In-beam gamma-ray and electron spectroscopy of ^{249,251}Md

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The odd-Z ^{251}Md nucleus was studied using combined gamma-ray and conversion-electron in-beam spectroscopy. Besides the previously observed rotational band based on the [521]1/2$^-$ configuration, a new rotational structure has been identified using gamma-gamma coincidences. The use of electron spectroscopy allowed the rotational bands to be observed over a larger rotational frequency range. Using the transition intensities that depend on the gyromagnetic factor, a [514]7/2$^-$ single-particle configuration has been inferred for the new band, i.e. the ground-state band. A physical background that dominates the electron spectrum with an intensity of $\simeq 60\%$ was well reproduced by simulating a set of unresolved excited bands. Moreover, a detailed analysis of the intensity profile as a function of the angular momentum provided a new method for deriving the orbital gyromagnetic factor, namely $g_K = 0.69^{+0.19}_{-0.16}$ for the ground-state band. The odd-Z ^{249}Md was studied using gamma-ray in-beam spectroscopy. Evidence for octupole correlations resulting from the mixing of the $\Delta l = \Delta j = 3$ [521]3/2$^-$ and [633]7/2$^+$ Nilsson orbitals were found in both ^{249,251}Md. A surprising similarity of the ^{251}Md ground-state band transition energies with those of the excited band of ^{255}Lr has been discussed in terms of identical bands. New Skyrme-Hartree-Fock-Bogoliubov calculations were performed to investigate the origin of the similarity between these bands.

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I. INTRODUCTION

Despite significant and steady advances in the synthesis of the heaviest elements, reaching the predicted superheavy island of stability is still a distant objective, due to the ever-decreasing cross-sections. Nevertheless, nuclear spectroscopy, mass measurements and laser spectroscopy of the heaviest nuclei have shown their effectiveness by providing information on the quantum nature of extreme mass nuclei [1–5], without which the nuclei would no longer be bound beyond $Z \simeq 104$. On the theoretical side, the island of enhanced stability has been predicted either around the proton number Z=114, 120 or 126 and neutron number N =172 or 184 [6–10]. The validity of these predictions in a region where the models are extrapolated is hence questionable, as is the concept of magic numbers in this region [11]. It is therefore essential to compare predictions to comprehensive, reliable and relevant spectroscopic data, in particular for deformed mid-shell nuclei where a large diversity of orbitals are accessible, some of which are involved in the structure of

heavier spherical nuclei, i.e. placed just above and below the predicted super-heavy spherical shell gaps.

The present study of the odd-Z ^{249,251}Md nuclei is an integral part of this approach by providing new inputs in terms of both proton single-particle and collective properties. We report on the previously unobserved ground-state (g.s.) band of ^{251}Md, assign its single-particle configuration and deduce the gyromagnetic factor. We also discuss the most intense transition observed in ^{251}Md using both γ-ray and conversion-electron spectroscopy, and in ^{249}Md using γ-ray spectroscopy alone, as being compatible with octupole correlations. Finally, a comparison of ^{251}Md with the ^{255}Lr nucleus revealed unexpected similarities between transition energies. The mechanism leading to these identical bands has been tested with new Hartree-Fock-Bogoliubov (HFB) calculations using a Skyrme functional and several parametrizations of pairing correlations.

II. EXPERIMENTAL DETAILS

The experiments were performed at the Accelerator Laboratory of the University of Jyväskylä. The ^{251}Md nuclei were populated using the fusion-evaporation reaction ^{205}Tl(^{48}Ca,2n)^{251}Md. The ^{48}Ca beam was provided at 218 MeV resulting in an energy at the middle of target of 214 MeV, at which the fusion-evaporation cross section is about 760 nb [12]. An average beam intensity of $\approx$ 9 particle nA was delivered during $\approx$ 230 hours of data taking. The ^{205}Tl targets, 99.45 % enrichment, $\approx$ 300 μg/cm^2 thick, were sandwiched between a C backing of 20 μg/cm^2 and a C protection layer of 10 μg/cm^2.

The ^{251}Md nuclei were separated from the beam and other unwanted products using the RITU gas-filled recoil separator [13, 14] operated at a He gas pressure of 0.4 mbar. Additional selection was made using the energy-loss ΔE and time-of-flight (ToF) measured with the GREAT focal plane spectrometer [15], ΔE being measured in a multi-wire proportional chamber (MWPC), and the ToF between the MWPC and a set of two Double-Sided Silicon Strip Detectors (DSSDs). The combined transmission and detection efficiency for the ^{251}Md residues was estimated at $\approx$ 30%. Formal identification using the characteristic α-decay (recoil-decay tagging) was not effective due to the low α-decay branching ratio of 9.5% for ^{251}Md [16]. Therefore only the recoil-tagging technique was used, which is adequate since only the reaction channel of interest is open. Gamma-rays and conversion-electrons emitted at the target position were detected using SAGE (Silicon And GErmanium) [17]: γ-rays were detected using Compton-suppressed HPGe detectors (20 coaxial and 24 clovers) having a total γ-ray photopeak efficiency of $\approx$ 10% at 200 keV, and an average energy resolution of 2.8 keV FWHM at 1 MeV. After being transported by a solenoid placed upstream the target and tilted 3.2° with respect to the beam axis, electrons were detected in a segmented Si detector, 1 mm thick.

The electron detection efficiency peaks at $\approx$ 6% for an energy of 120 keV with an average energy resolution of 6.5 keV FWHM in the 50-400 keV energy range. Low-energy atomic electrons were partly suppressed using an electrostatic barrier biased at -35 kV. Contour gates constraining SAGE time vs the ToF and SAGE time vs SAGE energy were used to clean the spectra. These gates were left wide enough to favour the statistics when using γ-γ coincidences (sections III A and IV). For an analysis that requires intensity measurement, the gates were tightened to favour cleanliness (sections III B and III C). This can lead however to a systematic error in the relative intensities of conversion-electrons versus γ-rays that was estimated at 20 %. The separation between the He gas and vacuum regions was made using two C windows, 50 μg/cm^2 thick, placed between the target and the electrostatic barrier. Digital signal processing was used for the SAGE array (100 MHz, 14 bits) while signals from the MWPC and the DSSDs were processed using standard analogue electronics and peak sensing ADCs.

The experimental conditions for the study of ^{249}Md were similar and are detailed in [18]. In brief, the nuclei of interest were produced using the fusion-evaporation reaction ^{203}Tl(^{48}Ca,2n)^{249}Md. The ^{203}Tl targets, 97.08 % enrichment, $\approx$ 280 μg/cm^2 thick, were sandwiched between a C backing of 20 μg/cm^2 and a C protection layer of 11 μg/cm^2. The ^{48}Ca beam was delivered at a beam energy of 219 MeV, resulting in an energy of $\simeq$ 215 MeV in the middle of the target. Data were taken during $\simeq$ 80 hours with a beam intensity of $\simeq$ 13 pnA. Only γ-rays were collected.

Data were handled using the triggerless Total Data Readout system [19] and sorted using the Grain software package [20]. The theoretical conversion coefficients were calculated using the BrIcc code [21].

III. ROTATIONAL BANDS IN ^{251}MD

A. Gamma-ray spectroscopy

The γ-ray singles spectrum resulting from the recoil-tagging technique is shown in Fig. 1(a). The previously observed rotational band structure, interpreted as being built on the proton Nilsson orbital [521]1/2$^-$ [12], is shown in Fig. 1(b). The spectrum was created from a sum of gates on the peaks of interest, projected from a matrix of recoil-gated γ-γ coincidences. Compared to the previous work, we cannot confirm the proposed transition at the highest rotation frequency with an energy of 483(1) keV for which only 6 counts were observed. We instead suggest a transition at 478(2) keV for which 8 counts were collected. There is also evidence for an additional transition with an energy of 513(1) keV ($\simeq$ 12 counts). A new structure with a γ-ray spacing of about half of the former has been found, therefore consistent with $\Delta I = 2$ E2 transitions within the two signature partners of a rotational structure (Fig. 1(c)). Despite

the low statistics, each transition resulting from the γ-γ analysis has been found in mutual coincidence with at least four other transitions in the same band. It should be noted that the transition at $\simeq 334$ keV is a doublet with the 335 keV transition of the $K^\pi = 1/2^-$ band. For the sake of clarity, a partial level scheme summarizing the results of this work is provided in Fig. 2.

The single-particle configurations considered in the following for the new band are those predicted at low energy by the macroscopic-microscopic models used in [22–24] and the self-consistent models used in this work (see section V B) as well as those observed by decay spectroscopy in the neighbouring Md isotopes [22, 25], which reduces the alternatives to the $[514]7/2^-$ ground-state and to the $[633]7/2^+$ single-particle configuration.
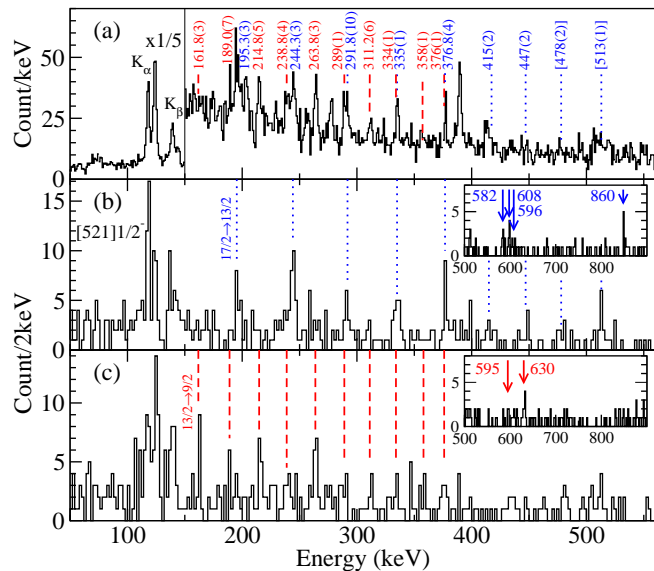

FIG. 1. (a) γ-ray spectra of ^{251}Md resulting from recoil-tagging. The spectra (b) and (c) were projected from a sum of gates on the peaks of interest using recoil-gated γ-γ coincidence data. The transitions in mutual coincidence are shown with dotted blue ($[521]1/2^-$) and dashed red (new band) lines.

Considering therefore a band-head angular momentum $I = K = 7/2$ for the new band, we can compare the experimental kinematic moment of inertia $\mathcal{J}^{(1)}$ calculated using different angular momenta $I_i \to I_f$ hypotheses for the transitions (or in other words the number of unobserved transitions), with the predictions of Chatillon *et al.* [12], He *et al.* [26] and Zhang *et al.* [27]. The best agreement has been obtained using $I_i = 13/2 \to 9/2$ for the transition at 161.8 keV. Extrapolating the $\mathcal{J}^{(1)}$ moment of inertia at lower rotational frequencies yields an energy of 133 keV for the unobserved $11/2 \to 7/2$ transition, and an energy of 61 keV for the $9/2 \to 7/2$ one. The latter is in perfect agreement with the decay spectroscopy of Asai *et al.* [3] which provides an energy of 62 keV for the first member of the $7/2^-$ rotational g.s. band.

