

# EFFECTS OF MAINSHOCK-AFTERSHOCK SEQUENCES ON FRAGILITY ANALYSIS OF RC BUILDINGS WITH AGEING

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## Abstract:

This paper presents the seismic vulnerability assessment of existing RC buildings designed according to previous non-seismic codes and exposed to various levels of corrosion and mainshock-aftershock sequences. A refined finite element model of an existing four-storey reinforced concrete building is adopted. A selection of twenty as-recorded natural ground motions are collected from international database to perform incremental dynamic analyses for the inelastic response of the testbed building. The effects of corrosion are applied on external beams and columns as to simulate a realistic exposure. The robust fragility assessment is conducted for a range of seismic intensity measures. Moreover, a new intensity measure, based on the modified acceleration spectrum intensity, is proposed. Such seismic parameter accounts for the elongation period experienced by structures during earthquake events and appears to be more reliable and accurate for corroded RC structures than the most commonly adopted peak ground acceleration and spectral acceleration at the first natural period. The results of the comprehensive numerical simulations contribute to providing relevant indications on the non-linear response of existing corroded buildings under multiple excitations and, highlight that current seismic codes are no longer conservative for such detrimental phenomena.

**Keywords:** Corrosion; ageing effects; mainshock and aftershocks; reinforced concrete structures; smooth bars; inelastic response.

## 1. Introduction

Many existing and newly reinforced concrete (RC) structures in seismic prone countries are designed to withstand single strong ground motions. However, the complexity of fault systems and the dynamic stresses generated by single events may trigger multiple aftershocks (Ruiz Garcia et al., 2012). Potentially, aftershocks may be either comparable or stronger than mainshocks. Due to the short time of occurrence after mainshocks, such aftershocks could completely change the inelastic response of RC structures and cause collapse.

36 Some existing studies have focused on the effects of earthquake swarms on the non-linear response  
37 of single-degree-of-freedom (SDOF) (i.e. Amadio et al., 2003; Hatzigeorgiou and Beskos, 2009;  
38 Sabegh and Ruiz Garcia, 2015). They investigated the effects of the earthquake sequences on q-factor  
39 and ductility of SDOF systems. The results of the numerical analyses indicated that the large damage  
40 accumulation due to mainshock-aftershock sequences implies a strong decay of the q-factor and an  
41 increasing demand in the inelastic displacement ratio, which depend on some parameters of the SDOF  
42 system and local site conditions such as structural period, available ductility, damping ratio and the  
43 type of the earthquake ground motion and soil. Conversely, some other researchers focused on the  
44 inelastic response of multiple-degree-of-freedom (MDOF) subjected to multiple ground motions (Li  
45 and Ellingwood, 2007; Hatzigeorgiou and Liolios 2010; Di Sarno, 2013; Hosseinpour et al., 2017,  
46 Aldenaby, 2018). On the one hand, Li and Ellingwood (2007) investigated the effects of sequential  
47 ground motions on steel moment frames and proposed a new methodology to incorporate the  
48 additional damage due to aftershocks in the performance-based assessment. On the other hand, Di  
49 Sarno (2013), Hatzigeorgiou and Liolios (2010), Hosseinpour et al., (2017), Aldenaby, (2018) carried  
50 out numerical simulations on the effects of such multiple earthquakes on RC framed structures.  
51 Moreover, a fragility assessment was also presented in Hosseinpour et al., (2017) and Aldenaby,  
52 (2018). The results of these comprehensive analyses led to either an increase in the inelastic  
53 displacement or even a collapse of RC frames, in comparison to an elastic or slightly inelastic  
54 behaviour of single ground motion-subjected structures. The fragility analysis highlighted the  
55 significant impact on the increasing failure probability of RC frames under multiple earthquakes. The  
56 accumulation of plastic deformation due to the short time of occurrence between two events showed  
57 an increment of inter-storey drift ratios and the incapability of such structures to redistribute the  
58 internal forces. All these studies suggest that an adequate and accurate hysteretic model, accounting  
59 for strength and stiffness degradation, should be considered in order to reliably predict the non-linear  
60 response of RC structures under such earthquake sequences.

61 Most of these studies on the non-linear behaviour of RC structures under motion sequences have  
62 utilized replicated or artificial aftershocks. However, such an approach may lead to unreliable results  
63 as aftershocks contain different characteristics from mainshocks, even if they occurred in the same  
64 region. Furthermore, those numerical simulations have been conducted mostly on two-dimensional  
65 models without any consideration for the interaction between frames and connections, and the  
66 possible exposure of such RC structures to aggressive environments, which may foster further  
67 damage and deterioration due to corrosion.

68 Corrosion has a destructive and extensive impact on RC civil infrastructure (Panchireddi et al., 2018;  
69 Ma et al., 2020, Guo et al., 2020; Di Sarno and Pugliese, 2020a, Di Sarno and Pugliese, 2020b).

70 Concrete and steel reinforcement are affected by corrosion differently. While concrete cover spalling  
71 and the reduction of the compressive strength are the main consequences for concrete (i.e. Coronelli  
72 and Gambarova, 2004), mass loss and reduction of mechanical properties are the corrosion effects for  
73 steel reinforcements (i.e. Cairns et al., 2005, Apostolopoulos et al. 2006, Imperatore et al., 2017).  
74 Additionally, high corrosion rates weaken the bond strength between the concrete and rebars (i.e.  
75 Almusallam et al., 1996; Bilcik and Holly, 2013; Coccia et al, 2016; Zhang et al. 2020) which may  
76 trigger the inelastic buckling. The effects of such inelastic instability for steel longitudinal bars lower  
77 the ultimate capacity of RC members and, thus, impact the global behaviour of the structure.  
78 Although, corrosion is difficult to model and simulate due to its unpredictable nature and complexity,  
79 it is, however, essential to provide guidelines for the assessment of the inelastic response of typical  
80 existing RC buildings when subjected to multiple earthquakes and corrosion.  
81 Many studies have dealt with the effects of corrosion on (RC bridges) unprotected structures (i.e.  
82 Gardoni et al., 2012; Ghosh and Sood, 2016, Shekhar et al., 2018) where the corrosion penetration  
83 could be included on the whole RC component. However, this scenario does not represent the real  
84 case of typical RC buildings as frames are protected by infills, and the corrosion path could stop on  
85 just one side. Only external RC components can be reasonably exposed to aggressive agents, leading  
86 to either a one- or two-sided attacks.  
87 For this purpose, this study investigates the seismic vulnerability of typical existing RC buildings  
88 under multiple earthquake excitations and various levels of corrosion rates. Firstly, a selection of  
89 twenty ground motions were collected from international database. Then, a description of the finite  
90 element (FE) model of the RC building, along with the calibration of the mesh size density of RC  
91 components through moment-curvature analysis, is provided. A brief introduction on the pitting  
92 corrosion model and seismic fragility assessment is also presented. A new formulated intensity  
93 measure for fragility assessment, named Modified Acceleration Spectrum Intensity (MASI), is  
94 introduced. Such seismic parameter was assessed using some criteria from the literature. Then, the  
95 seismic fragility curves of the corroded building for three limit states and three seismic intensity  
96 measures, through incremental dynamic analysis (IDA), are given. Finally, based on the numerical  
97 results, conclusion and suggestions for future works are provided.

