

# Bayesian Networks approach to fault diagnosis of a hydroelectric generation system

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**Abstract:** This study focuses on the fault diagnosis of a hydroelectric generation system with hydraulic-mechanical-electric structures. To achieve this analysis, a methodology combining Bayesian Networks approach and fault diagnosis expert system is presented, which enables the time-based maintenance to transform to the condition-based maintenance. First, fault types and the associated fault characteristics of the generation system are extensively analyzed to establish a precise Bayesian Network. Then, the Noisy-Or modelling approach is used to implement the fault diagnosis expert system, which not only reduces node computations without severe information loss but also eliminates the data dependency. Some typical applications are proposed to fully show the

36 methodology capability of the fault diagnosis of the hydroelectric generation system.

37 **Keywords:** hydroelectric generation system; fault diagnosis; Bayesian Network; expert system; state  
38 evaluation

## 40 **1. Introduction**

41 2015 United Nations Climate Change Conference promised that the raise of global warming is  
42 almost 2 °C compared to pre-industrial levels, which greatly promotes the electricity generation to  
43 turn to renewable energy such as hydropower generations [1]. China is leading to a hydropower  
44 boom, followed by India, Europe, the United States and Japan [2]. Hydropower plants have been  
45 built in more than 160 countries, with a total number of 11000 plants equipped with 27000  
46 hydro-turbine generator units at the end of 2017 [3]. In China, the hydropower capacity is expected  
47 to increase to 380 gigawatts by 2020 [4]. These hydropower plants are constructed at sites along  
48 rivers, including thirteen plants on the Salween or Nujiang, and twenty plants along the Brahmaputra  
49 [4]. In Brazil, 375 small hydropower plants with the total capacity of 4799 MW are currently running,  
50 and another 1701 MW installed capacity will be constructed in the next ten years [5]. Hydroelectric  
51 generation systems are under construction all over the world to ensure the enforcement of stricter  
52 energy and environmental policy. Obviously, the economic benefit and carbon dioxide mitigation of  
53 such hydroelectric generating systems are well known to the general public [6-11], but the stability  
54 and safety impacts of themselves still require enough attentions.

55 Faults in the hydroelectric generation systems (HGS) inevitably result in unexpected safety  
56 accidents with enormous maintenance costs [12-14]. National Energy Administration issued that  
57 80% of HGS' faults are caused by the vibration of the hydraulic-mechanic-electric components  
58 [15-16]. In general, the vibration in the HGS is defined as a drastic reciprocating motion caused by

59 unbalanced forces and uncertain disturbances [17-18]. For instance, 60% of the vibration faults are  
60 attributable to the out-of-balance rotating bodies and the pressure pulsation of flow passage  
61 components in Japan [19-20]. The current study of the HGS's faults mainly focuses on the  
62 constituent components (e.g. generators, hydro-turbines and pipelines) [21-23]. Additionally, the  
63 collection of the on-line monitoring data under the condition of fast information flow is another  
64 challenge for fault diagnosis of the HGS [24-25]. To adequately analyze the faults mechanism, to  
65 predict behavior of systems, to evaluate operating reliability and to decrease maintenance costs, are  
66 the challenging tasks. Hence, it is of primary importance to provide the powerful methodology for  
67 the fault diagnosis of HGSs not only of systems but also of data available.

68 Some popular efficient approaches, combining monitoring data and expert experiences, are  
69 developed for the fault diagnosis such as Fault-Tree Analysis (FTA), Event-Tree Analysis (ETA) and  
70 Bayesian Network (BN) [26-28]. FTA and ETA are applied to evaluate the reliability of systems,  
71 whereas these approaches lack lateral linkages between nodes and also require high-quality experts  
72 to cope with complicated computations [29]. In light of this, BN is widely used to overcome the  
73 limitations of FTA and ETA since it successfully incorporates expert experiences by means of lateral  
74 linkages [30-32]. However, the modelling of BN in practical applications is still difficult and tedious,  
75 especially for the complicated systems [33-34]. Thus, it is emergent to present suitable approaches to  
76 reduce node computations without severe information loss.

