

# A QM/MD coupling method to model the ion-induced polarization of graphene

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## Abstract

We report a new Quantum Mechanical/Molecular Dynamics (QM/MD) simulation loop to model the coupling between the electrons and atoms dynamics in solid/liquid interfacial systems. The method can describe simultaneously both the quantum mechanical surface polarizability emerging from the proximity to the electrolyte, and the electrolyte structure and dynamics. We tested the approach by simulating a non-changed graphene flake in contact with NaCl electrolyte solutions at varying concentrations, where we found that ions preferentially remained in solution and are only cations are mildly attracted to the surface of the graphene. This behaviour is found to originate from the relatively small adsorption energy compared to the value of the ion hydration energy, suggesting that larger ionic species, with lower solvation free energies, may be more likely to adsorb on the graphene surface in agreement with experimental data. The coupling procedure can be used to simulate a wide-range of experimental set-ups including electrified interfaces and can be employed to model all those solid-liquid interfacial systems where the electronic structure calculation can be carried out with approximate methods such as Density Functional Tight Binding whose reduced computational cost makes the coupling with a classical simulation engine computationally feasible.

## 1. Introduction

Graphene-based supercapacitors<sup>1-6</sup> (electrical double layer capacitors) are an emergent technology capable of energy storage and charge/discharge rates at levels that are orders of magnitude larger than conventional capacitors and batteries.<sup>7</sup> Their function leverages on the high relative surface area that accompanies low dimensional materials and on an electrostatic charge storage mechanism based on the physisorption of ionic species at the surface.<sup>5,8-10</sup> When the electrolyte is an aqueous solutions, experimental and theoretical investigations have proven that the kinetics and thermodynamics of the physisorption process are the result of a delicate balance between hydration free energy and surface effects. However, results can often appear contradictory; even small (atomic-scale) defects in the structure of the graphitic surface, its geometry, dimensionality and chemical modifications may extensively affect the experimental measurements. For example Yang *et al* report that the basal capacitance of graphene films made from graphene oxide is independent of the nature of the adsorbing cations,<sup>11</sup> however similar electrochemical measurements, performed on activated carbon, indicate that the capacitance is to some degree ion-specific ( $\text{Li}^+$  less adsorbed than  $\text{Na}^+$  and  $\text{K}^+$ ).<sup>12</sup> In contrast, experiments performed on single walled carbon nanotube (SWCNT) suggest that  $\text{Li}^+$  should have higher affinity to the surface than  $\text{Na}^+$  and  $\text{K}^+$ ,<sup>13</sup>

51 moreover, also show that the nature of the counterions also affect the results. Recently,  
52 Iamprasertkun *et al*, using Highly Ordered Pyrolytic Graphite (HOPG) as proxy for the  
53 graphene surface, found that the HOPG basal capacitance is ion-dependent with a trend  
54 that follows the ionic size and hydration free energy.<sup>14</sup>

55  
56 Rationalizing these ostensibly conflicted experimental results is a difficult task, which  
57 has led to an extensive catalogue of molecular simulations that attempt explain and  
58 predict ions adsorption at these interfaces. Classical molecular simulations have shown  
59 the importance of including a detailed atomistic description of the interface, which  
60 accounts for both the interactions within the first solvation shell and for long-range  
61 effects.<sup>15</sup> In particular, ions and water polarization, solvent exclusion, and hydrogen  
62 bonding rearrangements determine whether a particular ion is found at aqueous  
63 interfaces.<sup>16–18</sup> Despite these promising results, classical models often fail when  
64 simulating solid/liquid interfaces where polarizability effects play an important role,  
65 for instance in the modulation of the Coulomb interactions between electrolyte  
66 solutions and graphitic surfaces. In order to capture these important phenomena,  
67 molecular models employed to simulate interfacial systems need to include the  
68 polarizability of all the species involved. In the majority of classical simulations,  
69 however, only (if any) the polarizability of the electrolyte is included, assuming that  
70 the surface polarization has a negligible effect on water structuring and dynamics at the  
71 interface.<sup>19</sup> In the case of metallic/semimetallic surfaces, such as graphene or carbon  
72 nanotubes (CNT), which have an abundance of aromatic rings with delocalized  $\pi$ -  
73 electrons, this assumption is questionable. Recent Density Functional Theory (DFT)  
74 calculations have showed that small monovalent metal ions are able to significantly  
75 polarize carbonaceous nanostructures such as CNT<sup>20</sup> and graphene quantum dots.<sup>21</sup> In  
76 the latter case, the polarization effect is so important that the band-gap of the finite  
77 graphene sheet is also modified. The importance of surface polarization has recently  
78 been highlighted by other first-principles molecular dynamics (FPMD) simulations that  
79 showed that cations such as Na<sup>+</sup> preferentially reside at the interface when confined in  
80 a CNT.<sup>22</sup> This is in contrast to their behaviour at unstructured, non-polarizable surfaces,  
81 in which cations are repelled. Other simulations have also shown that by only  
82 incorporating the polarizability of the ions, molecular simulations predict the wrong  
83 adsorption tendency between Na<sup>+</sup> and K<sup>+</sup> on the surface of a CNT.<sup>23</sup>

84  
85 First principles based approaches are the only computational methods that can be used  
86 to capture the fluctuation of surface charges which is brought about by the presence of  
87 the electrolyte solutions. However due to their comparably high computational cost,  
88 FPMD simulations are typically restricted to several hundred water molecules,  
89 unrealistic low ionic concentrations and short dynamical trajectories on the order of  
90 hundreds of picoseconds. [a review?] Classical polarizable force fields for the surface  
91 and the electrolyte can be used to circumvent the problem of the conventional fixed-  
92 charge potential.<sup>24</sup> However, because of the semimetallic and 2D nature of graphene it  
93 is very difficult to know *a-priori* whether a model with atomic-centered polarizability  
94 can capture the polarization of graphene and a case-by-case parameterization might be  
95 needed. Recently we proposed a DFT free-energy optimized Lennard-Jones type  
96 potential to account of the polarization of all the system species.<sup>14</sup> The advantage of  
97 this approach is that the simulations are not slowed down by the inclusion of extra  
98 dummy charge points as in polarizable models and, since we used the implicit solvation  
99 model during the DFT calculations, both hydration and polarization effects were  
100 considered.<sup>25,26</sup> This model however has also shortcomings: it was parameterised using

101 a single ion so the effect of ionic screening due to multiple ions was only included via  
102 the (untested) standard Lorentz-Berthelot rules, and the model did not account for the  
103 polarization of the graphene surface due to the specific arrangement of the water  
104 molecules at the interface.<sup>27,28</sup>

105  
106 Finally, since in almost all applications and electrochemical experiments the graphitic  
107 surface is electrified, it is desirable to have a computational approach that is able in  
108 principle to describe the polarizability, while simultaneously accommodating for the  
109 presence of a net surface charge. Recently, Zhan *et al* used a fully integrated first  
110 principle/continuum model to investigate the cations adsorption on graphitic electrified  
111 surfaces.<sup>29</sup> The method accounts for the electronic structure of the surface and of the  
112 approaching single cation, treating these with DFT, and describes the rest of the  
113 electrolyte solution using the RISM approach (Reference Interaction Site Model)<sup>30</sup>  
114 These simulations, which can account also for the screening effect due to the ionic  
115 strength of the solution, show surface attraction for almost all cations investigated and  
116 indicated, in agreement with the experimental data of Iamprasertkun *et al*,<sup>31</sup> that the  
117 adsorption energy increases with the ionic radius. As presented, the method is yet to  
118 describe any of the dynamical aspects associated with ion adsorption process and also  
119 does not account explicitly for neither the water molecules and their rearrangement at  
120 the surface nor for the other ions in the electrolyte solutions.

121  
122 There is therefore the need to develop a new method that can capture simultaneously  
123 the structure and dynamics of the interface accounting for both the thermodynamics of  
124 the solution and the electronic polarization of the surface. Here we propose a novel  
125 Quantum Mechanical/ Classical Molecular Dynamics (QM/MD) approach that, taking  
126 advantage of the specific electronic structure of graphene, couples the semi-empirical  
127 calculation of the surface charge with the *classical* dynamics of the electrolyte. This is  
128 achieved creating a workflow where density functional tight binding (DFTB)  
129 calculations of the graphene atomic charges are nested in a loop of molecular dynamics  
130 simulations that allow the configuration of the electrolyte to evolve over time in  
131 response to the change in the graphene polarization. In what follows we present the  
132 core idea of the coupling, and apply the QM/MD procedure to the test case of an  
133 uncharged graphene sheet immersed in NaCl electrolyte solutions of different ionic  
134 strengths with the aim of quantifying the surface polarization and how it contributes the  
135 ion-adsorption mechanism.