## 98 2. Research Significance

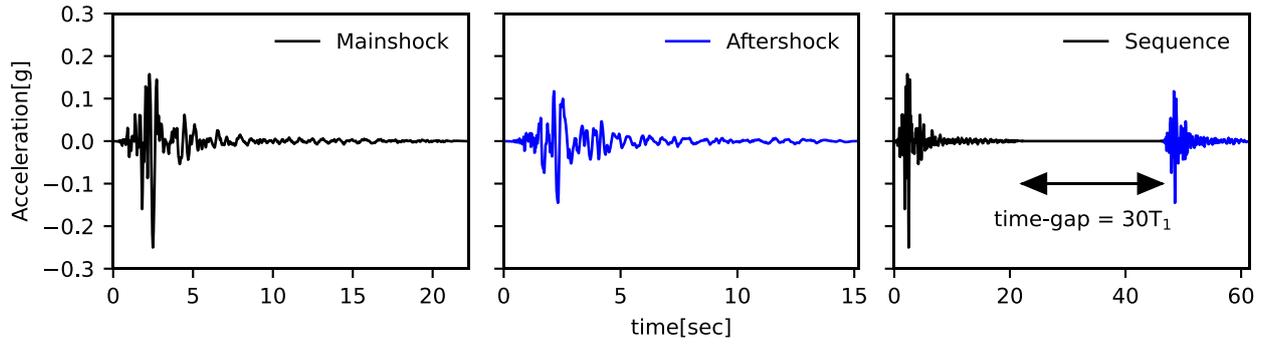
99 The research objectives of the present study are as follows:

- 100 • *Inelastic response of actual corroded RC buildings*: Incremental dynamic analyses will  
101 provide a relevant indication on the seismic response of existing RC buildings when exposed  
102 to corrosion and subjected to multiple earthquake loadings;

- 103 • *IDA analyses on a refined three-dimensional finite element model*: Previous research has  
104 primarily focused on a two-dimensional approach, while this study simulates the response of  
105 a three-dimensional model of a multi-storey residential building;
- 106 • *Seismic fragility analysis*: A probabilistic approach is herein used to evaluate the seismic  
107 vulnerability of a corroded 4-storey RC building considering three limit states, including  
108 Limited Damage, Severe Damage and Near Collapse. Structural performance points were  
109 taken as an average from non-linear static analyses using three different lateral loading  
110 patterns;
- 111 • *Evaluation of the adequacy of different intensity measure*. Three different parameters were  
112 used as IM: (i) peak ground acceleration, (ii) spectral acceleration for the first natural  
113 frequency of the building and (iii) Modified Acceleration Spectrum Intensity including the  
114 elongation period experienced by RC structures during the occurrence of earthquake events.  
115 The last two seismic intensity measures account for the elastic period of the corroded building.  
116 While the maximum inter-storey drift ratios were used as an engineering demand parameter  
117 (EDP)

### 118 3. GROUND MOTION SELECTION

119 In seismic-design, earthquake excitations are selected with regard to the site and structure  
120 specifications which require the response spectrum of natural records matching the target site  
121 response spectrum. Modern seismic codes specify that at least seven couples of ground motions  
122 should be considered to attain the mean inelastic response of RC structures (i.e. Eurocode 8 – Part 3,  
123 2004). A set of twenty natural as-recorded ground motions were collected from international  
124 databases (PEER NGA strong motion database) and employed in the FE model. Each earthquake  
125 sample consisted of two horizontal components (X and Y, global axes) to simulate a far-field  
126 condition (epicentral distance –  $R \geq 20\text{km}$ ). Table 1 provides the seismological parameters of the  
127 selected ground motion excitations. A time gap between mainshocks and aftershocks is assumed  
128 equal to thirty times the first fundamental frequency of the building to bring the structure to the rest  
129 and cease any movement caused by damping (Figure 1).



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Figure 1. An example of the mainshock, aftershock and earthquake sequence used in this study

