

1 **Divergent short and long-range behaviour in ion-irradiated**



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**Abstract**

Ion irradiation experiments and quantitative x-ray diffraction analysis were used to demonstrate that the lattice and structure behave very differently in a complex oxide,  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$ , under irradiation. Analysis of the structure reveals that with increasing fluence, the characteristic  $c/a$  ratio for  $\delta$ -phase converges to that of an ideal fluorite phase, whereas locally it produces a metaphase consisting of frozen nanoscale structures having bixbyite-like flavor that increase the overall stability and radiation response of the apparent long-range oxygen-deficient average fluorite structure.

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## 13 I. INTRODUCTION

14 Non-stoichiometric fluorite-related oxides are model systems to address fundamental ques-  
15 tions in inorganic compounds, and in particular the mechanisms of solid state reactions and  
16 transformations in solids. Systematic analysis of the thermodynamic properties of heteroge-  
17 neous equilibria shows that singularities of the physical properties (melting point, conduc-  
18 tivity, thermoelectricity, etc) do not necessarily occur for compositions with simple rational  
19 ratios. Wagner and Schottky [1] discussed the statistical thermodynamics of real compounds  
20 and proved the stoichiometry of ideal crystals has no special position, though the extent to  
21 which different substances may display a departure from stoichiometry depends on specific  
22 characteristics like the energies of lattice disorder and charge transfer. Oxygen deficient  
23 fluorites are grossly non-stoichiometric compounds and lattice energy calculations can lead  
24 to the conclusion that many of the observed non-stoichiometric phases can exhibit a high de-  
25 gree of metastability [2]. Indeed, in these systems, short-range interactions between defects,  
26 clusters and complex atomic arrangements can be strong and they can explain the observed  
27 variety of long-range structures encountered in these compounds. The delicate balance be-  
28 tween order, disorder, and metastability present in these systems makes them an interesting  
29 playground for studying their resilience to external perturbations, and in particular, to ion  
30 irradiation. Though the questions raised are fundamental, their impact on properties is also  
31 important. Structural stability is of particular interest in these complex oxides because these  
32 systems provide fascinating insights into the behavior of advanced nuclear ceramics and the  
33 long-term behaviour of spent fuels and nuclear wastefoms. The technological interest in  
34 these oxides also spans other areas as they find applications as solid-state electrolytes in  
35 fuel cells, and have interesting features that can be exploited in the engineering of thermal  
36 barrier coatings.

37 As the structures disorder, they become more complicated and difficult to describe. But  
38 disorder and complexity by themselves are neither good nor bad. It is the lack of precision  
39 in their description that often prevents us from navigating and managing this complexity. A  
40 complete description of all the phenomena occurring in fluorite-related materials disordered  
41 by ion irradiation is still out-of-reach.

42 The study of radiation effects in fluorite compounds and in fluorite derivative phases,  
43 including pyrochlore, weberite, and bixbyite systems is not a recent trend, though it is still

44 expanding. Pyrochlore and weberites [3] with  $A_2B_2O_7$  generic chemical formula are perhaps  
45 the simplest and least substoichiometric compounds in the  $AO_{2-x}$  system where there is a  
46 significant tendency for cations and anions to order. Several studies highlight the impact of  
47 the A- and B-site cation radii on the resistance to disorder or amorphisation produced by  
48 high pressure or radiation [4–10]. Bixbyite oxides ( $B_2O_3$ ), generally consist of a single-type  
49 of rare earth cation. These systems exhibit a consistent ordering of O vacancies in their  
50 ground state. Moreover, these structures display the highest oxygen deficiency among the  
51 fluorite-related systems. While recent structural studies using diffraction techniques assess  
52 the structural changes occurring in these single-element oxides [11–13], little is structurally  
53 known about multi-cation bixbyites [14, 15].

54 In between these two substoichiometric compositions of the oxygen-deficient fluorite sys-  
55 tems, another simple system that exhibits a consistent anion vacancy ordering, not neces-  
56 sarily involving cation ordering, is the  $\delta$ -phase structure. The radiation resistance of these  
57 structures has already been investigated using diffraction techniques but the details of the  
58 structural changes are not yet clear as there is no extensive and systematic study of these sys-  
59 tems using x-ray or neutron diffraction.  $\delta$ -phases are interesting systems in the large family  
60 of oxygen deficient fluorites [16]. The  $\delta$ -phase structure consists of edge and corner-sharing  
61 oxygen octahedra and oxygen vacancies are located in the ideal fluorite anion sublattice.  
62 These vacancies are generally found to order onto specific sites of the structure, leading to  
63 the appearance of superstructure reflections in the x-ray diffraction patterns. These weak  
64 reflections are produced by the combined effect of the composition modulation and of the  
65 displacive relaxation of the metal ions surrounding the anion vacant sites. The ideal oxy-  
66 gen stoichiometry (O/M) in  $\delta$ -phases is close to 1.714. Direct structural determination has  
67 found that the cations order only when the stoichiometry is  $A_6^{+3}B^{+6}O_{12}$  [17, 18], whereas the  
68 cations cannot order in compounds with stoichiometry  $A_4^{+3}B_3^{+4}O_{12}$ . The common character-  
69 istic symmetry of these phases is  $R\bar{3}$ , and they typically exhibit a moderate deviation (few  
70 %) from the ideal  $c/a$  ratio 0.9258 of a cubic fluorite described in this same lattice frame.

71 The structural characteristics of several irradiated  $\delta$ -phases [19–26] were studied and  
72 the common conclusion was the observation of a phase transformation towards an apparent  
73 disordered fluorite phase. The most comprehensive among these studies [20, 21] also discuss  
74 the qualitative formation of a bixbyite-like phase in low-energy irradiated  $\delta$ - $Sc_4Zr_3O_{12}$ . This  
75 transformation to bixbyite was in some way a mystery since group-subgroup analysis does not

76 allow for a direct transformation from the  $\delta$ -phase to a bixbyite. However, if one compares  
77 the polyhedral networks in these two structures, then one can find a slight similarity in  
78 the polyhedral networks. The bixbyite structure is only comprised of octahedra (slightly  
79 distorted octahedra [27]), while the  $\delta$ -phase is typically described as having 6-fold and 7-  
80 fold polyhedra. However, one of the M-O bond lengths in the 7-fold polyhedra is significantly  
81 longer such that the polyhedra resemble capped octahedra [28].

82 The aim of this work is not to provide a definitive blueprint for the global changes occur-  
83 ring in all fluorite-derived structures, but rather to offer a fresh explanation for the following  
84 phenomena: (1) the critical structural changes involved; (2) how structure supports radiation  
85 resistance; (3) how to find a balance between global long-range and diverse local structural  
86 features; and (4) how this can lead to effective engineering of fluorite-related materials. In  
87 order to establish these quantitative features, we analyze structural characteristics of a the  
88 swift heavy ion irradiated  $\delta$ -phase compound, namely  $\text{Sc}_4^{+3}\text{Hf}_3^{+4}\text{O}_{12}$  using high-resolution  
89 x-ray powder diffraction.

## 90 II. EXPERIMENTAL PROCEDURES

91 Powders of scandium sesquioxide ( $\text{Sc}_2\text{O}_3$ , 99.99%) and hafnium oxide ( $\text{HfO}_2$ , 99.95%)  
92 purchased from Alfa Aesar were calcined at 700 °C and weighed to obtain a 4:3:12 stoi-  
93 chiometric ratio of Sc:Hf:O. The mixture was ball milled in a high energy SPEX<sup>®</sup> 8000D  
94 dual mixer/mill using zirconia ceramic vial set and two 12.7 mm zirconia ceramic balls in  
95 an isopropanol medium for 8 hours. The powder mixture was cold pressed into pellets of  
96 13 mm in diameter and a thickness of 10 mm using a stainless steel die and plunger. The  
97 pellets were then sintered in air, first at 1200 °C for 48 hours and then again at 1600 °C for  
98 72 hours. The heating and cooling rates during both sintering cycles were kept at 5 °C/min.  
99 Samples were ground again between the two sintering cycles. The as-synthesized pellets  
100 were close to 95% of the theoretical density and x-ray powder diffraction was performed to  
101 assess their phase purity. Qualitative analysis of the diffraction patterns showed formation  
102 of a rhombohedral  $\delta$ -phase that matched closely with structures reported in the literature  
103 [16, 29].