## 136 137 **2. Method**

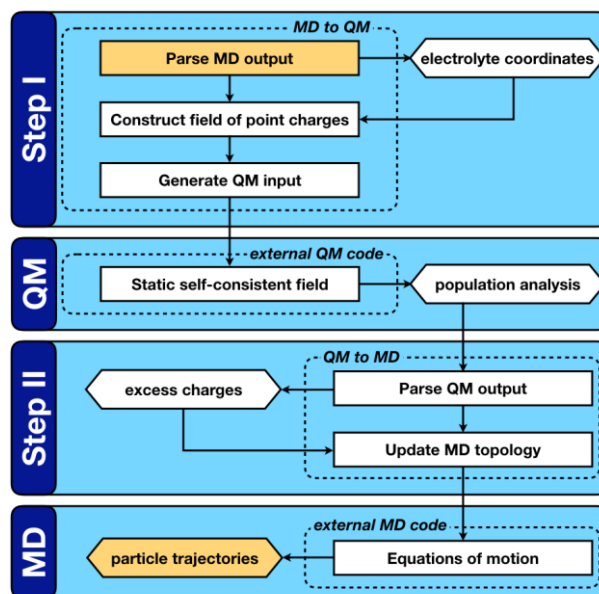
138  
139 In this work, we developed a novel QM/MD workflow to introduce within a classical  
140 model, the electrolyte-induced polarization of the graphene flake. The procedure takes  
141 into account the dependence of the surface polarization on the electrolyte configuration  
142 recalculating the partial charges associated to each carbon atom every  $\tau$  ps of a  
143 molecular dynamics simulation, during which the atoms in the electrolyte solution are  
144 allowed to move.

145  
146 Electronic structure calculations of the graphene atoms are carried out using the self-  
147 consistent charge density functional tight binding, SCC-DFTB, approach, which is an  
148 approximation to Kohn-Sham density functional theory.<sup>32</sup> We opted for SCC-DFTB  
149 over other electronic structure methods owing to its favourable accuracy-computational  
150 viability tradeoffs.<sup>33</sup> The DFTB method offers extremely rapid solutions of the

151 electronic problem since it utilizes parameterized Hamiltonian matrix elements.  
 152 Moreover, the second order, SCC approximation captures redistribution of electronic  
 153 density in the form of atomic charges. For the interested reader, there are several  
 154 instances where this method has been recounted in great detail.<sup>32,34</sup>

155  
 156 When coupled to a classical atomistic environment, which includes water and ions,  
 157 SCC-DFTB has proven very successful in describing charge transport phenomenon in  
 158 biomolecular systems.<sup>35-40</sup> These examples share striking similarities with the surface-  
 159 electrolyte interfaces present in graphene-based supercapacitors. Yet, an important  
 160 difference is that, in the most common applications of SCC-DFTB/MM simulations,  
 161 the primary interest is the dynamical behaviour of the quantum mechanically embedded  
 162 region, with the classical part providing the aqueous background environment. Instead,  
 163 in the study of non-faradic ion-surface interactions we are concerned with the  
 164 structuring and dynamical evolution of the classical components of the simulation, the  
 165 ionic species and the water molecules. Consequently, these QM/MD simulations are  
 166 most reliant on the ability of SCC-DFTB to reproduce the correct electronic band  
 167 structure and static polarizability of graphene,<sup>41</sup> and the striking features of 0  
 168 dimensional graphene flakes that arise due to quantum confinement effects.<sup>42-44</sup>

169  
 170 The computational workflow makes iterative calls between Molecular Dynamics (MD)  
 171 and SCC-DFTB software as shown schematically in Figure 1. More specifically, in the  
 172 MD to QM step the coordinates of the electrolyte, i.e. those associated with ions and  
 173 solvent molecules, are converted into a set of point charges  $\{Q_i^{sol}\}$ . The set  $\{Q_i^{sol}\}$  then  
 174 forms a background electrostatic potential for the quantum mechanical calculations.  
 175 For anions and cations the values of  $Q_i$  are chosen according to the formal charges  
 176 associated with the specific ions involved (for example  $\pm 1$  for monovalent ions),  
 177 while for the water molecules the partial charges associated to the oxygen and hydrogen  
 178 atoms are taken from the chosen water model (in this case SCP/E<sup>45</sup> see more below).  
 179



180  
 181 **Figure 1:** Schematic representation of the QM/MD workflow. Key computable quantities are  
 182 represented by hexagonal boxes and square boxes represent computational processes. The two boxes  
 183 coloured gold link sequential iterations.  
 184

185 In the QM step the quantum mechanically derived charges on the carbon and hydrogen  
186 atoms in the graphene flakes are extracted from the SCC-DFTB output data and used  
187 to update the force-field for the MD simulation. The graphene charges are obtained  
188 from a Mulliken population analysis<sup>46</sup> and converted into an excess-charge  
189 representation,  $\{\tilde{q}_i\}$ , the details of which are provided below. Whilst we recognize that  
190 Mulliken population analysis can be highly sensitive to the adopted basis set, in our  
191 case this charge partitioning scheme has the distinct advantage of ensuring the full  
192 equivalence between the DFTB and classical forces acting on the electrolyte atoms,<sup>47</sup>  
193 we verified this numerically below.

194  
195 Due to the finite size of the graphene flake, the large permanent polarization of the C-  
196 H bonds at the graphene flake edges give rise to the formation of a molecular  
197 quadrupole moment in the plane of the graphene flake. This has a disproportionately  
198 strong role in the ensuing ion adsorption behaviour,<sup>48-50</sup> resulting in the over-binding  
199 of cations and under-binding of anions when compared with semi-infinite graphene  
200 models.<sup>24</sup> In order to remove this edge effect, we define a set of so-called excess charges  
201 that are computed in between the QM and MD steps. Let  $q_i^{\text{vacuum}}$  be the computed  
202 Mulliken charge on an atom  $i$  in the pristine graphene flake in vacuum, and  $q_i$  be the  
203 Mulliken charge on the same atom computed from one of the solvated snapshots during  
204 the QM/MD loop. Then we define the excess charge  $\tilde{q}_i$  as

$$\tilde{q}_i = q_i - q_i^{\text{vacuum}} \quad 1$$

205  
206  
207  
208  
209 This set of excess charges is constructed such that the permanent C-H bond dipoles are  
210 neutralized, while the polarization brought about by the point charges is maintained  
211 since  $q_i^{\text{vacuum}} \approx 0$  for bulk atoms and  $q_i \approx q_i^{\text{vacuum}}$  for edge atoms.

212  
213 The system, described by the new set of carbon partial charges,  $\{\tilde{q}_i\}$ , is propagated  
214 using classical molecular dynamics, and the recalculation of the  $\{\tilde{q}_i\}$  is performed at  
215 fixed time intervals,  $\tau$ . Whilst the overall length of the QM/MD simulation is subject  
216 to the usual atomistic MD considerations (equilibration of energy, temperature and  
217 pressures), the choice of  $\tau$  is more delicate and discussed in more detail below.

### 218 219 220 **3. Computational Details**

221 In order to investigate the behaviour of ions at the graphene-electrolyte interface we  
222 use our QMMD strategy on a system comprised of a graphene flake solvated in NaCl  
223 solutions. The simulation box has dimensions  $7.21 \times 7.87 \times 10.00$  nm and is filled  
224 with fully dissociated NaCl electrolyte solutions at 3 different ionic concentrations: 0.0  
225 (e.g. single ion), 0.5 and 1.0 M. The graphene flake has an overall diameter of 5nm.  
226 The positions of the atoms in the graphene flake are kept fixed during MD simulations.  
227 Figure 3 shows snapshots on the simulation box.

228  
229 Molecular dynamics calculations in the NVT ensemble are carried out using the  
230 GROMACS code,<sup>51,52</sup> version 2018.4. A time step of 1 fs and the leapfrog algorithm  
231 are used to integrate the equations of motion at a constant temperature of 298.15 K,  
232 which is kept constant using the Nosé-Hoover thermostat ( $\tau_T = 0.1$  ps). Long-range  
233 electrostatic interactions are treated using the reaction field approach, with a cutoff of  
234 1.4 nm. Non-bonded interactions are computed using a Lennard-Jones 12-6 potential,

235 which is truncated smoothly at 1.2 nm using a switch function starting at a distance of  
236 1.0 nm.