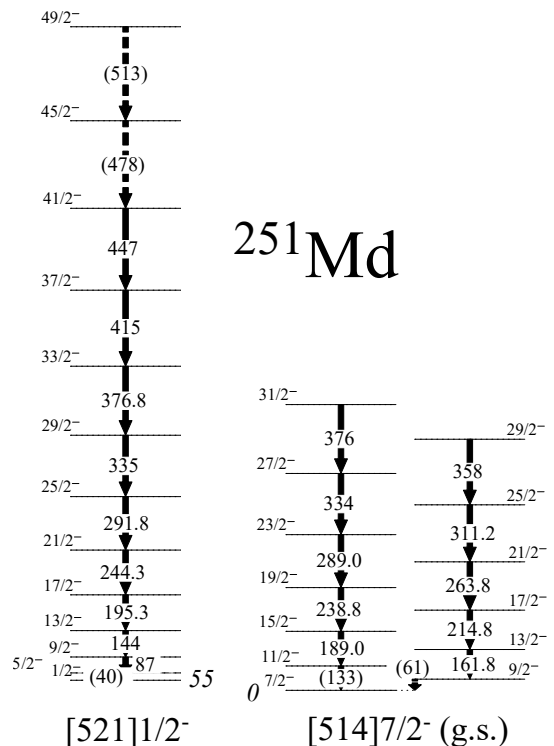As shown in the inset of Figs. 1(b) and (c), the two

FIG. 2. Partial level scheme of ^{251}Md resulting from this work. All spins and parities are tentative. The band-head energies are taken from [16].

rotational bands are in coincidence with γ-rays around 582, 596, 608 and 860 keV, 595 and 630 keV, respectively. Although there are other candidate peaks visible in this region, only those listed here produce coincidences with the rotational band. In the even-even actinide nuclei, transitions in this energy range are typically observed in the de-excitation of vibrational states, e.g. 2^- states in ^{246}Cm [28], ^{250}Fm [29] or ^{252}No [30]. Also, in the odd-proton ^{255}Lr, de-excitation of high-K rotational bands proceed via transition in this energy range [31]. However, in our case, coincidences did not allow us to make the link with a collective structure at higher energy.

B. Electron spectroscopy

Turning to in-beam conversion electron spectroscopy, the analysis was based only on the total recoil-gated spectrum due to the paucity of γ-electron coincidence data. The experimental spectrum shown in Fig. 3(a) was obtained by subtracting the random-correlated background using time gates before and after events in prompt coincidence. L and M components from the 195 (L,M195) and 244.7 keV (L244) transitions belonging to the $K^\pi = 1/2^-$ band are clearly apparent. Clearly visible are the L and M conversion lines of a transition at 144 keV, which fits well with the extrapolated energy for the $13/2^- \to 9/2^-$ $E2$ transition. The corresponding γ-ray overlaps with the $K\beta_2$ X-ray line, which explains why it cannot be

evidenced using γ-ray spectroscopy alone. The most intense transition at 389 keV will be discussed further in section IV.
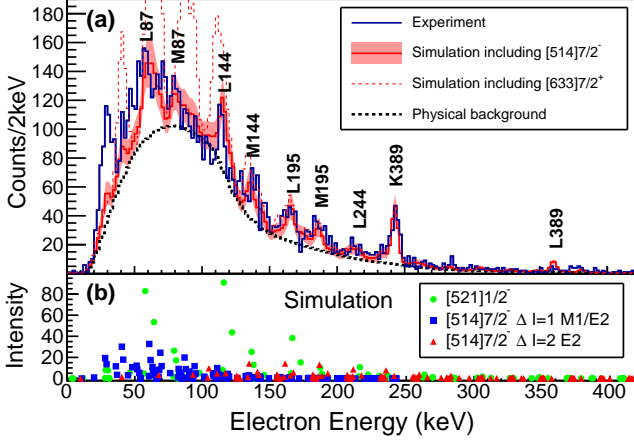

FIG. 3. (a) The experimental ^{251}Md electron spectrum (solid blue line) is compared to simulations including a physical background (dotted black line) and discrete peaks. The simulation (solid red line with the propagated uncertainties in shaded red) corresponds to the sum of the transition at 389 keV, the $K^\pi = 1/2^-$ band, the new rotational band using the [514]7/2$^-$ configuration and the physical background. A similar simulation assuming the [633]7/2$^+$ configuration for the new band is shown with a dashed red line. The peaks are labelled with the transition energies preceded by the electronic shell. (b) The simulated transition intensities corrected according to the experimental detection efficiency are shown with green circles for the $K^\pi = 1/2^-$ band. For the new band, $\Delta I = 1$ ($\Delta I = 2$) transitions are shown with blue squares (red triangles) assuming the [514]7/2$^-$ configuration.

We also observed peaks below 100 keV with no counterpart in the γ-ray spectrum. In order to fully understand the electron spectrum and possibly constrain the single-particle configurations, we have performed a simulation of the conversion-electron spectra. The ingredients for the $K^\pi = 1/2^-$ band were the experimental energies and intensities. The band was subsequently extrapolated at lower energies using a smooth moment of inertia resulting in transition energies of 87 keV ($9/2^- \to 5/2^-$) and 40 keV ($5/2^- \to 1/2^-$), the former being evidenced in the electron spectrum (Fig. 3(a)). These energies are strongly similar to those of bands based on the same single-particle configuration in the neighbouring ^{247}Bk and ^{251}Es [32]. The transition intensity within the band was deduced from the γ-ray spectra, corrected for the internal conversion, and assumed constant for the transitions at 40, 87 and 144 keV. The corresponding electron intensities, after taking into account the detector response, are shown with green circles in Fig. 3(b).

A different approach has been adopted for the new rotational band: in that case the transition intensities were simulated using the electromagnetic properties (electric quadrupole and magnetic dipole moments) as an input assuming either the [514]7/2$^-$ or [633]7/2$^+$ single-particle configuration. The rotational band was first extrapolated at higher angular momenta using a smooth moment of inertia. The total experimental intensity profile (converted plus radiative) as a function of the angular momentum, $N(I)$, was fitted using a Fermi distribution $N(I) = a/(1+\exp[(I-b)/c])$. This prescription provided the normalisation factor a, the average angular momentum entry point $b = 14\hbar$, and the diffuseness $c = 3\hbar$. It is interesting to note that the intensity profile inferred here corresponds remarkably well to that measured for ^{254}No at similar conditions of excitation energy and angular momentum for the compound nucleus [33]. The intensity of the stretched $E2$ and of the mixed $\Delta I = 1$ $E2/M1$ transitions connecting the two signature partner bands were subsequently calculated from the particle plus rotor model [34] using the reduced radiative transition probabilities $B(M1)$ and $B(E2)$:

$$B(M1) = \frac{3}{4\pi}\ (g_K - g_R)^2\ K^2 \langle I_i K 10 | I_f K \rangle^2\ [\mu_N^2], \quad (1)$$

$$B(E2) = \frac{5}{16\pi}\ e^2 Q_0^2 \langle I_i K 20 | I_f K \rangle^2\ [e^2\text{fm}^4], \qquad (2)$$

with $g_R \simeq Z/A$ being the rotational gyromagnetic factor, μ_N the Bohr magnetron, Q_0 the electric quadupole moment. The orbital gyromagnetic factor has been approximated as $g_K = (g_s\Sigma + g_l\Lambda)/K$, where $g_{s(l)}$ is the nucleon spin (orbital) gyromagnetic factor. For the protons we adopted $g_s = 5.59$ and $g_l = 1$. A reduction of the spin gyromagnetic factor $g_s^{\text{eff}} = 0.6 g_s^{\text{free}}$ was used, a value generally adopted for heavy nuclei. The relations above result in $g_K = 0.66$ and $g_K = 1.34$ for the [514]7/2$^-$ and [633]7/2$^+$ configurations, respectively. The transition rates, corrected for internal conversion and according to the intensity profile $N(I)$ were subsequently used to simulate the transition intensities along the rotational band.

The resulting simulated electron intensities for the [514]7/2$^-$ hypothesis are shown in Fig. 3(b) with red triangles for the stretched $E2$ transitions and with blue squares for $\Delta I = 1$ transitions. As a result, the electron spectrum is dominated by $\Delta I = 1$ transitions. The complexity of the spectrum is obvious along with a fragmented intensity pattern. However, the simulation of the new band essentially generates tails in the peaks of the $K^\pi = 1/2^-$ band. This is due to two factors: (i) most of the conversion-electron energies of the new band are often found close to some of the $K^\pi = 1/2^-$ band (ii) the intensity of the new band is lower than that of $K^\pi = 1/2^-$ band.

Experimentally resolving all peaks was not possible given the detector resolution and the collected statistics. The simulated intensity assuming the [633]7/2$^+$ configuration has similar features but with a larger contribution of $M1$ transitions (larger $|g_K - g_R|$ value). Since the total transition intensity was normalized from the γ-ray spectrum, the resulting electron intensities would exceed

those of the $[514]7/2^-$ case by a factor of ≈ 3, which is clearly not compatible with the measurement and this rules-out the $[633]7/2^+$ configuration.

After summing the $[521]1/2^-$ and $[514]7/2^-$ contributions, there is still a large background in the electron spectrum peaking at ≈ 80 keV. In Fig. 3(a) a simulation corresponding to a set of rotational bands with K and the moment of inertia randomly sampled is shown with a dotted black line. More precisely, each configuration has been chosen either as a proton 1qp excitation with $1/2 \leq K \leq 13/2$ or a single proton excitation coupled to a 2qp either proton or neutron having $0 \leq K_{2qp} \leq 8$ and anti-parallel spin coupling. The moment of inertia was randomly selected around the value measured for yrast or high-K rotational bands in the Fm-Lr region. We have arbitrarily taken a fraction of 50% proton 1qp excitations, 25% proton 3qp excitations and 25% 1qp proton $\otimes$ 2qp neutron configuration. As shown in Fig. 3(a), the spectrum resulting from this simulation reproduces the experimental background remarkably well, with the only adjusted parameter being its total intensity. It should be noted however that the shape of this physical background is largely independent on the assumptions discussed above. Conversely, it mainly results from a convolution of the electron detection efficiency and the internal conversion coefficients. No physics ingredients such as the angular momentum entry point, average gyromagnetic factor or average moment of inertia notably change the background shape. This background is however fully consistent with rotational bands unresolved experimentally, or from the continuum. Its intensity can be estimated at a level of 60% of the total ^{251}Md population. This conclusion is entirely consistent with those of Butler et $al.$ in the case of ^{254}No, for which an electron background has been well reproduced using a set of $K = 8$ rotational bands with 40% intensity [35]. The decay spectroscopy of ^{254}No unambiguously confirms the presence of a $K^\pi = 3^+$ 2qp state at about 1 MeV and of an isomeric $K^\pi = 8^-$ 2qp state at about 1.3 MeV [36–39], on top of which rotational bands were observed. It was shown in particular in [39] that the $K^\pi = 8^-$ isomeric state is fed with an intensity ratio of 28 (2) %. Thus, most of the unresolved background identified by Butler et $al.$ arises from the de-excitation of a band based on a high $K^\pi = 8^-$ state. Using in-beam γ-ray spectroscopy, a rotational band based on a $K^\pi = 8^-$ isomeric state was also observed in ^{250}Fm [29] and in ^{252}No [30], with an isomeric ratio of 37 (2) % [40] and $\simeq 30$ % [41], respectively. A similar situation is thus expected in odd-mass nuclei with the presence of high-K 3qp states. It should be noted that a high-K isomer has been recently evidenced in ^{251}Md [42]. It is therefore realistic to interpret the observed electron background in ^{251}Md as corresponding to several unresolved bands, built either on high-K 3qp states or on low-lying single-particle configurations such as $[633]7/2^+$ or $[521]3/2^-$. However, band intensities are expected to be more fragmented compared to even-even nuclei due to the presence of several single particle-states

at low excitation energy.

We have also simulated the γ-ray counterpart of this physical background, which, interestingly, also reproduces well the γ-ray background shape in the 150 - 600 keV energy range. With regard to X-rays, their intensity turns out to be very sensitive to K, as expected from the strong K dependence of the $B(M1)$ rates (Eq.(1)), but no definitive conclusion can be drawn from the present work.

Finally, the total simulated spectrum ($[521]1/2^-$ and $[514]7/2^-$ configurations, transition at 389 keV plus the physical background) is shown using a solid red line with the envelope corresponding to the uncertainty propagation (Fig. 3(a)). The global shape is well reproduced except at $\simeq 40$ keV, interpreted as the energy tail of delta electrons that were not cut by the electrostatic barrier nor by the electronic threshold. The same simulation assuming the $[633]7/2^+$ configuration is shown with a red dashed line for comparison, clearly overestimating the measured intensity and again ruling-out this configuration.