104 The rest of the pellets were used for irradiation experiments. Prior to irradiations, these  
105 pellets were cut into discs of 2 mm thickness and polished with diamond lapping films down

106 to 1  $\mu\text{m}$ . The final polishing was performed using colloidal silica to remove residual damage  
 107 due to polishing. To study the radiation response of  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$ , samples were irradiated  
 108 at room temperature with 92 MeV  $\text{Xe}^{26+}$  ions at the IRRSUD beamline in GANIL, France,  
 109 using time-integrated fluxes (fluences) ranging from  $10^{11}$  to  $10^{14}$  ions/ $\text{cm}^2$ . The flux of ions  
 110 during irradiation was  $10^9$  ions/ $\text{cm}^2/\text{s}$  and the sample surface was kept normal to the ion  
 111 beam direction. Fig. 1a shows the partitioning of energy loss for each Xe ion into nuclear  
 112 and electronic stopping power components, as a function of depth in the  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$  target  
 113 material. The integrated energy losses from electronic and nuclear components calculated  
 114 from their respective stopping powers are 87.5 and 3.4 MeV. It is important to observe in  
 115 Fig. 1a that electronic stopping far exceeds nuclear stopping over nearly the entire range of  
 116 the Xe ions in the  $\text{Sc}_4\text{Hf}_3\text{O}_{12}$  target (at least until the depth of 7.5  $\mu\text{m}$  in the target where  
 117 the ion implantation occurs).

118 X-ray powder diffraction measurements were performed on samples irradiated with flu-  
 119 ences exceeding  $10^{12}$  ions/ $\text{cm}^2$ , that correspond to the conditions of a uniformly irradiated  
 120 surface due to multiple ion-track overlaps. Diffraction measurements were performed using  
 121 a Bruker D8 Advance diffractometer equipped with a Göbel mirror for Cu  $K\alpha$  radiation and  
 122 a NaI scintillation detector. Data collections were performed in a  $\theta - \theta$  geometry performing  
 123 symmetric step scans of the detector and the x-ray source ( $\Delta 2\theta = 0.02^\circ$ ) with a step time  
 124 of 2 sec/step.  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$  presents a significant advantage for the x-ray diffraction anal-  
 125 ysis compared to other compounds belonging to this same family because of the excellent  
 126 scattering contrast between Sc and Hf ions.

127 Fig. 1b shows the depth profile of implanted Xe ions in  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$ , calculated using  
 128 SRIM [30] for  $10^{14}$  ions/ $\text{cm}^2$ . Based on SRIM, the projected range,  $R_p$ , of 92 MeV Xe  
 129 ions in  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$  is 8  $\mu\text{m}$ , with a longitudinal straggling of 0.7  $\mu\text{m}$ . Fig. 1b also shows  
 130 the penetration depth of Cu- $K\alpha$  x-rays in  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$ . The x-ray diffracted signal in  $\delta\text{-}$   
 131  $\text{Sc}_4\text{Hf}_3\text{O}_{12}$  comes from a variable penetration depth not exceeding 5  $\mu\text{m}$ . Clearly, over  
 132 this range in target depth, no significant Xe ion implantation occurs. In summary, Fig. 1  
 133 shows that electronic energy loss dominates significantly over nuclear energy loss for 92  
 134 MeV Xe in  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$ , over nearly the entire range of the implanted Xe ions; addition-  
 135 ally, x-ray diffraction measurements at low angles ( $2\theta < 45$ ) are only sensitive to electronic  
 136 radiation damage effects (essentially, no nuclear radiation damage effects contribute to the  
 137 measurements performed in this study). Rietveld refinements were performed using the soft-

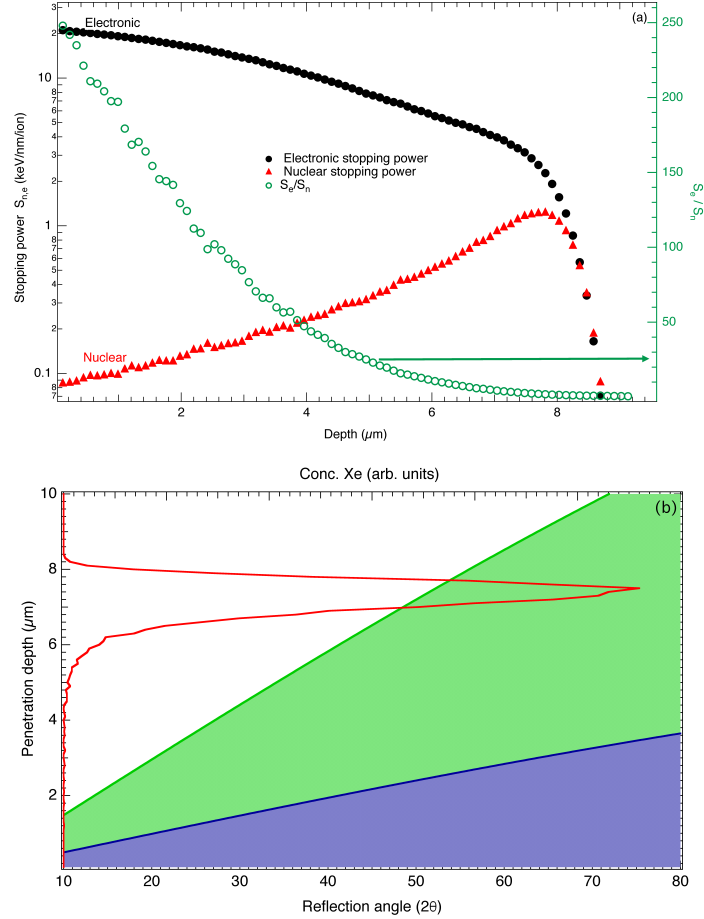


FIG. 1. (a) Electronic versus nuclear energy loss for 92 MeV Xe ions in  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$ . The abscissa indicates distance into the target, specifically distance normal to the target surface. The projected (longitudinal) range of the incident Xe ions is approximately  $8\mu\text{m}$ . The ordinate on the left shows incident ion energy loss (due to either electronic (black circles) or nuclear (ballistic) (red triangles) mechanisms) on the logarithmic scale, while that on the right shows the ratio of electronic to nuclear energy loss (green open circles). Calculations were performed using the so-called "quick SRIM" calculations option within the SRIM code for ion stopping in solids [30]. (b) Comparison of the penetration depth of Cu-K $\alpha$  x-rays in  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$  as a function of the scattering angle (blue,  $2\theta$ , bottom scale) and Xe implantation profile (red line, top scale): according to the Beer-Lambert law and for a Bragg-Brentano experiment geometry, 63.2% of the scattered signal at a given angle comes from a shallow region below the sample surface whose depth is below the blue line. The green line is intended to indicate that 95% of the signal arises from depths below this line. Below  $2\theta = 45^\circ$ , more than 95% of the scattered x-ray photons come from a region where no implantation occurs.

ware Jana2000 [31] and 3D structure visualization models were obtained using the software VESTA [32].

### III. LOCAL ORDER

The interaction of an impinging x-ray beam with a crystal produces a discrete set of scattered beams forming a periodic lattice of sharp reflections (Bragg reflections), the so-called reciprocal space of the crystal. Any kind of crystal imperfection (stacking faults, chemical disorder, lattice vibrations, ...) perturbing the long-range crystalline order reduces the intensity of the Bragg reflections by a large attenuation factor. But the overall scattered intensity is conserved, and this loss of intensity of the Bragg reflections is, however, recovered under the form of a very weak and broad diffuse intensity that adds to the background and it is spread over particular positions in the reciprocal space. This broad x-ray scattering intensity is called diffuse scattering. The deviation from the perfect crystalline order can occur because of atomic displacements or related to atomic substitutions, or due to a combination of the two effects. When the diffracted beam is measured without energy resolution, it is not possible to discriminate between a dynamic origin of the diffuse scattering (lattice vibrations) or a static origin (crystal imperfections). In this setup, the diffuse scattering intensity, gives directly the instantaneous spatial correlations of the order parameter  $\xi$  :  $S(\mathbf{q}, t = 0) = |\xi_q|^2$  where  $\xi_q$  is the  $q$ -th component of the Fourier transform of a spatially-dependent atomic displacement wave or density concentration wave occurring in the crystal [33–35]. The spatial correlation length of the  $q$ -th component of the order parameter can be obtained from the breadth of the diffuse scattering within the Ornstein-Zernike formalism [36, 37]. Using a correlated microdiffraction model developed by Neder et al. [38] it is possible to model the diffuse scattering produced by correlated nanodomains introducing a difference structure where the atoms represent the difference between the average structure and the nanodomain structure. Scherrer-type peak broadening can be included in this "correlated-model" structure, and it describes the characteristic long-range correlation length of the average structure and the shorter-range averaged size of the correlation domains responsible for the diffuse scattering. Eventually, a microstrain-type peak broadening can also be introduced to account for defect-induced elastic fluctuations of the lattice parameter.

