## Journal Name

### ARTICLE TYPE

Cite this: DOI: 00.0000/xxxxxxxxx

Received Date Accepted Date

DOI: 00.0000/xxxxxxxxx

# Computational screening for nested organic cage complexes $^{\dagger}$

Enrico Berardo,<sup>*a*</sup> Rebecca L. Greenaway,<sup>*b*</sup> Marcin Miklitz,<sup>*a*</sup> Andrew I. Cooper<sup>*b*</sup> and Kim E. Jelfs<sup>\**a*</sup>

Supramolecular self-assembly has allowed the synthesis of beautiful and complex molecular architectures, such as cages, macrocycles, knots, catenanes, and rotaxanes. We focus here on porous organic cages, which are molecules that have an intrinsic cavity and multiple windows. These cages have been shown to be highly effective at molecular separations and encapsulations. We investigate the possibility of complexes where one cage sits within the cavity of another. We term this a 'nested cage' complex. The design of such complexes is highly challenging, so we use computational screening to explore 8712 different pair combinations, running almost 0.5M calculations to sample the phase space of the cage conformations. Through analysing the binding energies of the assemblies, we identify highly energetically favourable pairs of cages in nested cage complexes. The vast majority of the most favourable complexes include the large imine cage reported by Gawroński and co-workers using a [8+12] reaction of 4-*tert*-butyl-2,6-diformylphenol and *cis,cis*-1,3,5-triaminocyclohexane. The most energetically favourable nested cage complex combines the Gawroński cage with a dodecaamide cage that has six vertices, which can sit in the six windows of the larger cage. We also identify cages that have favourable binding energies for self-catenation.

Supramolecular chemistry involves 'chemistry beyond the molecule' and can enable the assembly of incredibly complex, and beautiful, structures. Examples include cages, <sup>1–3</sup> macrocycles, <sup>4</sup> and more complex, interlocked, structures such as catenanes, <sup>5</sup> rotaxanes, <sup>6</sup> knots, <sup>7</sup> and molecular machines.<sup>8,9</sup> The potential possible combinations of organic building blocks to form these complex architectures is vast, and therefore the design of these molecules is challenging and normally based on the chemical experience of synthetic chemists and small changes to existing structures. While many interlocked organic species such as catenanes have been reported, no example of an organic cage completely encapsulated inside the cavity of a second organic cage has been reported to date. Even considering other species beyond organic cages, there are few examples of 'nested cages' or 'Russian doll complexes'. There are examples

of macrocycle-in-a-macrocycle complexes, <sup>10–13</sup> including Russian doll concentric porphyrin nanorings, <sup>14</sup> and fullerene/macrocycle complexes. <sup>15,16</sup> Some metal-organic nested cage complexes have been reported; <sup>17</sup> perhaps the most relevant are those complexes that involve the encapsulation of a small organic cage within a metal-organic cage, <sup>18,19</sup> or the formation of multi-layered DNA nanocages. <sup>20</sup> However, the nesting of an organic cage within another organic cage remains a challenging target, and if realised would demonstrate fine control over supramolecular assembly.

Porous organic cages (POCs) are an example of a porous molecular material, where the porosity of the material originates in the intrinsic cavity of the cage molecule. A POC can be defined as having an internal cavity with multiple entry and exit routes through which guests can access the central cavity.<sup>3</sup> POCs have been reported in a variety of sizes, shapes and topologies (see examples in Figure 1), although the total number reported is only on the order of 200 molecules. The majority of POCs are made through the use of dynamic covalent chemistry (DCC), in particular imine condensation reactions, the reversible nature of which allows for error correction during the synthesis of these high symmetry products, often in high yield. There are also examples of POCs catenating to form interlocked structures with another molecule of the same cage species.<sup>21–25</sup> This catenation can typically be controlled by the functionalisation of the cage;

<sup>&</sup>lt;sup>a</sup> Department of Chemistry, Imperial College London, Molecular Sciences Research Hub, White City Campus, Wood Lane, London W12 0BZ, United Kingdom. Tel: +44 (0)20 759 43438; E-mail: k.jelfs@imperial.ac.uk

<sup>&</sup>lt;sup>b</sup> Department of Chemistry and Materials Innovation Factory, University of Liverpool, 51 Oxford Street, Liverpool L7 3NY, United Kingdom.

<sup>†</sup> Electronic Supplementary Information (ESI) available: Additional figures and tables. The structures of the individual cage molecules and the best self-catenation and nested cage complexes are provided at https://github.com/JelfsMaterialsGroup/Nested-cages. See DOI: 00.0000/00000000.

for instance, the position of the alkyl groups, which can introduce multiple pores of different sizes within a single complex.<sup>22</sup> Potential applications of POCs include their use as encapsulants,<sup>26</sup> in catalysis,<sup>27</sup> molecular separations,<sup>28–31</sup> as sensors,<sup>32,33</sup> and in porous liquids.<sup>34</sup>

It is possible to use computer simulations to assist in the design and discovery of porous organic cages. 38 First, starting from the precursors of the cage synthesis reaction, the outcome in terms of the molecular mass and topology of the cage can be hard to predict, since small changes in the precursors are known to have led to large changes in topology and consequently the properties of the cages.<sup>39</sup> It has been shown that it is possible to predict the topology by examining the relative energies of the different possible assemblies, <sup>40,41</sup> or further, by considering the formation mechanisms of the cage products.<sup>42</sup> While most studies to date have focused upon a posteriori rationalisation of previously reported systems, we have recently shown it is possible to identify trends in the reaction outcomes and therefore assist in the discovery process during a larger-scale robotic screening of 78 potential cage reactions.<sup>23</sup> It is also possible to predict shape persistency, the ability for a cage to maintain an internal void in the absence of solvent.<sup>43,44</sup> The solid-state structure of materials and their properties can be predicted from molecular structures using crystal structure prediction (CSP) techniques.<sup>45-49</sup> Molecular-level calculations of binding energies of dimer pairs can also assist in predicting the preferential binding modes in the solid-state, for example the preference to racemise or form enantiopure structures.<sup>50</sup> The properties of the materials can be also understood or predicted a priori once the structures are known.<sup>38,51,52</sup>

We report here a computational screening study where we conduct almost 0.5M calculations in order to search for elusive nested organic cage complexes. Through an examination of binding energies, we identify the most promising candidate cages for forming such complexes and analyse which systems are the most suitable for targeting for synthesis. Alongside this, we compare the competing pathways of self-catenation of the cages, which further identifies promising candidates for that type of assembly.