237

238 In all simulations the graphene atoms are frozen, for the intermolecular parameters, we  
239 have used the following parameters: Water in our simulations is modelling using the  
240 SPC/E model<sup>45</sup> with the SETTLE algorithm used to maintain rigid molecule  
241 geometries.<sup>53</sup> This is compatible with the Werder water-graphene parameters that give  
242 rise to the experimentally measured water contact angle.<sup>1,5</sup> Cl and Na ion parameters,  
243 also compatible with the SPC/E model, are taken from the work of Cheatham *et al.*<sup>55</sup>

244

245 To avoid complications associated with interacting point charges subject to periodic  
246 boundary conditions, single-point SCC-DFTB calculations have been carried out in  
247 open-boundary conditions using the DFTB+ code.<sup>33</sup> In the volume occupied by the  
248 simulation box, the continuum is described by point charges, representative of the  
249 classical water molecules and ions. The coordinates of the graphene flake are fixed, C-  
250 C (1.427 Å) and C-H (1.089 Å) bond lengths were optimized at the periodic PBE-DFT  
251 level. The empirical description of the interactions between C and H atoms are provided  
252 by the mio-1-1 parameter set.<sup>32</sup>

253

254 In order to minimize the time associated to the QM calculations, both the choice of the  
255 SCC threshold and the Fermi temperature have been optimized by carrying out several  
256 DFTB test calculations using different values of these simulation parameters. It was  
257 observed (see supporting information Figure S1) that both parameters have a sizeable  
258 effect on the simulation time and relatively minimal impact on the values of the atomic  
259 charges. Considering that the charges are used as data in a classical force field, an error  
260 of less than 1% was deemed acceptable. Therefore, unless otherwise stated explicitly,  
261 the SCC threshold was always set to  $1 \times 10^{-2}$  Hartree and a Fermi temperature to 300  
262 K. In each SCC-DFTB step the orbitally resolved charges for each graphene atom are  
263 initialized from optimized charges from the DFTB previous step. Following testing of  
264 the change in average atomic charges at 2 fs intervals, 0.011  $e$ , we determined that  
265 DFTB calculations performed at  $\tau = 5$  ps intervals yield an accurate representation of  
266 the charge in polarization, 0.015  $e$ , without dramatically reducing the dynamics  
267 simulation time (see supporting information Figure S2).

268

269

## 4. Results

270

### A. Calculation of the graphene polarization from DFTB

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273 One aspect of the QM/MD procedure that has to be verified is the capability of the  
274 DFTB approach to correctly reproduce the graphene polarizability using the point-  
275 charge description of the ions. For this we calculate the charge distribution of a C96  
276 graphene flake simulated at the DFT and DFTB levels of theory with a point charge  
277 ( $q = -1.0 e$ ) placed directly above the centre of the flake at a distances,  $d_{\perp}$ , varying  
278 between 0.3 and 0.6 nm, as depicted in Figure 2(a).

279

280 In these tests the DFT calculations are carried out using the Gaussian 09 software  
281 distribution; electronic wavefunctions are expanded in the 6-31G basis set<sup>56-58</sup> with the  
282 three parameter, hybrid B3LYP functional<sup>59</sup> used to describe electron exchange and  
283 correlation interactions. This computational setup has been selected over other possible  
284 basis set XC potential combinations since it matches the original DFTB mio-1-1

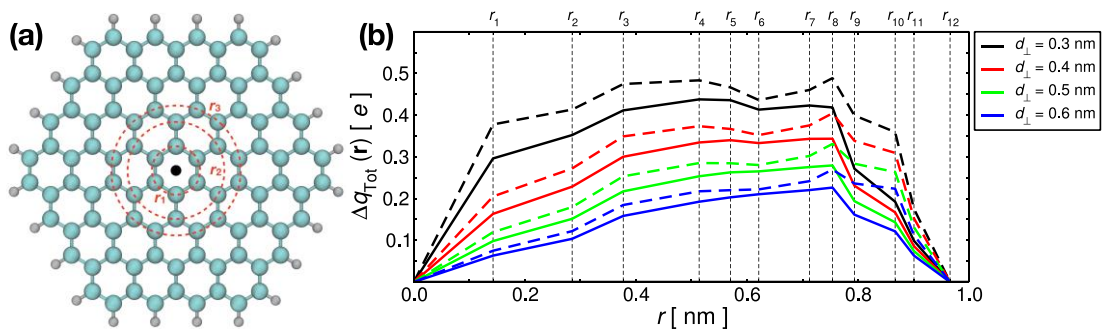
285 Hamiltonian parameterization.<sup>32</sup> In addition, the use of a smaller basis set allows us to  
 286 avoid known complications associated with the use of diffuse orbitals in the modelling  
 287 of highly symmetric aromatic systems.<sup>60</sup>

288  
 289 To map the redistribution of charge density in response to the proximity of the point  
 290 charge, in Figure 2(b) we plot the integrated total atomic charge difference  $\Delta q_{\text{Tot}}$   
 291

$$292 \quad \Delta q_{\text{Tot}}(\mathbf{r}) = \int_0^{|\mathbf{r}|} \left[ \sum_i \tilde{q}_i(\mathbf{r}) \right] d\mathbf{r} \quad 2$$

293  
 294 as a function of the radial distance from the centre of the flake. Here  $\mathbf{r}$  is the vector  
 295 which describes the position of an atom relative to the centre of the flake and  $\tilde{q}_i$  is the  
 296 computed charge difference on atom  $i$  between the polarized and unpolarized graphene  
 297 flake as described by Equation 1. This analysis captures the accumulation and depletion  
 298 of charge density within each atomic ring of the graphene flake. In response to the  
 299 (negative) point charge, we observe positive charge accumulates in the innermost  
 300 atomic rings  $r_1$  to  $r_3$ . In the buffer region, which is defined from  $r_4$  to  $r_8$ , the presence  
 301 of the ion is less strongly felt and changes to the polarization are considerably smaller.  
 302 Finally, to compensate for the accumulation of charge density close to the point charge,  
 303 positive charge density is lost from the outer regions  $r_9$  to  $r_{12}$ . As anticipated, the  
 304 polarization of the flake increases as the point charge is brought closer to the flake, a  
 305 trend captured by both DFT and DFTB. Our results indicate that B3LYP describe a  
 306 slightly more polarizable graphene flake than DFTB (5-8% more charge is displaced  
 307 by the periphery to the centre of the flake). However, given that B3LYP can  
 308 overestimate the static polarizability by up to 4% with respect to higher levels of  
 309 theory,<sup>61</sup> we deem the DFTB to be acceptable for the QM/MD simulations carried out  
 310 here.

311 Figure 2(b) clearly indicates that the surface charge redistribution induced by the  
 312 proximity of the ion is sizable and cannot be neglected during a simulation. Figure 2(b)  
 313 allows also to appreciate the non-local nature of the charge redistribution which affects  
 314 carbon atoms as far as 3 bonds suggesting that atomic-centered polarizable models  
 315 might fall short in capturing the full physics of the physisorption.  
 316  
 317



318  
 319  
 320 **Figure 2:** (a) Geometry of the hexagonal C96 graphene flake; dashed red circles illustrate radially  
 321 equivalent atoms at increasing distances  $r$  from the location of the point charge (black dot). (b) Plot  
 322 comparing the DFTB (solid) and DFT (dashed) integrated Mulliken charges as a function of radius  $r$   
 323 and point-charge adsorption height  $d_{\perp}$  ( $q = -1.0 e$ ). Vertical dashed lines mark the radii of the C  
 324 atoms in the C96 flake.

325

326 This method neglects the possible charge-transfer that may occur between ions and  
 327 surface during adsorption.<sup>29</sup> This is a short-range interaction which, at the reported  
 328 adsorption heights relevant for solvated cations and anions ( $\approx 3 \text{ \AA}$ ), accounts for less  
 329 than  $0.04 e$  ( $\text{Li}^+$ ,  $\text{Na}^+$ ,  $\text{K}^+$ ), becomes negligible compared to the magnitude of the overall  
 330 Coulomb and Lennard-Jones non-bonded interactions. This term, being very short  
 331 range, could be anyway incorporated into the short range non-bonded interaction if  
 332 desired.

333

### 334 *B. Numerical Equivalence of Coulomb Forces based on Mulliken Charges*

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336 In order to verify full consistency in the calculation of the Coulomb interactions in the  
 337 DFTB and MD parts of the loop, we demonstrate numerically that the interaction  
 338 between a classical point charge  $Q$  and a molecule in a DFTB simulation is equivalent  
 339 to the Coulomb interaction between  $Q$  and the set of Mulliken charges  $\{q_\alpha\}$  associated  
 340 with those atoms, which inform the atomic charges in our MD simulations.