C. Intensity profile

The experimental intensity profile of stretched $E2$ transitions for the $K^\pi = 7/2^-$ g.s. band is shown in Fig. 4. The intensities were taken from the γ-rays in the 189.2 keV ($I_i = 15/2$) to 311.3 keV ($I_i = 25/2$) range, corrected from the internal conversion. Only statistical uncertainties were considered here since a systematic error would simply scale the distribution. Although associated with large error bars, oscillations around $I_i = 21/2$ are clearly visible. The intensity profile resulting from the band simulation discussed above for a gyromagnetic factor $g_K = 0.66$ is shown with blue squares.

This simulated profile reproduces the experimental data remarkably well, notably the oscillations and an intensity jump between the states with $I_i = 23/2$ and $21/2$. Below $I_i = 23/2$, the $\Delta I = 1$ transition energies are lower than the K electron binding energy (145.6 keV) while they are higher above. This change results in a sharp decrease of the $M1$ internal conversion coefficient by a factor of $\simeq 5$ and consequently in a lowering of the $\Delta I = 1$ transition rate below $I_i = 23/2$. The other impact is an increased stretched $E2$ transition rate below $I_i = 23/2$, clearly visible in the simulation and evidenced in the experimental data. For comparison, the intensity profile assuming the $[633]7/2^+$ configuration ($g_K = 1.34$) is shown with green triangles. Although the jump is still present at the same angular momentum, the intensity profile departs significantly.

The gyromagnetic factor g_K can be deduced using the likelihood estimator, its logarithm being plotted in the inset of figure 4. More precisely, the intensity profile was simulated for different g_K values and compared to the experimental data using the estimator. The curve allowed us to deduce the most likely gyromagnetic factor
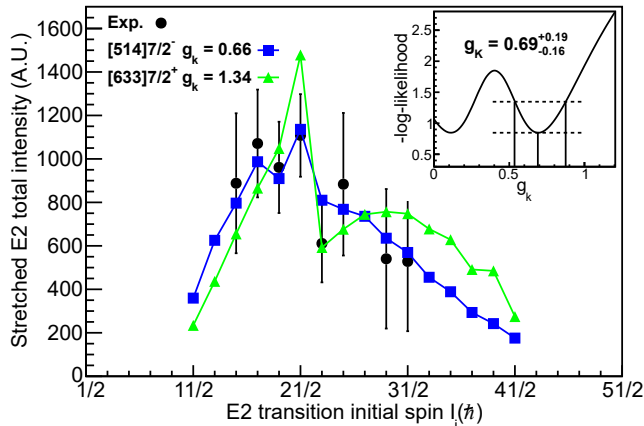
FIG. 4. The experimental intensity profile for the $K = 7/2$ band as a function of the angular momentum, shown with black dots, is compared to the band simulation assuming either a gyromagnetic factor of $g_K = 0.66$ (blue squares) or $g_K = 1.34$ (green triangles). The experimental gyromagnetic factor was deduced using the likelihood estimator, -log-likelihood being plotted in the inset.

$g_K = 0.69^{+0.19}_{-0.16}$, which is in remarkable agreement with the value $g_K = 0.66$ estimated above using the particle-plus-rotor model. It should be noted that the likelihood estimator is symmetric with respect to $g_R = Z/A$ therefore the value $g_K = 0.11$ is still possible, but not favoured since it does not correspond to any expected single-particle configuration at low excitation energy.

IV. EVIDENCE FOR OCTUPOLE CORRELATIONS IN ^{249,251}MD

The most intense ^{251}Md peak in both γ-ray and conversion-electron spectra corresponds to a transition at 389 keV. Although this transition collects about 16 % of the de-excitation flow (compared to $\simeq 10\%$ and $\simeq 12\%$ for the $K^\pi = 1/2^-$ and $K^\pi = 7/2^-$ band, respectively), no coincident transition has been observed with a sufficient confidence level. Its experimental conversion coefficient $\alpha_K = 1.84 \pm 0.3(\text{stat}) \pm 0.4(\text{syst})$ is, within the uncertainties, only compatible with an $M2$ multipolarity as shown in Table I. We also extracted a L-shell conversion coefficient $\alpha_L = 0.75 \pm 0.2(\text{stat}) \pm 0.2(\text{syst})$. This value can be considered as an upper limit since the region of the L conversion is not background free. However, α_L is again compatible with an $M2$ multipolarity.

An $M2$ transition of pure single-particle character would have a half-life of ≈ 23 ns therefore out of the view of the SAGE γ-ray detection. A rate enhancement is however possible if the initial and final states are coupled via a 2^- octupole phonon. Several examples of octupole-vibration coupling have been observed in the actinide region. First examples were reported in the ^{246,248}Cm and ^{248,249}Cf by Yates *et al.* using transfer reactions [43, 44].

A more recent example has been provided in ^{251}Fm [45].

The occurrence of octupole correlations arise when orbitals with $\Delta l = \Delta j = 3$ are close in energy. In the $Z \sim 100, N \sim 152$ region, this is realised on the neutron side for the $\{[512]5/2^+(g_{9/2}), [734]9/2^-(j_{15/2})\}$ orbits. For the protons the pair candidates are $\{[512]5/2^-(f_{7/2}), [624]9/2^+(i_{13/2})\}$ and $\{[521]3/2^-(f_{7/2}), [633]7/2^+(i_{13/2})\}$; all these pairs favour a $K^\pi = 2^-$ octupole phonon as the lowest collective excitation. Although the $[521]3/2^-$, $[512]5/2^-$ and $[633]7/2^+$ orbitals have not yet been observed in ^{251}Md, the second pair is a better candidate since both orbitals have been predicted at lower energy compared to the first pair [16, 24]. In that case, the $3/2^-$ state would have a $[633]7/2^+ \otimes 2^-$ component and therefore pushed-down compared to pure single-particle predictions.

The 389 keV transition can be hence tentatively assigned to a $3/2^- \to 7/2^+$ transition that could be, because of the coupling with an octupole phonon, of mixed $E3/M2$ character. We calculated the δ^2 mixing ratio for a $E3/M2$ transition using

$$\delta^2(E3/M2) = \frac{T_\gamma(E3)}{T_\gamma(M2)} = \frac{\alpha_K(M2) - \alpha_K(\text{Exp.})}{\alpha_K(\text{Exp.}) - \alpha_K(E3)}. \quad (3)$$

Because of the large experimental uncertainties, our measurement is compatible with no mixing. However an upper limit, within one sigma, of $\delta^2(E3/M2) \leq 0.35$ can be provided, which would nevertheless leave the possibility of a substantial $E3$ component.

Interestingly, a transition at 387 keV has been evidenced in the neighbouring ^{249}Md as shown in Fig. 5. This transition is the most intense in the recoil-tagged spectrum apart from a contamination of ^{203}Tl Coulex (a); its intensity decreases using γ-γ coincidences (b), consistent with only few radiative transitions in coincidences as in ^{251}Md, and finally the transition is still present when tagging on the ^{249}Md α decay (c). The energy and characteristics similar to ^{251}Md suggests a transition of similar nature in both isotopes. This is consistent with the fact that several calculations predict a very similar single-particle structure of ^{249}Md and ^{251}Md [16, 23, 24].

V. COMPARISON OF ^{251}MD WITH ^{255}LR

A. Similarity of transition energies: a possible case of identical bands

An unexpected feature of the $K^\pi = 7/2^-$ g.s. rotational band of ^{251}Md is its resemblance to the excited band of ^{255}Lr [46], both based on the $[514]7/2^-$ orbital. The transition energies are indeed identical within the uncertainties up to $I_i = 23/2$, beyond which the difference slowly increases (Table II [1]). On the other hand,

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[1] It should be noted that no spins were suggested for the transitions in [46]. The spins proposed in the evaluation [47] should be

TABLE I. Internal conversion coefficient for a transition proceeding via K or L atomic shell with an energy of 389 keV. The theoretical coefficients [21] for $E1$, $M1$, $E2$, $M3$, $E3$, $M3$ multipolarities are compared to the experimental value.

	$E1$	$M1$	$E2$	$M2$	$E3$	$M3$	Exp.
α_K	$2.266\ 10^{-2}$	$8.476\ 10^{-1}$	$5.906\ 10^{-2}$	1.496	$1.465\ 10^{-1}$	3.551	$1.84 \pm 0.3 \pm 0.4$
α_L	$4.813\ 10^{-3}$	$1.851\ 10^{-1}$	$6.846\ 10^{-2}$	$6.594\ 10^{-1}$	$5.037\ 10^{-1}$	2.337	$0.75 \pm 0.2 \pm 0.2$
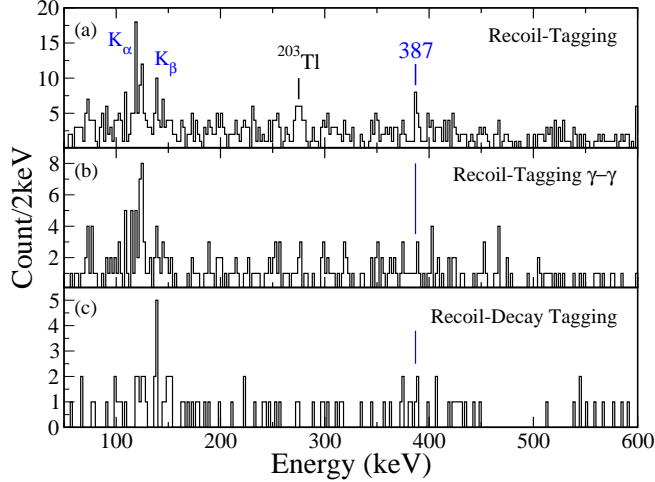
FIG. 5. Gamma-ray spectra of ^{249}Md resulting from (a) recoil-tagging, (b) sum of γ-γ recoil-tagged coincidences, (c) recoil-decay tagging using a maximum correlation time of 200 s between the recoil implantation and the subsequent α decay. It should be noted that the statistics was not sufficient to establish rotational structures on a solid basis.

TABLE II. Rotational band transition energies (keV) and initial angular momentum I_i for ^{251}Md (this work) and ^{255}Lr [46]. Tentative transitions are written in brackets.

| | $[514]7/2^-$ | | | $[521]1/2^-$ | |
$I_i(\hbar)$	^{251}Md	^{255}Lr	$I_i(\hbar)$	^{251}Md	^{255}Lr
13/2	161.8 (3)		9/2	[87]	
15/2	189.0 (7)	189 (1)	13/2	144 (1)	
17/2	214.8 (5)	215 (1)	17/2	195.3 (3)	196.6 (5)
19/2	238.8 (4)	239 (1)	21/2	244.3 (3)	247.2 (5)
21/2	263.8 (3)	264.6 (5)	25/2	291.8 (10)	296.2 (5)
23/2	289 (1)	288.4 (5)	29/2	335 (1)	342.9 (5)
25/2	311.2 (6)	314.0 (5)	33/2	376.8 (4)	387 (1)
27/2	334 (1)	338 (1)	37/2	415 (2)	430 (1)
29/2	358 (1)	359 (1)	41/2	447 (2)	
31/2	376 (1)	384 (1)	45/2	[478 (2)]	
33/2			49/2	[513 (1)]	

rotational bands based on the $[521]1/2^-$ configuration do not exhibit similarities at such a level of precision. Such a phenomenon of identical rotational bands (IBs) was first observed in a pair of superdeformed bands (SD) of ^{151}Tb (first excited band) and ^{152}Dy (yrast band) [48], later confirmed in numerous cases and turned out to be emblematic of SD bands. The phenomenon of IBs has also been observed at intermediate and normal deformations, with bands having a variable degree of similarity, and sometimes with IBs for nuclei that differ substantially in mass ([49] and references therein).