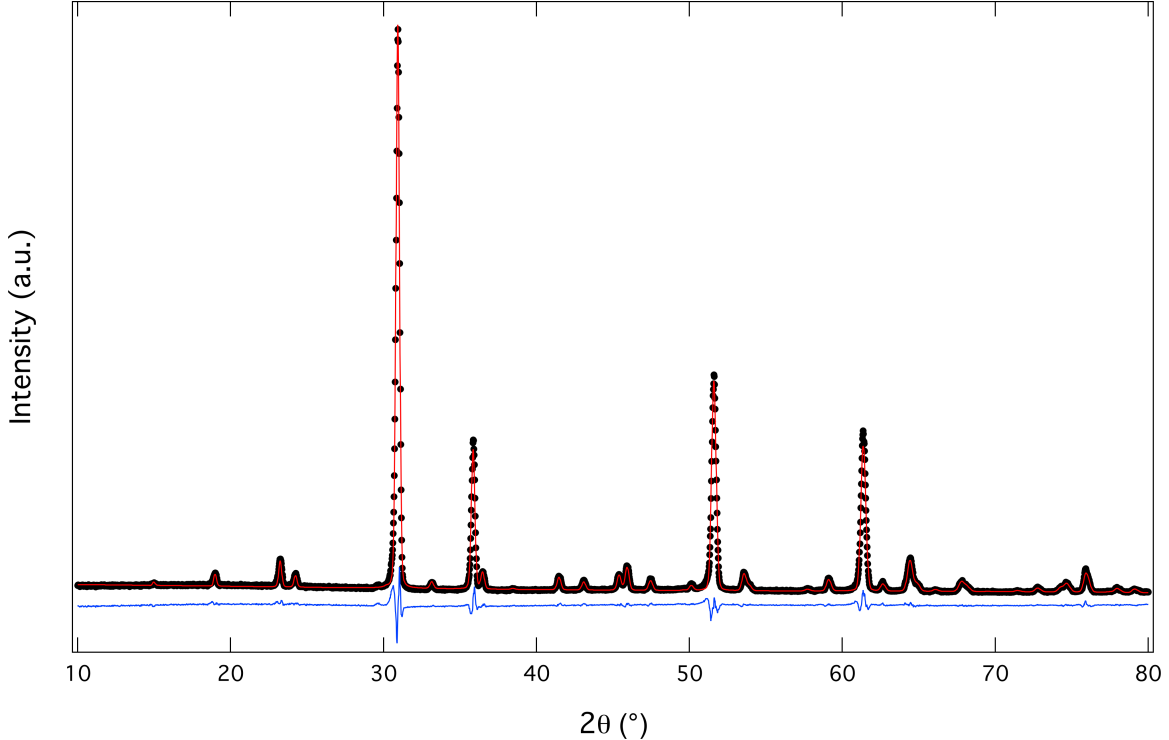


FIG. 2. Observed (black dots), calculated (red solid line) XRD pattern for pristine  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$  showing a good Rietveld refined fit with the structural model shown in table I. The blue solid line indicates the difference between the observed and calculated patterns.

#### 168 IV. PRISTINE $\delta - \text{Sc}_4\text{Hf}_3\text{O}_{12}$

169 The Rietveld refinement of the pristine diffraction pattern uses the prototype  $\delta$ -phase  
 170 model for  $\text{A}_6\text{BO}_{12}$  [17, 18] as a starting point. In these structures, the hexavalent metal  
 171 ion occupies consistently the 3a positions of the  $R\bar{3}$  space group. The trivalent metal ions  
 172 occupy the 18f Wyckoff positions. O vacancies are localized at 6c positions. In  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$ ,  
 173 Sc and Hf cannot order in the same way as their relative ratio is different, and they were  
 174 evenly distributed over each of these two cation sites in such a way as to maintain the 4:3  
 175 cation stoichiometry.

176 The refinement of this initial model against the pristine sample data allows us to check the  
 177 validity of the assumption that O vacancies are confined to the 6c Wyckoff position. Also,  
 178 the relative occupancy of Sc and Hf was refined independently for the 3a and 18f Wyckoff  
 179 positions occupied by cations. The refined and experimental patterns display a very good  
 180 agreement as displayed in Fig. 2. The refined model provides the calculated stoichiome-



181 try of  $\text{Sc}_{4.01}\text{Hf}_{2.99}\text{O}_{12}$ , in excellent agreement with the desired 4:3:12 stoichiometry. The  
 182 metal distributions onto the two families of metal sites are not random as initially expected:  
 183 scandium ions display a mild preference for the 18f sites, while the hafnium ions display a  
 184 preference for the 3a sites. The refined structural parameters are summarized in Table I.  
 185 To reduce the overall number of parameters, a common isotropic thermal displacement  
 186 parameter was used for all the atoms.

TABLE I. Structural parameters of the refined  $\delta$ -phase model for ( $R\bar{3}$ ,  $a=b=9.3626(4)$ ,  $c=8.6920(7)$   
 $\text{\AA}$ ,  $Z=3$ ).  $R_{wp}=9.64\%$ ,  $\text{GoF}=2.3$ ,  $R_B=2.4\%$ .

Site	$x$	$y$	$z$	Occ	$U_{iso}(\text{\AA}^2)$
(Hf, Sc) <sub>1</sub> 3a	0	0	0	0.54(1), 0.46(1)	0.003(1)
(Hf, Sc) <sub>2</sub> 18f	0.2568(2)	0.0426(3)	0.3523(2)	0.409(8), 0.591(8)	0.003(1)
O <sub>□</sub> 6c	0	0	1/4	0	
O <sub>1</sub> 18f	0.815(2)	0.789(2)	0.617(2)	1	0.003(1)
O <sub>2</sub> 18f	-0.160(2)	-0.462(2)	0.226(2)	1	0.003(1)

187 For the purpose of this study we refer to the  $\text{A}_4^{+3}\text{B}_3^{+4}\text{O}_{12}$  stoichiometry as  $\delta$ -phase. The  
 188 diffraction pattern consists of two types of reflections, strong intense peaks belonging to an  
 189 average fluorite lattice, and weak super-lattice peaks whose intensity depends on the specific  
 190 ordering of anion vacancies and the corresponding relaxation of the cations from the ideal  
 191 fluorite positions.

192 The  $c/a$  ratio obtained from the refinement of the pristine  $\delta$ -phase is 0.92837(9), which  
 193 is more elongated than the corresponding value for an ideal fluorite structure. In addition,  
 194 the atomic volume for pristine  $\delta\text{-Sc}_4\text{Hf}_3\text{O}_{12}$  was determined to be 11.5765  $\text{\AA}^3/\text{atom}$ .

