt} (T_{box}(t)V_{box}(t)) = \rho_o C_{p,o} \Delta_{box} (q(t)T(t)) + A_{box} N_{box}(t), \quad (\text{A11})$$

518 where subscript box indicates the different ocean boxes/layers in the model, $A = \sum_{box}^{ocean} A_{box}$ is the
519 area of the ocean, equal to the area of the atmosphere, h_{atm} is the thickness of the slab atmosphere,
520 $T_{atm}(t)$ in K is the temperature of the slab atmosphere, $q(t)$ is the volume transport in Sv, $T_{box}(t)$ in
521 K is the ocean temperature for each ocean box, $N_{box}(t)$ and $N(t)$ in Wm^{-2} are the heat flux from the
522 atmosphere into each ocean box and into the entire ocean, respectively, with N_{therm} and N_{deep} being
523 zero as the thermocline and the deep ocean are not in direct contact with the atmosphere, $N_{TOA}(t)$
524 in Wm^{-2} is the net downward heat flux entering the system at the top of the atmosphere in response
525 to the carbon emissions, $\rho_a = 1 \text{ kg m}^{-3}$ and $\rho_o = 1025 \text{ kg m}^{-3}$ are a referenced atmosphere and
526 ocean density, respectively, and $C_{p,a} = 1000 \text{ J kg}^{-1} \text{ K}^{-1}$ and $C_{p,o} = 4000 \text{ J kg}^{-1} \text{ K}^{-1}$ are the

527 specific heat capacities for the atmosphere and ocean, respectively. There is no net ocean heat
 528 uptake in the pre-industrial, $N(t_o) = 0$, and the ocean heat uptake due to the increase in radiative
 529 forcing, $N(t) - N(t_o) = N(t)$, is distributed equally over the ocean surface area. The net downward
 530 heat flux, $N_{TOA}(t)$, and the instantaneous flux of heat from the ocean into the atmosphere (defined
 531 as positive upwards), $N_{TOA}(t) - N(t)$, in response to the carbon emissions, are expressed as

$$N_{TOA}(t) = R(t) - \lambda \Delta T_{atm}(t), \quad (\text{A12a})$$

$$N_{TOA}(t) - N(t) = c(\Delta T_{surf}(t) - \Delta T_{atm}(t)), \quad (\text{A12b})$$

532 where λ in $\text{W m}^{-2} \text{K}^{-1}$ is the climate feedback parameter, c in $\text{W m}^{-2} \text{K}^{-1}$ is an air-sea heat
 533 transfer parameter, Δ is the change relative to the pre-industrial, and $T_{surf}(t)$ in K is the temperature
 534 of the ocean surface, which is defined by an area-weighted average of the temperature for the boxes
 535 in contact with the atmosphere. In the main text, T_{atm} is referred to as T for simplicity.

536 The changes in the carbon budget of the global model driven by the imposed carbon emissions,
 537 $F_{em}(t)$ in $\text{mol C m}^{-2} \text{s}^{-1}$ are described by

$$M_a \frac{d}{dt} (CO_2(t)) + \rho_o \sum_{box}^{ocean} \frac{d}{dt} (DIC_{box}(t) V_{box}(t)) = A F_{em}(t), \quad (\text{A13a})$$

$$M_a \frac{d}{dt} (CO_2(t)) = A (F_{em}(t) - F(t)), \quad (\text{A13b})$$

$$\rho_o \sum_{box}^{ocean} \frac{d}{dt} (DIC_{box}(t) V_{box}(t)) = A F(t), \quad (\text{A13c})$$

$$F(t) = \frac{1}{A} \sum_{box}^{ocean} (A_{box} F_{box}(t)), \quad (\text{A13d})$$

538 with the changes in the carbon budget of each individual box being described by

$$\rho_o \frac{d}{dt} (DIC_{box}(t) V_{box}(t)) = \rho_o \Delta_{box} (q(t) DIC(t)) + A_{box} F_{box}(t), \quad (\text{A14})$$

539 where $CO_2(t)$ is the atmospheric CO_2 , M_a is the number of moles of gas in the atmosphere,
 540 $DIC_{box}(t)$ in mol C kg^{-1} is the dissolved inorganic carbon for each ocean box, $F_{box}(t)$ and $F(t)$

541 in $\text{mol C m}^{-2}\text{s}^{-1}$ are the carbon flux from the atmosphere into each ocean box and into the entire
542 ocean, respectively, with F_{therm} and F_{deep} being zero as the thermocline and the deep ocean are not
543 in direct contact with the atmosphere. There is no net ocean carbon uptake in the pre-industrial,
544 $F(t_o) = 0$, and the ocean carbon uptake due to the carbon emissions, $F(t) - F(t_o) = F(t)$, is
545 distributed equally over the ocean surface area, and is expressed as

$$F(t) = \rho_o K_g (K_o(t) CO_2(t) - [CO_2(t)]_{surf}), \quad (\text{A15})$$

546 where K_g in m s^{-1} is the air-sea gas transfer coefficient, $K_o(t)$ in mol C kg^{-1} is the solubility
547 of carbon in the ocean water and $[CO_2(t)]_{surf}$ in mol C kg^{-1} is the dissolved CO_2 at the ocean
548 surface. The dissolved CO_2 at the ocean surface is estimated based on the partitioning of the
549 dissolved inorganic carbon at the surface using the iterative algorithm of Follows et al. (2006) by
550 ignoring changes in biology or weathering, and by assuming the total alkalinity remains constant.
551 This partitioning method accounts for the evolution of the ocean carbon equilibrium coefficients
552 with changes in temperature and solves for the changes in the ocean pH with changes in the
553 dissolved CO_2 . The surface DIC of the ocean is defined from a volume weighting of the DIC in
554 the boxes in contact with the atmosphere.

555 A summary for the values of parameters in the box model with overturning that are kept constant
556 in the sensitivity experiment is provided in the supplementary information.

557 **References**

558 Allen, M. R., D. J. Frame, C. Huntingford, C. D. Jones, J. A. Lowe, M. Meinshausen, and N. Mein-
559 shausen, 2009: Warming caused by cumulative carbon emissions towards the trillionth tonne.
560 *Nature*, **458**, 1163–1166, doi:10.1038/nature08019.

- 561 Andrews, T., J. M. Gregory, and M. J. Webb, 2015: The dependence of radiative forcing and
562 feedback on evolving patterns of surface temperature change in climate models. *Journal of*
563 *Climate*, **28** (4), 1630–1648, doi:10.1175/JCLI-D-14-00545.1.
- 564 Andrews, T., J. M. Gregory, M. J. Webb, and K. E. Taylor, 2012: Forcing, feedbacks and climate
565 sensitivity in CMIP5 coupled atmosphere-ocean climate models. *Geophysical Research Letters*,
566 **39** (9), doi:10.1029/2012GL051607.
- 567 Andrews, T., and M. J. Webb, 2018: The dependence of global cloud and lapse rate feedbacks
568 on the spatial structure of tropical Pacific warming. *Journal of Climate*, **31** (2), 641–654, doi:
569 10.1175/JCLI-D-17-0087.1.
- 570 Archer, D., 2005: Fate of fossil fuel CO₂ in geologic time. *Journal of Geophysical Research:*
571 *Oceans*, **110** (C9), doi:10.1029/2004JC002625.
- 572 Armour, K. C., C. M. Bitz, and G. H. Roe, 2013: Time-varying climate sensitivity from regional
573 feedbacks. *Journal of Climate*, **26** (13), 4518–4534, doi:10.1175/JCLI-D-12-00544.1.
- 574 Arora, V. K., and Coauthors, 2013: Carbon-concentration and carbon-climate feedbacks in CMIP5
575 Earth system models. *Journal of Climate*, **26** (15), 5289–5314, doi:10.1175/JCLI-D-12-00494.
576 1.
- 577 Banks, H. T., and J. M. Gregory, 2006: Mechanisms of ocean heat uptake in a coupled climate
578 model and the implications for tracer based predictions of ocean heat uptake. *Geophysical Re-*
579 *search Letters*, **33** (7), doi:10.1029/2005GL025352.
- 580 Ceppi, P., and J. M. Gregory, 2017: Relationship of tropospheric stability to climate sensitivity and
581 Earth’s observed radiation budget. *Proceedings of the National Academy of Sciences*, **114** (50),
582 13 126–13 131, doi:10.1073/pnas.1714308114.

583 Cheng, W., J. C. H. Chiang, and D. Zhang, 2013: Atlantic meridional overturning circulation
584 (AMOC) in CMIP5 models: RCP and historical simulations. *Journal of Climate*, **26** (18), 7187–
585 7197, doi:10.1175/JCLI-D-12-00496.1.

586 Church, J. A., and Coauthors, 2011: Revisiting the Earth’s sea-level and energy budgets from 1961
587 to 2008. *Geophysical Research Letters*, **38** (18), L18 601, doi:10.1029/2011GL048794.

588 Follows, M. J., T. Ito, and S. Dutkiewicz, 2006: On the solution of the carbonate chemistry system
589 in ocean biogeochemistry models. *Ocean Modelling*, **12**, 290–301, doi:https://doi.org/10.1016/
590 j.ocemod.2005.05.004.