It is worth reminding that, at moderate deformation, the classical moment of inertia of a rigid homogeneous body is proportional to $A^{5/3}(1 + 0.31\beta)$ [50]. Phrased differently, the transition energies of such rotating rigid bodies scale with $A^{-5/3}$ for the same deformation. Therefore, for the ^{251}Md-^{255}Lr pair, an energy difference of $\simeq$ 3% between the transition energies of the two bands is expected in such a purely macroscopic framework, significantly higher than the observation. For the pair of bands based on the $7/2^-$ single-particle state, 5 transitions are identical within one keV, which could be con-

sidered as not very impressive at first sight compared to e.g. the phenomenon in SD bands. As we will discuss in the following, this case turns out to be however unique in the transuranium region. It is also interesting to note that the transition energies for the $K^\pi = 1/2^-$ band are larger in ^{255}Lr than in ^{251}Md, while the opposite effect is expected according to the $A^{-5/3}$ scaling of rotational energies at fixed angular momentum and deformation.

Numerous mechanisms have been advocated to explain the IB phenomenon such as (i) the spin alignment of specific orbitals along the rotation axis in the strong coupling limit of the particle-rotor model, (ii) the role of symmetries and in particular the pseudo-SU(3) scheme, (iii) the role of orbitals not sensitive to the rotation in particular those having a high density in the equatorial plane (low number of nodes n_z in the plane perpendicular to the symmetry axis), (iv) the role of time-odd terms, etc.: see [49] and references therein. None of them were fully satisfactory since they were neither predictive nor capable of identifying the underlying mechanism. Some global analyses using mean-field approaches suggest that the mechanism is not as simple as a quantum alignment or purely related to single-particle properties, but results from a cancellation of several contributions (deformation, mass, pairing), resulting in the identical bands (e.g. [51–54]).

Identical bands were previously reported in even-even transuranium nuclei [55]: the 3 or 4 first ground-state band transitions in ^{240}Pu, ^{244,246}Cm, ^{250}Cf are identical within 2 keV. The more recent improved spectroscopy of ^{240}Pu [56], ^{246}Cm and ^{250}Cf [57] has shown that the transitions energies deviate significantly above $I_f = 8$. More

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excluded since the lowest unobserved transitions, because highly converted, were ignored in the evaluated level scheme.

impressive are the ground-state bands of ^{236,238}U that are identical up to spin $I_f = 22^+$ within 2 keV [55]. In this reference, this has been interpreted in this region of mid-shell nuclei as the filling of orbitals driving small deformation changes that counteract the mass dependence. In any event, even if these bands cannot all be qualified as being identical, these cases recall that the systematics of moments of inertia can locally deviate very strongly from the overall scaling with $A^{5/3}$ [50].

To establish whether other identical bands are present in the transuranium region, we have inspected all bands having at least 8 measured transitions, which represent 30 cases in even-even nuclei and 29 bands in odd-N or -Z nuclei (odd-odd nuclei were not considered). The data were taken from the Evaluated Nuclear Structure Data File (ENSDF) and from more recent publications or unpublished works [40, 57, 58]. This survey revealed two other even-even pairs that are identical within 2 keV for the four lowest spin transitions: they are respectively ^{236}Pu and ^{242}Pu, and ^{250}Fm and ^{254}No. The equality of the transitions is however verified over few transitions only. We also mention the case of the (^{246}Pu-^{252}No) pair whose transition energies are identical within 2 keV up to $I_f = 6$. This case can be hardly explained as these nuclei differ by 8 protons and 2 neutrons, and may be considered as an accidental degeneracy. It is worth mentioning that the general trend of the 2^+ collective state in the $N = 152$, $Z = 100$ region can be well explained by a change of the moment of inertia because of a reduction/increase in pairing correlations when approaching/leaving the deformed shell gaps (see the discussion in e.g. [2]). Several nuclei, however, deviate from this trend (in particular the Cf isotopes). No explanation that would convincingly explain all cases has been found so far. Also, octupole correlations have been evidenced in the $^{240-244}$Pu [56, 59] isotopes. Clearly beyond-mean field effects have to be taken into account in that case. Except the ^{251}Md-^{255}Lr pair, we have not identified other cases of odd-mass nuclei having identical transitions between them, or having identical transitions with one of their neighbouring even-even nuclei.

An intriguing fact in the IBs discussed here is that the nuclei differ by four mass units, more precisely an alpha particle. In the rare-earth region, an alpha chain of even-even nuclei with bands identical up to $I_f = 12$ has been identified: ^{156}Dy, ^{160}Er, ^{164}Yb, ^{168}Hf, ^{180}Os (and ^{172}W to a lesser extent) [60]. An interpretation based on the algebraic interacting boson model was proposed in the same reference. The quadrupole moment is linked to the $N_p N_n$ product, N_p (N_n) being the number of valence protons (neutrons) with respect to the nearest magic shell. This product is similar for all these nuclei and moreover in the language of the interacting boson model, these nuclei form a F-spin multiplet having the same number of valence particles $N_p + N_n$, i.e. they are predicted to have a similar structure. However, the major drawback of this approach is that it over-predicts the occurrence of identical bands. Deficiencies to reproduce the gyromagnetic

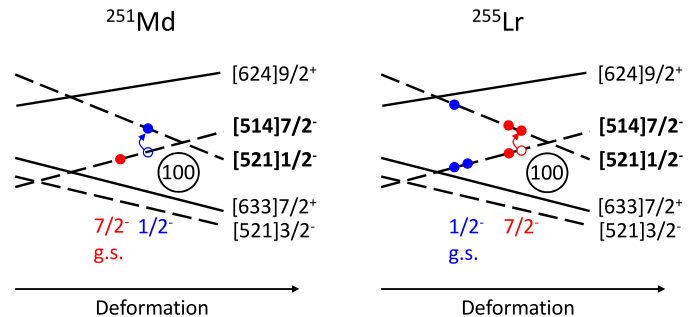factor for these nuclei have also been noticed [61].

FIG. 6. Schematic proton Nilsson diagram for ^{251}Md and ^{255}Lr inspired from calculations using a Woods-Saxon potential (see e.g. [62]).

The nuclear structure and deformation can be expected to change when filling deformation-driving orbitals (either down- or up- sloping as a function of the deformation driving the nucleus toward larger or lower deformation, respectively). In this respect, is interesting to note that because of the sequential filling of proton levels, the ground-state and the first excited state configuration of ^{251}Md vs ^{255}Lr are interchanged. Depending on its characteristics, the additional occupied pair of orbits in ^{255}Lr can lead to subtle deformation changes between the two nuclei, see Fig. 6.

In the ground state of ^{251}Md, one level out of the pair of up-sloping [514]7/2$^-$ orbitals is filled, while in ^{255}Lr the 7/2$^-$ state corresponds to the same configuration plus a pair of filled [521]1/2$^-$ down-sloping orbitals, the latter driving the nucleus towards slightly larger deformations. The deformation-driving effect in ^{255}Lr for this configuration goes therefore in the same direction as the overall $A^{5/3}$ macroscopic dependence of the rigid moment of inertia. The filling of orbitals as such can therefore not explain the experimental finding of identical 7/2$^-$ bands, quite on the contrary: based on this simple argument the two bands should be even more different than can be expected from the global scaling of moments of inertia. On the other hand, the [514]7/2$^-$ pair is filled for the 1/2$^-$ ^{255}Lr ground state, therefore driving the nucleus towards a lower deformation compared to the ^{251}Md 1/2$^-$ excited state, which goes in the opposite direction as the $A^{5/3}$ trend: a mechanism consistent with identical bands for the [521]1/2$^-$ configuration, again in contradiction with the experimental finding.

Furthermore there is a pair of neutron orbits that is filled to pass from ^{251}Md to ^{255}Lr, namely in the [734]9/2$^-$ Nilsson orbital. According to calculations using a Woods-Saxon potential (see e.g. [62]) or calculations presented below (see the self-consistent Nilsson diagram Fig. 8), this level is not sloping around the ground-state deformation, which justifies ignoring neutron levels at the present level of discussion.

There is also the experimental observation to consider

that the transition energies for the $K^\pi = 1/2^-$ bands change in the opposite direction to that expected from the $A^{-5/3}$ scaling. Moreover from a purely macroscopic point of view, the deformation of ^{255}Lr should decrease from $\beta \simeq 0.3$ to $\simeq 0.21$ to compensate for the mass difference ($A^{5/3}$ term) and lead to the same energies as ^{251}Md. Therefore the mass-deformation compensation mechanism discussed above does not have the correct order of magnitude since only small deformation changes are expected, and cannot explain simultaneously the larger transition energies for the $K^\pi = 1/2^-$ ^{255}Lr band and IBs for the $K^\pi = 7/2^-$ bands, unless one assumes that there is an additional mechanism that decreases the moment of inertia in ^{255}Lr. If the mechanism is the same for both configurations, then it just has the right size for the $7/2^-$ bands to make them identical, but "overshoots" for the $1/2^-$ bands.

The mass-deformation compensation mechanism resulting from the filling of levels is therefore unable to explain the experimental findings. There clearly have to be additional compensation effects, for example from changes in pairing correlations or the alignment of single-particle states as proposed in [51, 55, 63–65] for the observation of identical bands found for pairs of rare-earth nuclei.

In this respect, it is interesting to note that the ^{251}Md and ^{255}Lr nuclei are the neighbours of ^{250}Fm and ^{254}No respectively with one additional proton. As already mentioned, the yrast bands of these two even-even nuclei are also identical for the first four transitions. For the same reasons discussed above for the case of ^{251}Md and ^{255}Lr, the mass-deformation compensation mechanism can also not explain the similarity between the yrast band of ^{250}Fm and ^{254}No. With ^{250}Fm being proton magic deformed and ^{254}No neutron magic deformed, a simple explanation of the change in moment of inertia in terms of a change in pairing correlations is also not straightforward. The rotational $K^\pi = 1/2^-$ bands of ^{251}Md and ^{255}Lr can be phenomenologically described by the coupling of a proton in the $K^\pi = 1/2^-$ orbit to the ground-state band of ^{250}Fm and ^{254}No, respectively. In the most basic version of such model [50], one automatically obtains identical $K^\pi = 1/2^-$ bands in ^{251}Md and ^{255}Lr as well. This is however not observed, indicating that there are additional changes that are not the same when passing from ^{250}Fm to ^{251}Md and from ^{254}No to ^{255}Lr, respectively. For the $K^\pi = 7/2^-$ bands the situation is even more complicated since for ^{251}Md the $K^\pi = 7/2^-$ band could be interpreted as a proton in the $K^\pi = 7/2^-$ orbit coupled to the ground-state band of ^{250}Fm, whereas for ^{255}Lr the $K^\pi = 7/2^-$ band corresponds a 2p-1h excitation relative to the ground-state band of ^{254}No.

B. Self-consistent mean-field analysis

To better understand the conditions for the emergence of identical bands for the nuclei studied here, we performed microscopic cranked self-consistent-mean-field calculations for the $K^\pi = 1/2^-$ and $K^\pi = 7/2^-$ bands in ^{249}Md, ^{251}Md, and ^{255}Lr. The calculations were made with the coordinate-space solver MOCCa [66, 67] that is based on the same principles as the code used for the Skyrme-HFB calculations reported in [10, 12, 16, 46]. We employ the recent SLy5s1 parameterization of the Skyrme energy density functional (EDF) [68] that was adjusted along similar lines as the widely-used SLy4 parameterization [69] used in those references, but with a few differences in detail, the most important one being a constraint on the surface energy coefficient that leads to a much better description of fission barriers of heavy nuclei [70]. As pairing interaction we choose a so-called "surface pairing" with cutoffs as defined in [71].

It turns out that, for a given Skyrme interaction, the similarity of in-band γ-ray energies for different nuclei depends very sensitively on choices made for the treatment of pairing correlations. To illustrate this finding, four different options will be compared. The first one is the HFB + Lipkin-Nogami (HFB+LN) scheme as defined in [71] with a pairing strength of $-1250\,\mathrm{MeV\,fm^3}$ for protons and neutrons that was adjusted to describe superdeformed rotational bands in the neutron-deficient Pb region. This prescription has also been used in [12, 16, 46]. The second option is a HFB+LN scheme with a reduced pairing strength of $-1014\,\mathrm{MeV\,fm^3}$ that was adjusted to reproduce the kinematic moment of inertia of ^{252}Fm at low spin when used with SLy5s1 [72]. While the LN scheme is a popular prescription to avoid the breakdown of HFB pairing correlations in the weak-pairing limit, it is known to have some conceptual problems, the most prominent one not being variational. As an alternative, Erler *et al.* [73] proposed a small modification that can be applied to any pairing interaction and that prevents the breakdown of pairing when being inserted into a standard HFB calculation. Their fully variational stabilized HFB scheme was used as a third pairing option, again with a surface pairing interaction of strength $-1250\,\mathrm{MeV\,fm^3}$. As the fourth option we use the standard HFB scheme as the most basic reference case, again with a pairing strength of $-1250\,\mathrm{MeV\,fm^3}$.