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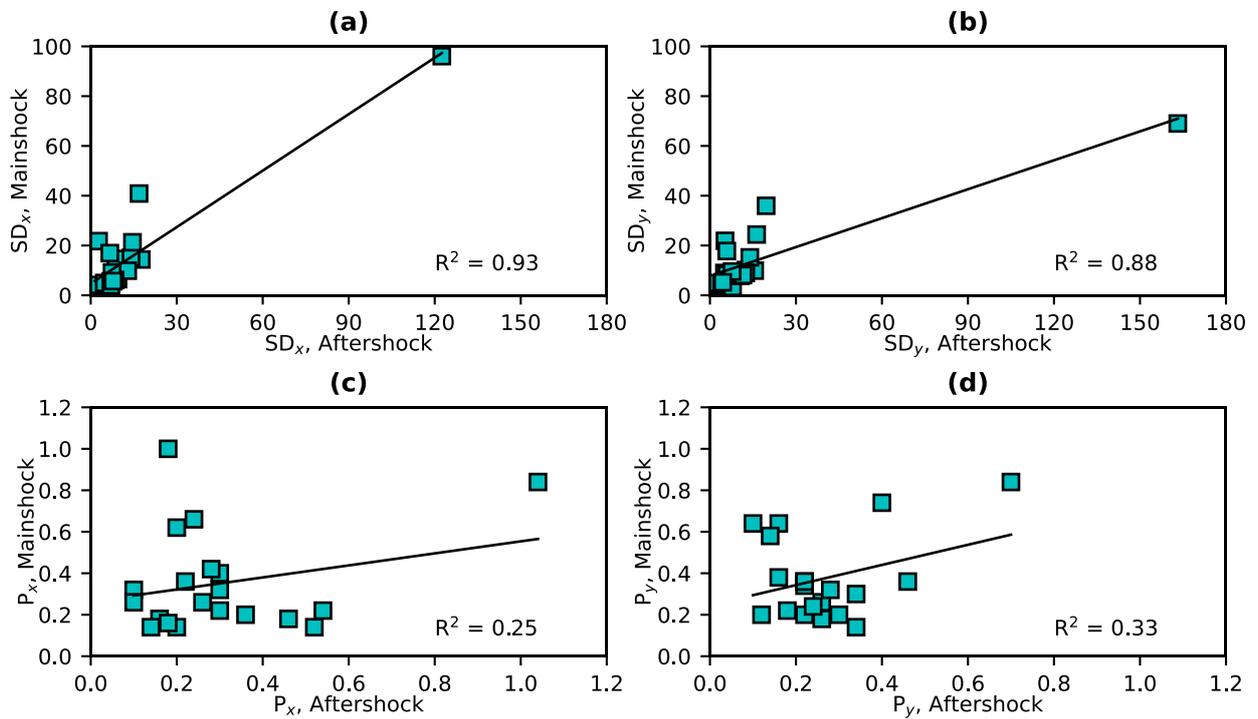
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The statistical correlation of significant duration (X and Y) and predominant period (X and Y) for mainshock and aftershock ground motion pairs was investigated and depicted in Figures 2 (Song et al., 2014). Aftershocks were found mildly correlated to their mainshock counterpart for the significant duration and weakly correlated for the predominant period.

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Figure 2. Correlation between mainshocks and aftershocks: (a) Significant Duration along X; (b) Significant Duration along Y; (c) Predominant Period along X and (d) Predominant Period along Y

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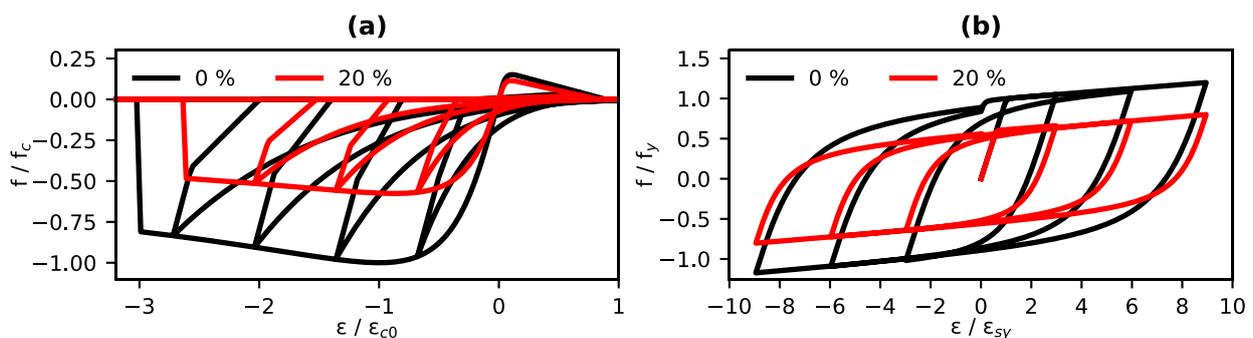
#### 4. RC BUILDING MODEL

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An existing four-storey RC building was used as testbed and implemented in an advanced FE software (Seismostruct, 2018). Cross-sections of columns were 350x350 mm<sup>2</sup> for the ground floor and

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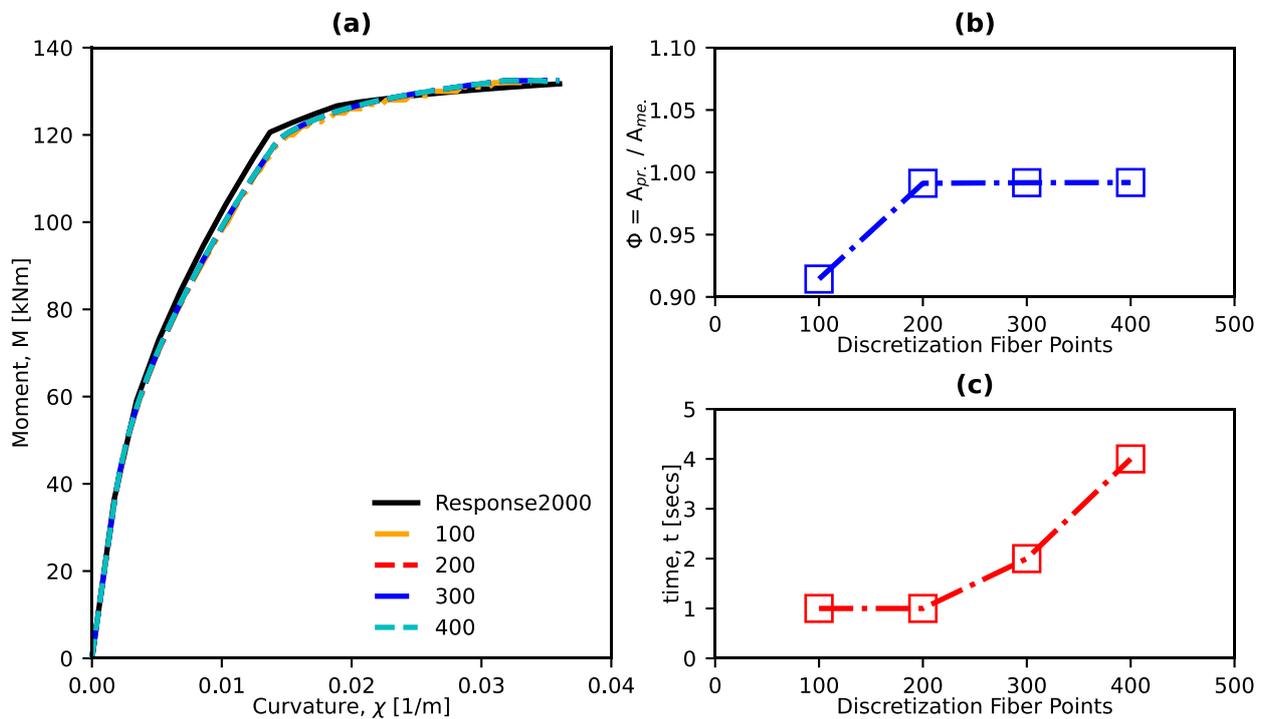
144 300x300 mm<sup>2</sup> for the remaining floors, reinforced with 6-Φ16mm longitudinal rebars and Φ6mm  
 145 transverse stirrups with 150mm spacing. The beams had different cross-sections (edged beams  
 146 300x500 mm<sup>2</sup>, internal beams 800x200 mm<sup>2</sup>), mainly reinforced with Φ14- Φ10 longitudinal bars  
 147 and Φ6 transverse rebars with 200mm spacing. The initial compressive strength of the concrete and  
 148 yielding stress of steel reinforcement were taken equal to 20 MPa and 440 MPa, respectively,  
 149 according to original design specifications and some studies from the literature for existing RC  
 150 buildings built in Italy between the 60s and 70s (i.e. Verderame et al., 2010; De Luca and Verderame,  
 151 2013; Manfredi et al., 2014). Then, a confidence factor of 1.2 was applied due to the uncertainties  
 152 and incomplete information for materials and geometry. Both columns and beams were discretized  
 153 into small fibres for the cross-sectional response, using various degrees of mesh density and defined  
 154 with proper stress-strain relationships. To adequately predict the response of RC columns and beams,  
 155 accurate models for concrete (cover and core) and steel reinforcements should be considered. Chang-  
 156 Mander (1989) and Monti-Nuti (1992) constitutive material models for concrete and steel  
 157 reinforcement were herein used (Figures 3). Such materials have been numerically identified to  
 158 accurately simulate the seismic response of un-corroded and corroded RC components (Di Sarno and  
 159 Pugliese, 2019 and 2020a).