195 Fig. 3 displays a projection of the refined structure showing the occupancy of cations  
 196 over the 3a and 18f Wyckoff positions and the atomic relaxations. The metal ions at 3a  
 197 positions are 6-fold coordinated with the O2 anions forming a regular octahedron with 6  
 198 identical metal-oxygen bonds (2.019(11)  $\text{\AA}$ ). Here, the environment of the 3a site is very  
 199 compact as outlined by the large values of the Hf and Sc bond valence sums that are 4.63(7)  
 200 and 3.79(6) respectively. On the other hand, a distorted polyhedron (capped octahedron)  
 201 with 7 different bonds ranging from 2.022(16) to 2.476(14)  $\text{\AA}$  is formed by the cations at  
 202 the 18f positions with O1 and O2 anions. These bonds are much shorter than what can

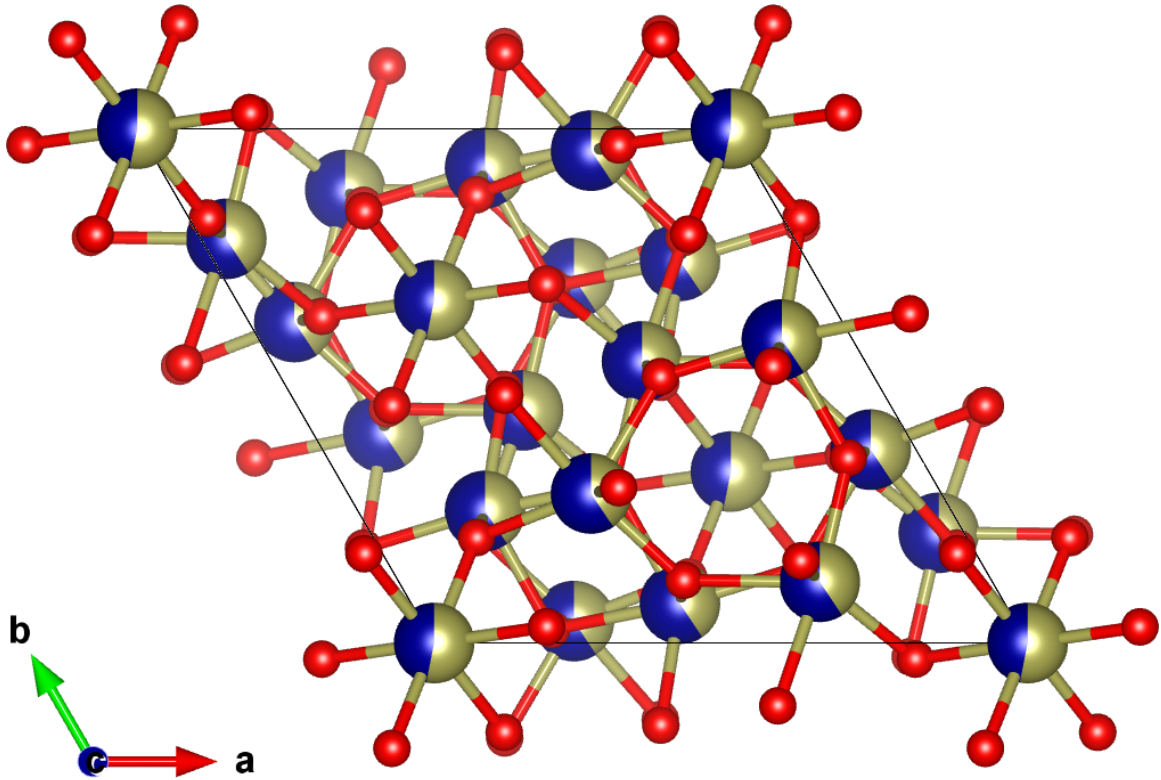


FIG. 3. 3D ball and stick structural model of  $\text{Sc}_4\text{Hf}_3\text{O}_{12}$  projected along the  $c$ -axis. The dual colored atoms display cations with a fractional occupancy of Sc (Blue) and Hf (Gold).

203 be expected for Sc and Hf, suggesting that these atoms are actually in an environment  
 204 much smaller than desirable and more adapted to cations with smaller sizes and/or higher  
 205 formal valence. It is useful to point out that the longest bond is demonstrably longer than  
 206 the other six, and it contributes effectively only for 6% to the overall bond valence sum  
 207 of the cations at 18f positions. This long bond is formed with an O2 atom. For that  
 208 reason, the cations at 18f positions can be approximately described as a 6-fold coordinated  
 209 distorted octahedron. The volume of the polyhedron at 3a is  $10.356 \text{ \AA}^3$  while that at 18f  
 210 is  $11.581 \text{ \AA}^3$  (it would be  $15.281 \text{ \AA}^3$ , should the longest bond be taken into account in the  
 211 capped octahedron description). The octahedron at the 3a position has a corner-sharing  
 212 connectivity with the 6 neighbouring 6-fold coordinated polyhedra of the second type (18f),  
 213 whereas the 18f polyhedra display an edge-sharing connectivity among themselves in addition  
 214 to the corner sharing connectivity already described. This description is adopted in the rest  
 215 of this paper. (If the 18f polyhedra were assumed to be 7-fold coordinated capped octahedra,  
 216 the connectivity would be exclusively edge sharing for all polyhedra, but the analysis of the

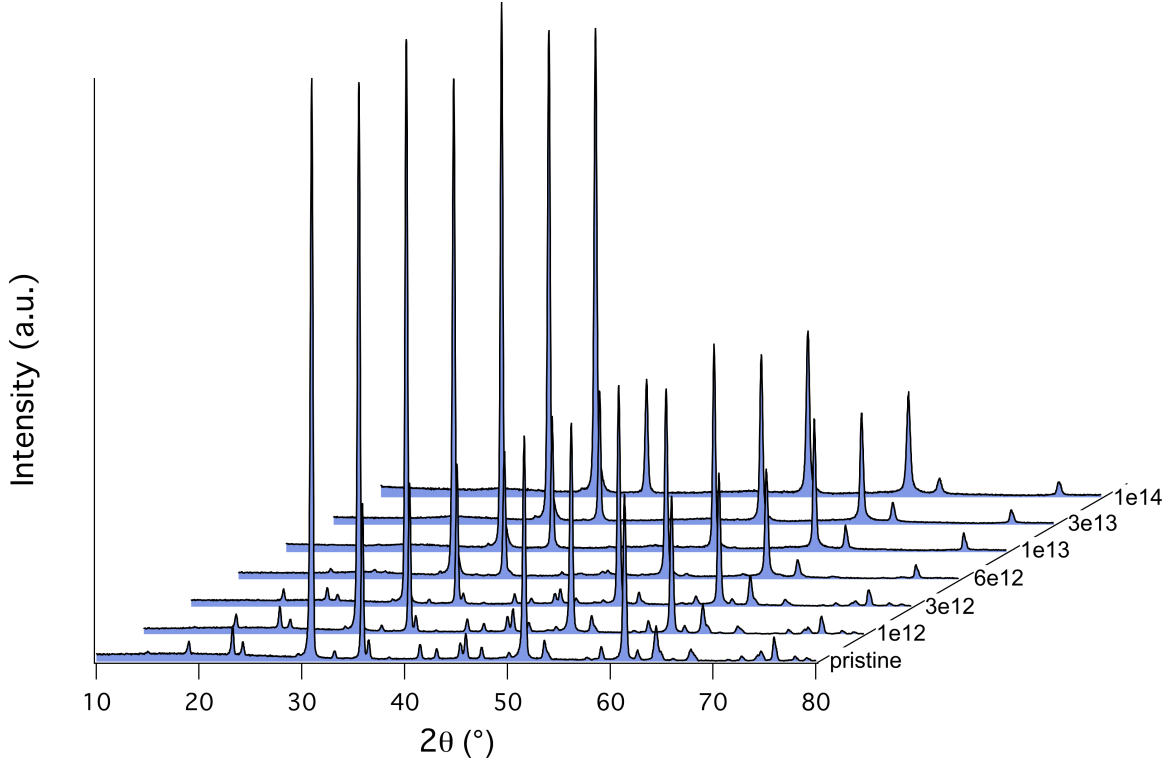


FIG. 4. x-ray diffraction patterns obtained from pristine and 92 MeV Xe irradiated  $\text{Sc}_4\text{Hf}_3\text{O}_{12}$  at fluences ranging from  $10^{12} - 10^{14}$   $\text{Xe}/\text{cm}^2$ . The vanishing of superlattice reflections characteristic of the trigonal  $\delta$ -phase occurs above  $6 \times 10^{12}$   $\text{Xe}/\text{cm}^2$ . Before that apparent long-range symmetry changes, the intensity of those superlattice reflections decreases continuously due to a progressive change in the crystal structure.

217 volumes of these capped octahedra is quantitatively less convenient, though it leads to the  
 218 same conclusions.)