77 This study aims to provide an efficient computational methodology for the fault diagnosis of the  
78 HGS. To establish a precise Bayesian Network of the HGS, we fully analyze the complex fault types  
79 and their associated fault characteristics. The Noisy-Or modelling approach is used to eliminate the  
80 data dependency and to reduce node computations. The fault diagnosis expert system is proposed

81 that is beneficial to the condition-based maintenance at the lowest cost. Finally, some typical  
82 applications are done to fully show the methodology capability of the fault diagnosis of the  
83 hydroelectric generation system.

84 This study is structured as follows. Section 2 describes the global methodology of the BN fault  
85 diagnosis of the HGS. Section 3 presents the BN fault diagnosis model considering the hydraulic,  
86 mechanical and electric factors. Section 4 performs the applications of the fault diagnosis model of  
87 the HGS. Conclusions and discussions in section 5 summary this study.

## 88 **2. Methodology**

89 This section is dedicated to the overall theoretical background of the methodology adopted in  
90 the present study. A brief description of BN, Noisy-Or model and expert system is presented.

### 91 **2.1 Bayesian Network**

92 BN is a statistical graphical model that combines the probability theory with the graphic theory  
93 [35]. A complete BN is comprised of nodes, connecting arrows and the Conditional Probability  
94 Tables (CPTs), which is represented by a Directed Acyclic Graph (DAG). The BN displays the cause  
95 and effect relationships between the network variables, as shown in Fig. 1.

96

97 **Fig. 1** An example of BN.

98 The implementation of BN relying on the Bayes theorem is defined as: The exhaustive event set  
99  $\{B_1, B_2, \dots, B_n\}$  and the event  $A$  exist in a sample space  $\Omega$ , and they respectively meet the conditions  
100 of  $P(B_i) > 0$  ( $i = 1, 2, 3, \dots, n$ ) and  $P(A) > 0$ . Hence, we get [36-37]:

$$101 \quad P(B_i | A) = \frac{P(A | B_i)P(B_i)}{\sum_{j=1}^n P(A | B_j)P(B_j)}, \quad i = 1, 2, 3, \dots, n \quad (1)$$

102 To enable the inference analysis of the BN, Eq. (1) is subject to the following conditional

103 independence hypothesis:

104 The variable nodes ( $X_1, X_2, \dots, X_n$ ) in the BN are conditionally independent for their father nodes. This

105 means that the variable nodes satisfy the joint probability in Eq. (2).

$$106 \quad P(X_1, X_2, \dots, X_n) = \prod_{i=1}^n P(X_i | pa_i), \quad (2)$$

107 where  $pa_i$  denotes the father node set of  $X_i$ .

## 108 2.2 Noisy-Or model

109 The major work of BN is to determine the CPT, whereas the deduction of the joint probability is

110 growing exponentially with the increase of variable nodes. For the BN with  $n$ th binary discrete nodes,

111 it generally requires  $2^n$ th conditional probabilities to describe the network model. To reduce node

112 computations, Noisy-Or modelling approach is applied in the BN calculation. A typical Noisy-Or

113 model [38-39] is expressed as

$$114 \quad \begin{cases} P_i = \frac{P(y|X_i) - P(y|\bar{X}_i)}{1 - P(y|\bar{X}_i)} \\ P(y|X_p) = 1 - \prod_{X_i \in X_T} (1 - P_i) \\ P(X_i = \text{Only} | Y) = \frac{P_i \cdot P(X_i = T)}{P(Y)} \end{cases}, \quad (3)$$

115 where  $y$  is a safety accident,  $X_p$  is the set of fault nodes expressed by  $X_1, X_2, \dots, X_n$ ;  $X_T$  is the truth

116 set of fault nodes;  $P_i$  is the probability of  $y$  if or only if  $X_i = \text{True}$ .