For the further discussion it is important to recall that SLy5s1 does not reproduce the empirical deformed shell closures at $Z = 100$ and $N = 152$ [2–4], a property that it shares with SLy4 and almost all other available nuclear EDFs that have been applied to the spectroscopy of very heavy nuclei so far [10, 74]. Instead, SLy5s1 gives prominent deformed proton gaps at $Z = 98$ and $Z = 104$, and an additional deformed neutron gap at $N = 150$, see Figs. 7 and 8. For the Md and Lr isotopes discussed here, the Fermi energy is in the direct vicinity of these shell closures, which has some influence on the calculated properties of their rotational bands.

Independent on the pairing option chosen, we find a calculated $1/2^-$ ground state for ^{249}Md and ^{251}Md, but a $7/2^-$ ground state for ^{255}Lr. In each case, the other state is a low-lying excitation at less than 160 keV. This
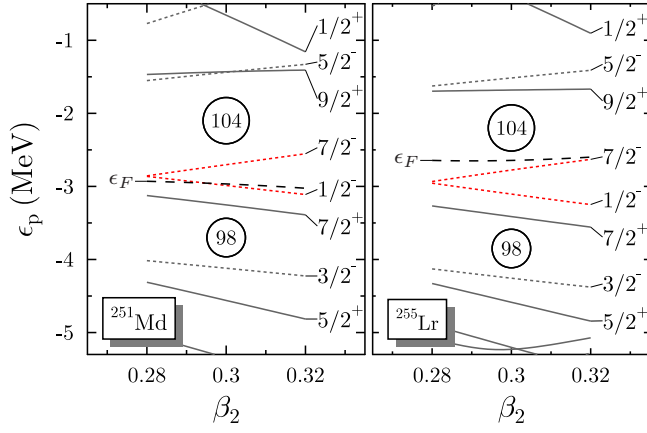
FIG. 7. Nilsson diagram of proton single-particle levels around the Fermi energy for mass quadrupole deformations β_2 as defined in [70] around those of the ground state for false vacua of ^{251}Md and ^{255}Lr, calculated with SLy5s1 and stabilized HFB pairing. The $K^\pi = 1/2^-$ and $K^\pi = 7/2^-$ levels are highlighted in color. The Fermi energy ϵ_F is indicated by a dashed line in each panel.
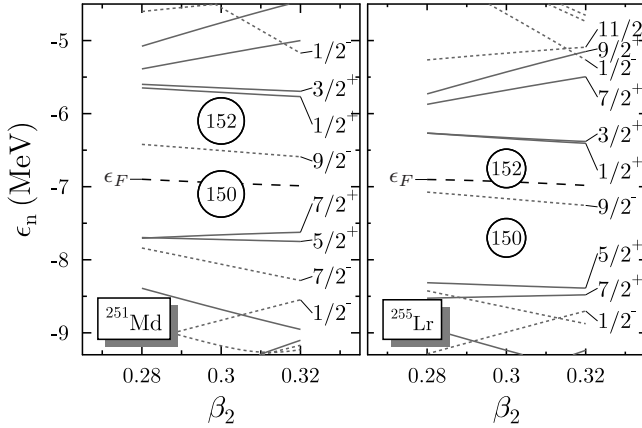

FIG. 8. Same as Fig. 7, but for neutrons

result is at variance with experimental data, for which the relative order of these levels is the other way round [16]. This finding is intimately connected to the incorrect deformed gaps found in the Nilsson diagram of Fig. 7: in order to obtain the correct level sequence, the $K^\pi = 1/2^-$ level has to be pushed up relative to the other levels such that it is above the $K^\pi = 7/2^-$ level at all relevant deformations. This would open up a gap at $Z = 100$ and significantly reduce the $Z = 104$ gap, see the detailed discussion of this point in [16]. Similar problems for the relative position of these two levels were found for virtually all widely-used nuclear EDFs [10, 74]. It is noteworthy that the UNIDEF1$^{\rm SO}$ parametrisation of [75] for which the spin-orbit interaction has been fine-tuned to give deformed $Z = 100$ and $N = 152$ shell gaps does not improve on the relative position of these two levels.

In addition, it predicts that the $9/2^+[624]$ level is nearly degenerate with them, which is difficult to reconcile with the systematics of band heads in this region.

The Nilsson diagrams of Figs. 7 and 8 have been calculated for false vacua, meaning fully paired HFB states that have the correct odd particle number on average. It is noteworthy that the relative positions of many neutron and proton levels visibly change when going from ^{251}Md to ^{255}Lr: filling a further pair of neutron and proton orbits changes all other levels through self-consistency. Such self-consistent rearrangement of deformed shells seems to be a general feature of heavy deformed nuclei when calculated within self-consistent models [74].
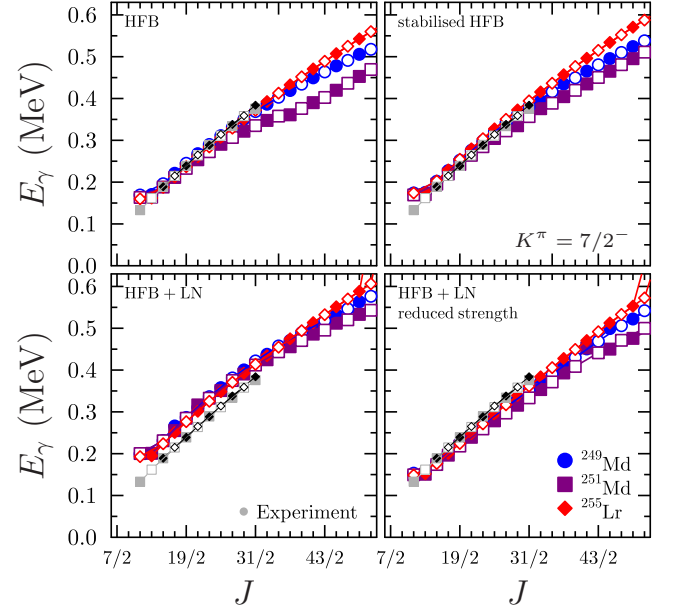

FIG. 9. γ-ray energies for $E2$ transitions in the $K^\pi = 7/2^-$ band calculated with SLy5s1 and the pairing options for the three nuclei as indicated. Calculated values are plotted in colour as indicated, whereas experimental values are plotted with smaller grey and black symbols for ^{251}Md and ^{255}Lr, respectively. Full symbols indicate transitions in the favored band, open symbols transitions in the non-favored band.

The rotational levels in each band have been constructed by solving the cranked HFB equations with a constraint on the collective angular momentum $I_z = \langle \hat{J}_z \rangle$ such that $J(J+1) = I_z^2 + K^2$, with K held fixed at $7/2$ or $1/2$, respectively. Note that K refers to the long axis of the nucleus that is perpendicular to the axis of collective rotation. In that case K is associated with the expectation value of the x component of the alignment vector D_x as defined in the appendix of Ref. [76]. This prescription to relate I_z and J is not the only possible choice [77], and others will lead to slightly different values for γ-ray energies. It also constitutes an approximation, as in a self-consistent calculation the value of K of the blocked quasiparticle cannot be held fixed at some half-integer value, and can also differ slightly from the many-body

expectation value of the same operator.

The odd particle can be put either into the orbit with $+K$ or $-K$, which leads to two different solutions of the HFB equations that we identify with the states in the two signature-partner bands that can be observed experimentally. For each band, the blocked quasiparticle state was selected such that the intrinsic state has the correct eigenvalue of the signature operator $\hat{R}_z = \exp(-i\pi\hat{J}_z)$ for a given total angular momentum J [77]. With increasing spin I_z, this leads to a signature splitting between the two calculated partner bands into an energetically favored and non-favored band, where for near-axial systems, such as those discussed here the band with the $J = K$ band head is the lower one. For the calculated and observed $K^\pi = 7/2^-$ bands the signature splitting is too small to be resolved on the plots. For the calculated $K^\pi = 1/2^-$ band, however, it is quite substantial. As there are no experimental data for the non-favored $K^\pi = 1/2^-$ band, we will not discuss its properties here.
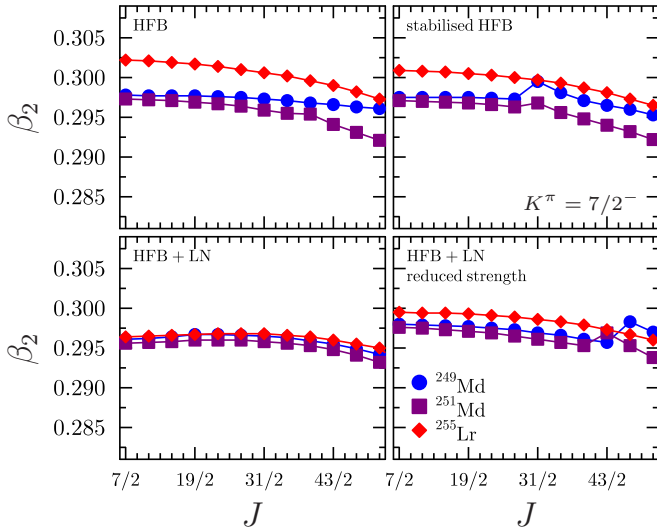

FIG. 10. Dimensionless mass quadrupole deformation β_2 of states obtained when blocking the favored orbit for the $K^\pi = 7/2^-$ band, calculated with SLy5s1 and the pairing options for the three nuclei as indicated.

The resulting γ-ray energies for $E2$ transitions in the two $K^\pi = 7/2^-$ bands are displayed in Fig. 9. It is immediately visible that the calculated energies depend significantly on the pairing option. To understand the origin of the differences between pairing options and nuclei, Fig. 10 displays the corresponding dimensionless mass quadrupole deformation

$$\beta_2 = \frac{4\pi}{3R^2 A}\sqrt{\frac{5}{16\pi}}\,Q_0\,, \qquad (4)$$

where $R \equiv 1.2\,A^{1/3}$, and Fig. 11 the corresponding dispersion of particle number $\langle(\Delta N)^2\rangle = \langle N^2\rangle - \langle N\rangle^2$. The latter is a measure for the amount of pairing correlations.
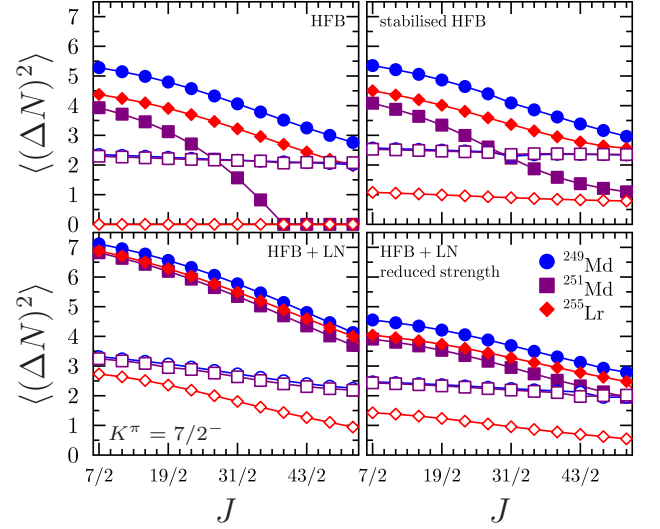

FIG. 11. Dispersion of neutron number (filled symbols) and proton number (open symbols) of states obtained when blocking the favored orbit for the $K^\pi = 7/2^-$ band, calculated with SLy5s1 and the pairing options for the three nuclei as indicated.