## 219 V. IRRADIATED $\delta - \text{Sc}_4\text{Hf}_3\text{O}_{12}$

220 Fig. 4 shows the measured diffraction patterns of the pristine and irradiated  $\delta$ -phase  
 221 samples. A gradual decrease of the superlattice reflections characteristic of the  $\delta$ -phase  
 222 is observed in the initial stages of the irradiation. These superlattice reflections are also  
 223 increasingly broadened while the reflections corresponding to a fluorite average structure  
 224 are only marginally affected by a microstrain effect related to an inhomogeneous defect  
 225 buildup. This suggests the characteristic correlation length of the  $\delta$ -phase, is continuously  
 226 reduced as the irradiation proceeds. The underlying mechanism controlling these changes

227 is not clear, but partial healing of the defects can be achieved by the significant atomic  
228 transport occurring in the anion sublattice. The corresponding correlation length of the  
229 damaged  $\delta$ -phase remains much larger than the transverse dimension of the region impacted  
230 by a single ion track as long as these superlattice reflections are observed. Above  $6 \times 10^{12}$   
231 Xe/cm<sup>2</sup>, these superlattice reflections vanish, leaving behind only the parent fluorite peaks  
232 and diffuse scattering. This indicates that irradiation-induced defects cause the ordered  
233  $\delta$ -phase structure to transition to something resembling a defect fluorite phase that still  
234 possesses residual short-range order. Rietveld refinements of diffraction patterns up to the  
235 fluence of  $6 \times 10^{12}$  Xe/cm<sup>2</sup> were carried out using the  $\delta$ -phase model obtained from the pristine  
236 sample. The refinement of the pattern at  $10^{13}$  Xe/cm<sup>2</sup> does not provide the proper feedback  
237 for determining the phases of the atomic displacements and this leads to larger thermal  
238 displacement parameters in the average fluorite structure. Hence, from here onward, the  
239 observed reflections were only refined using a fluorite average structure while the diffuse  
240 scattering can be modeled using a correlated microdomain approach.

241 Ion irradiation in this  $\delta$ -phase produces two different types of observable changes. The  
242 first type of modification concerns long-range perturbation of the lattice related to elastic  
243 and polar interactions among structural defects. These changes alter the volume of the  
244 reference cell and its shape that was characterised by the  $c/a$  ratio in this present case.  
245 The second type of modifications are short-range and affect more directly the relaxation of  
246 the atomic structure characterized by composition and relaxation of the atomic positions.  
247 They can then also induce polymorphism of the structural motifs, and change the polyhedra  
248 connectivity's thus building-up competition between local configurations.

249 Changes in the average atomic volume and  $c/a$  lattice parameter obtained from these  
250 refinements are displayed in Fig. 5. The atomic volume and the  $a$ -lattice parameter increase  
251 with increasing fluence. At lower fluences, a progressive convergence of  $c/a$  towards the ideal  
252 fluorite ratio (0.9258) is observed. Then, at  $10^{13}$  Xe/cm<sup>2</sup>, a sudden decrease in the  $c$ -lattice  
253 parameter occurs, pinning the  $c/a$  to the ideal value. This change is concomitant with the  
254 disappearance of the superlattice reflections.

255 On the other hand, the thermal displacement parameter (Uiso) displayed in Fig. 6 shows a  
256 gradual increase before practically saturating after the transformation to long-range fluorite.  
257 This indicates a high degree of displacive disorder in the long-range average fluorite structure.  
258 The overall atomic displacement parameter ADP(Uiso) is  $0.003 \text{ \AA}^2$  for the pristine sample

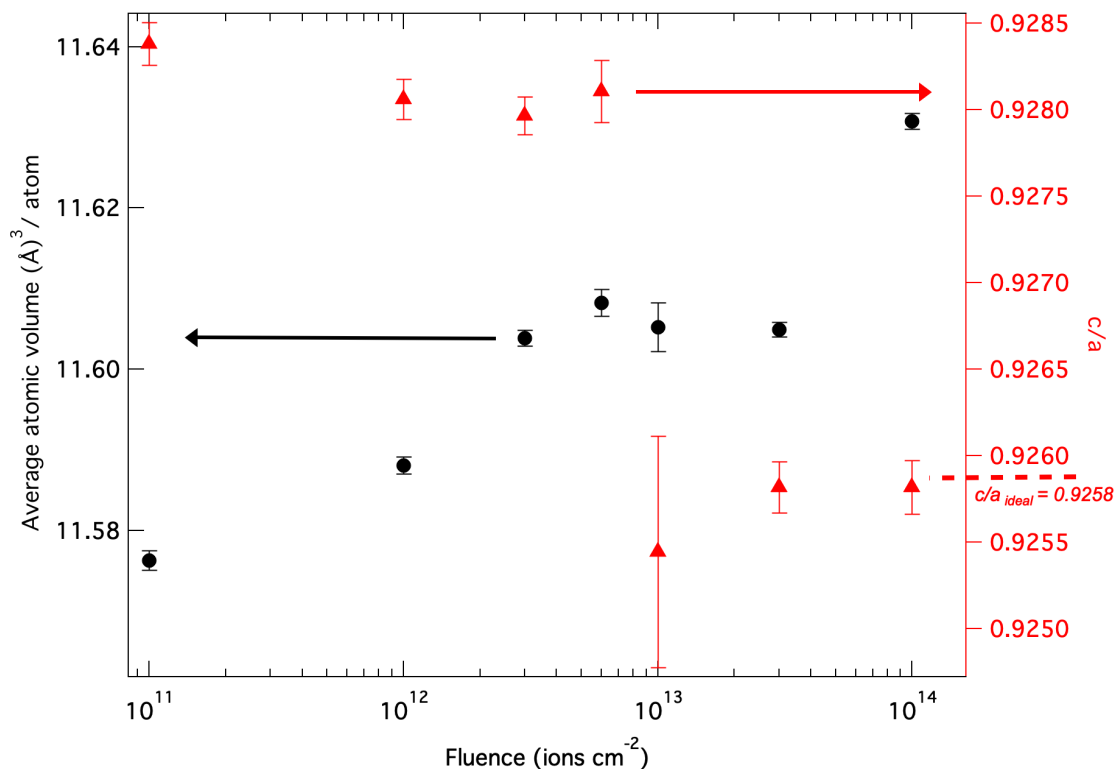


FIG. 5. Changes in the average atomic volume (black circles) and  $c/a$  lattice parameter (red triangles) as a function of Xe fluence. The average atomic volume displays a monotonic increase as a function of the fluence, regardless of the symmetry changes. The  $c/a$  on the other hand shows an abrupt change above  $6 \times 10^{12}$  ions/cm<sup>2</sup> marking a change in the long-range symmetry. Ideal  $c/a$  for fluorite is shown as dotted line. For comparison purposes, the lattice parameters were always calculated in the trigonal symmetry of the pristine phase, though above  $10^{13}$  ions/cm<sup>2</sup> the lattice becomes cubic. Note that the  $c/a$  ratio and atomic volume for pristine  $\delta$ -Sc<sub>4</sub>Hf<sub>3</sub>O<sub>12</sub> (not shown here) are 0.92837(9) and 11.5765 Å<sup>3</sup>/atom, respectively and are extremely close to those obtained for the sample irradiated with  $1 \times 10^{11}$  ions/cm<sup>2</sup>.

259 and it increases steadily at higher fluences to saturate around 0.03 Å<sup>2</sup>. Figure S2 in the  
 260 supplementary information file is included to display the evolution of ADP (Uiso) as a  
 261 function of the fluence on a linear scale which shows the value for the pristine sample.