## 117 2.3 Fault diagnosis expert system

118 Fault diagnosis expert system is an intelligent tool that integrates expert experiences and

119 Bayesian inferences, and it has significant advantages of the comprehensive collection of expert

120 knowledge, the accurate simulation of expert thinking and the precision of fault diagnosis. The

121 schematic diagram of the fault diagnosis expert system is performed in Fig. 2. The development of

122 the efficient fault diagnosis expert system will be beneficial to the condition-based maintenance at

123 the lowest cost.

124

125 **Fig. 2** Schematic diagram of a fault diagnosis expert system.

## 126 **2.4 Global methodology**

127 Based on the above descriptions, Fig. 3 is plotted to show the global methodology of Bayesian  
128 fault diagnosis of the HGS. The calculation process plan is concluded in the following steps:

129 (1) Using expert experiences and monitoring data to collect the hydraulic, mechanical and  
130 electric fault types in the HGS and also to investigate their associated fault characteristics. Based on  
131 this, a fault diagnosis model of Bayesian network for the HGS is presented.

132 (2) The expert system gives the prior probabilities of nodes, and the Noisy-Or modelling  
133 approach is employed to reduce the node computations.

134 (3) Based on the Bayes theorem, we conduct the Bayesian fault diagnosis inference of the HGS.  
135 The obtained posterior probabilities are used to perform the diagnostic fault locations and the  
136 relevant fault characteristics. If the actual fault component is included in the diagnostic fault  
137 locations, the maintenance worker is able to solve the problem in time. Conversely, if the diagnostic  
138 result is “No”, the Bayesian network will reassessment the posterior probabilities of fault locations in  
139 light of the updated CPT.

140 (4) Summarizing the frequent fault locations and their corresponding fault characteristics to  
141 diminish the operation loss and maintenance loss in hydropower stations.

142

143 **Fig. 3** The global methodology of fault diagnosis of the hydroelectric generation system. CPT refers

144 to the condition probability table. HGS refers to the hydroelectric generation system.

145

### 146 **3. Model**

147 To model a BN of fault diagnosis, the critical task is to analyze the complex fault types and their  
148 associated fault characteristics in the HGS. we extensively collect the faults data of the HGS from  
149 literatures, on-site visit, and expert advice. In general, the HGS's fault refers to that the system works  
150 abnormally with enormous vibrations and can even lead to accidental shutdown or component  
151 damage since about 80 percent of HGS's faults are caused by component vibrations. Statistically, the  
152 disturbing forces (i.e. the rotational unbalanced force of rotors, the hydraulic unbalanced force and  
153 the unbalanced magnetic pull) with different magnitudes, directions and frequencies will influence  
154 the performance of vibrations. Based on the operating characteristic of the HGS, the disturbing  
155 forces are attributed to the hydraulic, mechanical and electric factors. Hence, the fault types and the  
156 associated fault characteristics can be performed in the fault diagnosis BN of the HGS, as shown in  
157 Fig. 4.

158

159 **Fig. 4** The Bayesian network of the fault diagnosis of the HGS coupling with hydraulic, mechanical  
160 and electric factors.

161

### 162 **4. Case Study**

163 The mechanical fault, as the most important influence factor on the safety of the HGS, is  
164 selected as a case study for the application of the BN proposed in this work. The typical mechanical  
165 fault (i.e. the rubbing fault MF2, the misalignment fault of rotor MF3 and the mechanical axial crack  
166 MF4) and their associated fault characteristics (i.e. the vibration with doubled frequency  $F2F0$  and

167 the vibration with third frequency F3F0) are finally modeled a studied BN, as shown in Fig. 5. In the  
 168 actual operation of hydropower stations, the rubbing fault (MF2) is triggered by improper assembly,  
 169 shafting bend, rotor imbalance and mechanical looseness, resulting in enormous vibrations and  
 170 noises. The misalignment fault of rotor (MF3) generally leads to the deformation of shaft and rotor  
 171 swing, which significantly reduces the operating efficiency of the HGS. The mechanical axial crack  
 172 (MF4) has obvious adverse effects on the stiffness of shaft, which can cause unexpected shaft-broken  
 173 accidents with the increase of load and turbine speed.