341

342 We consider a classical point charge  $Q = -1.00 e$  approaching the centre of a benzene  
 343 molecule. DFTB simulations are carried out according to the method outlined in the  
 344 Computational details section, with the exception that the threshold for convergence on  
 345 the SCC-DFTB solution is set at  $1 \times 10^{-6} E_{\text{H}}$  and the Fermi temperature to 10 K, this  
 346 ensures convergence of the total energy. At each adsorption height,  $d$ , the force is  
 347 extracted from the total energies of the DFTB simulations using a five-point stencil  
 348 finite differences approach based on a series of equidistant simulations,

349

$$350 \quad F = \frac{E_{-2\Delta d}^{\text{Tot}} + E_{+\Delta d}^{\text{Tot}} - E_{-\Delta d}^{\text{Tot}} - E_{+2\Delta d}^{\text{Tot}}}{12\Delta d} \quad 3$$

351

352

353 Here  $\Delta d (= 0.01 \text{ \AA})$  is the spacing between ion height in each simulation and  $E_{\pm i\Delta d}^{\text{Tot}}$  is  
 354 the DFTB total energy at the adsorption height  $\pm i\Delta d$ .

355

356 The Coulomb Force between the  $Q$  and  $\{q_\alpha\}$  is computed vectorially as the sum

357

$$358 \quad F = \frac{Q}{4\pi\epsilon_0} \sum_{\alpha} \frac{q_{\alpha}}{|\mathbf{r}_{Qq}|^3} \mathbf{r}_{Qq} \quad 4$$

359

360

361 where  $\mathbf{r}_{Qq}$  is the vector which gives the distance between the charges.

362

<b>Method</b>	<b>2.00 \AA</b>	<b>3.00 \AA</b>	<b>10.00 \AA</b>
DFTB Total Energy	87.45	-27.55	-0.35
Coulomb Force	87.43	-27.54	-0.35

363 **Table 1:** The total force exerted on a classical point charge for different adsorptions heights, computed  
 364 as the first derivative of the DFTB total energy (eq. 1) and as the Coulomb force between the point charge  
 365 and Mulliken charges on the atoms in a benzene molecule (eq. 2). All values reported in  $\text{kJ mol}^{-1}\text{nm}^{-1}$

366

367 In table 1 we compare the total Coulomb force exerted on the classical point charge for  
 368 three difference adsorption heights 2.00, 3.00 and 10.00 \AA. To within  $0.02 \text{ kJ mol}^{-1}\text{nm}^{-1}$



369 <sup>1</sup> the SCC-DFTB and classical coulomb forces are the identical, implying that Mulliken  
370 charges are fully transferable between our adopted methods.

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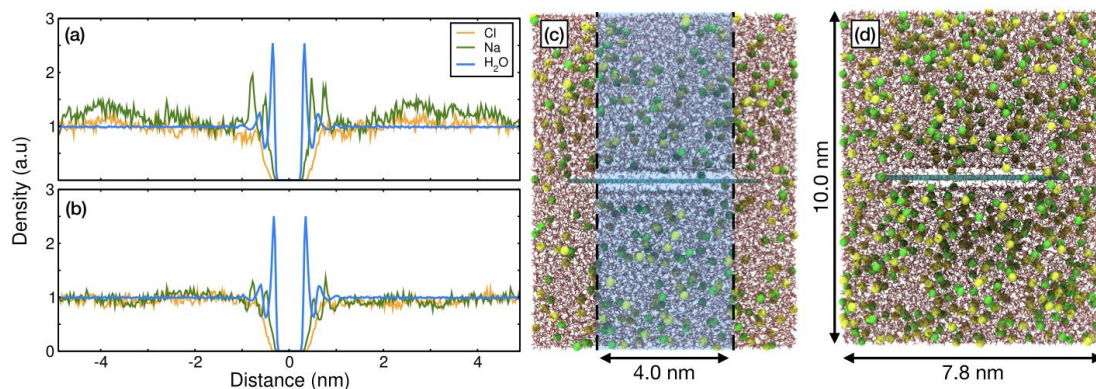
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### C. QM/MD simulations of graphene-electrolyte interfaces

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374 To understand the behaviour of the graphene-electrolyte interface, we start by  
375 considering the density across the simulation box. In order to compensate for the fact  
376 that our graphene is finite, a *restricted* density profile is calculated, this means that  
377 contributions to the density profile are limited to a 2 nm radius around the vector which  
378 passes directly through the centre of the flake (radius  $\approx 2.5$ nm) as shown in Figure 3(c).  
379 This calculation removes from the results the effect of the graphene edges where the  
380 water and ions arrange differently.

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**Figure 3:** The restricted, normalised electrolyte densities in the direction parallel to the graphene surface normal for (a) 0.5 and (b) 1.0 M NaCl concentrations. (c-d) representative snapshots of the two different concentration simulation boxes, C, Na and Cl atoms are coloured cyan, green and yellow respectively.

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Water in our simulations follows the typical SPC/E water-graphene structure,<sup>19,54,62</sup> with densities that are symmetric about the plane of the flake and two strong peaks at 3.4, 6.3 Å, and a third identifiable peak at 10.0 Å. It has been suggested that the increased order of the water molecules at this type of interface (electrolyte-graphene-electrolyte) is brought about by water-water interactions through the seemingly invisible graphene layer.<sup>24</sup> Our simulations have been carried out at two electrolyte concentrations, 0.5 and 1.0 M; in both cases the reduced density of Cl<sup>-</sup> close to the graphene indicates that the anion preferentially resides within the bulk water at distances greater than 1.0 nm from the flake. This result is in disagreement with our previous work that uses the conductor-like polarizable continuum model to optimize the Lennard-Jones carbon-ion force field parameter, where we found a (mild) attraction of the anion to the graphene surface.<sup>14</sup> The weak attraction of the anion to the surface of the graphene flake is instead in agreement to the behaviour shown by smaller F<sup>-</sup> ions,<sup>24</sup> which are modelled based on a classical polarizable force field model and the hybrid first principles/continuum approach by Zhan *et al.*<sup>29</sup> The Na ions have an increased density and demonstrate structuring at the interface. There are two strong peaks at 4.9 and 7.3 Å, which are directly in between the closest two water layers.

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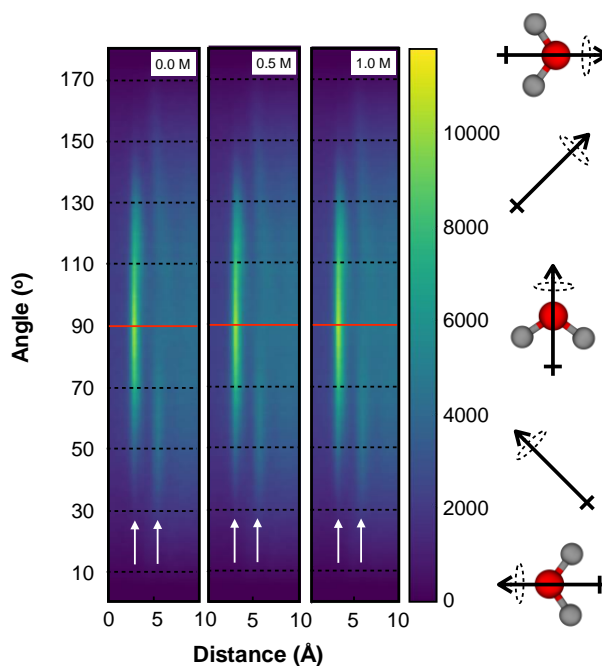
Previous work has shown that the presence and concentration of salts in the electrolyte seems to have very little effect on the overall structuring of water at the interface,<sup>24,63</sup> the QM/MD simulations confirm this. We also find that the relative positions of the water and Na<sup>+</sup> peaks in the density profile are unchanged moving from 0.5 to 1.0 M concentration. Yet, at higher concentrations, it appears that Na<sup>+</sup> ions are less likely to

410 form structures at the interface since the peaks are significantly less intense with respect  
411 to bulk.

412

413 Further inspection of the simulations reveals additional emergent features in the  
414 QM/MD model, especially when compared with fully *ab-initio* molecular dynamics  
415 simulations of (comparatively smaller) graphene-water interfaces.<sup>64</sup> In addition to the  
416 layering of the water present in the density profile (Figure 3), the orientation of the  
417 molecular dipole moments relative to the plane of the graphene can provide extra  
418 information on fine structuring of the graphene-H<sub>2</sub>O interface.