591 Forster, P. M., T. Andrews, P. Good, J. M. Gregory, L. S. Jackson, and M. Zelinka, 2013: Evalu-
592 ating adjusted forcing and model spread for historical and future scenarios in the CMIP5 gener-
593 ation of climate models. *Journal of Geophysical Research: Atmospheres*, **118** (3), 1139–1150,
594 doi:10.1002/jgrd.50174.

595 Friedlingstein, P., M. Meinshausen, V. K. Arora, C. D. Jones, A. Anav, S. K. Liddicoat, and
596 R. Knutti, 2014: Uncertainties in CMIP5 climate projections due to carbon cycle feedbacks.
597 *Journal of Climate*, **27** (2), 511–526, doi:10.1175/JCLI-D-12-00579.1.

598 Frölicher, T. L., J. L. Sarmiento, D. J. Paynter, J. P. Dunne, J. P. Krasting, and M. Winton, 2015:
599 Dominance of the Southern Ocean in anthropogenic carbon and heat uptake in CMIP5 models.
600 *Journal of Climate*, **28** (2), 862–886, doi:10.1175/JCLI-D-14-00117.1.

601 Garuba, O. A., and B. A. Klinger, 2016: Ocean heat uptake and interbasin transport of the passive
602 and redistributive components of surface heating. *Journal of Climate*, **29** (20), 7507–7527, doi:
603 10.1175/JCLI-D-16-0138.1.

- 604 Garuba, O. A., J. Lu, F. Liu, and H. A. Singh, 2018: The active role of the ocean in the temporal
605 evolution of climate sensitivity. *Geophysical Research Letters*, **45** (1), 306–315, doi:10.1002/
606 2017GL075633.
- 607 Geoffroy, O., D. Saint-Martin, and A. Ribes, 2012: Quantifying the sources of spread in climate
608 change experiments. *Geophysical Research Letters*, **39** (24), doi:10.1029/2012GL054172.
- 609 Gillet, N. P., V. K. Arora, D. Matthews, and M. R. Allen, 2013: Constraining the ratio of global
610 warming to cumulative CO₂ emissions using CMIP5 simulations. *Journal of Climate*, **26**, 6844–
611 6858, doi:10.1175/JCLI-D-12-00476.1.
- 612 Gnanadesikan, A., 1999: A simple predictive model of the structure of the oceanic pycnocline.
613 *Science*, **283**, 2077–2081, doi:10.1126/science.283.5410.2077.
- 614 Goodwin, P., R. G. Williams, M. J. Follows, and S. Dutkiewicz, 2007: Ocean-atmosphere parti-
615 tioning of anthropogenic carbon dioxide on centennial timescales. *Global Biogeochemical Cy-
616 cles*, **21** (1), GB1014, doi:10.1029/2006GB002810.
- 617 Goodwin, P., R. G. Williams, and A. Ridgwell, 2015: Sensitivity of climate to cumulative carbon
618 emissions due to compensation of ocean heat and carbon uptake. *Nature Geoscience*, **8**, 29–34,
619 doi:10.1038/ngeo2304.
- 620 Goodwin, P., R. G. Williams, R. G. Ridgwell, and M. J. Follows, 2009: Climate sensitivity to the
621 carbon cycle modulated by past and future changes to ocean chemistry. *Nature Geoscience*, **2**,
622 145–150, doi:10.1038/ngeo416.
- 623 Gregory, J. M., 2000: Vertical heat transports in the ocean and their effect on time-dependent
624 climate change. *Climate Dynamics*, **16**, 501–515, doi:10.1007/s003820000059.

- 625 Gregory, J. M., and P. M. Forster, 2008: Transient climate response estimated from radiative
626 forcing and observed temperature change. *Journal of Geophysical Research: Atmospheres*, **113**,
627 D23 105, doi:10.1029/2008JD010405.
- 628 Gregory, J. M., and Coauthors, 2004: A new method for diagnosing radiative forcing and climate
629 sensitivity. *Geophysical Research Letters*, **31 (3)**, L03 205, doi:10.1029/2003GL018747.
- 630 Gregory, J. M., and Coauthors, 2005: A model intercomparison of changes in the Atlantic ther-
631 mohaline circulation in response to increasing atmospheric CO₂ concentration. *Geophysical*
632 *Research Letters*, **32 (12)**, doi:10.1029/2005GL023209.
- 633 Hawkins, E., and R. Sutton, 2009: The potential to narrow uncertainty in regional climate pre-
634 dictions. *Bulletin of the American Meteorological Society*, **90 (8)**, 1095–1108, doi:10.1175/
635 2009BAMS2607.1.
- 636 Held, I. M., M. Winton, K. Takahashi, T. Delworth, F. Zeng, and G. K. Vallis, 2010: Probing
637 the fast and slow components of global warming by returning abruptly to preindustrial forcing.
638 *Journal of Climate*, **23 (9)**, 2418–2427, doi:10.1175/2009JCLI3466.1.
- 639 Johnson, H. L., D. P. Marshall, and D. A. J. Sproson, 2007: Reconciling theories of a mechanically
640 driven meridional overturning circulation with thermohaline forcing and multiple equilibria.
641 *Climate Dynamics*, **29 (7)**, 821–836, doi:10.1007/s00382-007-0262-9.
- 642 Katavouta, A., R. G. Williams, P. Goodwin, and V. Roussenov, 2018: Reconciling atmospheric and
643 oceanic views of the Transient Climate Response to Emissions. *Geophysical Research Letters*,
644 **45 (12)**, 6205–6214, doi:10.1029/2018GL077849.

645 Kostov, Y., K. C. Armour, and J. Marshall, 2014: Impact of the Atlantic meridional overturning
646 circulation on ocean heat storage and transient climate change. *Geophysical Research Letters*,
647 **41** (6), 2108–2116, doi:10.1002/2013GL058998.

648 MacDougall, A. H., N. C. Swart, and R. Knutti, 2017: The uncertainty in the transient climate
649 response to cumulative CO₂ emissions arising from the uncertainty in physical climate parame-
650 ters. *Journal of Climate*, **30** (2), 813–827, doi:10.1175/JCLI-D-16-0205.1.

651 Marshall, D. P., and L. Zanna, 2014: A conceptual model of ocean heat uptake under climate
652 change. *Journal of Climate*, **27** (22), 8444–8465, doi:10.1175/JCLI-D-13-00344.1.

653 Matthews, H. D., N. P. Gillett, P. A. Stott, and K. Zickfeld, 2009: The proportionality of global
654 warming to cumulative carbon emissions. *Nature*, **459**, 829–833, doi:10.1038/nature08047.

655 McCarthy, G., and Coauthors, 2015: Measuring the Atlantic Meridional Overturning Circulation
656 at 26°N. *Progress in Oceanography*, **130**, 91 – 111, doi:https://doi.org/10.1016/j.pocean.2014.
657 10.006.

658 Myhre, G., E. J. Highwood, K. P. Shine, and F. Stordal, 1998: New estimates of radiative forcing
659 due to well mixed greenhouse gases. *Geophysical Research Letters*, **25**, 2715–2718, doi:10.
660 1029/98GL01908.

661 Raper, S. C. B., J. M. Gregory, and R. J. Stouffer, 2002: The role of climate sensitivity and ocean
662 heat uptake on AOGCM transient temperature response. *Journal of Climate*, **15** (1), 124–130,
663 doi:10.1175/1520-0442(2002)015<0124:TROCSA>2.0.CO;2.

664 Roemmich, D., J. Church, J. Gilson, D. Monselesan, P. Sutton, and S. Wijffels, 2015: Unabated
665 planetary warming and its ocean structure since 2006. *Nature Climate Change*, **5** (3), 240, doi:
666 https://doi.org/10.1038/nclimate2513.

- 667 Rose, B. E. J., K. C. Armour, D. S. Battisti, N. Feldl, and D. D. B. Koll, 2014: The dependence of
668 transient climate sensitivity and radiative feedbacks on the spatial pattern of ocean heat uptake.
669 *Geophysical Research Letters*, **41** (3), 1071–1078, doi:10.1002/2013GL058955.
- 670 Rugenstein, M. A., K. Caldeira, and R. Knutti, 2016: Dependence of global radiative feedbacks
671 on evolving patterns of surface heat fluxes. *Geophysical Research Letters*, **43** (18), 9877–9885,
672 doi:10.1002/2016GL070907.
- 673 Rugenstein, M. A. A., M. Winton, R. J. Stouffer, S. M. Griffies, and R. Hallberg, 2013: Northern
674 high-latitude heat budget decomposition and transient warming. *Journal of Climate*, **26** (2),
675 609–621, doi:10.1175/JCLI-D-11-00695.1.
- 676 Sabine, C. L., and Coauthors, 2004: The oceanic sink for anthropogenic CO₂. *Science*, **305** (5682),
677 367–371, doi:10.1126/science.1097403.
- 678 Solomon, S., G.-K. Plattner, R. Knutti, and P. Friedlingstein, 2009: Irreversible climate change
679 due to carbon dioxide emissions. *Proc. Natl. Acad. Sci. USA*, **106**, 1704–1709, doi:10.1073/
680 pnas.0812721106.
- 681 Talley, L. D., 1999: Some aspects of ocean heat transport by the shallow, intermediate and deep
682 overturning circulations. *Mechanisms of Global Climate Change at Millennial Time Scales*, P.
683 U. Clark and R. S. Webb and L. D. Keigwin, 1–22, doi:10.1029/GM112p0001.
- 684 Trossman, D. S., J. B. Palter, T. M. Merlis, Y. Huang, and Y. Xia, 2016: Large-scale ocean
685 circulation-cloud interactions reduce the pace of transient climate change. *Geophysical Re-*
686 *search Letters*, **43** (8), 3935–3943, doi:10.1002/2016GL067931.
- 687 Wigley, T. M. L., and M. E. Schlesinger, 1985: Analytical solution for the effect of increasing
688 CO₂ on global mean temperature. *Nature*, **315**, 649–652, doi:10.1038/315649a0.