160  
 161 Figure 3. Example of un-corroded and corroded constitutive material model: (a) Concrete Chang-Mander (1989) and (b)  
 162 Steel Monti-Nuti (1992)

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 164 The well-known and documented distributed-plasticity through force-based elements with five  
 165 integration points was adopted (Spacone et al., 1996, Part I and Part II), both for columns and beams.  
 166 Yet, the accuracy and reliability of the cross-sectional response of columns and beams strongly  
 167 depend upon the mesh density of the core and cover concrete. Thus, a calibration of such mesh size  
 168 was needed to find the best trade-off between efficiency and minimal computational cost demand. A  
 169 range of fibers between 100-to-400 was chosen to calculate the moment-curvature of a two-  
 170 dimensional inelastic force-based element implemented in the software. The numerical results were  
 171 validated against the moment-curvature generated by the analysis open-source program

172 Response2000 (Bentz and Collins, 2001) developed at the University of Toronto and shown in  
 173 Figures 4. Moreover, the area predicted (from the numerical analysis) over the area measured (from  
 174 Response2000) through the trapezoidal rule and the computational time were plotted versus the  
 175 numbers of discretized fibers in Figure 4b and 4c (users can choose the number of discretization  
 176 points ( $n_{dp}$ ), but the software will automatically divided the fibers for core and cover concrete as for  
 177 a non-uniform discretization).

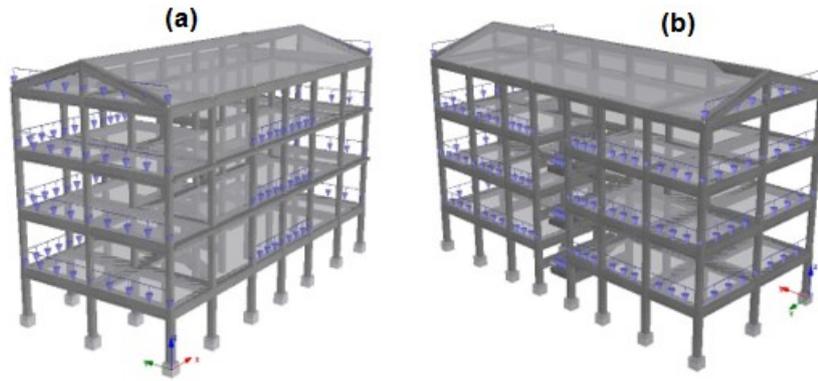


178  
 179 Figure 4. Moment-Curvature ( $M-\chi$ ) validation model in Seismostuct: (a)  $M-\chi$  comparison with different discretization  
 180 schemes; (b) Area predicted over area measured vs discretization schemes; (c) computational time cost demand vs  
 181 discretization schemes

182  
 183 Outcomes showed that a number of fibers beyond 200 did not further improve the accuracy of the  
 184 cross-sectional response (the ratio  $\Phi = A_{predicted}/A_{measured}$  was almost equal to 1 for  $n_{dp} \geq 200$ ), but  
 185 rather doubled the computational time. Therefore,  $n_{dp}$  equal to 200 was the compromise between  
 186 efficiency and numerical demand.

187 Rigid diaphragms were implemented to model slabs to ensure in-plane stiffness properties, while all  
 188 the joints were connected through fully-supported-rigid-connections (all degrees of freedom were  
 189 restrained) to the ground. A comprehensive and accurate loading analysis was conducted and applied  
 190 to building model. The FE model view is given in Figure 5.

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## 5. CORROSION MODELLING APPROACH

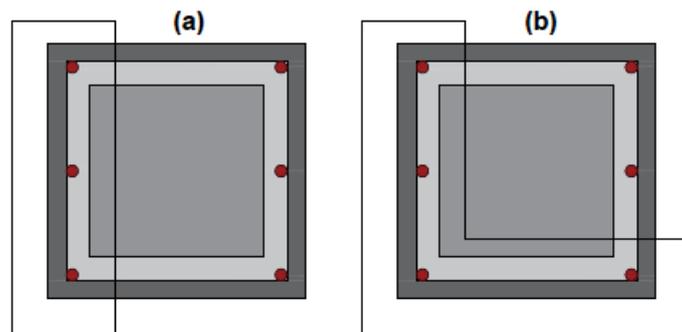
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Typically, RC components are protected by infills which can produce either a one- or two-sided attack; as a result, corrosion was applied only to external beams and columns in order to simulate a realistic exposure (Figure 6).