#### Methods

Through a literature search of reported intrinsically porous molecules,<sup>2,53</sup> we constructed a database of 132 candidate molecules. A complete list of the included cages, including images of the molecules, is given in Table S1, together with their numbering from 1 to 132. The set consists of 78 cages from a recently reported combined high-throughput robotic and computational screening study from Greenaway et al. 23, three [6+12] TCC cages from Stackhouse et al., 54 the carbon nanocage of Matsui et al.,<sup>55</sup> cucurbiturils CB[5], CB[6] and CB[7],<sup>56</sup> ExCage,<sup>37</sup> seven cages from Mastalerz and co-workers, 22,57-60 two hemicarceplexes from Cram and co-workers, <sup>61</sup> twenty-four imine and amide cages from Cooper and co-workers, 36,39,46,62-69 the triazine cage of Ding et al.,<sup>70</sup> BlueCage,<sup>71</sup> noria,<sup>72</sup> the alkyne cage from Doonan and co-workers, <sup>73</sup> crytophane, <sup>35</sup> a fluorescent cage from Mukherjee and co-workers, 33 a boronate cage from Iwasawa and co-workers, 74 an imine cage from Gawroński and coworkers,  $^{75}$  and four cages from Beuerle and co-workers.  $^{76,77}$  These molecules cover the full range of topologies and shapes reported for porous organic cages to date and range in maximum dimension from 13 to 47 Å and internal cavity diameter of 0 to 26 Å.

The cage structures were taken from reported crystal structures, or constructed manually for those structures where no Xray diffraction structure was reported. The manual construction involved a short molecular dynamics (MD) simulation that sampled several hundred conformations and selected the lowest energy conformation for further simulations. For a few cases where more than one enantiomer of the cage is possible, we used only enantiomer that was reported in the crystal structure. If there was positional isomerism, for example in methyl position for CC2, a random isomer was constructed to keep the number of calculations required feasible. The structural properties of the cages and their voids and windows are given in Table S2. All void sizes and window sizes were calculated with our pywindow software, with void sizes calculated as the diameter of the largest sphere that can fit in the cavity and window size as the diameter of the largest circle that can fit in a window.<sup>78</sup> The maximum diameter of a molecule was defined as the distance between the edges of the van der Waals spheres of the two atoms at the greatest distance from each other in the molecule. The average diameter of a molecule was determined as a mean distance from the centre of mass of a molecule to its van der Waals surface. The latter value can match the experimentally determined solvodynamic diameters.<sup>23</sup>

Pairing each molecule with every other molecule in our data set, including the self-catenation combination, made a total of 8712 pair combinations to be considered. To sample the possible relative orientations of each molecular pair, we considered 56 different but evenly spaced relative orientations by carrying out rotations of the polar and azimuthal angles of one cage while keeping the other in a fixed position. Each of these structures was geometry optimized so that the lowest energy orientation could be analysed further. Thus, we conducted a total of 487,872 calculations (8712 molecule pairs, each in 56 orientations). For all forcefield calculations, we used the OPLS3 forcefield<sup>79</sup> which we have previously shown effectively predicts the structure of flexible porous imine cages,<sup>41</sup> and is designed to be transferable to new organic systems. The calculations were carried out in Macromodel, using a conjugate gradient minimisation with a convergence criteria of a root mean square force below 0.05 kJ mol<sup>-1</sup>  $Å^{-1}$ . The individual cage structures were geometry optimised in isolation with the same setup. The binding energy for the lowest energy conformation of each cage pairing was then calculated as:

$$E_b = E_{cage \ pair} - E_{cage1} - E_{cage2} \tag{1}$$

where  $E_b$  is the binding energy,  $E_{cage\ pair}$  is the energy of the lowest energy conformation of a cage pair,  $E_{cage1}$  is the energy of the geometry optimised structure of the first cage in the pair and  $E_{cage2}$  that of the second cage in the pair. In the case of selfcatenated pairs,  $E_{cage1}$  is equal to  $E_{cage2}$ . We calculate the binding energies only at the forcefield level here, due to the large

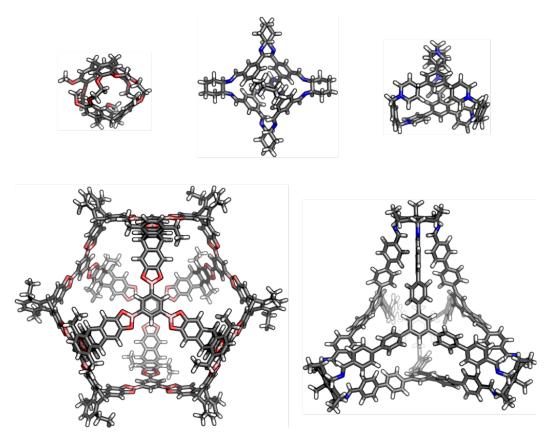


Fig. 1 Examples of previously reported porous organic cages that are a variety of sizes, shapes, and topologies; (top left) cryptophane<sup>35</sup>; (top centre) CC3<sup>36</sup>; (top right) ExCage<sup>37</sup>; (bottom left) a giant boronate cage,<sup>22</sup> and (bottom right) C26.<sup>23</sup>

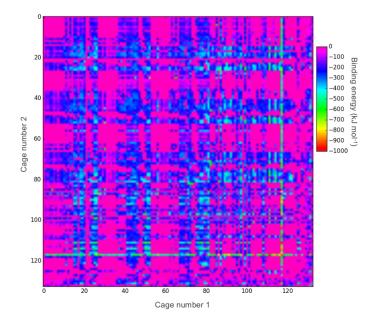
number of calculations (almost 0.5M) making higher level calculations computationally infeasible. While we recognise that this will mean the absolute values are not correct, the relative energies are useful to drive selection of systems for increased chance of synthetic realisation. We do not include any solvent effects here, as the experiments could eventually be tested in a range of different solvents, and thus a range of different dielectric constants could be applied in an implicit solvent model. We have previously shown that the primary influence of solvents in these systems is as a scaffolding effect, <sup>43</sup> which is not influenced by specific solvent-cage interactions, and therefore we believe it is reasonable to ignore these effects in a high-throughput screening study. The remaining cavity sizes of the nested cage and selfcatenation pairs were calculated with pywindow.