689 Williams, R. G., P. Goodwin, A. Ridgwell, and P. L. Woodworth, 2012: How warming and steric
690 sea level rise relate to cumulative carbon emissions. *Geophysical Research Letters*, **39**, L19 715,
691 doi:10.1029/2012GL052771.

692 Williams, R. G., P. Goodwin, V. M. Roussenov, and L. Bopp, 2016: A framework to understand
693 the Transient Climate Response to Emissions. *Environmental Research Letters*, **11**, doi:10.1088/
694 1748-9326/11/1/015003.

695 Williams, R. G., V. Roussenov, T. L. Frölicher, and P. Goodwin, 2017a: Drivers of continued
696 surface warming after the cessation of carbon emissions. *Geophysical Research Letters*, **44**,
697 10,633–10,642, doi:10.1002/2017GL075080.

698 Williams, R. G., V. Roussenov, P. Goodwin, L. Resplandy, and L. Bopp, 2017b: Sensitivity of
699 global warming to carbon emissions: Effects of heat and carbon uptake in a suite of Earth
700 system models. *Journal of Climate*, **30 (23)**, 9343–9363, doi:10.1175/JCLI-D-16-0468.1.

701 Winton, M., S. M. Griffies, B. L. Samuels, J. L. Sarmiento, and T. L. Frölicher, 2013: Connecting
702 changing ocean circulation with changing climate. *Journal of Climate*, **26 (7)**, 2268–2278, doi:
703 10.1175/JCLI-D-12-00296.1.

704 Xie, P., and G. K. Vallis, 2012: The passive and active nature of ocean heat uptake in
705 idealized climate change experiments. *Climate Dynamics*, **38 (3)**, 667–684, doi:10.1007/
706 s00382-011-1063-8.

707 Zickfeld, K., M. Eby, H. D. Matthews, and A. J. Weaver, 2009: Setting cumulative emissions
708 targets to reduce the risk of dangerous climate change. *Proc. Natl. Acad. Sci. USA*, **106**, 16 129–
709 16 134, doi:10.1073/pnas.0805800106.

710 **LIST OF TABLES**

711 **Table 1.** Sensitivity experiments: parameter space of the model ensembles. The venti-
 712 lation timescale sets the rate of ventilation of the ocean interior in the 1D box
 713 model. The Southern Ocean wind stress sets the strength of the overturning
 714 circulation. The isolation fraction sets the proportion of water that is subducted
 715 in the Southern Ocean. Note that the experiment with variations in both the
 716 mixed layer and the ventilation timescale consists of 4896 ensembles (51×96
 717 ensembles) and the experiment with variations in both Southern Ocean wind
 718 stress and isolation fraction consists of 8181 ensembles (101×81 ensembles). . . . 36

719 **Table 2.** Pre-industrial state in the box model with overturning for different choices of
 720 Southern Ocean wind stress, τ_{wind} , and isolation fraction, δ . The pre-industrial
 721 atmospheric $\text{CO}_2 = 280$ ppm is prescribed in all the ensembles. The pre-
 722 industrial distribution of heat and carbon, and the volume transports vary in
 723 the sensitivity experiments, so as an example values from three ensembles are
 724 presented. Subscripts N , S , $deep$, ml and $therm$ note the southern high latitude,
 725 the northern high latitude, the deep ocean, the mixed layer and the thermo-
 726 cline, respectively. Here the flux of heat and carbon into the ocean is shown
 727 in W and mol s^{-1} to highlight the thermal and carbon equilibrium state in the
 728 pre-industrial. . . . 37

729 TABLE 1. Sensitivity experiments: parameter space of the model ensembles. The ventilation timescale sets the
730 rate of ventilation of the ocean interior in the 1D box model. The Southern Ocean wind stress sets the strength of
731 the overturning circulation. The isolation fraction sets the proportion of water that is subducted in the Southern
732 Ocean. Note that the experiment with variations in both the mixed layer and the ventilation timescale consists
733 of 4896 ensembles (51×96 ensembles) and the experiment with variations in both Southern Ocean wind stress
734 and isolation fraction consists of 8181 ensembles (101×81 ensembles).

variable	lower limit	upper limit	interval of variation	number of ensembles
1D box model				
mixed-layer thickness (h_{ml})	50 m	300 m	5 m	51
ventilation timescale (τ_{vent})	100 y	2000 y	20 y	96
box model with overturning				
Southern Ocean wind stress (τ_{wind})	0.05 N m^{-2}	0.15 N m^{-2}	0.001 N m^{-2}	101
isolation fraction (δ)	10%	90%	1%	81

735 TABLE 2. Pre-industrial state in the box model with overturning for different choices of Southern Ocean wind
736 stress, τ_{wind} , and isolation fraction, δ . The pre-industrial atmospheric $\text{CO}_2 = 280$ ppm is prescribed in all the
737 ensembles. The pre-industrial distribution of heat and carbon, and the volume transports vary in the sensitivity
738 experiments, so as an example values from three ensembles are presented. Subscripts N , S , $deep$, ml and $therm$
739 note the southern high latitude, the northern high latitude, the deep ocean, the mixed layer and the thermocline,
740 respectively. Here the flux of heat and carbon into the ocean is shown in W and mol s^{-1} to highlight the thermal
741 and carbon equilibrium state in the pre-industrial.

variable	$\tau_{wind}=0.05 \text{ N m}^{-2}, \delta=50\%$	$\tau_{wind}=0.1 \text{ N m}^{-2}, \delta=50\%$	$\tau_{wind}=0.1 \text{ N m}^{-2}, \delta=90\%$
northern sinking, $q_{NA}(t_o)$	13 Sv	23.7 Sv	23.7 Sv
Ekman upwelling+eddy return flow, $q_{SO}(t_o)$	7.4 Sv	19.5 Sv	19.5 Sv
diapycnal upwelling, $q_v(t_o)$	5.6 Sv	4.2 Sv	4.2 Sv
upper ocean depth in low latitudes, $h(t_o)$	362 m	487 m	487 m
temperature, $T_N(t_o)$, $T_S(t_o)$ and $T_{deep}(t_o)$	5°C	5°C	5°C
temperature, $T_{ml}(t_o)$	25°C	25°C	25°C
temperature, $T_{therm}(t_o)$	10.7°C	13.2°C	6.7°C
heat uptake, $N_S(t_o)$	0 W	0 W	0 W
heat uptake, $N_N(t_o)$	-3×10^{14} W	-8×10^{14} W	-1.6×10^{14} W
heat uptake, $N_{ml}(t_o)$	3×10^{14} W	8×10^{14} W	1.6×10^{14} W
carbon, $DIC_N(t_o)$, $DIC_S(t_o)$ and $DIC_{deep}(t_o)$	2140 $\mu\text{mol kg}^{-1}$	2140 $\mu\text{mol kg}^{-1}$	2140 $\mu\text{mol kg}^{-1}$
carbon, $DIC_{ml}(t_o)$,	1945 $\mu\text{mol kg}^{-1}$	1945 $\mu\text{mol kg}^{-1}$	1945 $\mu\text{mol kg}^{-1}$
carbon, $DIC_{therm}(t_o)$,	2085 $\mu\text{mol kg}^{-1}$	2060 $\mu\text{mol kg}^{-1}$	2124 $\mu\text{mol kg}^{-1}$
carbon uptake, $F_S(t_o)$	0 mol s^{-1}	0 mol s^{-1}	0 mol s^{-1}
carbon uptake, $F_N(t_o)$	$7.4 \times 10^5 \text{ mol s}^{-1}$	$2 \times 10^6 \text{ mol s}^{-1}$	$3.9 \times 10^5 \text{ mol s}^{-1}$
carbon uptake, $F_{ml}(t_o)$	$-7.4 \times 10^5 \text{ mol s}^{-1}$	$-2 \times 10^6 \text{ mol s}^{-1}$	$-3.9 \times 10^5 \text{ mol s}^{-1}$