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Figure 6. Typical 350x350 mm<sup>2</sup> RC column. (a) one-sided and (b) two-sided attack

Since the RC building is close to a marine environment, the presence of high chloride contents is likely to generate localized corrosion. Pitting corrosion is more detrimental than uniform corrosion and it is related to the depth of pits along the steel bar. Thus, the mass and diameter losses of steel reinforcement refer to the ratio between the maximum pit depth and the mean of such pits along the bar (pitting factor – R), which can be expressed as follows:

$$R = \frac{X_{\max}}{X_{\text{mean}}} \quad (1)$$

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211 The maximum penetration ( $X_{max}$ ) of pitting corrosion is about four-to-eight times the average  
 212 penetration (uniform corrosion) on the steel rebars (Gonzales et al., 1995). Moreover, Yu et al. (2015)  
 213 carried out an experimental investigation to study the corrosion distribution of steel bars of RC beams  
 214 exposed to natural corrosion. They found that the pitting factor (R) ranged between 2.5 and 5.0;  
 215 however, the measured maximum depth of the corrosion penetration was equal to five over an average  
 216 cross-sectional loss of 5-to-20%. Thus, a pitting factor of 5 was assumed in this study.

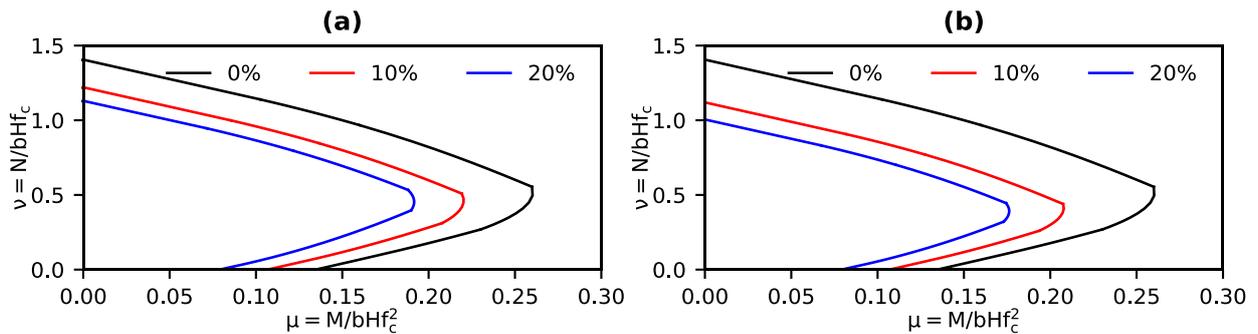
217 The corrosion reinforcement ratio (CR [%]) in terms of area loss was expressed as:

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$$CR[\%] = \frac{A_0 - A_p}{A_0} \times 100 \quad (2)$$

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220 where  $A_0$  is the area of the un-corroded steel bar, and  $A_p$  is the net cross-sectional area of the corroded  
 221 rebar. The model proposed by Rodriguez et al. (1997) was used to estimate the residual cross-section  
 222 area of steel bars. Hence, the compressive strength of the concrete and the mechanical properties of  
 223 steel reinforcement, in terms of strength and ductility, were modified according to Di Sarno and  
 224 Pugliese (2019 and 2020a). Figure 7 depicts the prediction of the residual capacity of the corroded  
 225 (one-side and two-side) RC cross-section according to the above-mentioned model.



226

227 Figure 7. Interaction surface axial load-bending moment: (a) one-sided attack; (b) two-sided attack

228 The main aspects in the structural modelling, such as the evolution and the reduction of the geometry  
 229 and material properties due to the effects of corrosion can be summarized, as follows (Figure 8):

- 230 - Reduction of steel rebars area using the Rodriguez's model;
- 231 - Change in the yielding and ultimate strength of the steel reinforcement;
- 232 - Change in the ductility (reduction of the ultimate strain) of steel rebars;
- 233 - Reduction of the strength and ductility of the concrete cover and core. (Concrete cracking is  
 234 associated with the strain at the peak of compressive strength and taken as  $\epsilon_{c0} = f_c^{0.25}/1100$   
 235 (Chang and Mander, 1989). It decreases with the reduction of the concrete compressive  
 236 strength. The value of the ultimate strain is taken three times  $\epsilon_{c0}$  (Chang and Mander, 1989),

237 and reduced accordingly. Once spalling of cover concrete occurs, this layer does not  
 238 contribute any longer to the response of the RC component);  
 239 - Reduction of the flexural stiffness of RC components ( $E_c = 8200f_c^{0.375}$ , decreases according  
 240 to the reduction of the concrete compressive strength);  
 241 Further details on the constitutive models of steel reinforcement and concrete, and the seismic  
 242 response of RC columns subjected to corrosion effects can be found in Di Sarno and Pugliese (2020a).