#### **Results and discussion**

Figure 2 shows a heat-map of the binding energies of all the possible pairings of the 132 organic cages. A total of 4947 pairings have a favourable (negative) binding energy, which equates to 57% of the possible pairings. Highly unfavourable pairings, for instance combining two small capsular cages that have very small internal cavities, can be seen in several regions; for example, the pink region for cages both numbered **27** to **36**. It is also possible to pick out "sweet-spots" where there are many favourable binding energies, and in particular cage **117** can be clearly identified as being selected in many of the most highly favourable binding energy pairs. Cage **117** is a large imine cage synthesised from an [8+12] reaction of 4-*tert*-butyl-2,6-diformylphenol and *cis,cis*-1,3,5-triaminocyclohexane by Gawroński and co-workers.<sup>75</sup> **117** has an approximately cuboctahedral shape, a maximum dimension of 34 Å, a void diameter of 13 Å, and six equally sized windows of 9 Å in diameter.

In theory, a favourable binding energy should be found in cases where there is a good match of the void size of the larger cage in the pairing with the dimensions of the smaller cage. However, in Figure S1, a heat-map of the difference in the void size of the larger cage to the maximum dimension of the smaller cage does not show any correlation with the binding energies in Figure 2. Similarly, there appears to be no correlation between the difference in those sizes and the binding energy (Figure S2). This suggests that there are many other factors, for instance symmetry and the intermolecular bonding available for a given cage pairing, that are influencing the binding energy.

In each case of pairing two different cages, there would be competition with each of the individual cages prefering to selfcatenate instead, which might be due to that potentially being thermodynamically favoured over forming a nested cage complex. We therefore compared the binding energies against the comparable self-catenation energies, and in Figure 3A we plot a heat-map that shows which pairings would energetically favour self-catenation (red) and which would favour forming a nested cage complex (blue). We find that all the pairings where self-



**Fig. 2** A 2D heat-map showing the binding energy for a pairing of two organic cages. Only energies below 0 kJ mol<sup>-1</sup> are shown. The plot is symmetric about the diagonal as a pairing of cage x and cage y is equivalent to a pairing of cage y and cage x.

catenation is preferred correspond to regions in Figure 2 where the binding energy for a nested cage pairing was unfavourable (pink). Therefore, if we replot Figure 2 with any pairings that would prefer self-catenation shown as energetically unfavourable, then there is no visual difference in the heat-map. Further, many of the pairings that might favour self-catenation over a nested cage complex are instances where even the self-catenation is energetically unfavourable. In Figure 3B, we show a heat-map of which pairings actually truly prefer self-catenation (yellow); *i.e.*, have both an energetically favourable binding energy for selfcatenation *and* self-catenation is energetically preferred over a nested cage complex. It is clear that it is very rare for the pairings to prefer self-catenation.

#### Cage pairings that prefer self-catenation

We will now examine the cage pairings that most preferred to self-catenate. The binding energies of all the favourable selfcatenations are shown in Figure S3 and the energies and structural features of the top 20 self-catenating molecules are shown in Table 1. The most favourable binding energy for self-catenation was -505 kJ mol<sup>-1</sup>, found for cage 81, although this falls to -291 kJ mol<sup>-1</sup> by the 20<sup>th</sup> best self-catenating cage. These binding energies are considerably less favourable than the best 20 nested cage complexes, which range in energy from -1023 to -660 kJ mol<sup>-1</sup>. Cage **97**, a large boronate ester cage reported by Mastalerz and co-workers,<sup>80</sup> which is ranked 13<sup>th</sup> by binding energy is closely related (differing only in the position of solubilising groups) to the boronate ester cage reported to self-catenate by Mastelerz and co-workers in 2014. 22 Whilst we did not include the exact molecule that Mastelerz reported in this study, the finding that 97 is energetically favourable towards self-catenation is very encouraging for our approach.

In all cases, the self-catenated complex is left with a considerable internal cavity, which could still host further guests. The cavities range from 7.5 - 15.7 Å, with the exception of cage **89** which has a much smaller cavity of 2.1 Å when self-catenated. We can examine the extent to which the structures are interlocked and compare this to the number of windows (Table 1). The number of windows in these best self-catenation pairs ranges from 3 to 8. In theory, a self-catenation that is maximally interlocked will have the same degree of interlocking as the number of windows, and this is also likely to lead to a more symmetric structure. This maximal interlocking occurs in 6 of the 20 best self-catenation pairs, and in all cases, these are instances where the individual cage has six windows.

The self-catenated structures of the three most energetically favoured combinations are shown in Figure 4, along with the chemical structures of the precursors for those cages. The images for the remaining structures in the top 20 are shown in Figure S4. All three of the best self-catenating cages approximate to (truncated) tetrahedrons, with 81 being a  $TCC1_{[6+12]}$  cage reported by Stackhouse et al.,<sup>54</sup> and 52 and 78 being two [4+4] cages recently reported by Greenaway et al..<sup>23</sup> The latter two cages differ only by the fact that the aromatic triamine of 52 is decorated with three methyl groups, whilst **78** is decorated with three ethyl groups. Only in the case of **78** are all of the windows interlocked. Due to this difference in interlocking between 52 and 78, this may be indicative that despite our best efforts for the large numbers of structures, we have not been able to fully sample the potential energy surface for every pair. However, we still believe it is sufficient to identify favourable pairings (such as cage 97). We also note the large size of all of the 'best' cages for self-catenation, naturally, with additional atoms, they are likely to have higher binding energies than smaller molecules. Indeed, this is the case for three smaller cages previously reported to self-catenate experimentally, cages 102 (imine cage CC2), 110 (imine cage CC1) and **112** (imine cage **CC4**),<sup>21</sup> which all had much less favourable binding energies for self-catenation than the top 20 reported in Table 1.

#### Cage pairings that prefer nested cage complexes

We now return to the energetically favourable nested cage complexes. First, we examined which cages are most frequently found in energetically favourable pairings. In Figure 5 there is a histogram of cages that are found in nested cage complexes with highly favourable binding energies,  $E_b < 500 \text{ kJ mol}^{-1}$ . The equivalent histogram for all binding energies that are negative is shown in Figure S5. The structures of the three most frequently found cages, and their precursors, are shown on the right of Figure 5. It is clear that cage 117 is found in highly favourable pairings many more times than any other cage (73 times), with the next most frequently found being cage 111 (21 times) and cage 114 (9 times), which are two very similar cages formed by reducing the imine [4+6] cage CC1 (cage 110) and functionalising with different acid chlorides to form the corresponding dodecaamide cages. 117 is a relatively large cage, with an internal cavity diameter of 12.9 Å, and is typically found as the outer cage