LIST OF FIGURES

- 743 **Fig. 1.** Idealised atmosphere-ocean models: (a) the 1D box model with three layers, a slab atmo-
 744 sphere (grey), ocean mixed layer (pale blue) and ocean interior (dark blue); and (b) the box
 745 model with overturning circulation including a slab atmosphere (grey), an upper layer of
 746 light water consisting of a thermocline layer (light blue) and a surface mixed layer (pale
 747 blue) in the low latitudes, and two upper layers at southern and northern high latitudes and
 748 a lower layer of dense water (darker shades of blue). The upper layer of light water in the
 749 low latitudes has a thickness of $h(t) = h_{therm}(t) + h_{ml}$. Heat and carbon fluxes into the atmo-
 750 sphere and from the atmosphere into the ocean driven by carbon emissions are denoted by
 751 red and blue arrows, respectively, while the volume transports between the different ocean
 752 layers are denoted by black arrows. The isolation fraction δ represents the proportion of
 753 mode waters formed in the Southern Ocean, which are shielded from the atmosphere in the
 754 low latitudes. 40
- 755 **Fig. 2.** The evolution of the volume transports and the thickness of the light waters from the pre-
 756 industrial state in the box model with overturning forced by emissions, from selected en-
 757 semble members with $\tau_{wind} = 0.05, 0.1$ and 0.15 N m^{-2} , corresponding to an overturning
 758 at the pre-industrial of $q_{NA}(t_0) = 13, 24$ and 35 Sv , respectively, and a fraction of isolation
 759 $\delta = 50\%$: (a) the volume rate of transformation of light water into dense water at the north-
 760 ern high latitudes, q_{NA} (Sv), equivalent to the strength of meridional overturning; (b) the
 761 volume rate of transformation of the dense water into light waters in the southern high lati-
 762 tudes, q_{so} (Sv), equivalent to the residual circulation; (c) the volume rate of transformation
 763 of dense waters into light waters associated with diapycnal mixing in low latitudes, q_v (Sv);
 764 and (d) the thickness of light waters, h (m). The thin black dotted line denotes the cessation
 765 of the emissions. 41
- 766 **Fig. 3.** Carbon and heat budgets in the 1D box model from an ensemble member with a mixed-layer
 767 thickness of $h_{ml} = 100 \text{ m}$ and a ventilation timescale of $\tau_{vent} = 1000 \text{ y}$ (left panels), and in the
 768 box model with overturning from an ensemble member with a Southern Ocean wind stress of
 769 $\tau_{wind} = 0.1 \text{ N m}^{-2}$, corresponding to an overturning at the pre-industrial of $q_{NA}(t_0) = 24 \text{ Sv}$,
 770 and a fraction of isolation of $\delta = 50\%$ (right panels): (a) and (c) the cumulative carbon
 771 emissions, $I_{em}(t)$ in PgC, and the changes in the atmosphere and ocean carbon inventories
 772 relative to the pre-industrial, $\Delta I_{atm}(t)$ and $\Delta I_{ocean}(t)$ in PgC, respectively, along with the
 773 carbon contribution to the TCRE, $R(t)/I_{em}(t)$ in $\text{W m}^{-2} (1000\text{PgC})^{-1}$; and (b) and (d) the
 774 radiative forcing, $R(t)$ in W m^{-2} , the radiative response, $\lambda \Delta T(t)$ in W m^{-2} , and the net heat
 775 uptake, $N(t)$ in W m^{-2} , along with the thermal contribution to the TCRE, $\Delta T(t)/R(t)$ in
 776 $\text{K} (\text{W m}^{-2})^{-1}$. The thin black dotted line denotes the cessation of the emissions. 42
- 777 **Fig. 4.** Sensitivity to the mixed-layer thickness from selected ensemble members with a ventila-
 778 tion timescale of $\tau_{vent} = 500 \text{ y}$ and mixed-layer thickness of $h_{ml} = 50, 100$ and 300 m
 779 (left panels) and to the rate of the ventilation of the ocean interior from selected ensem-
 780 ble members with a mixed-layer thickness of $h_{ml} = 100 \text{ m}$ and a ventilation timescale of
 781 $\tau_{vent} = 100, 500$, and 1000 y (right panels) in the 1D box model: (a) and (d) the TCRE,
 782 $\Delta T(t)/I_{em}(t)$ in $\text{K} (1000\text{PgC})^{-1}$; (b) and (e) carbon contribution to the TCRE, $R(t)/I_{em}(t)$
 783 in $\text{W m}^{-2} (1000\text{PgC})^{-1}$; and (c) and (f) thermal contribution to the TCRE, $\Delta T(t)/R(t)$ in
 784 $\text{K} (\text{W m}^{-2})^{-1}$. The thin black dotted line denotes the cessation of the emissions. 43
- 785 **Fig. 5.** Sensitivity to the mixed-layer thickness and the ventilation timescale in the 1D box model
 786 at year 10 (left panels), at year 100 (middle panels) and at year 500 (right panels): (a) the
 787 TCRE, $\Delta T(t)/I_{em}(t)$; (b) carbon contribution to the TCRE, $R(t)/I_{em}(t)$; and (c) thermal con-
 788 tribution to the TCRE, $\Delta T(t)/R(t)$. The estimates are based on the ensemble with variations
 789 in both the mixed-layer thickness and the ventilation timescale. 44

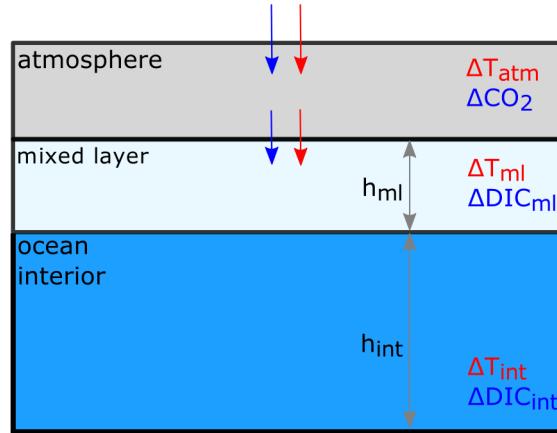
790 **Fig. 6.** Sensitivity to the strength of the overturning circulation from selected ensemble members
791 with a fraction of isolation $\delta = 50\%$ and a Southern Ocean wind stress $\tau_{wind} = 0.05, 0.1$
792 and 0.15 N m^{-2} corresponding to overturning at the pre-industrial of $q_{NA}(t_o) = 13, 24$
793 and 35 Sv , respectively (left panels), and to the fraction of isolation from selected ensemble
794 members with a Southern Ocean wind stress $\tau_{wind} = 0.1 \text{ N m}^{-2}$ corresponding to an
795 overturning at the pre-industrial of $q_{NA}(t_o) = 24 \text{ Sv}$ and a fraction of isolation $\delta = 10,$
796 50 and 90% (right panels) in the box model with overturning: (a) and (d) the TCRE,
797 $\Delta T(t)/I_{em}(t)$ in K (1000PgC)^{-1} ; (b) and (e) carbon contribution to the TCRE, $R(t)/I_{em}(t)$
798 in $\text{W m}^{-2} (1000\text{PgC})^{-1}$; and (c) and (f) thermal contribution to the TCRE, $\Delta T(t)/R(t)$ in
799 $\text{K (W m}^{-2})^{-1}$. The thin black dotted line denotes the cessation of the emissions. 45

800 **Fig. 7.** Sensitivity to the overturning strength, q_{NA} , and the fraction of isolation, δ , in the box model
801 with overturning at year 10 (left panels), at year 100 (middle panels) and at year 500 (right
802 panels): (a) the TCRE, $\Delta T(t)/I_{em}(t)$; (b) carbon contribution to the TCRE, $R(t)/I_{em}(t)$;
803 and (c) thermal contribution to the TCRE, $\Delta T(t)/R(t)$. A large isolation fraction implies
804 more subduction in the Southern Ocean and less atmosphere-ocean interaction in the low
805 latitudes. The estimates are based on the ensemble with variations in both the wind stress
806 and the fraction of isolation. 46