174

175 **Fig. 5** A simple BN of the hydraulic generating system with critical mechanical faults.

176 For the HGS's BN with critical mechanical faults performed in Fig. 5, the possible working  
 177 states of the fault nodes are "normal" and "trouble", as well as the fault frequencies for their  
 178 associated fault characteristics nodes include "high" and "low".

179 **Example 4.1:** Noisy-Or Model Applications

180 To reduce the complicated computations of CPT, the Noisy-Or model can significantly  
 181 eliminate disturbing influences between the fault node and the associated fault characteristics nodes.

182 Based on the Noisy-Or model (3), the CPT of node F2F0 and node F3F0 in Fig. 5 is calculated as:

183 i) CPT of node F2F0

184 According to expert experiences, the following probabilities are obtained as:

185  $P(MF2 = trouble) = 0.2, P(MF3 = trouble) = 0.2, P(MF4 = trouble) = 0.4;$

186  $P(y_1 | X_1) = P(F2F0 = high | MF2 = trouble) = 0.56, P(\bar{y}_1 | \bar{X}_1) = P(F2F0 = low | MF2 = normal) = 0.82;$

187  $P(y_1 | X_2) = P(F2F0 = high | MF3 = trouble) = 0.44, P(\bar{y}_1 | \bar{X}_2) = P(F2F0 = low | MF3 = normal) = 0.9;$

188  $P(y_1 | X_3) = P(F2F0 = high | MF4 = trouble) = 0.8, P(\bar{y}_1 | \bar{X}_3) = P(F2F0 = low | MF4 = normal) = 0.92.$

189 For the Noisy-Or model (3), the matrix of  $X_p = \{X_1 = \text{normal}, X_2 = \text{trouble}, X_3 = \text{trouble}\}$ ,

190 Substituting the above probabilities into the Noisy-Or model (3-1), we obtain

$$191 \quad \begin{cases} P_1 = \frac{P(y_1 | X_1) - P(y_1 | \bar{X}_1)}{1 - P(y_1 | \bar{X}_1)} = \frac{0.56 - (1 - 0.82)}{1 - (1 - 0.82)} = 0.4634 \\ P_2 = \frac{P(y_1 | X_2) - P(y_1 | \bar{X}_2)}{1 - P(y_1 | \bar{X}_2)} = \frac{0.44 - (1 - 0.9)}{1 - (1 - 0.9)} = 0.3778 \\ P_3 = \frac{P(y_1 | X_3) - P(y_1 | \bar{X}_3)}{1 - P(y_1 | \bar{X}_3)} = \frac{0.8 - (1 - 0.92)}{1 - (1 - 0.92)} = 0.7826 \end{cases} \quad (4)$$

192 Based on the Noisy-Or model (3-2) and Eq. (4), it can be obtained as

$$193 \quad \begin{cases} P(y | X_p) = 1 - \prod_{X_i \in X_p} (1 - P_i) = 1 - (1 - P_2)(1 - P_3) = 0.8647 \\ P(y | X_p) = 1 - \prod_{X_i \in X_p} (1 - P_i) = 1 - (1 - P_1)(1 - P_3) = 0.8833 \\ P(y | X_p) = 1 - \prod_{X_i \in X_p} (1 - P_i) = 1 - (1 - P_1)(1 - P_2) = 0.6661 \\ P(y | X_p) = 1 - \prod_{X_i \in X_p} (1 - P_i) = 1 - (1 - P_1)(1 - P_2)(1 - P_3) = 0.9274 \end{cases}, \quad (5)$$

194 where the fault node set  $X_p = \{X_1 = \text{normal}, X_2 = \text{trouble}, X_3 = \text{trouble}\}$  in Eq. (5-1),

195  $X_p = \{X_1 = \text{trouble}, X_2 = \text{normal}, X_3 = \text{trouble}\}$  in Eq. (5-2),  $X_p = \{X_1 = \text{trouble}, X_2 = \text{trouble}, X_3 = \text{normal}\}$  in Eq.