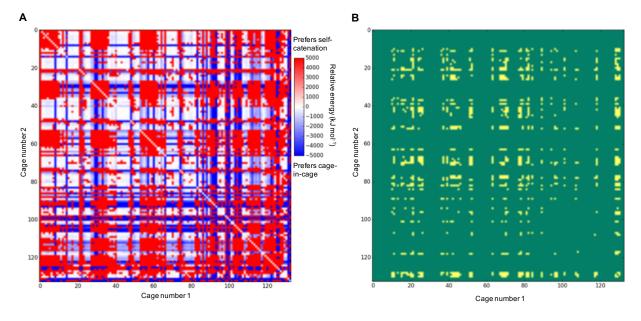
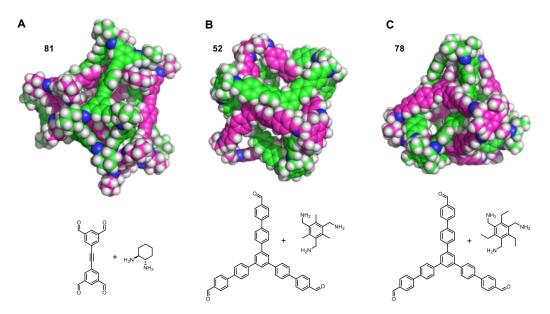


Fig. 3 2D heat-map plots considering the preference for self-catenation in the cage systems; (A) The relative energy difference between forming two self-catenating species or forming a nested cage complex; (B) This plot shows in yellow any systems whereby there is a 'true' preference for self catenation; that is both a energetic preference to self-catenate rather than form a nested cage complex, and there is a favourable (negative) binding energy for each of the self catenations. Other systems are shown in green.



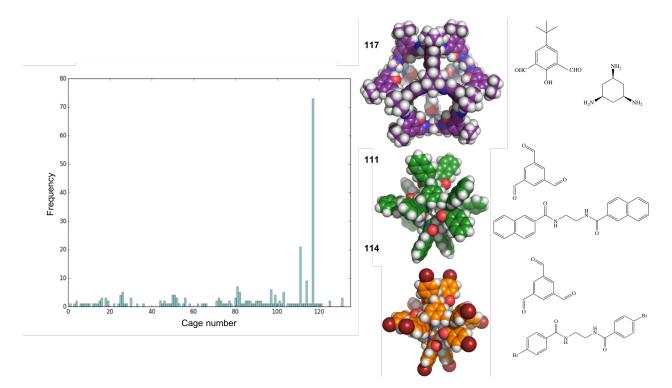
**Fig. 4** The three cage molecules that have the most energetically favourable self-catenations. One molecule is shown with green carbons and one with pink carbons in each case, with nitrogens in blue and hydrogens in white. The precursors required to form the cages are shown below, **52** and **78** only differ by three extra methyl groups on the vertices; (a) **81** ( $E_b = -505 \text{ kJ mol}^{-1}$ ); (b) **52** ( $E_b = -477 \text{ kJ mol}^{-1}$ ) and (c) **78** ( $E_b = -473 \text{ kJ mol}^{-1}$ ).

in nested cage complexes. By contrast, cages 111 and 114 are smaller with internal cavity diameters of 4.2 and 4.1 Å, respectively, and are always found as the inner cage in the complexes.

The binding energies and structural features of the top 20 nested cage complexes are shown in Table 2. In none of these instances is self-catenation energetically competitive. The most favourable binding energy for a nested cage complex was  $-1023 \text{ kJ mol}^{-1}$ , found for combining cages **111** and **117**, which

were also the two cages most frequently found in energetically favourable pairings. This pairing is  $148 \text{ kJ mol}^{-1}$  more favourable than the next best pairing, and by the  $20^{th}$  best pairing the binding energy has fallen to -660 kJ mol<sup>-1</sup>, although that is still more favourable than the best self-catenation pairing (-505 kJ mol<sup>-1</sup>). There are only 3 of the top 20 pairings where cage **117** is not involved. In the majority of cases, the space filling of a smaller cage inside a larger cage is relatively efficient, and only a small cavity

Rank	Cage number	Binding energy (kJ	Remaining cavity di-	Number of win-	Degree of inter-
		$mol^{-1}$ )	ameter (Å)	dows	locking
1	81	-505	10.5	8	4
2	52	-477	11.8	6	6
3	78	-473	9.5	6	6
4	89	-453	2.1	3	2
5	26	-453	12.1	6	6
6	25	-427	9.1	6	6
7	51	-387	8.7	6	6
8	77	-377	9.9	6	6
9	15	-365	8.3	4	3
10	71	-346	10.8	4	3
11	18	-345	9.8	4	2
12	69	-333	8.0	4	3
13	97	-325	15.7	6	6
14	20	-325	7.5	4	3
15	68	-320	8.2	4	3
16	45	-311	11.3	4	3
17	70	-309	7.8	4	3
18	19	-306	12.2	4	3
19	43	-303	8.7	4	3
20	41	-291	8.6	4	3



**Fig. 5** (left) A histogram showing the frequency a cage was found in energetically favourable ( $E_b < -500 \text{ kJ mol}^{-1}$ ) pair; (right) The three cage molecules that were found most frequently (**117**, **111** and **114**) in energetically favourable pairs, along with the precursors the cages are formed from. Carbons in **117** are shown in purple, in **111** in green and in **114** in orange. Nitrogens are in blue, oxygens in red and hydrogens in white.

remains in the complex, typically below 2.5 Å. However, there are exceptions; for example, the pairing of **97** and **117**, which has a remaining cavity of 6.7 Å, where **117** is now the the inner cage.

The structures of the five most energetically favoured nested cage complexes are shown in Figure 6, with the rest of the top 20

shown in Figure S6. All of the top 5 complexes involve cage **117**, which is shown in purple in the figures. It is likely that **117** is found in so many favourable complexes due to the large internal cavity of the cage (diameter 12.9 Å), and the fact that it has six relatively large windows (diameter 8.7 Å). The large size of the

Table 2 A summary of the 20 nested cage pairings with the most energetically favoured binding. "List 1" refers to cages made of precursors that are
commercially available or have easily synthesisable precursors and "List 2" refers to cages that meet "List 1" requirements, but are also known to form
readily and cleanly, with good yields. Molecules are denoted high symmetry if visual inspection suggests similar arrangements at each window of the
outer cage.