419



420

421 **Figure 4:** Two-dimensional histogram reporting the angular orientation of the water molecule molecular  
422 dipole moment relative to the graphene surface for three different salt concentrations. As a guide to the  
423 eye, white arrows indicate structuring and black arrows denote the orientation of the dipole for a given  
424 angle.

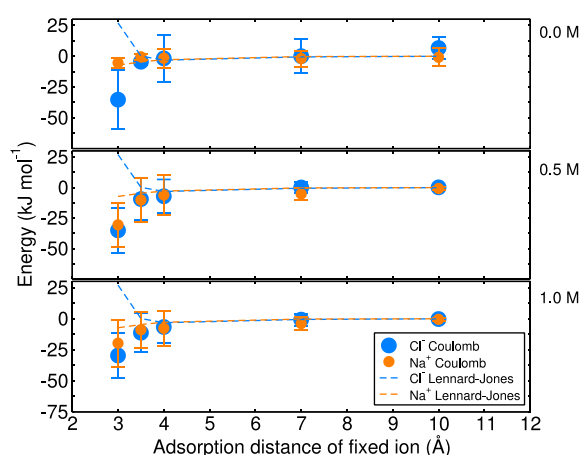
425

426 Figure 4 reports two-dimensional histograms, showing the distribution of molecular  
427 dipole moment angles relative to the graphene, as a function of vertical distance from  
428 the graphene flake for three different concentrations including a pure water (e.g. zero  
429 salt concentration). As depicted in Figure 4, an angle of 90° corresponds to parallel  
430 alignment of the water dipole moment and the surface. Acute angles are indicative of a  
431 tilting of the negative end of the dipole (O atoms) towards the surface, conversely  
432 obtuse angles correspond to a tilting of the positive end of the dipole (H atoms) towards  
433 the surface. In our simulations the molecular dipole moments within the first layer of  
434 water molecules are aligned parallel to the graphene surface. We observe dipoles  
435 within the range 70° and 110° and none oriented perpendicular to the surface. The same  
436 orientation of molecular dipole moments has also been observed in modelling based on  
437 *ab-initio* molecular dynamics: (70° to 110°),<sup>65</sup> (60° to 100°)<sup>64</sup> and polarizable force-  
438 field molecular dynamics: (65° to 120°),<sup>24</sup> and experimental measurements of water at  
439 hydrophobic interfaces.<sup>66</sup> This strict ordering of the molecular dipoles in the first layer  
440 induces a looser order in the second, with dipoles falling in the range 30° to 150°. B  
441 Beyond 1 nm the structure induced by the graphene flake is diminished and all dipole-  
442 surface angles are distributed homogeneously.

443

444 One of the key findings arising from the test deployment of the QM/MD loop is that, at  
 445 concentrations equal to and below 1.0 M – and in the absence of any external bias –  
 446 neither  $\text{Na}^+$  nor  $\text{Cl}^-$  ions totally dehydrate and adsorb on the graphene surface. We are  
 447 aware that this finding is in disagreement with recent quantum mechanical studies of  
 448 similar systems and force field calculations based on quantum mechanical  
 449 parameterizations.<sup>14</sup> Yet, in these specific cases, where graphene has been modelled  
 450 using finite graphene flakes: the ion-graphene molecular quadrupole interaction (which  
 451 is unquantified) plays an important role in determining the ion adsorption behaviour.<sup>49</sup>  
 452

453 The mild of ion adsorption can be understood by analysing the pairwise graphene-ion  
 454 Coulomb and Lennard-Jones contributions to the energy. To this end, we performed  
 455 simulations where one test ion (either  $\text{Na}^+$  or  $\text{Cl}^-$ ) is frozen at fixed heights above the  
 456 centre of the graphene flake. In these calculations, for each height the simulation was  
 457 run for 10 ns, with statistics collected after 5 ns every 5 ps. The resulting average  
 458 Coulomb energies, which vary with the graphene polarization, and Lennard-Jones  
 459 energies are plotted in Figure 5 for 3 different salt concentrations.  
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**Figure 5:** Plot showing averaged Coulomb (dots) and Lennard-Jones (dashed lines) energies between a single frozen ion and the graphene flake at difference adsorption distances and at different molar concentrations of electrolyte.

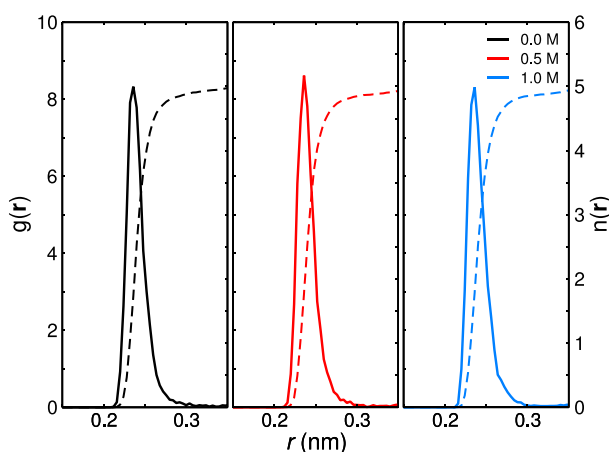
468 For distances equal to and greater than 4.0 Å, the short-range Coulomb and Lennard-  
 469 Jones energies are approximately equal to zero, independent of the specific ion type or  
 470 of the concentration of the solution. Closer to the graphene flake, the Lennard-Jones  
 471 interaction plays a different role depending on nature of test ion. At 3.0 Å the graphene-  
 472  $\text{Cl}^-$  Lennard-Jones energy is strongly repulsive, whilst the graphene- $\text{Na}^+$  interaction is  
 473 weakly attractive. At this distance the short-range Coulomb interaction between  $\text{Cl}^-$  and  
 474 the polarised graphene is strongly attractive, balancing the Lennard-Jones contribution.  
 475 For each of the considered concentrations, within the first standard deviation, the net  
 476 graphene- $\text{Cl}^-$  non-bonded interaction is neither attractive nor repulsive and therefore  
 477 we cannot reasonably expect sustained adsorption of the ion at the surface. As observed  
 478 before, the effect of electrolyte concentration is non-existent. It is interesting to notice  
 479 that this concentration effect is instead present when looking at the adsorption  
 480 behaviour of the  $\text{Na}^+$  ion. At extreme dilution (0.0M) the short-range graphene- $\text{Na}^+$   
 481 Coulomb energy is only weakly attractive; but becomes strongly attractive for higher  
 482 concentrations (0.5 and 1.0M). Consequently, the overall non-bonded interaction  
 483 between  $\text{Na}^+$  and graphene is also strongly attractive ( $\approx -30$  kJ mol), and we could

484 anticipate adsorption on the surface. Yet, as described above, the non-constrained  
485 QM/MD simulations (without fixed ions) at 0.5 and 1.0 M salt concentrations do not  
486 indicate total adsorption (i.e. full dehydration) of  $\text{Na}^+$  at the surface.

487

488 This phenomenon can be understood by considering the change in the Gibbs free energy  
489 during the dehydration of the ion ( $-\Delta G_{\text{hydration}}$ ), which was computed for our  
490 computational setup by Cheatham *et al* ( $369.9 \text{ kJ mol}^{-1}$ ).<sup>55</sup> This energy, calculated by  
491 thermodynamic integration, corresponds to the removal of all the 6 water molecules  
492 from the first solvation shell. By calculating the ion-O radial distribution function  
493 (RDF)  $g_{\text{NaO}}(\mathbf{r})$  (solid lines, Figure 6), we were able to compute the water molecule  
494 coordination number of the  $\text{Na}^+$  ion when frozen at a distance of  $3.0 \text{ \AA}$  above the  
495 graphene surface as the integral of the first RDF peak (dashed lines, Figure 6). For all  
496 concentrations considered, the coordination of the ion is approximately 4.8 water  
497 molecules, which is in excellent agreement with adsorbed configurations modelled by  
498 Williams *et al.*<sup>14</sup> As a first approximation, by simply considering the first dehydration  
499 free energy as  $-\frac{1}{6}\Delta G_{\text{hydration}} = -61.7 \text{ kJ mol}$ , it is clear that in the case of an unbiased  
500 simulations there is a strong thermodynamic drive for the ion to remain solvated.