With increasing J, all states become slightly triaxial, but the γ angles typically remain below 2 degrees.

Within a given pairing scheme, all calculated bands are very similar at low spin. There are, however, visible differences between the actual transition energies when comparing the four pairing schemes. For these nuclei that all are in the weak-pairing limit for either protons or neutrons or both, using stabilized HFB or HFB+LN instead of pure HFB reduces the moment of inertia when the calculations were done with the same pairing strength, as these schemes tend to enhance pairing correlations. For the lowest transitions, the best agreement between the bands in different nuclei is found for HFB, but at higher J the bands visibly differ for that scheme, in particular the one of ^{251}Md. This is a consequence of the breakdown of neutron pairing with increasing spin, which quickly increases the moment of inertia for this nucleus. Preventing the collapse of pairing with any of the other three pairing schemes brings the γ-ray transition energies much closer together over the entire band. It is to be noted that the breakdown of neutron pairing at high spin in ^{251}Md is an artifact of the too large $N = 150$ gap at the Fermi energy visible in Fig. 8. Similarly, the breakdown of proton pairing in the HFB calculation of ^{255}Lr is an artifact of the too large $Z = 104$ gap. Assuming that the deformed gaps were at $N = 152$ and $Z = 100$ instead, the relative amount of pairing correlations would be quite different: protons should be more paired in ^{255}Lr than in the two Md isotopes, while neutrons should be less paired in ^{255}Lr than the Md isotopes.

Figure 12 displays the γ-ray transition energies between levels in the $K^\pi = 1/2^-$ band of the same three

nuclei, and Figs. 13 and 14 show the corresponding deformations and dispersions of particle number. The overall trends are very similar to what is found for the $K^\pi = 7/2^-$ bands. Again, the very close agreement of transitions in HFB at low spin is spoiled when neutron pairing breaks down at higher spin, an effect that is visibly reduced when using stabilized HFB or the LN scheme, in particular at high pairing strength. It is noteworthy that the similarity of the three calculated $K^\pi = 1/2^-$ bands is slightly better than the agreement between the calculated three $K^\pi = 7/2^-$ bands, while for data this is the other way round. Differences between the transition energies between same levels in the different $K^\pi = 1/2^-$ bands are nevertheless still larger than what is found in experiment by about a factor of two.
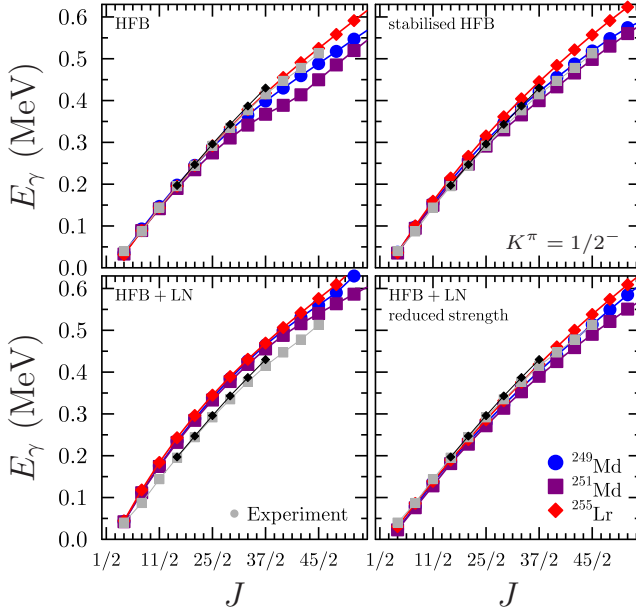

FIG. 13. Same as Fig. 10, but blocking the favored orbit for the $K^\pi = 1/2^-$ band.

FIG. 12. Same as Fig. 9, but blocking the favored orbit for the $K^\pi = 1/2^-$ band.
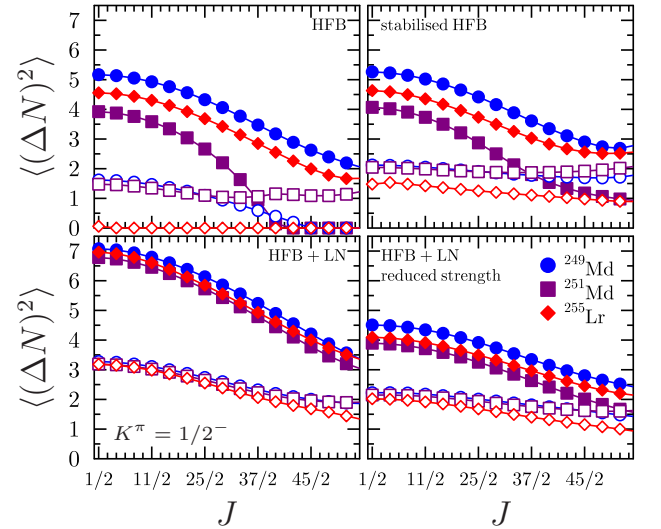
FIG. 14. Same as Fig. 11, but blocking the favored orbit for the $K^\pi = 1/2^-$ band.

In spite of the wrong relative order of the $1/2^-$ and $7/2^-$ proton levels, the down-sloping $1/2^-$ levels are almost empty in the calculated excited $7/2^-$ band of the Md isotopes, while they are almost completely filled for ^{255}Lr as one would expect if the level sequence were the one suggested by experiment as depicted in Fig. 6. Similarly, the up-sloping $7/2^-$ levels are almost empty for the $1/2^-$ band of the Md isotopes, whereas they are almost completely empty for ^{255}Lr as would be expected from the empirical shell structure. As proton pairing is weak for these odd-Z nuclides anyway, the blocked proton configurations are therefore not much affected by the imperfections of the single-particle spectrum.

That the deformation of the $7/2^-$ band of the two Md isotopes is slightly smaller than the deformation of the $7/2^-$ band of ^{255}Lr for all pairing options but HFB+LN, (see Fig. 9), is then a consequence of the two additionally
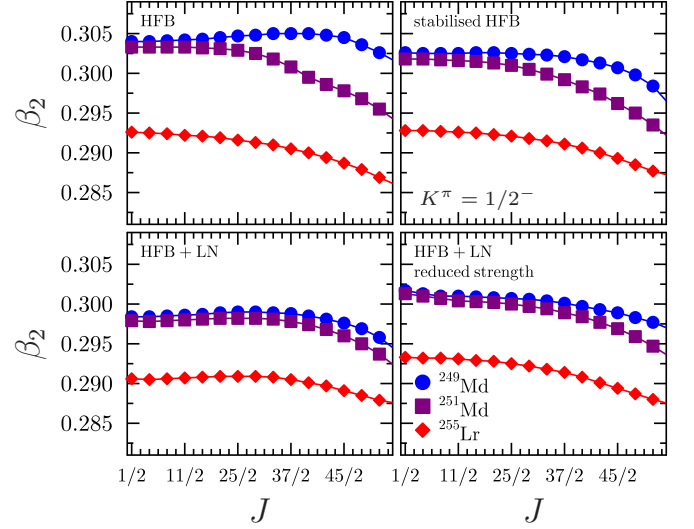
filled down-sloping, and therefore deformation-driving, $1/2^-$ levels as already discussed for the schematic Nilsson diagram of Fig. 6. The effect is not expected to be further changed by the occupying two $9/2^-$ neutron levels which have little effect on the deformation. Similarly, that the deformation of the $1/2^-$ band of the Md isotopes is larger than the deformation of the $7/2^-$ band (see Fig. 12) can then be attributed to the filling of the deformation-driving $1/2^-$ level, while the up-sloping $7/2^-$ is empty. The deformation of the $1/2^-$ bands of the Md isotopes is also larger than the deformation of the $1/2^-$ band of ^{255}Lr because the filled up-sloping $7/2^-$ levels in the lat-

ter drive the shape to smaller deformations.

The self-consistent calculations thereby confirm the schematic analysis of Fig. 6 concerning deformation changes, including the finding that deformation cannot be the sole explanation for the experimentally found reduction of the moment of inertia of both bands when going from ^{251}Md to ^{255}Lr, as it only brings a change into the right direction for the $1/2^-$ bands. Changes in pairing correlations also have to be an important factor. First of all, with increasing pairing correlations this simple picture of deformation changes driven by proton levels being filled or empty becomes blurred. Second, a reduction of pairing correlations in general reduces in-band transition energies [50, 77]. As shown in Figs 11 and 14, the calculated pairing correlations are lower in ^{255}Lr compared to ^{251}Md which should lead to an increase (decrease) of the moment inertia (transitions energies) in ^{255}Lr while the opposite trend is needed to reconcile the contradictions mentioned above.

To summarize the discussion, the similarity of calculated γ-ray energies in spite of sizable differences in the other properties discussed above points to accidental cancellation effects between the changes in shell structure, deformation and pairing as ingredients of the identical $K^\pi = 7/2^-$ bands and near-identical $K^\pi = 1/2^-$ bands in ^{251}Md and ^{255}Lr. However, it is difficult to quantify the changes brought by these effects, such that an additional mechanism might be at play that leads to a universal reduction of the moment of inertia of ^{255}Lr compared to ^{251}Md. Even if such a yet unidentified mechanism is needed, it is qualitatively described by the cranked HFB calculations, at least at low spin.

With increasing spin, the differences between the calculated bands become larger, as is the case for experiment. The calculations predict that the respective band of ^{249}Md will also be very similar to what was found for ^{251}Md and ^{255}Lr, again in spite the large differences between deformation and pairing. The sensitivity of the calculated γ-ray energies to details of the pairing scheme also suggests that obtaining identical bands to a precision that is comparable with experiment is essentially a fine-tuning problem. Using the SLy4 parametrization instead of SLy5s1 produces slightly different results, but leads to the same conclusions.

All of these conclusions have to remain qualitative, though, as it should not be forgotten that finding identical bands at the 1 keV level is beyond the limits of what can be expected for the systematic errors of the cranked HFB method as such. It is also difficult to assess the possible role of octupole correlations on the values for transition energies, as the coupling of states with octupole phonons is outside of the scope of any pure mean-field model. As a first step in that direction, exploratory beyond-mean field calculations including particle-number and angular-momentum projections on top of (parity-conserved) triaxial one-quasiparticle states were recently performed for ^{251}Md, using a variant of the Skyrme EDF designed for this particular purpose [78]. Although these calculations yield a too small moment of inertia, they appropriately predict a $K^\pi = 7/2^-$ ground state as well as the correct ordering of the levels in the signature partner bands.

VI. SUMMARY AND CONCLUSION

To summarize, this work provides the detailed properties of two rotational bands in the odd-Z ^{251}Md interpreted as built on the $[514]7/2^-$ and $[521]1/2^-$ Nilsson orbitals, the former being the g.s. band observed for the first time. Conversion electron spectroscopy allowed the rotational bands to be extended to lower rotational frequencies for the band based on the $[521]1/2^-$ Nilsson orbitals. The conversion electron intensity was also used to constrain the single particle configuration for the new band, hence excluding the $[633]7/2^+$ configuration. It was also shown that the band intensity profile in the presence of large internal conversion oscillates, providing a novel method to deduce the gyromagnetic factor. The most intense transition in both ^{249,251}Md has been tentatively interpreted as a $3/2^- \rightarrow 7/2^+$ $M2$ transition, its rate being probably enhanced by octupole correlations. The observation of several identical transitions in the ^{251}Md-^{255}Lr pair is the only case identified so far for odd-mass transuranium nuclei which moreover differ by four mass units. Arguments based on a mass-deformation-pairing compensation fail to explain the experimental similarities ($7/2^-$) and differences ($1/2^-$) between ^{251}Md and ^{255}Lr. An additional and unexplained mechanism reducing the moment of inertia in ^{255}Lr, that is probably independent on the filling of specific level, would explain simultaneously IBs for the $7/2^-$ configuration and even larger changes of the moment of inertia for the $1/2^-$ bands. New HFB calculations suggest there is not a simple mechanism leading to identical bands in the $A = 250$ mass region. Therefore the similarity can be hence considered as accidental. While the collective properties are generally well reproduced by the present calculations, our study of the particular case of similar bands points to the high sensitivity of the model to its ingredients and in particular to pairing correlations. From both an experimental and theoretical point of view, the present work provides a step towards a better description of the super-heavy nuclei region and the still speculative island of stability.