196 (5-3), and  $X_p = \{X_1 = \text{trouble}, X_2 = \text{trouble}, X_3 = \text{trouble}\}$  in Eq. (5-4).

197 Therefore, the CPT of node F2F0 is listed in table 1.

198 **Table 1** CPT of node F2F0

MF2	normal				trouble			
MF3	normal		trouble		normal		trouble	
MF4	normal	trouble	normal	trouble	normal	trouble	normal	trouble
low	1.000	0.2174	0.6222	0.1326	0.5366	0.1167	0.3339	0.0726
high	0.0000	0.7826	0.3778	0.8647	0.4634	0.8833	0.6661	0.9274

199

200 ii) CPT of node F3F0

201 Based on expert experiences, the probabilities are obtained as follows:

202  $P(y_2 | X_1) = P(F3F0 = \text{high} | MF2 = \text{trouble}) = 0.74$ ,  $P(\bar{y}_2 | \bar{X}_1) = P(F3F0 = \text{low} | MF2 = \text{normal}) = 0.95$ ;

203  $P(y_2 | X_2) = P(F3F0 = \text{high} | MF3 = \text{trouble}) = 0.45$ ,  $P(\bar{y}_2 | \bar{X}_2) = P(F3F0 = \text{low} | MF3 = \text{normal}) = 0.92$ ;

204  $P(y_2 | X_3) = P(F3F0 = high | MF4 = trouble) = 0.35$ ,  $P(\overline{y_2} | \overline{X_3}) = P(F3F0 = low | MF4 = normal) = 0.88$ .

205 Then, based on the Noisy-Or model (3), we can get:

$$206 \quad \begin{cases} P_1 = \frac{P(y_2 | X_1) - P(y_2 | \overline{X_1})}{1 - P(y_2 | \overline{X_1})} = \frac{0.74 - (1 - 0.95)}{1 - (1 - 0.95)} = 0.7263 \\ P_2 = \frac{P(y_2 | X_2) - P(y_2 | \overline{X_2})}{1 - P(y_2 | \overline{X_2})} = \frac{0.45 - (1 - 0.92)}{1 - (1 - 0.92)} = 0.4022, \\ P_3 = \frac{P(y_2 | X_3) - P(y_2 | \overline{X_3})}{1 - P(y_2 | \overline{X_3})} = \frac{0.35 - (1 - 0.88)}{1 - (1 - 0.88)} = 0.2614 \end{cases} \quad (6)$$

$$207 \quad \begin{cases} P(y | X_p) = 1 - \prod_{X_i \in X_p} (1 - P_i) = 1 - (1 - P_2)(1 - P_3) = 0.5585 \\ P(y | X_p) = 1 - \prod_{X_i \in X_p} (1 - P_i) = 1 - (1 - P_1)(1 - P_3) = 0.7978 \\ P(y | X_p) = 1 - \prod_{X_i \in X_p} (1 - P_i) = 1 - (1 - P_1)(1 - P_2) = 0.8364 \\ P(y | X_p) = 1 - \prod_{X_i \in X_p} (1 - P_i) = 1 - (1 - P_1)(1 - P_2)(1 - P_3) = 0.8792 \end{cases}, \quad (7)$$

208 where the fault nodes set  $X_p = \{X_1 = normal, X_2 = trouble, X_3 = trouble\}$  in Eq. (7-1),

209  $X_p = \{X_1 = trouble, X_2 = normal, X_3 = trouble\}$  in Eq. (7-2),  $X_p = \{X_1 = trouble, X_2 = trouble, X_3 = normal\}$  in Eq.