262 The six identical metal to oxygen bond lengths for 3a octahedra (those at the corners of  
 263 Fig. 3) increase from 2.019(11) Å to 2.164(16) Å while the average of the 6 shorter bond  
 264 lengths for the cations at 18f positions decreases from 2.15 Å to 2.13 Å. It can be seen  
 265 that the shared edges among 18f octahedra are shortened after irradiation, which is a result

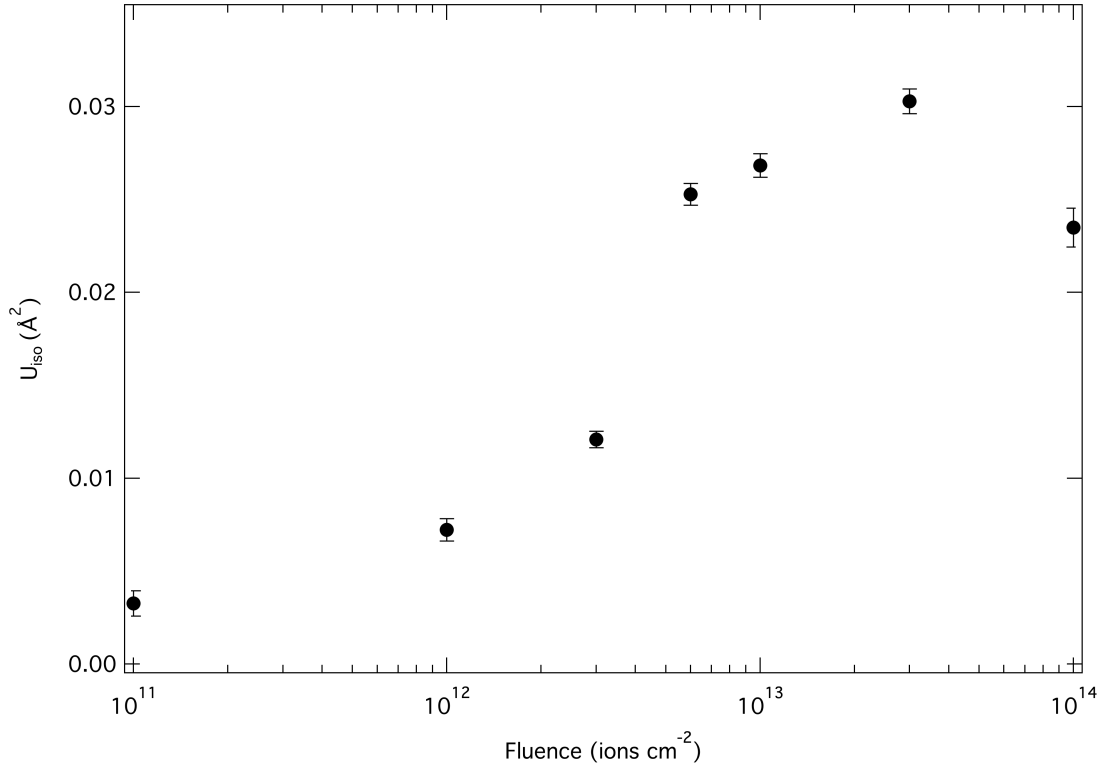


FIG. 6. Thermal displacement parameters ( $U_{\text{iso}}$ ) as a function of fluence for pristine and 92 MeV Xe irradiated  $\text{Sc}_4\text{Hf}_3\text{O}_{12}$ .  $U_{\text{iso}}$  parameters were obtained after Rietveld refinement and indicates an increase of disorder in the  $\delta$ -phase which gradually saturates when the structure is transformed to a defect fluorite phase.

266 of the swelling of 3a-type octahedra. These modifications to the structural motif cause an  
 267 overall increase in the distortion of the structure that is not akin to the convergence toward  
 268 a long-range fluorite as observed for the lattice parameters. At lower fluence, a quantitative  
 269 evolution of polyhedral volumes can be obtained in the  $\delta$ -phase structure. A 23% increase in  
 270 the volume of octahedra around the 3a site is observed between the pristine and the sample  
 271 irradiated at a fluence of  $6 \times 10^{12}$  Xe/cm<sup>2</sup>, whereas a decrease of 10% in the octahedral  
 272 volume around the 18f site is also observed. The change in volume of these polyhedra at  
 273  $6 \times 10^{12}$  Xe/cm<sup>2</sup> converges to the volumes observed in the two bixbyite polyhedra (10.42  
 274 and 12.95 Å<sup>3</sup>). Hence, the local and long-range changes are thus divergent and the local  
 275 structure is not averaging to an ideal fluorite where cation and anion vacancies are distributed  
 276 at random.

277 Indeed, at  $10^{13}$  Xe/cm<sup>2</sup> a diffuse scattering signal appears (Fig. 7). The angular posi-

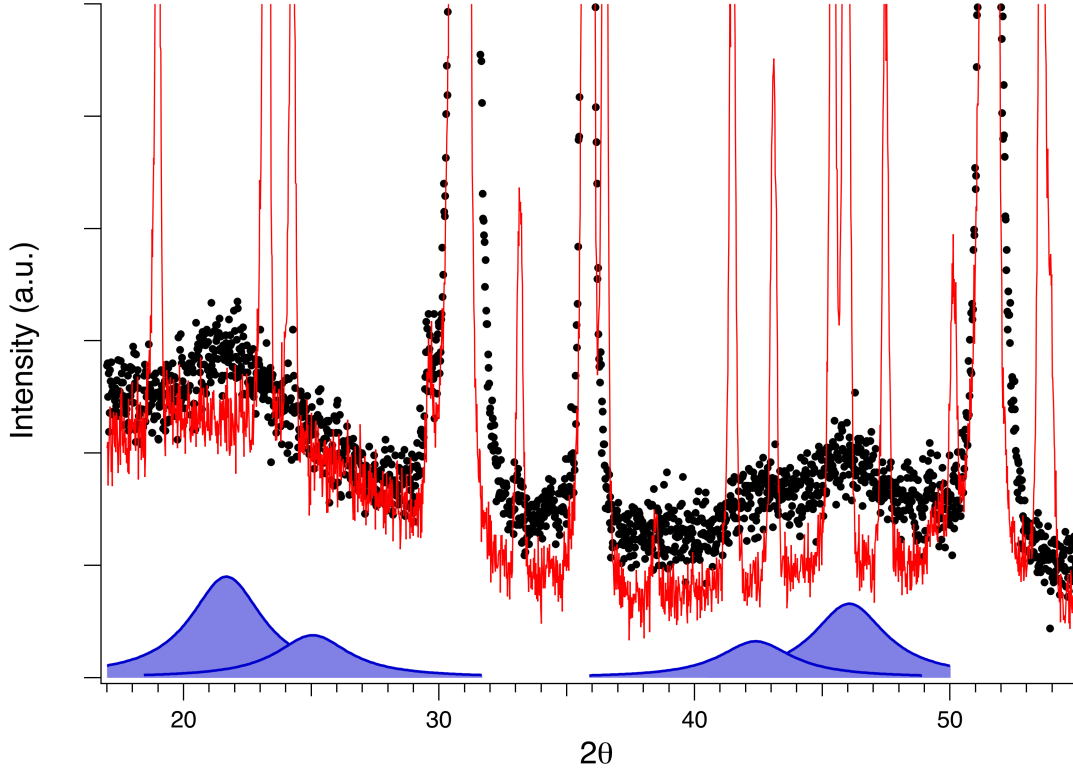


FIG. 7. XRD patterns obtained from  $\text{Sc}_4\text{Hf}_3\text{O}_{12}$ , pristine delta phase (solid red) and irradiated with  $10^{14}$  Xe/cm<sup>2</sup> (black dots) showing emergence of diffuse scattering (blue peaks) at the angular positions corresponding to (211), (220), (332), and (413) superlattice reflections of bixbyite-related structures ( $Ia\bar{3}$ ,  $a_B=2a_F$ )

278 tions of the diffuse scattering components of the scattering do not change at fluences above  
 279  $10^{13}$  Xe/cm<sup>2</sup>. These positions do not overlap with the positions of the pristine  $\delta$ -phase  
 280 superlattice peaks but rather correspond to new positions compatible with superlattice  
 281 reflections of a bixbyite-type structure. In spite of the O stoichiometry, these positions  
 282 are not compatible with a pyrochlore structural arrangement because they do not satisfy  
 283 the F-center extinction rules. Also, the diffuse signal at (211) is not compatible with a  
 284  $a_W = \sqrt{2}a_F, b_W = 2a_F, c_W = \sqrt{2}a_F$  Imma weberite arrangement.