Rank	Inner cage	Outer cage	Binding energy (kJ mol <sup>-1</sup> )	Remaining cavity di- ameter (Å)	List 1	List 2	High symme- try
1	111	117	-1023	2.2	✓	✓	$\checkmark$
2	103	117	-875	2.5	<b>v</b>		$\checkmark$
3	4	117	-862	0.7	1		
4	114	117	-852	2.0	<b>√</b>	<b>√</b>	$\checkmark$
5	117	97	-807	6.7	<b>√</b>	<b>√</b>	$\checkmark$
6	91	117	-782	0.0			
7	116	117	-781	2.1	<b>√</b>	✓	<b>↓</b>
8	86	117	-775	1.4			
9	113	117	-732	2.4			$\checkmark$
10	89	117	-718	1.8			
11	56	117	-714	0.5	<b>√</b>	<b>↓</b>	
12	26	117	-714	3.9	$\checkmark$		
13	71	117	-690	0.3	<b>√</b>		
14	117	81	-688	6.6	<b>v</b>		
15	30	52	-678	1.0	<b>v</b>	<b>V</b>	
16	90	117	-674	2.2	✓	<b>V</b>	
17	111	50	-666	2.5	✓	<b>\</b>	<b>↓</b>
18	48	117	-664	3.0	✓		
19	111	52	-661	2.4	✓	<b>√</b>	<b>↓</b>
20	28	117	-660	0.0	1	1	

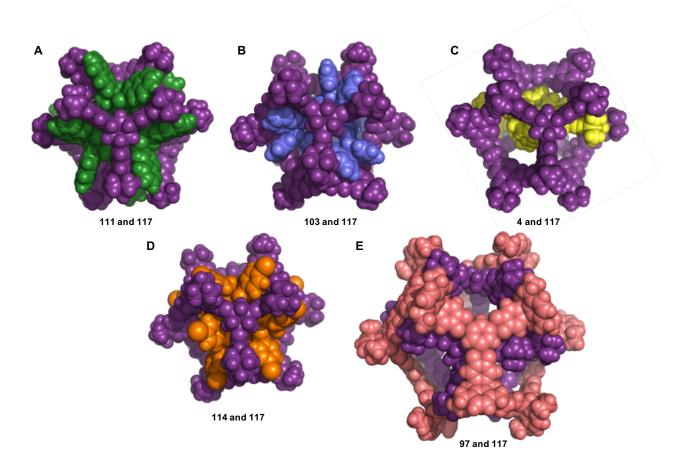
window diameter means that many of the inner cages can have their vertices aligned so as to sit inside or through the window, forming favourable intermolecular interactions with the windows of **117**. The fact that **117** has six windows is also significant, as 45% of the cages in our data set are formed from [4+6] reactions into structures that have six vertices. Each of these vertices can then sit in one of the six windows of **117**, as is the case in many of the best structures, including the top two hits (Figure 6).

As our goal in making these computational predictions is the eventual synthetic realisation of the nested cage complexes, we now consider the synthetic route to realisation of the top 20 pairings. This will allow us to suggest the most promising targets for synthesis. We considered both the availability and ease of synthesis of the precursors, and how readily and with what yield the cages have been reported to be synthesised. With that in mind, we considered whether the cages met two separate sets of criteria. The first set of criteria includes cages that could be synthesised from commercially available precursors or precursors that are readily synthesisable in a reasonable number of steps ("List 1"). This does not consider how readily and cleanly cage formation has been reported, allowing us to include cages from our recent high-throughput screen<sup>23</sup> that were attempted but either did not form or formed mixtures experimentally. We still include them here as it could be the case that the synthesis in a nested cage complex allows templating of the cage that did not previously form. The second set of criteria is more stringent, using all the initial criteria with the additional requirement that the cages have been reported to be synthesised readily and cleanly, eliminating all failed syntheses, reports of mixtures forming, and low yielding reactions ("List 2"). The complete characterisation of each individual cage into these criteria is given in Table S3, and which list criteria are met for each of the top 20 nested cage complexes are given in Table 2. We also visually inspected the complexes for their symmetry, denoting the complexes as high symmetry if there were similar arrangements of the molecules at each window of the outer cage (Table 2). We would expect that high symmetry complexes would be particularly favoured and therefore might have a higher chance of synthetic realisation.

The vast majority of the nested cage complexes meet the initial criteria (95%), whereas only 56% of the complexes meet the more stringent criteria. Only 40% of the cage pairings are deemed to be high symmetry, and overall only 6 of the complexes (30%) meet both the stringent criteria and are high symmetry. We would expect these six complexes to be the most promising for synthetic realisation of a nested cage complex. These complexes were ranked  $1^{st}$ ,  $4^{th}$ ,  $5^{th}$ ,  $7^{th}$ ,  $17^{th}$ , and  $19^{th}$  purely based on binding energies. Therefore, the most promising nested cage complex still remains the combination of cages **111** and **117**. Further, the best four of these six complexes all include **117** as the outer cage, but the last two complexes include cage **111** as the inner cage with two different outer cages.

#### Conclusions

To our knowledge, an organic nested cage complex has not been previously reported. Here, we have screened 132 organic cage



**Fig. 6** The five nested cage complexes with the most energetically favourable binding energies; (a) **111** and **117** ( $E_b = -1023 \text{ kJ mol}^{-1}$ ); (b) **103** and **117** ( $E_b = -875 \text{ kJ mol}^{-1}$ ); (c) **4** and **117** ( $E_b = -862 \text{ kJ mol}^{-1}$ ); (d) **114** and **117** ( $E_b = -852 \text{ kJ mol}^{-1}$ ); (e) **97** and **117** ( $E_b = -807 \text{ kJ mol}^{-1}$ ). Cage colouring as: **4**, yellow; **97**, salmon pink; **103**, indigo; **111**, green; **114**, orange and **117**, purple.

molecules for their potential in forming energetically favourable nested cage complexes. We have also considered which cages are energetically favourable for self-catenation instead. The large number of possible combinations and the need to sample many different relative orientations of the cages in each pairing meant that we conducted almost half a million calculations in this study. Through calculating the binding energy of the cage pairings, we were then able to identify which self-catenated complexes and which nested cage complexes were most energetically favourable. We also considered the degree of interlocking, symmetry of the arrangements, and the ease of synthesis of the precursors and of the individual cage molecules to analyse which are the most promising candidates for attempts at synthesis.

The three most favourable cages for self-catenation were found to be a **TCC1**<sub>[6+12]</sub> large truncated tetrahedron (cage **81**), <sup>54</sup> and two related large tetrahedral cages formed from a [4+4] imine reaction, that differ only in the alkyl functionalisation of the triamine vertex (**52** and **78**).<sup>23</sup> Of these, cages **52** and **78** would be the most promising for synthesis because they were formed cleanly and in good yield. The nested cage complexes were found to be energetically much more favourable than the self-catenation reactions, and in all of the top nested cage complexes, the alternative self-catenation reactions were never found to be energetically competitive. The large [8+12] imine cage from Gawroński and co-workers (cage 117),<sup>75</sup> was found to be involved in the largest number of favourable nested cage complexes by a considerable margin, typically as the outer cage. The frequency that 117 was involved in favourable nested cage complexes can in large part be attributed to the fact that it has six large windows, which are a good symmetry match for encapsulating inner cages that have six vertices that can sit in each of the windows of 117, which is the case for 45% of the cages in our data set. The next most frequently found cage in the complexes was cage 111, which is a dodecaamide cage that has six vertices. The highest binding energy pairing involves cages 111 and 117, in an arrangement where pairs of naphthalene arms at each vertex of 111 sit in the windows of 117, with favourable intermolecular interactions that make the binding energy particularly favourable.