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**Figure 6:** The first peak in the computed Na-O radial distribution function  $g(\mathbf{r})$  (solid lines) and cumulative integral, used to extrapolate the average coordination number  $n(\mathbf{r})$ , (dotted lines) for systems with  $\text{Na}^+$  fixed at  $3.0 \text{ \AA}$  above the graphene flake at different electrolyte concentrations.

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## 1. Conclusions

523

524 This work couples DFTB with classical MD to investigate the non-faradic interfacial  
525 properties of carbon-based solid/liquid interfaces. Unlike other DFTB/MM approaches  
526 the primary focus here is on the classical component of the system. The method  
527 developed simultaneously captures (i) the quantum mechanically informed surface  
528 polarizability, (ii) an explicit description of the electrolyte including its rearrangement  
529 at the surface and (iii) the dynamical behaviour of fully-solvated ions.

530

531 The method was applied to charge neutral graphene flakes, 5 nm in diameter, immersed  
532 in NaCl solutions of different concentrations for which the surface charge redistribution  
533 brought about by the proximity of the ions is large and delocalized over several carbon  
534 atoms. Density profiles and molecular dipole moment analysis suggests that water and  
535 Na<sup>+</sup> ions structure at the interface whereas Cl<sup>-</sup> ions remain in bulk solution. We noticed  
536 that the electrolyte concentration does not have any effects on the adsorption of the  
537 anion but strengthens that of the cations when moving from extreme dilution to  
538 moderate electrolyte concentration. Further analysis on the energies of various fixed-  
539 ion configurations reveals that the lack of overall adsorption can be rationalized as the  
540 adsorbed ion graphene configuration being thermodynamically disfavoured in  
541 comparison to the solvated ion configuration. This leads to the conclusion that charge  
542 transfer between the graphene and ions is unlikely to occur since the ions never get  
543 close enough to the surface for the transfer to take place and that the ions adsorption is,  
544 in the configuration explored here, only driven by the thermodynamic of the solution.

545

546 In principle, this method can be applied to a wide array of polarisable materials,  
547 electrolyte solutions and their interfaces and different experimental set-ups. In addition,  
548 this method opens up the possibility for the simulation of electrified interfaces where  
549 the true chemical nature of the surface can be taken into account.

550

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552

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558

## 559 **References**

560

- 561 (1) Wang, Y.; Shi, Z.; Huang, Y.; Ma, Y.; Wang, C.; Chen, M.; Chen, Y.  
562 Supercapacitor Devices Based on Graphene Materials. *J. Phys. Chem. C* **2009**,  
563 *113* (30), 13103–13107. <https://doi.org/10.1021/jp902214f>.
- 564 (2) Liu, C.; Yu, Z.; Neff, D.; Zhamu, A.; Jang, B. Z. Graphene-Based Supercapacitor  
565 with an Ultrahigh Energy Density. *Nano Lett.* **2010**, *10* (12), 4863–4868.  
566 <https://doi.org/10.1021/nl102661q>.
- 567 (3) Yu, A.; Roes, I.; Davies, A.; Chen, Z. Ultrathin, Transparent, and Flexible  
568 Graphene Films for Supercapacitor Application. *Appl. Phys. Lett.* **2010**, *96*  
569 (25), 253105. <https://doi.org/10.1063/1.3455879>.
- 570 (4) Zhang, L. L.; Zhou, R.; Zhao, X. S. Graphene-Based Materials as  
571 Supercapacitor Electrodes. *J. Mater. Chem.* **2010**, *20* (29), 5983.  
572 <https://doi.org/10.1039/c000417k>.

- 573 (5) Huang, Y.; Liang, J.; Chen, Y. An Overview of the Applications of Graphene-  
574 Based Materials in Supercapacitors. *Small* **2012**, *8* (12), 1805–1834.  
575 <https://doi.org/10.1002/sml.201102635>.
- 576 (6) Tan, Y. B.; Lee, J.-M. Graphene for Supercapacitor Applications. *J. Mater.*  
577 *Chem. A* **2013**, *1* (47), 14814. <https://doi.org/10.1039/c3ta12193c>.
- 578 (7) Simon, P.; Gogotsi, Y. Materials for Electrochemical Capacitors. *Nat. Mater.*  
579 **2008**, *7*, 845–854.
- 580 (8) Mauter, M. S.; Elimelech, M. Environmental Applications of Carbon-Based  
581 Nanomaterials. *Environ. Sci. Technol.* **2008**, *42* (16), 5843–5859.  
582 <https://doi.org/10.1021/es8006904>.
- 583 (9) Dai, L.; Chang, D. W.; Baek, J.-B.; Lu, W. Carbon Nanomaterials for Advanced  
584 Energy Conversion and Storage. *Small* **2012**, *8* (8), 1130–1166.  
585 <https://doi.org/10.1002/sml.201101594>.
- 586 (10) Avouris, P.; Chen, Z.; Perebeinos, V. Carbon-Based Electronics. *Nat.*  
587 *Nanotechnol.* **2007**.
- 588 (11) Yang, H.; Yang, J.; Bo, Z.; Chen, X.; Shuai, X.; Kong, J.; Yan, J.; Cen, K. Kinetic-  
589 Dominated Charging Mechanism within Representative Aqueous  
590 Electrolyte-Based Electric Double-Layer Capacitors. *J. Phys. Chem. Lett.*  
591 **2017**, *8* (15), 3703–3710. <https://doi.org/10.1021/acs.jpcl.7b01525>.
- 592 (12) Qu, Q. T.; Wang, B.; Yang, L. C.; Shi, Y.; Tian, S.; Wu, Y. P. Study on  
593 Electrochemical Performance of Activated Carbon in Aqueous Li<sub>2</sub>SO<sub>4</sub>,  
594 Na<sub>2</sub>SO<sub>4</sub> and K<sub>2</sub>SO<sub>4</sub> Electrolytes. *Electrochem. Commun.* **2008**, *10* (10),  
595 1652–1655. <https://doi.org/10.1016/j.elecom.2008.08.020>.
- 596 (13) Li, X.; Rong, J.; Wei, B. Electrochemical Behavior of Single-Walled Carbon  
597 Nanotube Supercapacitors under Compressive Stress. *ACS Nano* **2010**, *4*  
598 (10), 6039–6049. <https://doi.org/10.1021/nn101595y>.
- 599 (14) Williams, C. D.; Dix, J.; Troisi, A.; Carbone, P. Effective Polarization in  
600 Pairwise Potentials at the Graphene–Electrolyte Interface. *J. Phys. Chem.*  
601 *Lett.* **2017**, *8* (3), 703–708. <https://doi.org/10.1021/acs.jpcl.7b02783>.
- 602 (15) Zaera, F. Probing Liquid/Solid Interfaces at the Molecular Level. *Chem. Rev.*  
603 **2012**, *112* (5), 2920–2986. <https://doi.org/10.1021/cr2002068>.
- 604 (16) Levin, Y. Polarizable Ions at Interfaces. *Phys. Rev. Lett.* **2009**, *102* (14),  
605 147803. <https://doi.org/10.1103/PhysRevLett.102.147803>.
- 606 (17) Persson, K.; Sethuraman, V. A.; Hardwick, L. J.; Hinuma, Y.; Meng, Y. S.; van  
607 der Ven, A.; Srinivasan, V.; Kostecky, R.; Ceder, G. Lithium Diffusion in  
608 Graphitic Carbon. *J. Phys. Chem. Lett.* **2010**, *1* (8), 1176–1180.  
609 <https://doi.org/10.1021/jz100188d>.
- 610 (18) McCaffrey, D. L.; Nguyen, S. C.; Cox, S. J.; Weller, H.; Alivisatos, A. P.; Geissler,  
611 P. L.; Saykally, R. J. Mechanism of Ion Adsorption to Aqueous Interfaces:  
612 Graphene/Water vs. Air/Water. *Proc. Natl. Acad. Sci.* **2017**, *114* (51),  
613 13369–13373. <https://doi.org/10.1073/pnas.1702760114>.
- 614 (19) Ho, T. A.; Striolo, A. Polarizability Effects in Molecular Dynamics Simulations  
615 of the Graphene-Water Interface. *J. Chem. Phys.* **2013**, *138* (5), 054117.  
616 <https://doi.org/10.1063/1.4789583>.
- 617 (20) Kulik, H. J.; Schwegler, E.; Galli, G. Probing the Structure of Salt Water under  
618 Confinement with First-Principles Molecular Dynamics and Theoretical X-  
619 Ray Absorption Spectroscopy. *J. Phys. Chem. Lett.* **2012**, *3* (18), 2653–2658.  
620 <https://doi.org/10.1021/jz300932p>.