210 (7-3), and  $X_p = \{X_1 = trouble, X_2 = trouble, X_3 = trouble\}$  in Eq. (7-4).

211 Thus, the CPT of node F3F0 is listed in Tab. 2.

212 **Table 2** CPT of node F3F0

MF2	normal				trouble			
	normal		trouble		normal		trouble	
MF3	normal	trouble	normal	trouble	normal	trouble	normal	trouble
low	1.000	0.7386	0.5978	0.4415	0.2737	0.2022	0.1636	0.1208
high	0.0000	0.2614	0.4022	0.5585	0.7263	0.7978	0.8364	0.8792

213

#### 214 **Example 4.2:** BN-Based Fault Diagnosis of the HGS

215 Using Bayes theory presented in the methodology section, we establish the fault diagnosis

216 expert system of the HGS that integrates expert experiences and Bayesian inferences. The BN

217 inference is utilized to give some typical applications of the BN-Based fault diagnosis of the HGS.

218 Six cases are performed as follows.

219       • Case 1: Assuming the fact is the increasing vibration with doubled frequency. That is, the  
220 probability of the fault characteristic node F2F0 in “high” state is 1. Using the Bayesian diagnosis  
221 inference (the definition is revealed in the literature [40]), its father nodes probabilities including the  
222 rubbing fault MF2, the misalignment fault of rotor MF3 and the mechanical axial crack MF4 in  
223 “trouble” states are 0.3110, 0.2892 and 0.7718, respectively. The calculated result indicates that the  
224 HGS’s fault is most likely due to the mechanical axial crack with the occurrence of the increasing  
225 vibration with doubled frequency.

226       • Case 2: When the on-line monitoring system captures the increasing signal of the vibration  
227 with third frequency, the probability of the fault characteristic node F3F0 in “high” state equals to 1.  
228 Similarly, the nodes probabilities of the rubbing fault MF2, the misalignment fault of rotor MF3 and  
229 the mechanical axial crack MF4 in “trouble” states are therefore calculated as 0.5230, 0.3663 and  
230 0.5665, respectively. This means that the mechanical rubbing and axial crack are able to result in the  
231 fault of the HGS.

232       • Case 3: The HGS shows the vibration with doubled frequency and third frequency. As a  
233 result, the probability for the fault characteristic nodes F2F0 and F3F0 in the “high” state is 1. The  
234 nodes probabilities of the rubbing fault MF2, the misalignment fault of rotor MF3 and the  
235 mechanical axial crack MF4 in “trouble” states are obtained as 0.5145, 0.3568 and 0.7013 by means  
236 of Bayesian diagnosis inferences, respectively. Therefore, the mechanical axial crack may be  
237 considered as the main influence factor on the operating safety of the HGS in this case.

238       • Case 4: Assuming the fault of the mechanical axial crack is found by maintenance workers,  
239 and the on-line monitoring system also captures the increasing signal of the vibration with doubled  
240 frequency. Based on the Bayesian support inference in literatures [40-41], its father nodes

241 probabilities of the rubbing fault MF2 and the misalignment fault of rotor MF3 in “trouble” states are  
242 0.2181 and 0.2150, respectively. Meanwhile, the parallel node probability of the vibration with third  
243 frequency F3F0 in the “high” state is 0.4325.

244 Comparing with case 3, the probability for the occurrence of the rubbing fault and the  
245 misalignment fault of rotor significantly decreases if the fault of mechanical axial crack already  
246 exists in the HGS. Additionally, the hydropower station is suggested to develop the protection  
247 strategies to cope with the increase of the vibration with third frequency in advance.

248 • Case 5: If the fault of the mechanical axial crack and the fault characteristic of the  
249 increasing vibration with third frequency occur during the maintenance task, the CPT of neighbor  
250 nodes using the Bayesian support inference are obtained. Specifically, its father nodes probabilities  
251 of the rubbing fault MF2 and the misalignment fault of rotor MF3 in “trouble” states are 0.3881 and  
252 0.2969, meanwhile the parallel node probability of the vibration with doubled frequency F2F0 in the  
253 “high” state is 0.8434.