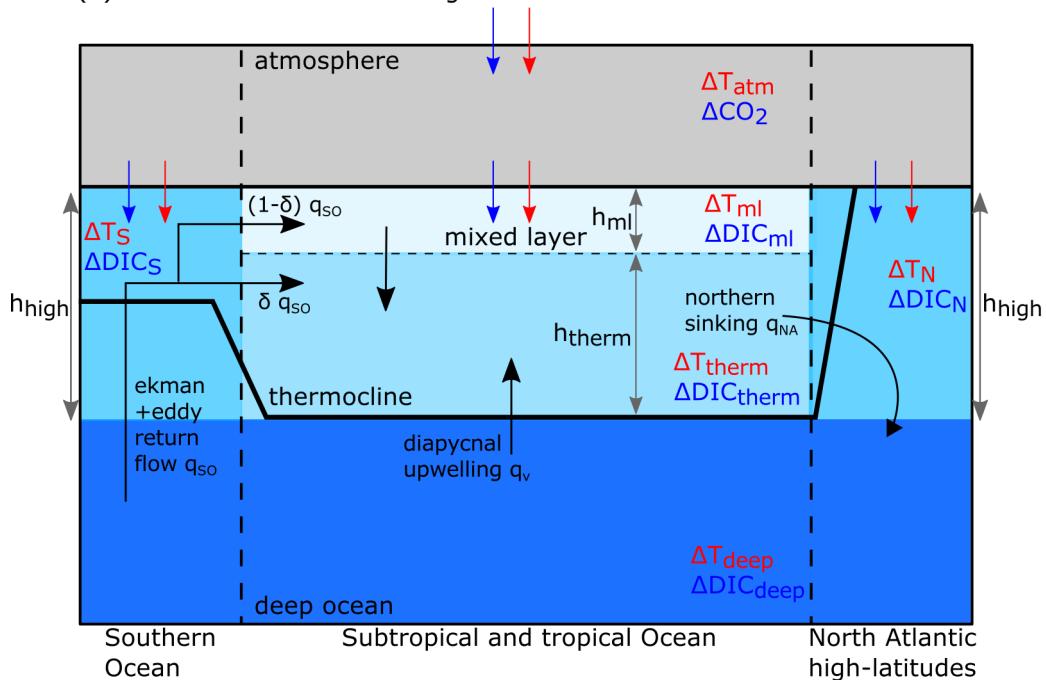
807 **Fig. 8.** The variability of the TCRE (black lines) and its partition into a carbon contribution,
808 $R(t)/I_{em}(t)$ (blue lines), and a thermal contribution, $\Delta T(t)/R(t)$ (red lines). The variabil-
809 ity in the 1D box model driven by (a) the combined changes in the mixed-layer thickness
810 and the ventilation timescale; and separately by (b) changes in the mixed-layer thickness
811 and (c) changes in the ventilation timescale. The variability in the box model with over-
812 turning driven by (d) the combined changes in the strength of the overturning circulation
813 and the isolation fraction; and separately by (e) changes in the strength of the overturning
814 and (f) changes in the isolation fraction. The variability is represented by the coefficient of
815 variation, defined by the standard deviation divided by the mean for the model ensemble for
816 each set of ventilation experiment (Table 1). The x axes denoting years is presented in a
817 logarithmic scale. The thin black dotted line denotes the cessation of the emissions. 47

818 **Fig. 9.** The variability of the TCRE (black lines) and its partition into a carbon contribution,
819 $R(t)/I_{em}(t)$ (blue lines), and a thermal contribution, $\Delta T(t)/R(t)$ (red lines) driven by differ-
820 ent aspects of the ocean ventilation for different carbon emission rate and timing of cessation
821 of emissions: (a) the mixed-layer thickness; (b) the ventilation timescale; (c) the strength of
822 the overturning circulation; and (d) the isolation fraction. The variability is represented by
823 the coefficient of variation, defined by the standard deviation divided by the mean for the
824 model ensemble for each set of ventilation experiment (Table 1). The x axes denoting years
825 is presented in a logarithmic scale. The thin black dotted line denotes the cessation of the
826 emissions. 48