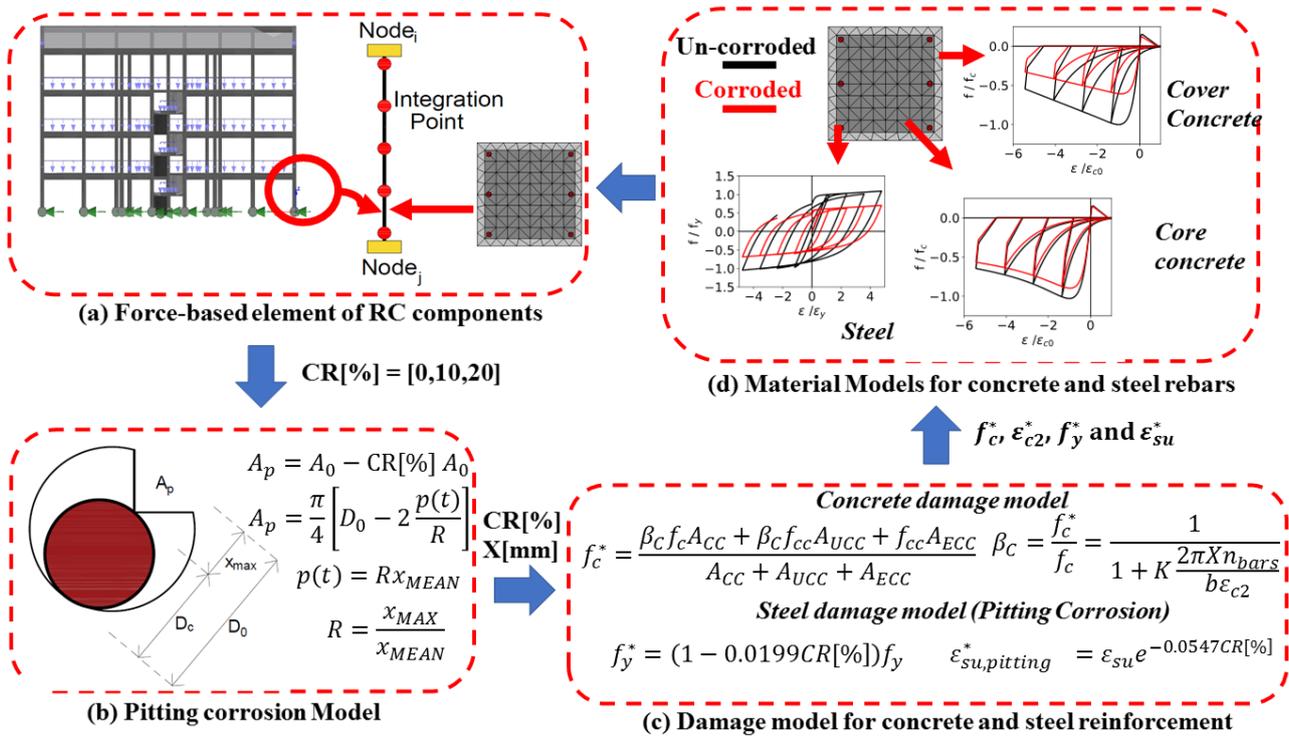


Figure 8. Simulation procedure of pitting corrosion

## 6. SEISMIC FRAGILITY EVALUATION

246 The inelastic response of the existing RC building was evaluated through the IDA procedure  
 247 (Vamvatsikos and Cornell, 2002). The structure was subjected to three different earthquake  
 248 excitations, i.e. (a) mainshock, (b) aftershock and (c) mainshock-aftershock sequence, and various  
 249 levels of corrosion rates, i.e. CR [%] = 0%,10%, and 20%.

250 The set of ground motions were adequately scaled to simulate the linear and nonlinear response of  
 251 the RC building using the hunt-fill algorithm (Vamvatsikos and Cornell, 2004). This method was  
 252 used to (a) pick an initial elastic brunch (e.g. PGA = 0.005g) with six steps until the first non-  
 253 convergence issue was obtained in terms of infinite value of the inter-storey displacement, and (b)  
 254 the inelastic response (“flatline”) with two additional steps. Such additional scaling-coefficients  
 255 referred to either the structure collapse or large inter-storey drift ratios. A typical relationship between  
 256 damage measure quantity (engineering demand parameter - EDP) and intensity measure (IM) was

257 then obtained by interpolation. EDP was herein related to the maximum inter-storey displacement  
 258 ( $\vartheta_{MAX}$ ). Then, the seismic fragility analysis was carried out.

259 The seismic probability risk assessment method is the most widely adopted approach for the  
 260 evaluation of the global and local response of RC structures. Such seismic vulnerability assessment  
 261 requires the definition of a specific limit to obtain the probability of exceedance by using the  
 262 following relationship (3):

$$P(EDP_i \geq EDP_{LS}|IM = x) = \Phi \left[ \frac{1}{\beta_i} \ln \left( \frac{IM}{LS_i} \right) \right] \quad (3)$$

263 where P is the probability of exceedance of the specified limit state based on ground motion intensity,  
 264  $\Phi$  is the probability density function of a normal distribution,  $\beta_i$  is the lognormal standard deviation,  
 265 and  $LS_i$  is the median value that represented a ground motion intensity that has 50% probability for  
 266 the occurrence of the defined limit state.

267 Three limit states were explicitly adopted in this study such as limited damage (LD), significant  
 268 damage (SD) and near collapse (NC). Such structural limits were identified by performing nonlinear  
 269 static analyses on the existing RC building, in both global directions X and Y, including three  
 270 different lateral loading patterns (the mean values were obtained using the square root of sum of  
 271 squares - SRSS) and the examined levels of corrosion. The maximum inter-storey drift ratio (MIDR)  
 272 threshold values are shown in Table 2. Further details on the definition of the performance points can  
 273 be found in the study of [Di Sarno and Pugliese \(2020a\)](#).

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Table 1. Limit States expressed as inter-storey drift ratio, IDR [%]

Corrosion Rate - CR [%]	NC [%]	SD [%]	LD [%]
0	2.30	1.87	1.06
10	1.69	1.44	0.93
20	1.21	1.17	0.90

276 (*Keynote*: NC = Near Collapse; SD = Severe Damage; LD = Limited Damage).

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## 278 7. SEISMIC INTENSITY MEASURE

279 The probabilistic approach for the evaluation of the seismic vulnerability of RC structures is related  
 280 to an appropriate estimation of the seismic intensity measure that leads to an adequate characterization  
 281 of the relationship between the earthquake excitation features and the inelastic behaviour of RC  
 282 structures. Since IM is capable of quantitatively affecting the seismic response, a proper choice should  
 283 be then carried out. This study investigates three different IMs: (a) peak ground acceleration (PGA),  
 284 (b) spectral acceleration at the first natural period of the building ( $Sa[T_1]$ ), and the modified

285 acceleration spectrum intensity (MASI) that accounts for the elongation period of the structure during  
 286 an earthquake occurrence.