We can now suggest the most promising routes for synthetic realisation of a nested cage complex. The most promising complex is that containing **111** and **117**. Given the irreversible nature of the inner cage **111**, there are two viable approaches to synthesising the nested cage complex with **117**. The first would be to use the inner cage **111** as a template and attempt a one-pot reaction with the precursors for the outer cage **117** or, alternatively, the reversible outer cage could be formed separately and then mixed with the inner cage and allowed to equilibrate. A range of different solvents and additives could be trialled for both of these approaches, as well as recrystallisation screens, which is how previous organic cage catenanes were initially discovered.

Due to the high frequency with which 117 occurred in energetically favourable complexes however, we would also suggest that it is worth screening for complexes combining 117 with a wider range of potential cages, particularly smaller cages with six vertices that we find to be good partner cages for 117. It will be important to take into consideration the reversible nature of alternative organic cage partners, particularly those formed through imine condensations, where competing reactions to form new species may occur over forming a nested cage complex, such as scrambled statistical distributions<sup>81</sup> or socially self-sorted structures.<sup>82</sup> Furthermore, a similar screen could also be attempted with cage 111, which was found to partner favourably with many cages. We hope that by narrowing down the thousands of possibilities for nested cage complexes to just a handful, this computational study stimulates synthetic work and assists in the realisation of the first organic nested cage complex.

#### **Conflicts of interest**

There are no conflicts to declare.

#### Acknowledgements

We thank the Royal Society for a University Research Fellowship (K. E. J.), the EPSRC (EP/M017257/1, EP/P005543/1, EP/R005710/1 and EP/N004884/1) and the ERC through grant agreement no. 758370 (ERC-StG-PE5-CoMMaD) for funding. We thank Filip Szczypiński for valuable discussions.

#### Notes and references

- 1 F. Beuerle and B. Gole, *Angew. Chem. Int. Ed.*, 2018, **57**, 4850–4878.
- 2 T. Hasell and A. I. Cooper, Nature Rev. Mater., 2016, 1, 10686.
- 3 M. Mastalerz, Angew. Chem. Int. Ed., 2010, 49, 5042-5053.
- 4 Z. Liu, S. K. M. Nalluri and J. F. Stoddart, *Chem. Soc. Rev.*, 2017, **46**, 2459–2478.
- 5 G. Gil-Ramírez, D. A. Leigh and A. J. Stephens, *Angew. Chem. Int. Ed.*, 2015, **127**, 6208–6249.
- 6 M. Xue, Y. Yang, X. Chi, X. Yan and F. Huang, *Chem. Rev.*, 2015, **115**, 7398–7501.
- 7 S. D. P. Fielden, D. A. Leigh and S. L. Woltering, *Angew. Chem. Int. Ed.*, 2017, **56**, 11166–11194.
- 8 S. Erbas-Cakmak, D. A. Leigh, C. T. McTernan and A. L. Nussbaumer, *Chem. Rev.*, 2015, **115**, 10081–10206.
- 9 S. Kassem, T. van Leeuwen, A. S. Lubbe, M. R. Wilson, B. L. Feringa and D. A. Leigh, *Chem. Soc. Rev.*, 2017, 46, 2592– 2621.
- 10 S. Y. Kim, I. S. Jung, E. Lee, J. Kim, S. Sakamoto, K. Yamaguchi and K. Kim, Angew. Chem. Int. Ed., 2001, 40, 2119– 2121.
- 11 H. Danjo, Y. Hashimoto, Y. Kidena, A. Nogamine, K. Katagiri, M. Kawahata, T. Miyazawa and K. Yamaguchi, *Org. Lett.*, 2015, **17**, 2154–2157.

- 12 W. Gong, X. Yang, P. Y. Zavalij, L. Isaacs, Z. Zhao and S. Liu, *Chem. Eur. J.*, 2016, **22**, 17612–17618.
- 13 K. Cai, M. C. Lipke, Z. Liu, J. Nelson, T. Cheng, Y. Shi, C. Cheng, D. Shen, J.-M. Han, S. Vemuri, Y. Feng, C. L. Stern, W. A. Goddard, M. R. Wasielewski and J. F. Stoddart, *Nature Commun.*, 2018, **9**, 5275–528–52833.
- 14 S. A. L. Rousseaux, J. Q. Gong, R. Haver, B. Odell, T. D. W. Claridge, L. M. Herz and H. L. Anderson, J. Am. Chem. Soc., 2015, 137, 12713–12718.
- 15 T. Kawase, K. Tanaka, N. Shiono, Y. Seirai and M. Oda, *Angew. Chem. Int. Ed.*, 2004, **43**, 1722–1724.
- 16 H. Ueno, T. Nishihara, Y. Segawa and K. Itami, Angew. Chem. Int. Ed., 2015, 54, 3707–3711.
- 17 B. Sun, M. Wang, Z. Lou, M. Huang, C. Xu, X. Li, L.-J. Chen, Y. Yu, G. L. Davis, B. Xu, H.-B. Yang and X. Li, *J. Am. Chem. Soc.*, 2015, **137**, 1556–1564.
- 18 D. Zhang, T. K. Ronson, J. L. Greenfield, T. Brotin, P. Berthault, E. Léonce, J.-L. Zhu, L. Xu and J. R. Nitschke, J. Am. Chem. Soc., 2019, 141, 8339–8345.
- 19 T. Sawada, H. Hisada and M. Fujita, J. Am. Chem. Soc., 2014, 136, 4449–4451.
- 20 Z. Liu, C. Tian, J. Yu, Y. Li, W. Jiang and C. Mao, J. Am. Chem. Soc., 2015, 137, 1730–1733.
- 21 T. Hasell, X. Wu, J. T. A. Jones, J. Bacsa, A. Steiner, T. Mitra, A. Trewin, D. J. Adams and A. I. Cooper, *Nature Mater*, 2010, 2, 750–755.
- 22 G. Zhang, O. Presly, F. White, I. M. Oppel and M. Mastalerz, Angew. Chem. Int. Ed., 2014, 53, 5126–5130.
- 23 R. L. Greenaway, V. Santolini, M. J. Bennison, B. M. Alston, C. J. Pugh, M. A. Little, M. Miklitz, E. G. B. Eden-Rump, R. Clowes, A. Shakil, H. J. Cuthbertson, H. Armstrong, M. E. Briggs, K. E. Jelfs and A. I. Cooper, *Nature Communications*, 2018, **9**, 2849.
- 24 Y. Li, K. M. Mullen, T. D. W. Claridge, P. J. Costa, V. Felix and P. D. Beer, *Chem. Commun.*, 2009, **36**, 7134–71373.
- 25 H. Li, H. Zhang, A. D. Lammer, M. Wang, X. Li, V. M. Lynch and J. L. Sessler, *Nature Chem.*, 2015, 7, 1003 –1008.
- 26 M. Yoshizawa, M. Yoshizawa, J. K. Klosterman, J. K. Klosterman, M. Fujita, M. Fujita and M. Fujita, *Angew. Chem. Int. Ed.*, 2009, 48, 3418–3438.
- 27 T.-C. Lee, E. Kalenius, A. I. Lazar, K. I. Assaf, N. Kuhnert, C. H. Grün, J. Jänis, O. A. Scherman and W. M. Nau, *Nature Chem.*, 2013, 5, 376–382.
- 28 A. Kewley, A. Stephenson, L. Chen, M. E. Briggs, T. Hasell and A. I. Cooper, *Chem. Mater.*, 2015, **27**, 3207–3210.
- 29 T. Mitra, K. E. Jelfs, M. Schmidtmann, A. Ahmed, S. Y. Chong, D. J. Adams and A. I. Cooper, *Nature Chem.*, 2013, 5, 276– 281.
- 30 T. Hasell, M. Miklitz, A. Stephenson, M. A. Little, S. Y. Chong, R. Clowes, L. Chen, D. Holden, G. A. Tribello, K. E. Jelfs and A. I. Cooper, J. Am. Chem. Soc., 2016, 138, 1653–1559.
- 31 L. Chen, P. S. Reiss, S. Y. Chong, D. Holden, K. E. Jelfs, T. Hasell, M. A. Little, A. Kewley, M. E. Briggs, A. Stephenson, K. M. Thomas, J. A. Armstrong, J. Bell, J. Busto, R. Noel,