254 Comparing with the separate occurrence of the increasing vibration with third frequency in case  
255 2, the occurrence probability of the rubbing fault and the misalignment fault of rotor decreases when  
256 the fault of the mechanical axial crack and the fault characteristic of the increasing vibration with  
257 third frequency occur at the same time. In this situation, case 5 is easy to lead to the increase of the  
258 vibration with doubled frequency, which should be pay more attentions in the actual operation of  
259 hydropower stations.

260 • Case 6: For the HGS existing in the fault of the mechanical axial crack and the fault  
261 characteristic of the increasing vibrations with both third frequency and doubled frequency, the CPT  
262 of neighbor nodes are calculated using the Bayesian support inference. That is, the probabilities of

263 the rubbing fault MF2 and the misalignment fault of rotor MF3 in “trouble” states are 0.4109 and  
264 0.3113, respectively.

265 From the analysis of cases 3 and 6, when the HGS shows the same fault characteristic except for  
266 the mechanical axial crack, the occurrence probability of the rubbing fault and the misalignment fault  
267 of rotor will decrease.

268 In conclusion, the calculated results in cases 1 to 3 are validated in refs. [42-46], and the  
269 diagnostic results obtained in cases 4 to 6 are consistent with ref. [47].

270

## 271 **5. Conclusions and discussion**

272 In this work, the fault diagnosis method for the hydroelectric generation system coupling with  
273 hydraulic, mechanical and electric factors is presented. The methodology adopted in this work is  
274 based on the Bayesian Networks approach and the expert system. Herein a complete Bayesian  
275 network fault diagnosis model of the generating system is implemented that takes into consideration  
276 the comprehensive knowledge of the vibration fault types and the associated fault characteristics.  
277 The Noisy-Or modelling approach is used to calculate the CPT of the presented Bayesian network to  
278 overcome the limitation of the complicated node computations and data dependency in current  
279 approaches. The final implementation of the fault diagnosis expert system realizes the combination  
280 of expert experiences and Bayesian inferences. The obtained results allow to develop the time-based  
281 maintenance to the condition-based maintenance, which achieves the goal of the reduction of the  
282 maintenance costs in hydropower stations. In addition, historical data collected from a hydropower  
283 station is a good method to improve the accuracy of the diagnosis, while it is extremely difficult to  
284 obtain diagnosis from manufacturers since such data are confidential. To propel the future study of

285 historical data parameter learning or other data-based methods, we are attempting to cooperate with  
286 potential hydropower stations to carry out some experiments of the generating system. The above  
287 illustrations have been added to the manuscript to guide our future work. Moreover, the future work  
288 is designed to the extraction of the common fault characteristics to improve the coupling relationship  
289 of the electric faults with the mechanical hydraulic fault network.

290

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298

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426

427 **Graphical Abstract:** Global hydropower growth continues to accelerate with 25% of total  
428 capacity installed in just the last 10 years. This accelerating expansion and the important storage  
429 facility hydropower means it is increasingly important to understand the reasons for operational  
430 failures. Fault diagnosis of a hydroelectric generation system is a critical science and engineering  
431 problem to improve the safety of hydropower stations. To enable the risk quantification in the  
432 process of fault diagnosis, fault types and associated fault characteristics of a hydroelectric  
433 generation system are extensively analyzed to model a precise Bayesian Network. Noisy-Or  
434 modelling approach is used for the implementation of fault diagnosis expert system, which not only  
435 reduces the computation of nodes probability without severe information loss but also eliminate the  
436 data dependency. A typical application is proposed to fully show the capability of the presented  
437 methodology of the HGS's fault diagnosis. The graphical table is shown in Fig. 6.

438

439 **Fig. 6** General technical route of this paper.

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