287 PGA is the most widely adopted parameter for engineering applications as it is explicitly related to  
 288 the inertia forces that appear in structures. Although widely used, it has been criticized for its weak  
 289 correlation with  $\vartheta_{MAX}$ . Thus, it is often challenging to obtain a reasonable fitting. An overestimation,  
 290 in fact, of the structural seismic vulnerability may occur as a result of this weak correlation.  $S_a$  is the  
 291 spectral acceleration that represents a measure of what the structure experiences during an earthquake,  
 292 while  $S_a[T_1]$  is the spectral acceleration concerning the first natural period of the structure. The last  
 293 parameter is commonly used because of its accurate fitting with the EDP and for its adequate  
 294 correlation with ground motion and building information. As a result, modal analyses were performed  
 295 for each level of corrosion and  $T_1$  used for computing the spectral acceleration. MASI is the modified  
 296 acceleration spectrum intensity. Such seismic IM requires the definition of two periods of vibration  
 297 of an RC structure. Typically, strong ground motions force the structures to elongate their natural  
 298 periods and, thus, a direct measure of the inelastic response of the building and the associated damage.  
 299 Although laborious to estimate, Eurocode 8 (EN 1998 – Part-3, 2004) states that the maximum  
 300 elongation period due to the non-linear behaviour is twice the fundamental period of the structure,  
 301 which is reasonable for existing non-seismic designed structures. It can be defined as follows:

$$MASI = \int_{T_1}^{2T_1} S_a(T) dT \quad (4)$$

302  
 303 To find out whether or not an IM is optimal, some researchers (e.g. Mackie et al., 2001; Cornell et  
 304 al., 2002; Giovenale et al., 2004; Luco et al., 2007; Padgett et al., 2008, among others) proposed  
 305 feasible criteria such as efficiency, sufficiency, practicality, proficiency and hazard computability.  
 306 The efficiency criterion refers to the dispersion of the seismic demand, that is the logarithmic standard  
 307 deviation ( $\sigma_{\log \eta | IM}$ ) of the pair EDP-IM. Low values of  $\sigma_{\log \eta | IM}$  results in less dispersion of EDP-IM  
 308 interpolation.

$$E \left[ \left( \frac{\theta_{MAX}}{\theta_{LSi}} \middle| IM_i \right) \right] = \log \eta | IM = \log a + b \log IM \quad (5)$$

$$\sigma_{\log \eta | IM} = \sqrt{\frac{\sum_{i=1}^n \left( \log \frac{\theta_{MAX}}{\theta_{LSi}} - \log \eta | IM \right)^2}{n - 2}} \quad (6)$$

310

311 Practicality is associated with the dependency of the intensity measure to the seismic demand. Such  
312 IM refers to the slope of the fitting curve ( $b$  in eq. 5). The larger the values of the slope, the more  
313 practical the IM is. Proficiency was introduced by Padgett et al. (2008), and it is an explicit measure  
314 for balancing the efficiency and practicality. It is defined as the ratio between the logarithmic standard  
315 deviation of the seismic demand and the slope of the fitting curve. Small values of this ratio imply  
316 higher proficiency for IM ( $\psi = \sigma_{\log \eta_{IM}}/b$ ). Finally, the sufficiency is a measure of the statistical  
317 independence from the ground motion parameters (e.g. magnitude). The sufficiency can be estimated  
318 through the slope of the linear regression between the residuals (EDP-IMs) and magnitude of the  
319 selected ground motions. The smaller the slope, the higher the sufficiency.

320 To obtain the relationship between EDP and IM for the entire the case-studies (mainshock, aftershock  
321 and mainshock-aftershock sequence), the set of twenty ground motions were employed in the FE  
322 model in both global directions (X and Y), while the SRSS was used to combine those parameters.  
323 The values of  $\mathfrak{G}_{MAX}$  obtained from the numerical analysis were normalized with respect to the limit  
324 state of SD. However, it can be demonstrated that each limit state leads to the same result.

325 Evaluation of the optimal IM for the case-study RC building was conducted using the three  
326 earthquake scenarios (aftershock, mainshock, and mainshock-aftershock sequence motions) and  
327 shown in Figures 9, 10 and 11. As illustrated in the figures, MASI appeared to be the most efficient  
328 IM as it allows to obtain a reduced variability in the structural response due to its lowest value of the  
329 standard error compared to the other examined IMs. The high efficiency of MASI could probably lie  
330 in the relevant inelastic effects of higher modes included in the period range  $T_1 - 2T_1$  that allowed to  
331 capture the degree of non-linearity of the structural response. The last finding was also observed when  
332 corrosion increased. Similar results were obtained for  $Sa(T_1)$  which exhibited a slight increase in the  
333 standard error when the building was subjected to the effects of corrosion. Such a gap disappeared  
334 for the seismic sequence (mainshock-aftershock), possibly due to the damage accumulation and larger  
335 natural frequencies (beyond  $2T_1$ ) experienced from the structure during the occurrence of the multiple  
336 excitation, which was not included in the evaluation of MASI. Conversely, the highest dispersion  
337 exhibited by PGA demonstrated its poor effectiveness to measure the damage potential for RC  
338 structures.

339 Instead, large values of the slope of the data interpolation line allowed to recognize the high  
340 practicality of all IMs, even when the RC building was under earthquake sequences and increasing  
341 level of corrosion, which implied a strong correlation of such seismic intensity parameters with the  
342 engineering demand by means of the inter-storey displacement.

343 Moreover, Figures 9, 10 and 11 show that MASI was the most proficient IM considering the entire  
344 earthquake and corrosion case-studies. The last finding indicates that such a seismic parameter needs

345 reduced number of non-linear analyses to estimate the seismic vulnerability of a corroded and  
346 uncorroded RC structure under various earthquake condition while reducing the uncertainty into the  
347 model analysis.

348 Figures 12 depict the evaluation of the sufficiency for the investigated IMs. The results illustrate that  
349 PGA is strongly correlated to the earthquake features because of its highest slope of the fitting curve.  
350 On the other hand, MASI seemed to be completely independent from the earthquake characteristics  
351 with the approximately zero slope of the linear interpolation. This last observation could be confirmed  
352 by the structural information parameters included in the evaluation of such IM, which is reliable and  
353 accurate even when the building is subjected to detrimental effects (i.e. pitting corrosion)

## 354 8. SEISMIC FRAGILITY ANALYSIS

355 The damage analysis is herein used to estimate the probability of failure for specific limit states. Such  
356 failure probability is investigated at both components and global systems as a function of the inelastic  
357 response, and for a given intensity measure. The statistical approach used for this type of analyses,  
358 which correlates the demand and the capacity, is the “fragility analysis”. Three limit states are  
359 discussed hereafter: (a) Limited Damage – LD, (b) Severe or Significant Damage – SD, and (c) Near  
360 Collapse – (NC).