- 621 (21) Colherinhas, G.; Fileti, E. E.; Chaban, V. V. The Band Gap of Graphene Is  
622 Efficiently Tuned by Monovalent Ions. *J. Phys. Chem. Lett.* **2015**, *6* (2), 302–  
623 307. <https://doi.org/10.1021/jz502601z>.
- 624 (22) Kulik, H. J.; Schwegler, E.; Galli, G. Probing the Structure of Salt Water under  
625 Confinement with First-Principles Molecular Dynamics and Theoretical X-  
626 Ray Absorption Spectroscopy. *J. Phys. Chem. Lett.* **2012**, *3* (18), 2653–2658.  
627 <https://doi.org/10.1021/jz300932p>.
- 628 (23) Pham, T. A.; Mortuza, S. M. G.; Wood, B. C.; Lau, E. Y.; Ogitsu, T.; Buchsbaum,  
629 S. F.; Siwy, Z. S.; Fornasiero, F.; Schwegler, E. Salt Solutions in Carbon  
630 Nanotubes: The Role of Cation– $\pi$  Interactions. *J. Phys. Chem. C* **2016**, *120*  
631 (13), 7332–7338. <https://doi.org/10.1021/acs.jpcc.5b12245>.
- 632 (24) Pykal, M.; Langer, M.; Blahová Prudilová, B.; Banáš, P.; Otyepka, M. Ion  
633 Interactions across Graphene in Electrolyte Aqueous Solutions. *J. Phys.*  
634 *Chem. C* **2019**, *123* (15), 9799–9806.  
635 <https://doi.org/10.1021/acs.jpcc.8b12055>.
- 636 (25) Tomasi, J.; Mennucci, B.; Cammi, R. Quantum Mechanical Continuum  
637 Solvation Models. *Chem. Rev.* **2005**, *105* (8), 2999–3094.  
638 <https://doi.org/10.1021/cr9904009>.
- 639 (26) Cossi, M.; Rega, N.; Scalmani, G.; Barone, V. Energies, Structures, and  
640 Electronic Properties of Molecules in Solution with the C-PCM Solvation  
641 Model. *J. Comput. Chem.* **2003**, *24* (6), 669–681.  
642 <https://doi.org/10.1002/jcc.10189>.
- 643 (27) Ma, J.; Michaelides, A.; Alfè, D.; Schimka, L.; Kresse, G.; Wang, E. Adsorption  
644 and Diffusion of Water on Graphene from First Principles. *Phys. Rev. B* **2011**,  
645 *84* (3), 033402. <https://doi.org/10.1103/PhysRevB.84.033402>.
- 646 (28) Brandenburg, J. G.; Zen, A.; Fitzner, M.; Ramberger, B.; Kresse, G.; Tsatsoulis,  
647 T.; Grüneis, A.; Michaelides, A.; Alfè, D. Physisorption of Water on Graphene:  
648 Subchemical Accuracy from Many-Body Electronic Structure Methods. *J.*  
649 *Phys. Chem. Lett.* **2019**, *10* (3), 358–368.  
650 <https://doi.org/10.1021/acs.jpcclett.8b03679>.
- 651 (29) Zhan, C.; Cerón, M. R.; Hawks, S. A.; Otani, M.; Wood, B. C.; Pham, T. A.;  
652 Stadermann, M.; Campbell, P. G. Specific Ion Effects at Graphitic Interfaces.  
653 *Nat. Commun.* **2019**, *10* (1), 4858. [https://doi.org/10.1038/s41467-019-](https://doi.org/10.1038/s41467-019-12854-7)  
654 [12854-7](https://doi.org/10.1038/s41467-019-12854-7).
- 655 (30) Nishihara, S.; Otani, M. Hybrid Solvation Models for Bulk, Interface, and  
656 Membrane: Reference Interaction Site Methods Coupled with Density  
657 Functional Theory. *Phys. Rev. B* **2017**, *96* (11), 115429.  
658 <https://doi.org/10.1103/PhysRevB.96.115429>.
- 659 (31) Iamprasertkun, P.; Hirunpinyopas, W.; Keerthi, A.; Wang, B.; Radha, B.;  
660 Bissett, M. A.; Dryfe, R. A. W. Capacitance of Basal Plane and Edge-Oriented  
661 Highly Ordered Pyrolytic Graphite: Specific Ion Effects. *J. Phys. Chem. Lett.*  
662 **2019**, *10* (3), 617–623. <https://doi.org/10.1021/acs.jpcclett.8b03523>.
- 663 (32) Elstner, M.; Porezag, D.; Jungnickel, G.; Elsner, J.; Haugk, M.; Frauenheim, Th.;  
664 Suhai, S.; Seifert, G. Self-Consistent-Charge Density-Functional Tight-Binding  
665 Method for Simulations of Complex Materials Properties. *Phys. Rev. B* **1998**,  
666 *58* (11), 7260–7268. <https://doi.org/10.1103/PhysRevB.58.7260>.
- 667 (33) Aradi, B.; Hourahine, B.; Frauenheim, Th. DFTB+, a Sparse Matrix-Based  
668 Implementation of the DFTB Method †. *J. Phys. Chem. A* **2007**, *111* (26),  
669 5678–5684. <https://doi.org/10.1021/jp070186p>.

- 670 (34) Koskinen, P.; Mäkinen, V. Density-Functional Tight-Binding for Beginners.  
671 *Comput. Mater. Sci.* **2009**, *47* (1), 237–253.  
672 <https://doi.org/10.1016/j.commatsci.2009.07.013>.
- 673 (35) Bondar, A.-N.; Fischer, S.; Smith, J. C.; Elstner, M.; Suhai, S. Key Role of  
674 Electrostatic Interactions in Bacteriorhodopsin Proton Transfer. *J. Am.*  
675 *Chem. Soc.* **2004**, *126* (44), 14668–14677.  
676 <https://doi.org/10.1021/ja047982i>.
- 677 (36) Bondar, N.; Elstner, M.; Fischer, S.; Smith, J. C.; Suhai, S. Can Coordinate  
678 Driving Describe Proton Transfer Coupled to Complex Protein Motions?  
679 *Phase Transit.* **2004**, *77* (1–2), 47–52.  
680 <https://doi.org/10.1080/01411590310001622455>.
- 681 (37) Riccardi, D.; Schaefer, P.; Yang, Yu, H.; Ghosh, N.; Prat-Resina, X.; König, P.;  
682 Li, G.; Xu, D.; Guo, H.; et al. Development of Effective Quantum  
683 Mechanical/Molecular Mechanical (QM/MM) Methods for Complex  
684 Biological Processes. *J. Phys. Chem. B* **2006**, *110* (13), 6458–6469.  
685 <https://doi.org/10.1021/jp056361o>.
- 686 (38) Xu, D.; Guo, H.; Cui, Q. Antibiotic Binding to Divalent  $\beta$ -Lactamase L1 from  
687 *Stenotrophomonas Maltophilia* : SCC-DFTB/CHARMM and DFT Studies †. *J.*  
688 *Phys. Chem. A* **2007**, *111* (26), 5630–5636.  
689 <https://doi.org/10.1021/jp068746s>.
- 690 (39) Phatak, P.; Ghosh, N.; Yu, H.; Cui, Q.; Elstner, M. Amino Acids with an  
691 Intermolecular Proton Bond as Proton Storage Site in Bacteriorhodopsin.  
692 *Proc. Natl. Acad. Sci.* **2008**, *105* (50), 19672–19677.  
693 <https://doi.org/10.1073/pnas.0810712105>.
- 694 (40) Woiczikowski, P. B.; Kubař, T.; Gutiérrez, R.; Caetano, R. A.; Cuniberti, G.;  
695 Elstner, M. Combined Density Functional Theory and Landauer Approach  
696 for Hole Transfer in DNA along Classical Molecular Dynamics Trajectories. *J.*  
697 *Chem. Phys.* **2009**, *130* (21), 215104. <https://doi.org/10.1063/1.3146905>.
- 698 (41) Balog, R.; Jørgensen, B.; Nilsson, L.; Andersen, M.; Rienks, E.; Bianchi, M.;  
699 Fanetti, M.; Lægsgaard, E.; Baraldi, A.; Lizzit, S.; et al. Bandgap Opening in  
700 Graphene Induced by Patterned Hydrogen Adsorption. *Nat. Mater.* **2010**, *9*  
701 (4), 315–319. <https://doi.org/10.1038/nmat2710>.
- 702 (42) Kuc, A.; Heine, T.; Seifert, G. Structural and Electronic Properties of  
703 Graphene Nanoflakes. *Phys. Rev. B* **2010**, *81* (8), 085430.  
704 <https://doi.org/10.1103/PhysRevB.81.085430>.
- 705 (43) Shi, H.; Barnard, A. S.; Snook, I. K. Quantum Mechanical Properties of  
706 Graphene Nano-Flakes and Quantum Dots. *Nanoscale* **2012**, *4* (21), 6761.  
707 <https://doi.org/10.1039/c2nr31354e>.
- 708 (44) Huang, Z.; Qu, J.; Peng, X.; Liu, W.; Zhang, K.; Wei, X.; Zhong, J. Quantum  
709 Confinement in Graphene Quantum Dots: Quantum Confinement in  
710 Graphene Quantum Dots. *Phys. Status Solidi RRL - Rapid Res. Lett.* **2014**, *8*  
711 (5), 436–440. <https://doi.org/10.1002/pssr.201409064>.
- 712 (45) Berendsen, H. J. C.; Grigera, J. R.; Straatsma, T. P. The Missing Term in  
713 Effective Pair Potentials. *J. Phys. Chem.* **1987**, *91* (24), 6269–6271.  
714 <https://doi.org/10.1021/j100308a038>.
- 715 (46) Mulliken, R. S. Electronic Population Analysis on LCAO–MO Molecular Wave  
716 Functions. *I. J. Chem. Phys.* **1955**, *23* (10), 1833–1840.  
717 <https://doi.org/10.1063/1.1740588>.