285 The bixbyite-like arrangement hypothesis is also in agreement with the observation of  
 286 diffuse spots at the bixbyite reciprocal lattice points by TEM in low-energy irradiation  
 287 experiments on  $\delta$ -phase samples [20, 21]. While pyrochlore and weberite structures are  
 288 characterized by a cation site preference onto the A and B sites of the generic  $A_2B_2O_7$   
 289 chemical formula, in the bixbyite-related structures  $M_2O_{3.5}$  a pronounced cation selectivity

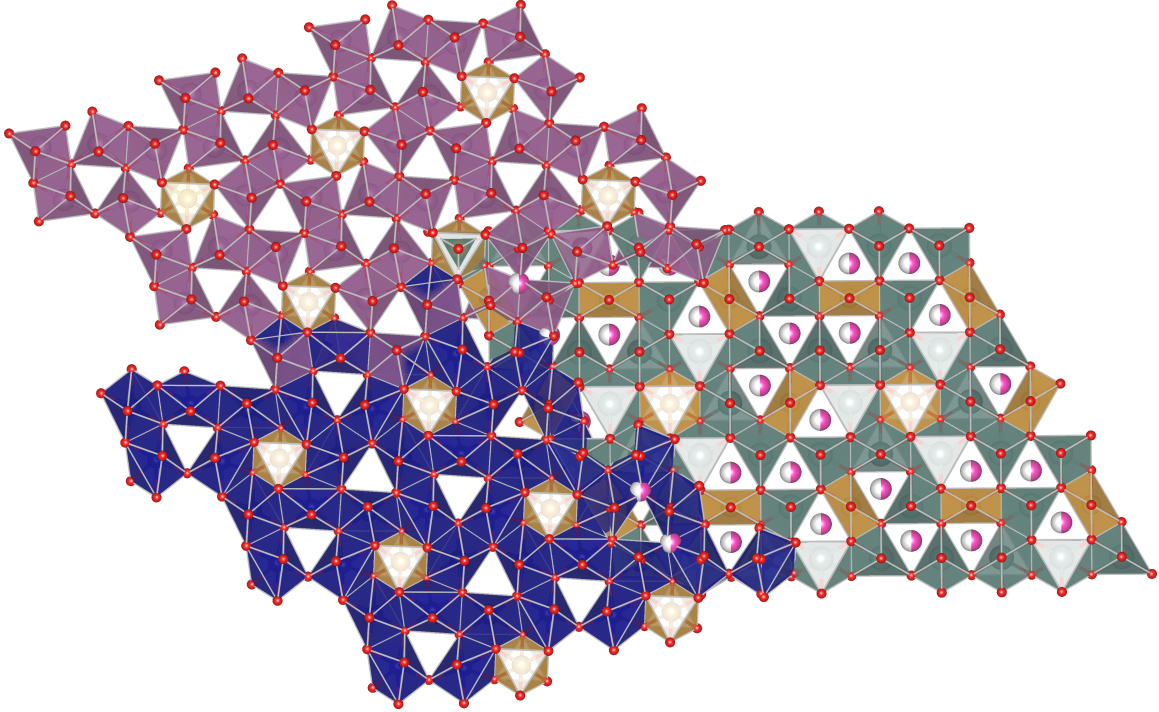


FIG. 8. Schematic changes induced by the ion irradiation on the occupancies of the anion sublattice. The blue and purple structures represent the pristine structure with the two polyhedra descriptions, the green structure on the right the bixbyite-like arrangement where half of the oxygen vacant sites are on average randomly filled (displayed as half coloured pink spheres).

290 is not expected and the bixbyite order displayed schematically in Fig. 8 is only given by the  
 291 stacking of the O vacancies and the atom position relaxation they induce. This particular  
 292 order might be related to the moderate cation selectivity and the pronounced O vacancy  
 293 ordering already observed in the pristine  $\delta$ -phase of this compound. The correlation length  
 294 of this local structure is about 4 nm, as derived from the integral breadth of the diffuse  
 295 signal. Previously, ion tracks consisting of a disordered fluorite core with 3–4 nm in diameter  
 296 were reported in swift heavy ion irradiated  $\delta$ - $\text{Sc}_4\text{Zr}_3\text{O}_{12}$  [22]. The corresponding lattice  
 297 parameter of the present bixbyite-related local phase is about 9.99(3) Å. Therefore, this  
 298 phase is almost 2.4 % denser than the average long-range radiation-induced oxygen deficient  
 299 fluorite phase and also 1.9 % denser than the pristine  $\delta$ -phase, marking another departure  
 300 from the evolution in volume of the long-range average-fluorite phase.

301 We note here that the damage evolution revealed by our XRD measurements is also not  
 302 compatible with conventional radiation-induced phase transformation models, such as the



303 "Gibbons" cascade overlap models [39, 40]. These models require that the latent damage in  
304 the cascade regions produces a second phase that is not correlated and generally incoherent  
305 with the pristine (unirradiated) material. On the contrary, our latent damage regions are  
306 likely coherent with the undamaged regions (evidence for this is provided in TEM images in  
307 Tang et al. [22], where they observed coherence between latent tracks and pristine material  
308 in swift heavy ion-irradiated  $\text{Sc}_4\text{Zr}_3\text{O}_{12}$  (the oxide structure and irradiation conditions in  
309 Tang et al. are very similar to the compound and experimental conditions used in this  
310 study). Furthermore, were we to have coexisting delta and disordered fluorite phases in our  
311 low-fluence microstructures (i.e., fluences ranging from  $10^{11} - 6 \times 10^{12}$  ions/cm<sup>2</sup>), we should  
312 expect to resolve two sets of XRD peaks: one from the rhombohedrally-distorted  $\delta$ -phase  
313 ( $c/a$  greater than ideal), the second from the cubic disordered fluorite phase (with the ideal  
314  $c/a$  ratio). We do not observe this hypothetical mixture at any fluence, based on our XRD  
315 measurements.

## 316 VI. DISCUSSION AND CONCLUSION

317 According to the previous work of Ishimaru et al. [20] low energy ion irradiation (300  
318 keV Kr and up to a fluence of  $3 \times 10^{16}$  ions/cm<sup>2</sup>) induces structural changes in the  $\delta$ -phase  
319 compound  $\text{Sc}_4\text{Zr}_3\text{O}_{12}$ . Using cross section TEM, two different phases were observed in the  
320 sample. These phases occur in two separate layers located above the pristine sample sub-  
321 strate: the diffraction pattern from the layer immediately above the substrate only presented  
322 spots characteristic of a fluorite phase, while the layer closer to the surface presented addi-  
323 tional diffuse spots obeying the selection rules of  $\text{Ia}\bar{3}$  space group. This was then indexed  
324 with a bixbyite-type structure. The authors concluded that this phase was likely formed  
325 by some sort of re-arrangements of oxygen vacancies within the fluorite layer. The exist-  
326 tence of the two layers seems related to the characteristics of the low energy irradiation,  
327 where damage occurs in the absence of implanted ions in the bixbyite-type layer, where as  
328 damage coincides with significant ion implantation in the fluorite-like layer. In the present  
329 experiment, no implantation occurs within the layer probed by x-rays and indeed, only a  
330 disordered fluorite with bixbyite local flavour is observed.

331 Group-subgroup analysis establishes that there is no direct compatibility relation between  
332 bixbyite and  $\delta$ -phase, thus preventing the existence of an order parameter describing the

333 direct transformation. The only possible pathway to connect the two phases is through  
334 an intermediate fluorite phase that shares the specific symmetry elements of bixbyite and  
335  $\delta$ -phase. Bixbyite and  $\delta$ -phase share a unique feature among the phases observed in the  
336 pseudo binary phase diagrams of type  $A_2^{+3}O_3-B^{+4}O_2$ : these two phases are the only ones  
337 where the metal ions are 6-fold coordinated with O anions.

338 The  $\delta$ -phase can also be viewed as having a capped octahedra which is found in the  
339 A-type  $M_2O_3$  compounds. A known high temperature phase transformation occurs from  
340 the A-type into a C-type bixbyite in some of these rare earth oxides. Hence it is possible  
341 to change from 7-fold to 6-fold in these sesquioxides and the same is likely to occur in  
342 the  $\delta$ -structure. Therefore, it is likely that these two phases actually exhibit some sort of  
343 competition. Though the two phases have qualitatively similar polyhedra, they do not have  
344 exactly the same connectivity, and this explains the different O stoichiometries.