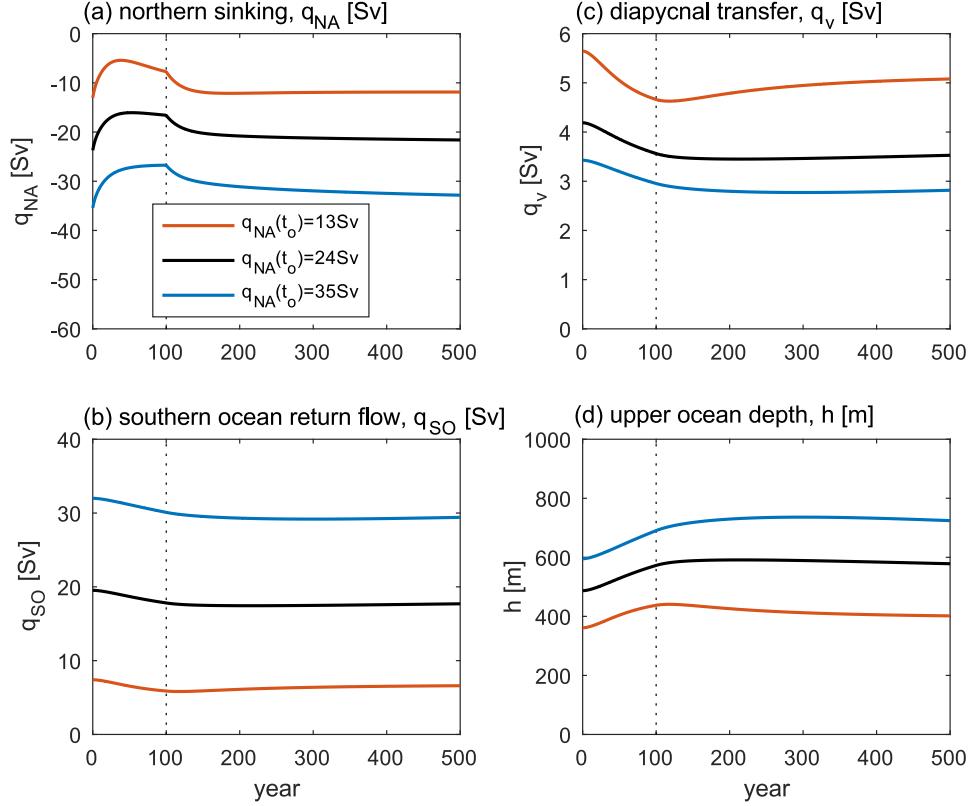
(a) 1D box model



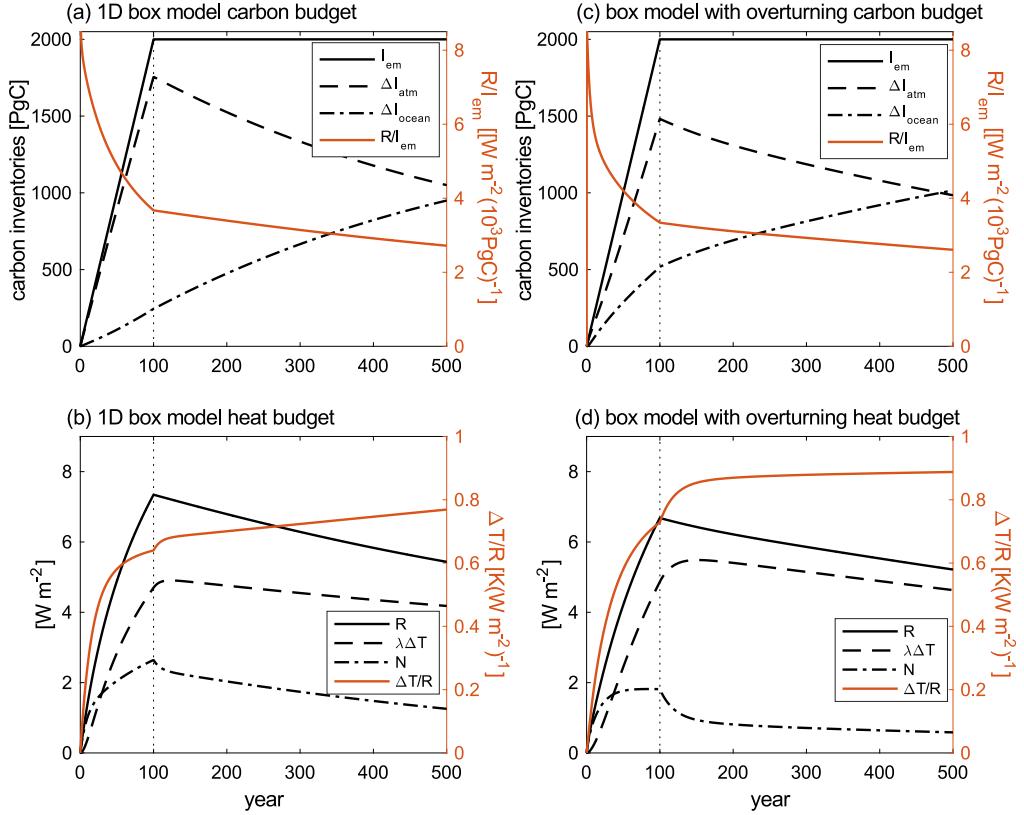
(b) box model with overturning



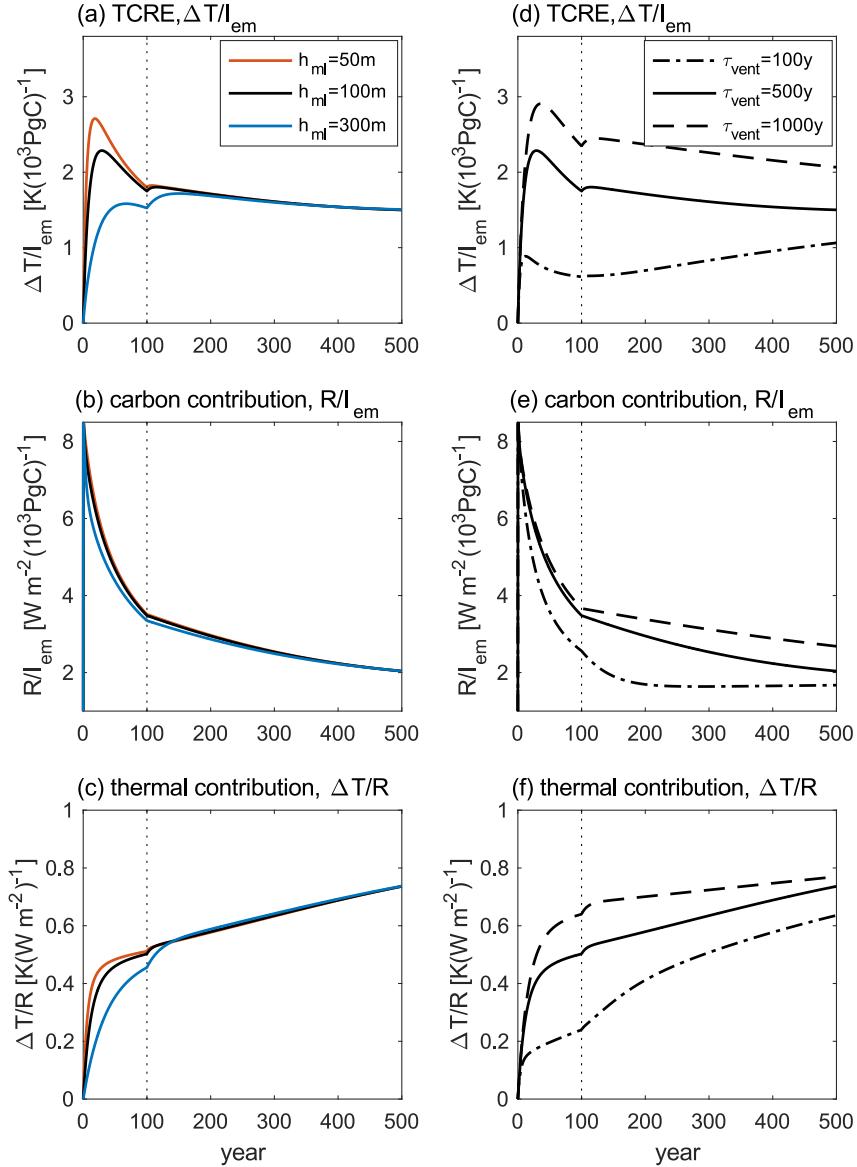
827 FIG. 1. Idealised atmosphere-ocean models: (a) the 1D box model with three layers, a slab atmosphere (grey),
 828 ocean mixed layer (pale blue) and ocean interior (dark blue); and (b) the box model with overturning
 829 including a slab atmosphere (grey), an upper layer of light water consisting of a thermocline layer (light blue)
 830 and a surface mixed layer (pale blue) in the low latitudes, and two upper layers at southern and northern high
 831 latitudes and a lower layer of dense water (darker shades of blue). The upper layer of light water in the low
 832 latitudes has a thickness of $h(t) = h_{therm}(t) + h_{ml}$. Heat and carbon fluxes into the atmosphere and from the
 833 atmosphere into the ocean driven by carbon emissions are denoted by red and blue arrows, respectively, while
 834 the volume transports between the different ocean layers are denoted by black arrows. The isolation fraction δ
 835 represents the proportion of mode waters formed in the Southern Ocean, which are shielded from the atmosphere
 836 in the low latitudes.



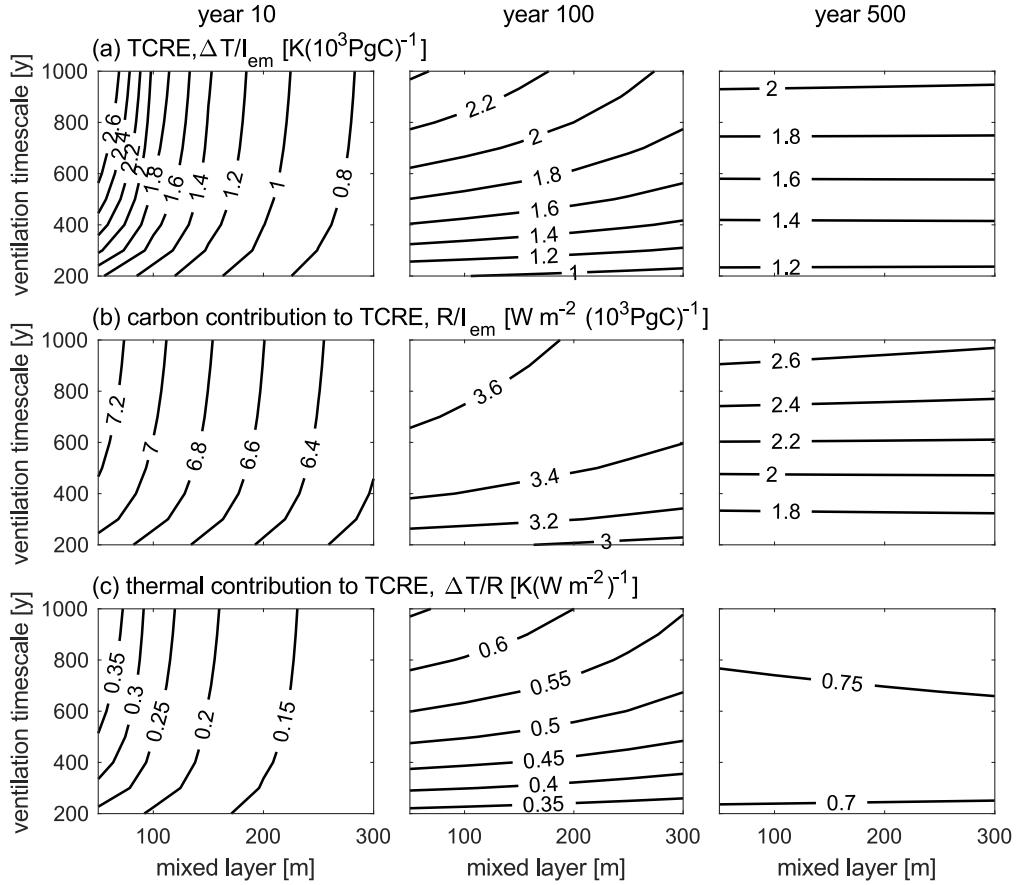
837 FIG. 2. The evolution of the volume transports and the thickness of the light waters from the pre-industrial
838 state in the box model with overturning forced by emissions, from selected ensemble members with $\tau_{wind} = 0.05$,
839 0.1 and 0.15 N m^{-2} , corresponding to an overturning at the pre-industrial of $q_{NA}(t_0) = 13, 24$ and 35 Sv ,
840 respectively, and a fraction of isolation $\delta = 50\%$: (a) the volume rate of transformation of light water into
841 dense water at the northern high latitudes, q_{NA} (Sv), equivalent to the strength of meridional overturning; (b)
842 the volume rate of transformation of the dense water into light waters in the southern high latitudes, q_{so} (Sv),
843 equivalent to the residual circulation; (c) the volume rate of transformation of dense waters into light waters
844 associated with diapycnal mixing in low latitudes, q_v (Sv); and (d) the thickness of light waters, h (m). The thin
845 black dotted line denotes the cessation of the emissions.