J. Liu, D. M. Strachan, P. K. Thallapally and A. I. Cooper, *Nature Mater.*, 2014, **13**, 954–960.

- 32 M. Brutschy, M. W. Schneider, M. Mastalerz and S. R. Waldvogel, *Adv. Mater.*, 2012, **24**, 6049–6052.
- 33 K. Acharyya and P. S. Mukherjee, Chem. Commun., 2014, 50, 15788–15791.
- 34 N. Giri, M. G. Del Pópolo, G. Melaugh, R. L. Greenaway, K. Rätzke, T. Koschine, L. Pison, M. F. C. Gomes, A. I. Cooper and S. L. James, *Nature*, 2015, **527**, 216–220.
- 35 T. Brotin and J.-P. Dutasta, Chem. Rev., 2009, 109, 88-130.
- 36 T. Tozawa, J. T. A. Jones, S. I. Swamy, S. Jiang, D. J. Adams, S. Shakespeare, D. Bradshaw, T. Hasell, S. Y. Chong, C. Tang, S. Thompson, J. Parker, A. Trewin, J. Bacsa, A. M. Z. Slawin, A. Steiner and A. I. Cooper, *Nature Mater.*, 2009, 8, 973–978.
- 37 E. J. Dale, N. A. Vermeulen, A. A. Thomas, J. C. Barnes, M. Juríček, A. K. Blackburn, N. L. Strutt, A. A. Sarjeant, C. L. Stern, S. E. Denmark and J. F. Stoddart, *J. Am. Chem. Soc.*, 2014, 136, 10669–10682.
- 38 J. D. Evans, K. E. Jelfs, G. M. Day and C. J. Doonan, *Chem. Soc. Rev.*, 2017, 46, 3286–3301.
- 39 K. E. Jelfs, X. Wu, M. Schmidtmann, J. T. A. Jones, J. E. Warren, D. J. Adams and A. I. Cooper, *Angew. Chem. Int. Ed.*, 2011, 50, 10653–10656.
- 40 K. E. Jelfs, E. Eden, J. L. Culshaw, S. Shakespeare, E. O. Pyzer-Knapp, H. P. G. Thompson, J. Bacsa, G. M. Day and D. J. Adams, J. Am. Chem. Soc., 2013, 135, 9307–9310.
- 41 V. Santolini, M. Miklitz, E. Berardo and K. E. Jelfs, *Nanoscale*, 2017, **9**, 5280–5298.
- 42 G. Zhu, Y. Liu, L. Flores, Z. R. Lee, C. W. Jones, D. A. Dixon, D. S. Sholl and R. P. Lively, *Chem. Mater.*, 2017, **30**, 262–272.
- 43 V. Santolini, G. A. Tribello and K. E. Jelfs, *Chem. Commun.*, 2015, **51**, 15542–15545.
- 44 L. Turcani, R. L. Greenaway and K. E. Jelfs, Chem. Mater., 2019, 31, 714–727.
- 45 A. J. Cruz-Cabeza, G. M. Day and W. Jones, *Chem. Eur. J.*, 2009, **15**, 13033–13040.
- 46 J. T. A. Jones, T. Hasell, X. Wu, J. Bacsa, K. E. Jelfs, M. Schmidtmann, S. Y. Chong, D. J. Adams, A. Trewin, F. Schiffman, F. Cora, B. Slater, A. Steiner, G. M. Day and A. I. Cooper, *Nature*, 2011, **474**, 367–371.
- 47 E. O. Pyzer-Knapp, H. P. G. Thompson, F. Schiffmann, K. E. Jelfs, A. I. Cooper and G. M. Day, *Chem. Sci.*, 2014, 5, 2235–2245.
- 48 A. G. Slater, P. S. Reiss, A. Pulido, M. A. Little, D. L. Holden, L. Chen, S. Y. Chong, B. M. Alston, R. Clowes, M. Haranczyk, M. E. Briggs, T. Hasell, G. M. Day and A. I. Cooper, ACS Cent. Sci., 2017, 3, 734–742.
- 49 M. Bernabei, R. Pérez-Soto, I. Gomez Garcia and M. Haranczyk, *Mol. Syst. Des. Eng.*, 2019, 4, 912–920.
- 50 T. Hasell, S. Y. Chong, K. E. Jelfs, D. J. Adams and A. I. Cooper, *J. Am. Chem. Soc.*, 2012, **134**, 588–598.
- 51 M. Miklitz, S. Jiang, R. Clowes, M. E. Briggs, A. I. Cooper and K. E. Jelfs, *J. Phys. Chem. C*, 2017, **121**, 15211–15222.
- 52 J. S. Camp and D. S. Sholl, J. Phys. Chem. C, 2016, 120, 1110-

1120.