345 The bixbyite phase generally presents an extended domain of existence in the oxygen-  
346 excess range, as for instance in  $CeO_{2-x}$ ,  $TbO_{2-x}$ , and  $PrO_{2-x}$  [41, 42] ( $0.28 \leq x \leq 0.5$ ). Thus,  
347 the bixbyite signature from a structure with extra O atoms filling the bixbyite O vacancies  
348 would translate into weak superstructure peaks, similar to the diffuse scattering observed,  
349 as the amplitudes of the cation relaxations near the O vacancies would be smaller. This  
350 observation suggests that the bixbyite phase acts possibly as a chemical attractor, having  
351 some kind of exotic dynamics for local chaotic fluctuations of the oxygen stoichiometry. The  
352 bixbyite local configuration reached after ion irradiation is then a frozen metastable steady  
353 state where the phase trajectories evolving away from the  $\delta$ -phase composition remain in  
354 the vicinity of the bixbyite attractor. This particular characteristic of the bixbyite phase  
355 seems effective in supporting radiation tolerance, by creating a very large number frozen  
356 local configurations of lower symmetry: preserving a very large number of configurations  
357 that maximize and thereby stabilize the apparent long-range cubic symmetry. Systems ex-  
358 hibiting these characteristics can then be exploited to effectively engineer radiation resistant  
359 materials.

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# Divergent short and long-range behaviour in ion-irradiated



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## I. PROFILE FUNCTION MODEL

The instrumental function (Thompson-Cox-Hastings pseudo Voigt type) for the setup we used for these data collections is modeled using a simple Gaussian function ( $U, V, W$ ) where two of the three parameters were determined using a set of 22 well resolved peaks in the region  $21^\circ \leq 2\theta \leq 140^\circ$  of a LaB<sub>6</sub> standard (NIST). The  $V$  parameter was not required for achieving an accurate fit of the diffraction pattern. The Gaussian angular components  $W$  (constant) and the  $U$  ( $\tan^2 \theta$  dependence) are:

$$W = 0.0508(7)(^\circ), U = 0.0150(3)(^\circ)$$

The values of these parameters were kept fixed during the Rietveld refinements of the diffraction patterns of the  $\delta$ -phase samples. Only two additional terms,  $P$  and  $Y$ , that account for a Gaussian finite-size broadening and for a Lorentzian microstrain-type broadening respectively, were used to model the powder diffraction patterns.

## II. ATOMIC DISPLACEMENT PARAMETER

Figure S1 shows the evolution of ADP ( $U_{iso}$ ) as a function of the fluence on a linear scale which shows the value for the pristine sample. The overall atomic displacement parameter ADP was refined for all ions as there was no strong support for using different values for the anions and cations during the refinement of the pristine sample. The overall ADP ( $U_{iso}$ ) is  $0.003 \text{ \AA}^2$  for the pristine sample and it increases steadily at higher fluences to saturate around  $0.03 \text{ \AA}^2$ .

## III. OCCUPANCY OF VACANT 6c SITES

The particular ordering of the vacancies onto the 6c sites was noticed by Eyring (Eyring & Tai, Annu. Rev. Phys. Chem 24 189-206 (1973)) when discussing the  $\iota$ -phase of  $M_7O_{12}$  of various compounds noticing that all of them are isostructural ( $Ce_7O_{12}$ ,  $Tb_7O_{12}$ ,  $Sc_4Zr_3O_{12}$ , and  $Y_6UO_{12}$ ). It is also characteristic of the closely related  $\gamma$ -phase  $Sc_2Zr_5O_{13}$ . This feature is apparently strongly related to the long range trigonal symmetry of those phases. Since then, the 6c site has been confirmed as systematically totally empty in the family of ordered  $\delta$ -phase compounds with generic formula  $A_6BO_{12}$  using several techniques that include neutron



powder diffraction. The particular choice of stacking the O vacancies at the 6c positions is actually a requirement for explaining the intensities of the TEM diffraction patterns of this compound and  $\text{Sc}_4\text{Zr}_3\text{O}_{12}$ . Moreover, this point was checked during the refinement starting different refinements with various positive values for a partial occupancy of this site converge consistently towards the empty site solution. Therefore, it was chosen to fix the occupancy of this site to zero. The situation could nevertheless change rapidly at higher temperature because the oxygen mobility increases rapidly in these compounds. Note, the appearance of bixbyite-type diffuse scattering is evidence for a different distribution of the O vacancies where the 6c site is no longer empty.

#### IV. SUPPLEMENTARY FIGURES

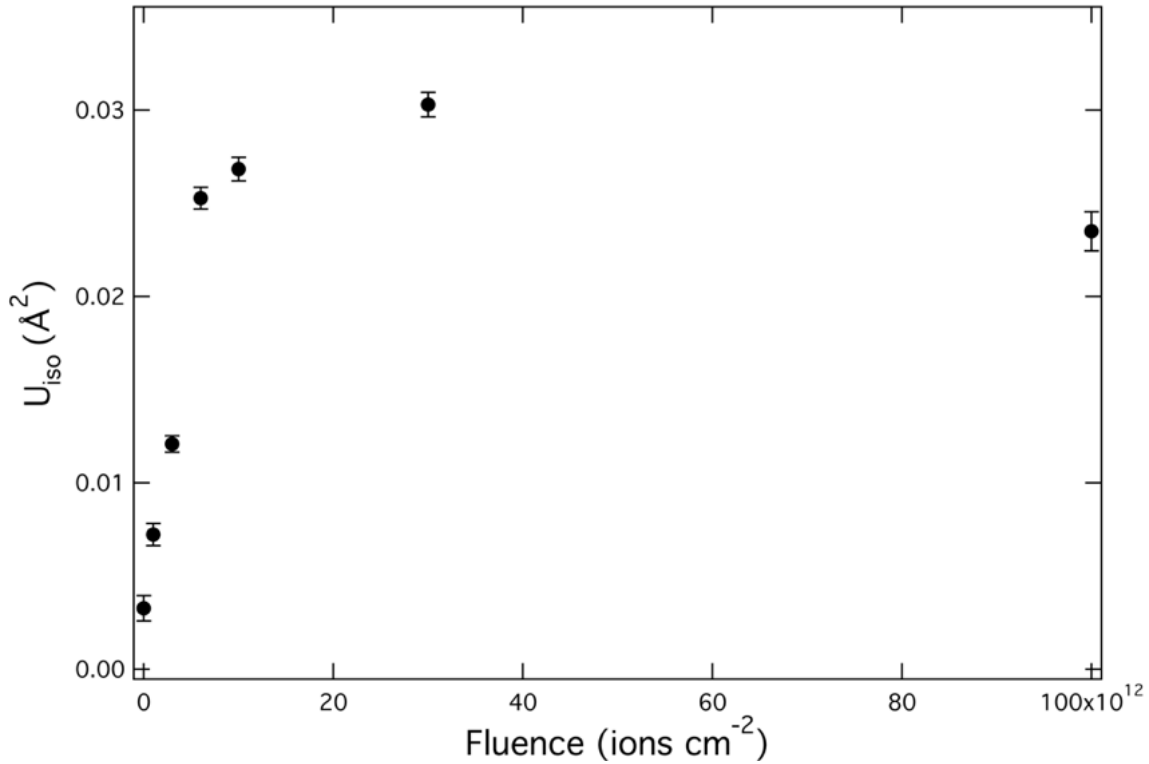


FIG. S1. Evolution of  $U_{iso}$  as a function of the fluence on a linear scale that includes the pristine sample.

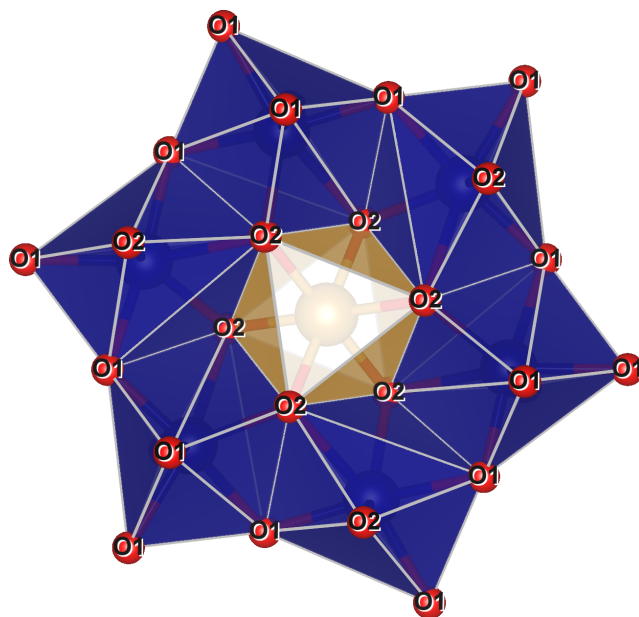


FIG. S2. Conventional building block of the  $\delta$ -phase consisting of seven polyhedra.