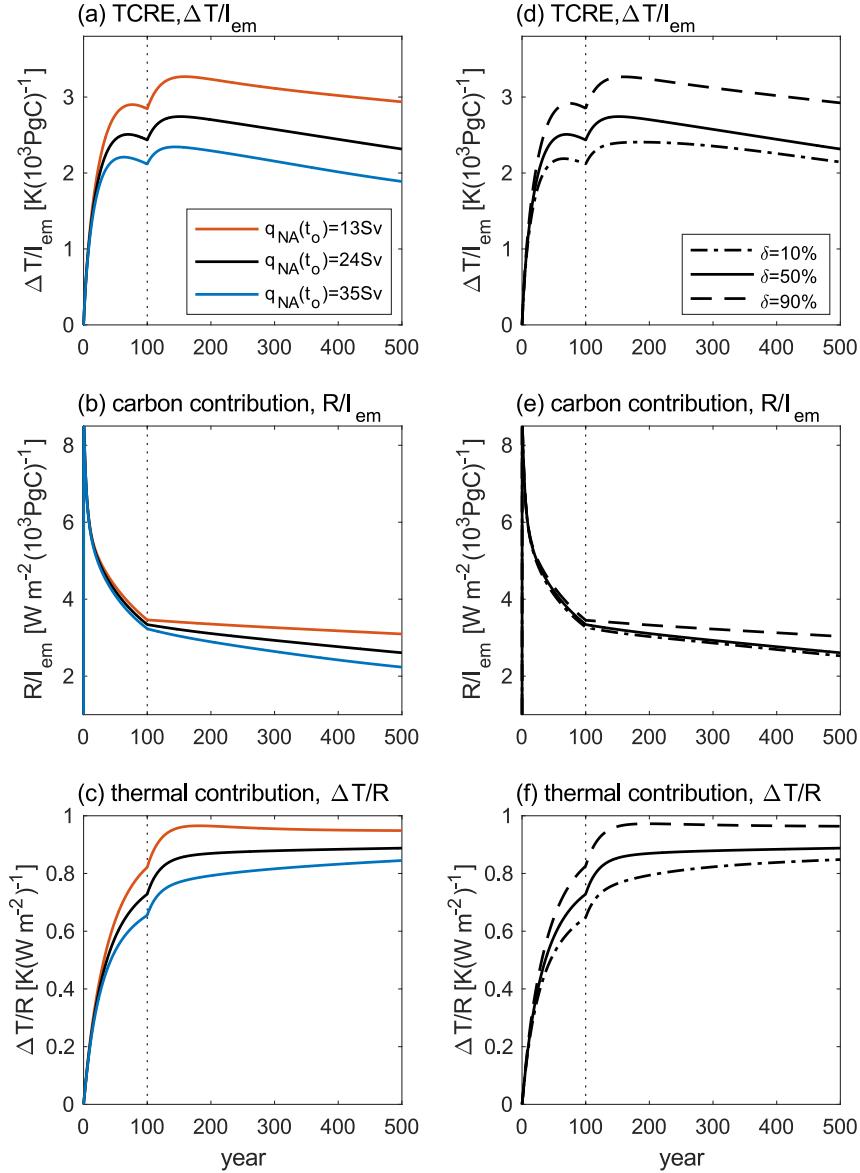
846 FIG. 3. Carbon and heat budgets in the 1D box model from an ensemble member with a mixed-layer thickness
 847 of $h_{ml} = 100$ m and a ventilation timescale of $\tau_{vent} = 1000$ y (left panels), and in the box model with overturning
 848 from an ensemble member with a Southern Ocean wind stress of $\tau_{wind} = 0.1$ N m⁻², corresponding to an
 849 overturning at the pre-industrial of $q_{NA}(t_o) = 24$ Sv, and a fraction of isolation of $\delta = 50\%$ (right panels): (a)
 850 and (c) the cumulative carbon emissions, $I_{em}(t)$ in PgC, and the changes in the atmosphere and ocean carbon
 851 inventories relative to the pre-industrial, $\Delta I_{atm}(t)$ and $\Delta I_{ocean}(t)$ in PgC, respectively, along with the carbon
 852 contribution to the TCRE, $R(t)/I_{em}(t)$ in W m⁻² (1000PgC)⁻¹; and (b) and (d) the radiative forcing, $R(t)$ in
 853 W m⁻², the radiative response, $\lambda\Delta T(t)$ in W m⁻², and the net heat uptake, $N(t)$ in W m⁻², along with the
 854 thermal contribution to the TCRE, $\Delta T(t)/R(t)$ in K (W m⁻²)⁻¹. The thin black dotted line denotes the cessation
 855 of the emissions.



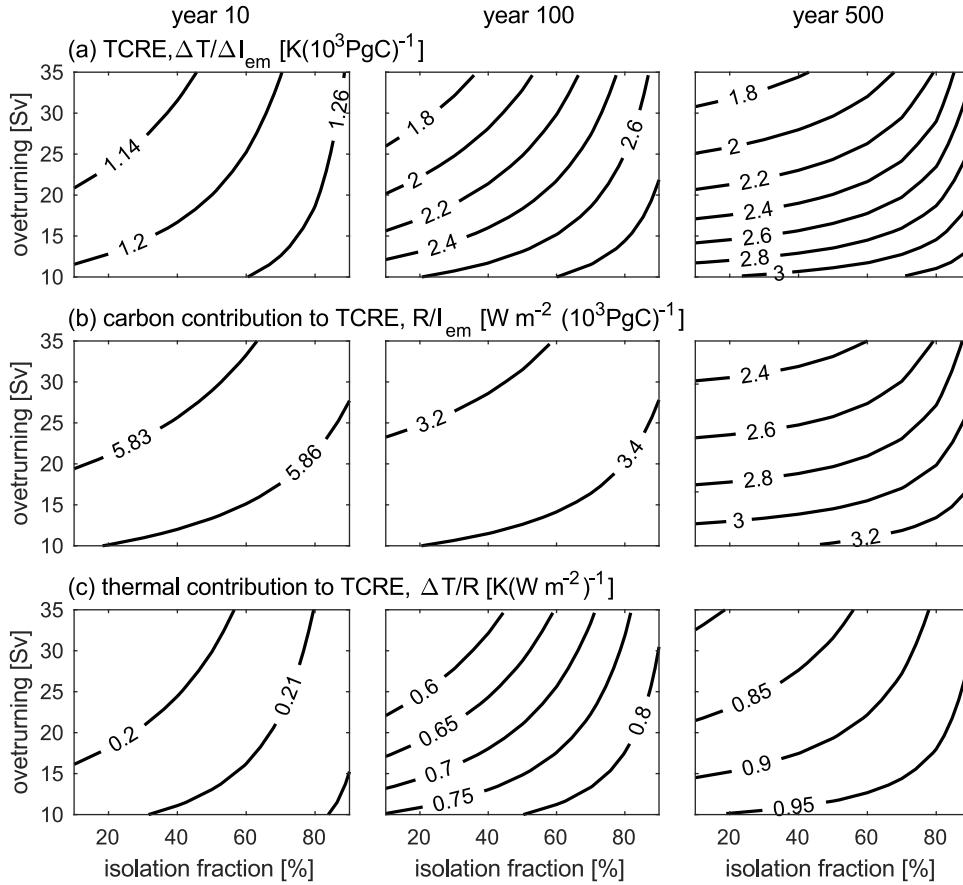
856 FIG. 4. Sensitivity to the mixed-layer thickness from selected ensemble members with a ventilation timescale
 857 of $\tau_{vent} = 500$ y and mixed-layer thickness of $h_{ml} = 50, 100$ and 300 m (left panels) and to the rate of the ven-
 858 tilation of the ocean interior from selected ensemble members with a mixed-layer thickness of $h_{ml} = 100$ m
 859 and a ventilation timescale of $\tau_{vent} = 100, 500,$ and 1000 y (right panels) in the 1D box model: (a) and
 860 (d) the TCRE, $\Delta T(t)/I_{em}(t)$ in $K(1000PgC)^{-1}$; (b) and (e) carbon contribution to the TCRE, $R(t)/I_{em}(t)$ in
 861 $W m^{-2}(1000PgC)^{-1}$; and (c) and (f) thermal contribution to the TCRE, $\Delta T(t)/R(t)$ in $K(W m^{-2})^{-1}$. The thin
 862 black dotted line denotes the cessation of the emissions.



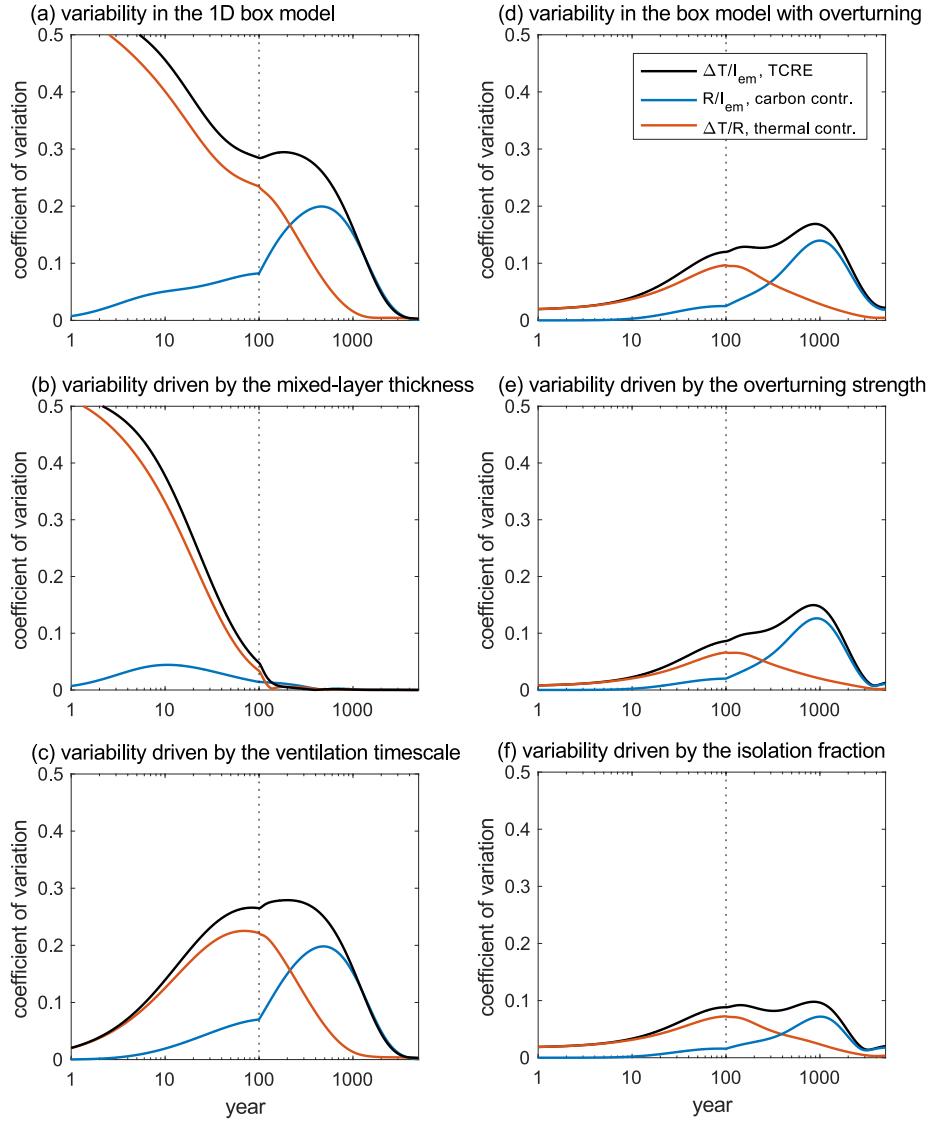
863 FIG. 5. Sensitivity to the mixed-layer thickness and the ventilation timescale in the 1D box model at year 10
 864 (left panels), at year 100 (middle panels) and at year 500 (right panels): (a) the TCRE, $\Delta T(t)/I_{em}(t)$; (b) carbon
 865 contribution to the TCRE, $R(t)/I_{em}(t)$; and (c) thermal contribution to the TCRE, $\Delta T(t)/R(t)$. The estimates are
 866 based on the ensemble with variations in both the mixed-layer thickness and the ventilation timescale.