[1] M. Block, D. Ackermann, K. Blaum, C. Droese, M. Dworschak, S. Eliseev, T. Fleckenstein, E. Haettner, F. Herfurth, F. Heßberger, S. Hofmann, J. Ketelae, J. Ketter, H.-J. Kluge, G. Marx, M. Mazzocco, Y. N. Novikov, W. R. Plaß, A. Popeko, S. Rahaman, D. Rodríguez, C. Scheidenberger, L. Schweikhard, P. G. Thirolf, G. K. Vorobyev, and C. Weber, Nature **463**, 785 (2010).

[2] Ch. Theisen, P. T. Greenlees, T.-L. Khoo, P. Chowdhury, and T. Ishii, Nucl. Phys. A **944**, 333 (2015).

[3] M. Asai, F. Heßberger, and A. Lopez-Martens, Nuclear Physics A **944**, 308 (2015).

[4] D. Ackermann and Ch. Theisen, Physica Scripta **92**, 083002 (2017).

[5] S. Raeder, D. Ackermann, H. Backe, R. Beerwerth, J. C. Berengut, M. Block, A. Borschevsky, B. Cheal, P. Chhetri, C. E. Düllmann, V. A. Dzuba, E. Eliav, J. Even, R. Ferrer, V. V. Flambaum, S. Fritzsche, F. Giacoppo, S. Götz, F. P. Heßberger, M. Huyse, U. Kaldor, O. Kaleja, J. Khuyagbaatar, P. Kunz, M. Laatiaoui, F. Lautenschläger, W. Lauth, A. K. Mistry, E. Minaya Ramirez, W. Nazarewicz, S. G. Porsev, M. S. Safronova, U. I. Safronova, B. Schuetrumpf, P. Van Duppen, T. Walther, C. Wraith, and A. Yakushev, Phys. Rev. Lett. **120**, 232503 (2018).

[6] S. Ćwiok, J. Dobaczewski, P.-H. Heenen, Magierski, and W. Nazarewicz, Nucl. Phys. A **611**, 211 (1996).

[7] K. Rutz, M. Bender, T. Bürvenich, T. Schilling, P.-G. Reinhard, J. A. Maruhn, and W. Greiner, Phys. Rev. C **56**, 238 (1997).

[8] T. Bürvenich, K. Rutz, M. Bender, P.-G. Reinhard, J. Maruhn, and W. Greiner, The European Physical Journal A - Hadrons and Nuclei **3**, 139 (1998).

[9] M. Bender, K. Rutz, P.-G. Reinhard, J. A. Maruhn, and W. Greiner, Phys. Rev. **C60**, 034304 (1999).

[10] J. Dobaczewski, A. Afanasjev, M. Bender, L. Robledo, and Y. Shi, Nuclear Physics A **944**, 388 (2015).

[11] M. Bender, W. Nazarewicz, and P.-G. Reinhard, Phys. Lett. **B515**, 42 (2001).

[12] A. Chatillon, Ch. Theisen, E. Bouchez, P. A. Butler, E. Clément, O. Dorvaux, S. Eeckhaudt, B. J. P. Gall, A. Görgen, T. Grahn, P. T. Greenlees, R.-D. Herzberg, F. Heßberger, A. Hürstel, G. D. Jones, P. Jones, R. Julin, S. Juutinen, H. Kettunen, F. Khalfallah, W. Korten, Y. Le Coz, M. Leino, A.-P. Leppänen, P. Nieminen, J. Pakarinen, J. Perkowski, P. Rahkila, M. Rousseau, C. Scholey, J. Uusitalo, J. N. Wilson, P. Bonche, and P.-H. Heenen, Phys. Rev. Lett. **98**, 132503 (2007).

[13] M. Leino, J. Äystö, T. Enqvist, P. Heikkinen, A. Jokinen, M. Nurmia, A. Ostrowski, W. Trzaska, J. Uusitalo, K. Eskola, P. Armbruster, and V. Ninov, Nucl. Instrum. Methods Phys. Res. B **99**, 653 (1995).

[14] J. Sarén, J. Uusitalo, M. Leino, and J. Sorri, Nucl. Instrum. Methods Phys. Res. A **654**, 508 (2011).

[15] R. D. Page, A. N. Andreyev, D. E. Appelbe, P. A. Butler, S. J. Freeman, P. T. Greenlees, R.-D. Herzberg, D. G. Jenkins, G. D. Jones, P. Jones, D. T. Joss, R. Julin, H. Kettunen, M. Leino, P. Rahkila, P. H. Regan, J. Simpson, J. Uusitalo, S. M. Vincent, and R. Wadsworth, Nucl. Instrum. Methods Phys. Res. B **204**, 634 (2003).

[16] A. Chatillon, Ch. Theisen, P. Greenlees, G. Auger, J. Bastin, E. Bouchez, B. Bouriquet, J. Casandijan, R. Cee, E. Clement, R. Dayas, G. de France, R. de Toureil, S. Esckhaudt, A. Görgen, T. Grahn, S. Grevy, K. Hauschild, R.-D. Herzberg, P. Ikin, G. Jones, P. Jines, R. Julin, S. Juutinen, H. Kettunen, A. Korichi, W. Korten, Y. L. Coz, M. Leino, A. Lopez-Martens, S. Lukyanov, Y. Penionzhkevich, J. Perkowski, A. Pritchard, P. Rahkila, M. Rejmund, J. Saren, C. Scholey, S. Siem, M. Saint-Laurent, C. Simenel, Y. Sobolev, C. Stodel, J. Uusitalo, A. Villari, M. Bender, P. Bouche, and P.-H. Heenen, Eur. Phys. J. A **30**, 397 (2006).

[17] J. Pakarinen, P. Papadakis, J. Sorri, R. D. Herzberg, P. T. Greenlees, P. A. Butler, P. J. Coleman-Smith, D. M. Cox, J. R. Cresswell, P. Jones, R. Julin, J. Konki, I. H. Lazarus, S. C. Letts, A. Mistry, R. D. Page, E. Parr, V. F. E. Pucknell, P. Rahkila, J. Sampson, M. Sandzelius, D. A. Seddon, J. Simpson, J. Thornhill, and D. Wells, The European Physical Journal A **50**, 53 (2014).

[18] R. Briselet, C. Theisen, M. Vandebrouck, A. Marchix, M. Airiau, K. Auranen, H. Badran, D. Boilley, T. Calverley, D. Cox, F. Déchery, F. Defranchi Bisso, A. Drouart, B. Gall, T. Goigoux, T. Grahn, P. T. Greenlees, K. Hauschild, A. Herzan, R. D. Herzberg, U. Jakobsson, R. Julin, S. Juutinen, J. Konki, M. Leino, A. Lightfoot, A. Lopez-Martens, A. Mistry, P. Nieminen, J. Pakarinen, P. Papadakis, J. Partanen, P. Peura, P. Rahkila, J. Rubert, P. Ruotsalainen, M. Sandzelius, J. Saren, C. Scholey, J. Sorri, S. Stolze, B. Sulignano, J. Uusitalo, A. Ward, and M. Zielińska, Phys. Rev. C **99**, 024614 (2019).

[19] I. H. Lazarus, D. E. Appelbe, P. A. Butler, P. J. Coleman-Smith, J. R. Cresswell, S. J. Freeman, R. D. Herzberg, I. Hibbert, D. T. Joss, S. C. Letts, R. D. Page, V. F. E. Pucknell, P. H. Regan, J. Sampson, J. Simpson, J. Thornhill, and R. Wadsworth, IEEE Trans. Nucl. Sci. **48**, 567 (2001).

[20] P. Rahkila, Nucl. Instrum. Methods Phys. Res. A **595**, 637 (2008).

[21] T. Kibédi, T. Burrows, M. Trzhaskovskaya, P. Davidson, and C. Nestor, Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment **589**, 202 (2008).

[22] F. Heßberger, S. Hofmann, D. Ackermann, V. Ninov, M. Leino, G. Münzenberg, S. Saro, A. Lavrentev, A. Popeko, A. Yeremin, *et al.*, The European Physical Journal A-Hadrons and Nuclei **12**, 57 (2001).

[23] S. Ćwiok, S. Hofmann, and W. Nazarewicz, Nuclear Physics A **573**, 356 (1994).

[24] A. Parkhomenko and A. Sobiczewski, Acta Phys. Pol. B **35**, 2447 (2004).

[25] S. Antalic, F. P. Heßberger, S. Hofmann, D. Ackermann,

[25] S. Heinz, B. Kindler, I. Kojouharov, P. Kuusiniemi, M. Leino, B. Lommel, R. Mann, and Š. Šáro, The European Physical Journal A **43**, 35 (2010).

[26] Xiao-tao. He, Zhong-zhou. Ren, Shu-xin. Liu, and Enguang. Ahao, Nuclear Physics A **817**, 45 (2009).

[27] Z.-H. Zhang, X.-T. He, J.-Y. Zeng, E.-G. Zhao, and S.-G. Zhou, Phys. Rev. C **85**, 014324 (2012).

[28] U. Shirwadkar, S. K. Tandel, P. Chowdhury, T. L. Khoo, I. Ahmad, M. P. Carpenter, J. P. Greene, R. V. F. Janssens, F. G. Kondev, T. Lauritsen, C. J. Lister, D. Peterson, D. Seweryniak, X. Wang, and S. Zhu, Phys. Rev. C **100**, 034309 (2019).

[29] P. Greenlees, R.-D. Herzberg, S. Ketelhut, P. Butler, P. Chowdhury, T. Grahn, C. Cray-Jones, G. Jones, P. Jones, R. Julin, S. Juutinen, T. L. Knoo, M. Leino, S. Moon, M. Nyman, J. Pakarinen, P. Rahkila, D. Rostron, J. Saren, C. Scholey, J. Sorri, S. K. Tandel, J. Uusitalo, and M. Venhart, Phys. Rev. C **78**, 021303(R) (2008).

[30] B. Sulignano, C. Theisen, J.-P. Delaroche, M. Girod, J. Ljungvall, D. Ackermann, S. Antalic, O. Dorvaux, A. Drouart, B. Gall, A. Görgen, P. T. Greenlees, K. Hauschild, R.-D. Herzberg, F. P. Heßberger, U. Jakobsson, P. Jones, R. Julin, S. Juutinen, S. Ketelhut, W. Korten, M. Leino, A. Lopez-Martens, M. Nyman, A. Obertelli, J. Pakarinen, P. Papadakis, E. Parr, P. Peura, J. Piot, P. Rahkila, D. Rostron, P. Ruotsalainen, J. Sarén, C. Scholey, J. Sorri, J. Uusitalo, M. Venhart, and M. Zielińska, Phys. Rev. C **86**, 044318 (2012).

[31] H. B. Jeppesen, R. M. Clark, K. E. Gregorich, A. V. Afanasjev, M. N. Ali, J. M. Allmond, C. W. Beausang, M. Cromaz, M. A. Deleplanque, I. Dragojević, J. Dvorak, P. A. Ellison, P. Fallon, M. A. Garcia, J. M. Gates, S. Gros, I. Y. Lee, A. O. Macchiavelli, S. L. Nelson, H. Nitsche, L. Stavsetra, F. S. Stephens, and M. Wiedeking, Phys. Rev. C **80**, 034324 (2009).

[32] I. Ahmad, A. M. Friedman, R. R. Chasman, and S. W. Yates, Physical Review Letters **39**, 12 (1977).

[33] G. Henning, T. L. Khoo, A. Lopez-Martens, D. Seweryniak, M. Alcorta, M. Asai, B. B. Back, P. F. Bertone, D. Boilley, M. P. Carpenter, C. J. Chiara, P. Chowdhury, B. Gall, P. T. Greenlees, G. Gürdal, K. Hauschild, A. Heinz, C. R. Hoffman, R. V. F. Janssens, A. V. Karpov, B. P. Kay, F. G. Kondev, S. Lakshmi, T. Lauritsen, C. J. Lister, E. A. McCutchan, C. Nair, J. Piot, D. Potterveld, P. Reiter, A. M. Rogers, N. Rowley, and S. Zhu, Phys. Rev. Lett. **113**, 262505 (2014).