- 718 (47) Seabra, G. de M.; Walker, R. C.; Elstner, M.; Case, D. A.; Roitberg, A. E.  
719 Implementation of the SCC-DFTB Method for Hybrid QM/MM Simulations  
720 within the Amber Molecular Dynamics Package †. *J. Phys. Chem. A* **2007**, *111*  
721 (26), 5655–5664. <https://doi.org/10.1021/jp070071l>.
- 722 (48) Jenness, G. R.; Karalti, O.; Jordan, K. D. Benchmark Calculations of Water–  
723 Acene Interaction Energies: Extrapolation to the Water–Graphene Limit and  
724 Assessment of Dispersion–Corrected DFT Methods. **2010**, *9*.
- 725 (49) Kocman, M.; Pykal, M.; Jurečka, P. Electric Quadrupole Moment of Graphene  
726 and Its Effect on Intermolecular Interactions. *Phys. Chem. Chem. Phys.* **2014**,  
727 *16* (7), 3144. <https://doi.org/10.1039/c3cp54701a>.
- 728 (50) Cheng, J. L.; Vermeulen, N.; Sipe, J. E. Second Order Optical Nonlinearity of  
729 Graphene Due to Electric Quadrupole and Magnetic Dipole Effects. *Sci. Rep.*  
730 **2017**, *7* (1). <https://doi.org/10.1038/srep43843>.
- 731 (51) Berendsen, H. J. C.; van der Spoel, D.; van Drunen, R. GROMACS: A Message-  
732 Passing Parallel Molecular Dynamics Implementation. *Comput. Phys.*  
733 *Commun.* **1995**, *91* (1–3), 43–56. [https://doi.org/10.1016/0010-](https://doi.org/10.1016/0010-4655(95)00042-E)  
734 [4655\(95\)00042-E](https://doi.org/10.1016/0010-4655(95)00042-E).
- 735 (52) Spoel, D. V. D.; Lindahl, E.; Hess, B.; Groenhof, G.; Mark, A. E.; Berendsen, H. J.  
736 C. GROMACS: Fast, Flexible, and Free. *J. Comput. Chem.* **2005**, *26* (16), 1701–  
737 1718. <https://doi.org/10.1002/jcc.20291>.
- 738 (53) Miyamoto, S.; Kollman, P. A. Settle: An Analytical Version of the SHAKE and  
739 RATTLE Algorithm for Rigid Water Models. *J. Comput. Chem.* **1992**, *13* (8),  
740 952–962. <https://doi.org/10.1002/jcc.540130805>.
- 741 (54) Werder, T.; Walther, J. H.; Jaffe, R. L.; Halicioglu, T.; Koumoutsakos, P. On the  
742 Water–Carbon Interaction for Use in Molecular Dynamics Simulations of  
743 Graphite and Carbon Nanotubes. *J. Phys. Chem. B* **2003**, *107* (6), 1345–1352.  
744 <https://doi.org/10.1021/jp0268112>.
- 745 (55) Joung, I. S.; Cheatham, T. E. Determination of Alkali and Halide Monovalent  
746 Ion Parameters for Use in Explicitly Solvated Biomolecular Simulations. *J.*  
747 *Phys. Chem. B* **2008**, *112* (30), 9020–9041.  
748 <https://doi.org/10.1021/jp8001614>.
- 749 (56) Binkley, J. S.; Pople, J. A.; Hehre, W. J. Self-Consistent Molecular Orbital  
750 Methods. 21. Small Split-Valence Basis Sets for First-Row Elements. *J. Am.*  
751 *Chem. Soc.* **1980**, *102* (3), 939–947. <https://doi.org/10.1021/ja00523a008>.
- 752 (57) Francl, M. M.; Pietro, W. J.; Hehre, W. J.; Binkley, J. S.; Gordon, M. S.; DeFrees,  
753 D. J.; Pople, J. A. Self-consistent Molecular Orbital Methods. XXIII. A  
754 Polarization-type Basis Set for Second-row Elements. *J. Chem. Phys.* **1982**,  
755 *77* (7), 3654–3665. <https://doi.org/10.1063/1.444267>.
- 756 (58) Rassolov, V. A.; Ratner, M. A.; Pople, J. A.; Redfern, P. C.; Curtiss, L. A. 6-31G\*  
757 Basis Set for Third-Row Atoms. *J. Comput. Chem.* **2001**, *22* (9), 976–984.  
758 <https://doi.org/10.1002/jcc.1058>.
- 759 (59) Chai, J.-D.; Head-Gordon, M. Long-Range Corrected Hybrid Density  
760 Functionals with Damped Atom–Atom Dispersion Corrections. *Phys. Chem.*  
761 *Chem. Phys.* **2008**, *10* (44), 6615. <https://doi.org/10.1039/b810189b>.
- 762 (60) Bauschlicher, C. W. Basis Set Effects on the Geometry of C<sub>96</sub>H<sub>24</sub>. *Chem.*  
763 *Phys. Lett.* **2016**, *665*, 100–104.  
764 <https://doi.org/10.1016/j.cplett.2016.10.060>.
- 765 (61) Hait, D.; Head-Gordon, M. How Accurate Are Static Polarizability Predictions  
766 from Density Functional Theory? An Assessment over 132 Species at

767 Equilibrium Geometry. *Phys. Chem. Chem. Phys.* **2018**, *20* (30), 19800–  
768 19810. <https://doi.org/10.1039/C8CP03569E>.  
769 (62) Ho, T. A.; Striolo, A. Molecular Dynamics Simulation of the Graphene–Water  
770 Interface: Comparing Water Models. *Mol. Simul.* **2014**, *40* (14), 1190–1200.  
771 <https://doi.org/10.1080/08927022.2013.854893>.  
772 (63) Vácha, R.; Zangi, R.; Engberts, J. B. F. N.; Jungwirth, P. Water Structuring and  
773 Hydroxide Ion Binding at the Interface between Water and Hydrophobic  
774 Walls of Varying Rigidity and van Der Waals Interactions. *J. Phys. Chem. C*  
775 **2008**, *112* (20), 7689–7692. <https://doi.org/10.1021/jp800888b>.  
776 (64) Tocci, G.; Joly, L.; Michaelides, A. Friction of Water on Graphene and  
777 Hexagonal Boron Nitride from *Ab Initio* Methods: Very Different Slippage  
778 Despite Very Similar Interface Structures. *Nano Lett.* **2014**, *14* (12), 6872–  
779 6877. <https://doi.org/10.1021/nl502837d>.  
780 (65) Cicero, G.; Grossman, J. C.; Schwegler, E.; Gygi, F.; Galli, G. Water Confined in  
781 Nanotubes and between Graphene Sheets: A First Principle Study. **2008**,  
782 *130*, 1871–1878.  
783 (66) Stirnemann, G.; Rosky, P. J.; Hynes, J. T.; Laage, D. Water Reorientation,  
784 Hydrogen-Bond Dynamics and 2D-IR Spectroscopy next to an Extended  
785 Hydrophobic Surface. *Faraday Discuss.* **2010**, *146*, 263–281.  
786