- 53 G. Zhang and M. Mastalerz, Chem. Soc. Rev., 2014, 43, 1934– 1947.
- 54 C. Stackhouse, V. Santolini, R. Greenaway, M. A. Little, M. E. Briggs, K. E. Jelfs and A. I. Cooper, *Crystal Growth & Design*, 2018, **18**, 2759–2764.
- 55 K. Matsui, Y. Segawa and K. Itami, J. Am. Chem. Soc., 2014, 136, 16452–16458.
- 56 J. Kim, I.-S. Jung, S.-Y. Kim, E. Lee, J.-K. Kang, S. Sakamoto, K. Yamaguchi and K. Kim, J. Am. Chem. Soc., 2000, **122**, 540– 541.
- 57 M. Mastalerz, M. W. Schneider, I. M. Oppel and O. Presly, Angew. Chem. Int. Ed., 2011, 50, 1046–1051.
- 58 M. W. Schneider, I. M. Oppel and M. Mastalerz, *Chem. Eur. J.*, 2012, **18**, 4156–4160.
- 59 M. Mastalerz, Chem. Commun., 2008, 4756-4758.
- 60 M. W. Schneider, H.-J. Siegfried Hauswald, R. Stoll and M. Mastalerz, *Chem. Commun.*, 2012, 48, 9861–9863.
- 61 B. S. Park, C. B. Knobler and D. J. Cram, *Chem. Commun.*, 1998, **0**, 55–56.
- 62 N. Giri, C. E. Davidson, G. Melaugh, M. G. Del Pópolo, J. T. A. Jones, T. Hasell, A. I. Cooper, P. N. Horton, M. B. Hursthouse and S. L. James, *Chem. Sci.*, 2012, **3**, 2153–2158.
- 63 M. Liu, M. A. Little, K. E. Jelfs, J. T. A. Jones, M. Schmidtmann, S. Y. Chong, T. Hasell and A. I. Cooper, *J. Am. Chem. Soc.*, 2014, **136**, 7583–7586.
- 64 M. J. Bojdys, M. E. Briggs, J. T. A. Jones, D. J. Adams, S. Y. Chong, M. Schmidtmann and A. I. Cooper, J. Am. Chem. Soc., 2011, **133**, 16566–16571.
- 65 J. L. Culshaw, G. Cheng, M. Schmidtmann, T. Hasell, M. Liu, D. J. Adams and A. I. Cooper, J. Am. Chem. Soc., 2013, 135, 9307–9310.
- 66 M. E. Briggs, K. E. Jelfs, S. Y. Chong and C. Lester, *Crystal Growth & Design*, 2013, **13**, 4993–5000.
- 67 A. G. Slater, M. A. Little, A. Pulido, S. Y. Chong, D. Holden, L. Chen, C. Morgan, X. Wu, G. Cheng, R. Clowes, M. E. Briggs, T. Hasell, K. E. Jelfs, G. M. Day and A. I. Cooper, *Nature Chem.*, 2016, **9**, 17–25.
- 68 S. Jiang, J. Bacsa, X. Wu, J. T. A. Jones, R. Dawson, A. Trewin, D. J. Adams and A. I. Cooper, *Chem. Commun.*, 2011, 47, 8919–8922.
- 69 T. Hasell, J. L. Culshaw, S. Y. Chong, M. Schmidtmann, M. A. Little, K. E. Jelfs, E. O. Pyzer-Knapp, H. Shepherd, D. J. Adams, G. M. Day and A. I. Cooper, *J. Am. Chem. Soc.*, 2014, 136, 1438–1448.
- 70 H. Ding, Y. Yang, B. Li, F. Pan, G. Zhu, M. Zeller, D. Yuan and C. Wang, *Chem. Commun.*, 2015, **51**, 1976–1979.
- 71 N. Hafezi, J. M. Holcroft, K. J. Hartlieb, E. J. Dale, N. A. Vermeulen, C. L. Stern, A. A. Sarjeant and J. F. Stoddart, *Angew. Chem. Int. Ed.*, 2015, 54, 456–461.
- 72 H. Kudo, H. Kudo, R. Hayashi, R. Hayashi, K. Mitani, K. Mitani, T. Yokozawa, T. Yokozawa, N. C. Kasuga, N. C. Kasuga, T. Nishikubo and T. Nishikubo, *Angew. Chem. Int. Ed.*, 2006, 45, 7948–7952.

- 73 C. J. Doonan, C. J. Sumby, J. D. Evans, D. M. Huang, P. Valente and A. Burgun, *Chem. Commun.*, 2016, **52**, 8850–8853.
- 74 K. Ono, R. Aizawa, T. Yamano, S. Ito, N. Yasuda, K. Johmoto,
  H. Uekusa and N. Iwasawa, *Chem. Commun.*, 2014, 50, 13683–13686.
- 75 P. Skowronek, B. Warżajtis, U. Rychlewska and J. Gawroński, *Chem. Commun.*, 2013, **49**, 2524–3.
- 76 S. Klotzbach and F. Beuerle, Angew. Chem. Int. Ed., 2015, 127, 10497–10502.
- 77 S. Klotzbach, T. Scherpf and F. Beuerle, *Chem. Commun.*, 2014, **50**, 12454–12457.

- 78 M. Miklitz and K. E. Jelfs, J. Chem. Inf. Model., 2018, 58, 2387–2391.
- 79 E. Harder, W. Damm, J. Maple, C. Wu, M. Reboul, J. Y. Xiang, L. Wang, D. Lupyan, M. K. Dahlgren, J. L. Knight, J. W. Kaus, D. S. Cerutti, G. Krilov, W. L. Jorgensen, R. Abel and R. A. Friesner, J. Chem. Theory Comput., 2016, **12**, 281–296.
- 80 G. Zhang, O. Presly, F. White, I. M. Oppel and M. Mastalerz, Angew. Chem. Int. Ed., 2014, 53, 1516–1520.
- 81 S. Lee, A. Yang, T. P. Moneypenny and J. S. Moore, J. Am. Chem. Soc., 2016, **138**, 2182–2185.
- 82 F. Beuerle, S. Klotzbach and A. Dhara, *Synlett*, 2016, **27**, 1133–1138.