[34] A. Bohr and B. R. Mottelson, *Nuclear Structure Volume II* (W.A. Benjamin, Inc., Massachusetts; World Scientific 1998, 1999, 2008, 1979).

[35] P. A. Butler, R. D. Humphreys, P. T. Greenlees, R.-D. Herzberg, D. G. Jenkins, G. D. Jones, H. Kankaanpää, H. Kettunen, P. Rahkila, C. Scholey, J. Uusitalo, N. Amzal, J. E. Bastin, P. M. T. Brew, K. Eskola, J. Gerl, N. J. Hammond, K. Hauschild, K. Helariutta, F.-P. Heßberger, A. Hürstel, P. M. Jones, R. Julin, S. Juutinen, A. Keenan, T.-L. Khoo, W. Korten, P. Kuusiniemi, Y. Le Coz, M. Leino, A.-P. Leppänen, M. Muikku, P. Nieminen, S. W. Ødegård, T. Page, J. Pakarinen, P. Reiter, G. Sletten, C. Theisen, and H.-J. Wollersheim, Phys. Rev. Lett. **89**, 202501 (2002).

[36] R.-D.Herzberg, P. T.Greenlees, P. A.Butler, G. D.Jones, M.Venhart, I. G.Darby, S. Eeckhaudt, K. Eskola, T. Grahn, C. Gray-Jones, F. P. Heßer, P. Jones, R. Julin, S. Juutinen, S. Ketelhut, T. L. Khoo, W. Korten, M. Leino, A.-P. Leppänen, S. Moon, M. Nyman, R. Page, J. Pakarinen, A. Pritchard, P. Rahkila, P. Reiter, J. Saren, C. Scholey, A. Steer, Y. Sun, C. Theisen, S. Tandel, and J. Uusitalo, Nature **442**, 896 (2006).

[37] S. K. Tandel, T. L. Khoo, D. Seweryniak, G. Mukherjee, I. Ahmad, B. Back, R. Blinstrup, M. P. Carpenter, J. Chapman, P. Chowdhury, C. N. Davids, A. A. Hecht, A. Heinz, P. Ikin, R. V. F. Janssens, F. G. Kondev, T. Lauritsen, C. J. Lister, E. F. Moore, D. Peterson, P. Reiter, U. S. Tandel, X. Wang, and S. Zhu, Phys. Rev. Lett. **97**, 082502 (2006).

[38] R. Clark, K. Gregorich, J. Berryman, M. Ali, J. Allmond, C. Beausang, M. Cromaz, M. Deleplanque, I. Dragojevic, J. Dvorak, P. Ellison, P. Fallon, M. Garcia, J. Gates, S. Gros, H. Jeppesen, D. Kaji, I. Lee, A. Macchiavelli, K. Morimoto, H. Nitsche, S. Paschalis, M. Petri, L. Stavsetra, F. Stephens, H. Watanabe, and M. Wiedeking, Phys. Lett. B **690**, 19 (2010).

[39] F. P. Heßberger, S. Antalic, B. Sulignano, D. Ackermann, S. Heinz, S. Hofmann, B. Kindler, J. Khuyagbaatar, I. Kojouharov, P. Kuusiniemi, M. Leino, B. Lommel, R. Mann, K. Nishio, A. G. Popeko, Š. Šáro, B. Streicher, J. Uusitalo, M. Venhart, and A. V. Yeremin, The European Physical Journal A **43**, 55 (2010).

[40] S. Ketelhut, *Rotational Structures and High-K Isomerism in* $^{248,250}Fm$, Ph.D. thesis, University of Jyväskylä (2010).

[41] B. Sulignano, unpublished.

[42] T. Goigoux et al., in preparation.

[43] S. W. Yates, A. M. Friedman, and I. Ahmad, Phys. Rev. C **12**, 795 (1975).

[44] S. W. Yates, R. R. Chasman, A. M. Friedman, I. Ahmad, and K. Katori, Phys. Rev. C **12**, 442 (1975).

[45] K. Rezynkina, A. Lopez-Martens, K. Hauschild, I. Deloncle, S. Péru, P. Brionnet, M. L. Chelnokov, V. I. Chepigin, O. Dorvaux, F. Déchery, H. Faure, B. Gall, A. V. Isaev, I. N. Izosimov, D. E. Katrasev, A. N. Kuznetsov, A. A. Kuznetsova, O. N. Malyshev, A. G. Popeko, Y. A. Popov, E. A. Sokol, A. I. Svirikhin, and A. V. Yeremin, Physical Review C **97**, 054332 (2018).

[46] S. Ketelhut, P. T. Greenlees, D. Ackermann, S. Antalic, E. Clément, I. G. Darby, O. Dorvaux, A. Drouart, S. Eeckhaudt, B. J. P. Gall, A. Görgen, T. Grahn, C. Gray-Jones, K. Hauschild, R.-D. Herzberg, F. P. Heßberger, U. Jakobsson, G. D. Jones, P. Jones, R. Julin, S. Juutinen, T.-L. Khoo, W. Korten, M. Leino, A.-P. Leppänen, J. Ljungvall, S. Moon, M. Nyman, A. Obertelli, J. Pakarinen, E. Parr, P. Papadakis, P. Peura, J. Piot, A. Pritchard, P. Rahkila, D. Rostron, P. Ruotsalainen, M. Sandzelius, J. Sarén, C. Scholey, J. Sorri, A. Steer, B. Sulignano, Ch. Theisen, J. Uusitalo, M. Venhart, M. Zielinska, M. Bender, and P.-H. Heenen, Phys. Rev. Lett. **102**, 212501 (2009).

[47] E. Browne and J. Tuli, Nuclear Data Sheets **114**, 1041 (2013).

[48] T. Byrski, F. A. Beck, D. Curien, C. Schuck, P. Fallon, A. Alderson, I. Ali, M. A. Bentley, A. M. Bruce, P. D. Forsyth, D. Howe, J. W. Roberts, J. F. Sharpey-Schafer, G. Smith, and P. J. Twin, Phys. Rev. Lett. **64**, 1650 (1990).

[49] C. Baktash, B. Haas, and W. Nazarewicz, Annual Review of Nuclear and Particle Science **45**, 485 (1995).

[50] D. J. Rowe, *Nuclear collective motion: models and theory* (Methuen, London, 1970).

[51] I. Ragnarsson, Nuclear Physics A **520**, c67 (1990).

[52] I. Ragnarsson, Physics Letters B **264**, 5 (1991).

[53] Z. Szymanski, Phys. Rev. C **51**, R1090 (1995).

[54] W. Satuła, J. Dobaczewski, J. Dudek, and W. Nazarewicz, Phys. Rev. Lett. **77**, 5182 (1996).

[55] I. Ahmad, M. P. Carpenter, R. R. Chasman, R. V. F. Janssens, and T. L. Khoo, Phys. Rev. C **44**, 1204 (1991).

[56] X. Wang, R. V. F. Janssens, M. P. Carpenter, S. Zhu, I. Wiedenhöver, U. Garg, S. Frauendorf, T. Nakatsukasa, I. Ahmad, A. Bernstein, E. Diffenderfer, S. J. Freeman, J. P. Greene, T. L. Khoo, F. G. Kondev, A. Larabee, T. Lauritsen, C. J. Lister, B. Meredith, D. Seweryniak, C. Teal, and P. Wilson, Phys. Rev. Lett. **102**, 122501 (2009).

[57] S. Hota, *Spectroscopy of neutron-rich Pu, Cm and Cf nuclei via inelastic and transfer reactions*, Ph.D. thesis, University of Massachusetts Lowell (2012).

[58] B. Birkenbach, A. Vogt, K. Geibel, F. Recchia, P. Reiter, J. J. Valiente-Dobón, D. Bazzacco, M. Bowry, A. Bracco, B. Bruyneel, L. Corradi, F. C. L. Crespi, G. de Angelis, P. Désesquelles, J. Eberth, E. Farnea, E. Fioretto, A. Gadea, A. Gengelbach, A. Giaz, A. Görgen, A. Gottardo, J. Grebosz, H. Hess, P. R. John, J. Jolie, D. S. Judson, A. Jungclaus, W. Korten, S. Lenzi, S. Leoni, S. Lunardi, R. Menegazzo, D. Mengoni, C. Michelagnoli, T. Mijatović, G. Montagnoli, D. Montanari, D. Napoli, L. Pellegri, G. Pollarolo, A. Pullia, B. Quintana, F. Radeck, D. Rosso, E. Şahin, M. D. Salsac, F. Scarlassara, P.-A. Söderström, A. M. Stefanini, T. Steinbach, O. Stezowski, S. Szilner, B. Szpak, C. Theisen, C. Ur, V. Vandone, and A. Wiens, Phys. Rev. C **92**, 044319 (2015).

[59] I. Wiedenhöver, R. V. F. Janssens, G. Hackman, I. Ahmad, J. P. Greene, H. Amro, P. K. Bhattacharyya, M. P. Carpenter, P. Chowdhury, J. Cizewski, D. Cline, T. L. Khoo, T. Lauritsen, C. J. Lister, A. O. Macchiavelli, D. T. Nisius, P. Reiter, E. H. Seabury, D. Seweryniak, S. Siem, A. Sonzogni, J. Uusitalo, and C. Y. Wu, Phys. Rev. Lett. **83**, 2143 (1999).

[60] R. F. Casten, N. V. Zamfir, P. von Brentano, and W.-T. Chou, Phys. Rev. C **45**, R1413 (1992).

[61] A. E. Stuchbery, Nuclear Physics A **589**, 222 (1995).

[62] R. R. Chasman, I. Ahmad, A. M. Friedman, and J. R. Erskine, Rev. Mod. Phys. **49**, 833 (1977).

[63] J. M. Espino and J. D. Garrett, Nucl. Phys. A **492**, 205 (1989).

[64] F. S. Stephens, Nucl. Phys. A **520**, c91 (1990).

[65] J.-y. Zhang and L. L. Riedinger, Phys. Rev. Lett. **69**, 3448 (1992).

[66] W. Ryssens, *Symmetry breaking in nuclear mean-field models*, Ph.D. thesis, Université Libre de Bruxelles (2016).

[67] W. Ryssens, M. Bender, and P.-H. Heenen, MOCCa code (unpublished).

[68] R. Jodon, M. Bender, K. Bennaceur, and J. Meyer, Phys. Rev. C **94**, 024335 (2016).

[69] E. Chabanat, P. Bonche, P. Haensel, J. Meyer, and R. Schaeffer, Nucl. Phys. **A635**, 231 (1998), Nucl. Phys. **A643**, 441(E) (1998).

[70] W. Ryssens, M. Bender, K. Bennaceur, P.-H. Heenen, and J. Meyer, Phys. Rev. C **99**, 044315 (2019).

[71] C. Rigollet, P. Bonche, H. Flocard, and P.-H. Heenen, Phys. Rev. C **59**, 3120 (1999).

[72] M. Bender and P.-H. Heenen, to be published.

[73] J. Erler, P. Klüpfel, and P.-G. Reinhard, Eur. Phys. J. A **37**, 81 (2008).

[74] M. Bender and P.-H. Heenen, Journal of Physics: Conference Series **420**, 012002 (2013).

[75] Y. Shi, J. Dobaczewski, and P. T. Greenlees, Phys. Rev. C **89**, 034309 (2014).

[76] P. Olbratowski, J. Dobaczewski, and J. Dudek, Phys. Rev. C **73**, 054308 (2006).

[77] M. J. A. de Voigt, J. Dudek, and Z. Szymański, Rev. Mod. Phys. **55**, 949 (1983).

[78] P.-H. Heenen, B. Bally, M. Bender, and W. Ryssens, EPJ Web Conf. **131**, 02001 (2016).