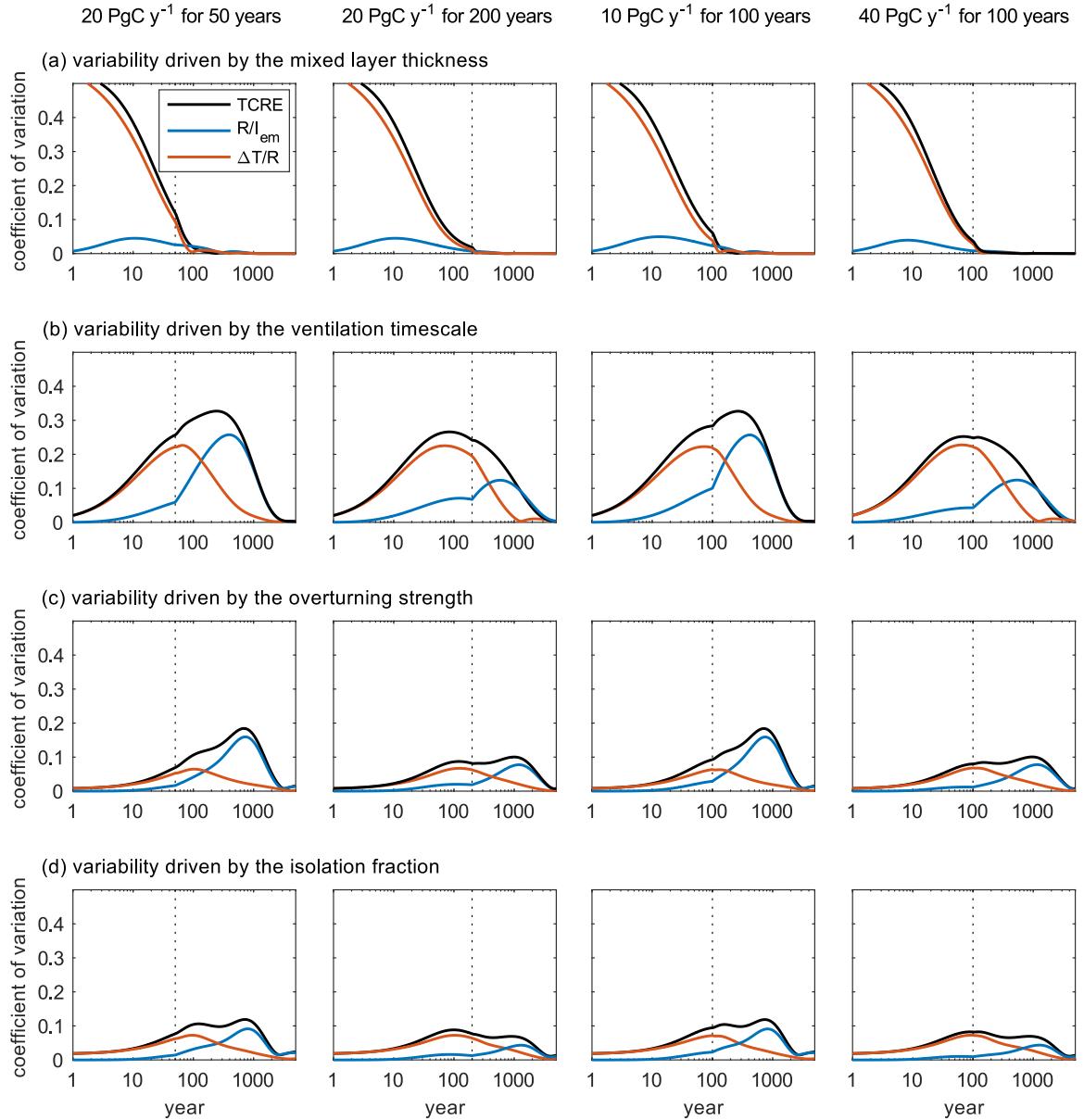
867 FIG. 6. Sensitivity to the strength of the overturning circulation from selected ensemble members with a
868 fraction of isolation $\delta = 50\%$ and a Southern Ocean wind stress $\tau_{wind} = 0.05, 0.1$ and 0.15 N m^{-2} corresponding
869 to an overturning at the pre-industrial of $q_{NA}(t_o) = 13, 24$ and 35 Sv , respectively (left panels), and to the
870 fraction of isolation from selected ensemble members with a Southern Ocean wind stress $\tau_{wind} = 0.1 \text{ N m}^{-2}$
871 corresponding to an overturning at the pre-industrial of $q_{NA}(t_o) = 24 \text{ Sv}$ and a fraction of isolation $\delta = 10, 50$ and
872 90% (right panels) in the box model with overturning: (a) and (d) the TCRE, $\Delta T(t)/I_{em}(t)$ in $\text{K} (1000\text{PgC})^{-1}$;
873 (b) and (e) carbon contribution to the TCRE, $R(t)/I_{em}(t)$ in $\text{W m}^{-2} (1000\text{PgC})^{-1}$; and (c) and (f) thermal
874 contribution to the TCRE, $\Delta T(t)/R(t)$ in $\text{K} (\text{W m}^{-2})^{-1}$. The thin black dotted line denotes the cessation of the
875 emissions.



876 FIG. 7. Sensitivity to the overturning strength, q_{NA} , and the fraction of isolation, δ , in the box model with
 877 overturning at year 10 (left panels), at year 100 (middle panels) and at year 500 (right panels): (a) the TCRE,
 878 $\Delta T(t)/I_{em}(t)$; (b) carbon contribution to the TCRE, $R(t)/I_{em}(t)$; and (c) thermal contribution to the TCRE,
 879 $\Delta T(t)/R(t)$. A large isolation fraction implies more subduction in the Southern Ocean and less atmosphere-
 880 ocean interaction in the low latitudes. The estimates are based on the ensemble with variations in both the wind
 881 stress and the fraction of isolation.



882 FIG. 8. The variability of the TCRE (black lines) and its partition into a carbon contribution, $R(t)/I_{em}(t)$ (blue
 883 lines), and a thermal contribution, $\Delta T(t)/R(t)$ (red lines). The variability in the 1D box model driven by (a) the
 884 combined changes in the mixed-layer thickness and the ventilation timescale; and separately by (b) changes in
 885 the mixed-layer thickness and (c) changes in the ventilation timescale. The variability in the box model with
 886 overturning driven by (d) the combined changes in the strength of the overturning circulation and the isolation
 887 fraction; and separately by (e) changes in the strength of the overturning and (f) changes in the isolation fraction.
 888 The variability is represented by the coefficient of variation, defined by the standard deviation divided by the
 889 mean for the model ensemble for each set of ventilation experiment (Table 1). The x axes denoting years is
 890 presented in a logarithmic scale. The thin black dotted line denotes the cessation of the emissions.



891 FIG. 9. The variability of the TCRE (black lines) and its partition into a carbon contribution, $R(t)/I_{em}(t)$ (blue
 892 lines), and a thermal contribution, $\Delta T(t)/R(t)$ (red lines) driven by different aspects of the ocean ventilation
 893 for different carbon emission rate and timing of cessation of emissions: (a) the mixed-layer thickness; (b) the
 894 ventilation timescale; (c) the strength of the overturning circulation; and (d) the isolation fraction. The variability
 895 is represented by the coefficient of variation, defined by the standard deviation divided by the mean for the model
 896 ensemble for each set of ventilation experiment (Table 1). The x axes denoting years is presented in a logarithmic
 897 scale. The thin black dotted line denotes the cessation of the emissions.