361

### 362 8.1 LIMITED DAMAGE

363 Current seismic regulations commonly account for single strong ground motions to evaluate the  
364 seismic response of RC structures; as a result, earthquake sequences and corrosion are often  
365 neglected. However, such detrimental phenomena could cause additional damage and deterioration  
366 that may lead to an overprediction of the actual response of existing RC buildings if those stated  
367 threshold limits (EN 1998 – Part-3, 2004) are being used. Therefore, the fragility curves were built  
368 using both the limit states from technical codes (i.e.  $d/H = 1\%$  for the limit state of LD; EC in Figures)  
369 and non-linear static pushover analyses (i.e. Table 2; SPO in Figures).

370 Figures 13 show the fragility curves and the difference in the failure probability of the RC building  
371 subjected to aftershock motions and various levels of corrosion. Although the limit state of LD  
372 occurred for low-scaled ground motions, results from the numerical simulations showed a significant  
373 reduction of the seismic capacity and a relevant increase in the failure probability of the corroded RC  
374 building. For the limit state of SPOs, the RC building with CR=10% exhibited the maximum increase  
375 in the probability of exceedance of 27.4% at a PGA of 0.251g, whereas for CR=20% the failure  
376 probability showed an increment of 27.2% at a PGA of 0.241g. On the contrary, it produced an

377 increase in the fragility equal to 20.2% and 23.2% at PGAs of 0.260g and 0.241g, respectively, for  
378 the limit state posed by Eurocode 8 (EN 1998 – Part-3, 2004). A more relevant impact of corrosion  
379 was instead observed for the IMs of MASI and Sa(T1). On the one hand, the probability of exceedance  
380 using the SPO limits ranged between 56.7% and 67.2% for the examined corrosion rates at almost  
381 the same Sa(T1) (0.240g), compared to 45.8% and 54.8% obtained from EC limits at a Sa(T1) of  
382 0.235g. On the other hand, MASI demonstrated an increase in the failure probability by 45.1% and  
383 53.7% for CR=10% and 20%, respectively, in contrast to the smaller values of 34.5% and 41.1% for  
384 the current technical codes.

385 Figures 14 and 15 show the seismic fragility assessment for the RC building subjected to mainshock  
386 and sequence motions. Compared to aftershock motions, mainshock and earthquake sequences  
387 produced larger inter-storey displacements and an increase in the structural vulnerability. The last  
388 observations can be explained by stronger and longer (in duration) ground motions and additional  
389 damage produced by multiple earthquakes.

390 It can be observed in Figures 14 that the corroded RC building (CR=20%) under mainshock motions  
391 exhibited the maximum increment in the failure probability of 66% and 71.5% for the IMs of MASI  
392 and Sa(T1), respectively, while PGA produced a more conservative increase (41.8%). Unlike  
393 mainshock earthquakes, the effects of sequential motions exposed the structure to larger inter-storey  
394 drift ratios and a faster redistribution of the seismic forces due to the short time of occurrence between  
395 the mainshock and the aftershock. The above implied further damage and an increase in the  
396 vulnerability of the RC structure, about 85.9% for the modified ASI and Sa(T1), and 45.6% for the  
397 PGA, which led to an increment 17% in contrast to the mainshock case-study. In addition, the fragility  
398 curves, both for mainshocks and multiple earthquakes, for the threshold limit stated in the Eurocode  
399 8 (EN 1998 – Part-3, 2004) were investigated. Such fragility curves yielded slightly more  
400 conservative failure probabilities as opposed to those obtained using the limits from the non-linear  
401 static pushover of the corroded building (Black lines in Figures 14 and 15). The last finding can be  
402 explained by similar values of the threshold limits stated in the Eurocode 8 (EN 1998 – Part-3, 2004)  
403 and those obtained from the non-linear static analyses.

404 Finally, the comparison of the fragility curves for each case-study ground motion demonstrated that  
405 the damage associated with the seismic sequences almost doubled the failure probability of the RC  
406 structure for each IMs compared to the aftershock and mainshock scenarios.

## 407 8.2 SEVERE DAMAGE

408 The limit state of severe damage (SD) usually occurs for high values of the scaled records when  
409 performing the IDAs, which implies more evident effects of corrosion due to the relevant decay of

410 both the structural stiffness and lateral strength. The threshold limit from the Eurocode 8 (EN 1998 –  
411 Part-3, 2004) for the SD, in terms of inter-storey drift ratio, was herein taken equal to 2%.

412 Figures 16 show the fragility assessment conducted for the RC building subjected to aftershock  
413 motions. Results from the numerical analyses demonstrated that the overall seismic fragility at the  
414 system level increased as the RC building continued to corrode. For example, for a ground motion  
415 with  $PGA = 0.4g$ , the probability that the pristine building could exceed the limit state of SD was  
416 30%, in comparison with 75% and 85% with  $CR=10\%$  and  $20\%$ , respectively. The maximum  
417 increment in the failure probability was achieved at PGAs of  $0.391g$  and  $0.341g$  with a total increase  
418 of 27.6% and 40.7 for the examined corrosion rates. Conversely, MASI and  $S_a$  produced completely  
419 different results as opposed to those obtained by using the PGA as IM. Although showing similar  
420 trends, the values of the failure probabilities over the corrosion rates of 10%-to-20% ranged between  
421 47.6% and 66.6%, and between 59.7% and 79% for MASI and  $S_a(T1)$ , respectively.

422 Moreover, it is worthy noticing that the maximum inter-storey drift ratio stated in the Eurocode 8 (EN  
423 1998 – Part-3, 2004) generated more conservative failure probabilities, especially for the corroded  
424 RC building. The last observation can be confirmed by the large difference between the two threshold  
425 interval limits (SPO and EC) used in this study.

426 Figures 17 and 18 show instead the fragility curves of the RC structure exposed to mainshock and  
427 earthquake sequences. Unlike the aftershock scenario, mainshocks and seismic sequences caused a  
428 major reduction of the seismic capacity of the building and, thus, a large increase in the failure  
429 probability. In comparison with MASI and PGA, the IM related to  $S_a(T1)$  provided the highest  
430 increment in the seismic fragility when the RC structure was subjected to mainshock excitations.  
431 Such failure probabilities were equal to 75% and 90% for  $CR=10\%$  and  $20\%$ , respectively. Similar  
432 results, in terms of seismic vulnerability increments, were obtained for MASI. Conversely, the RC  
433 building with  $CR=10\%$  exhibited a probability of exceedance of 44% at a PGA of  $0.231g$ , whereas  
434 for  $CR=20\%$  the failure probability showed an increment of 60.6% at a PGA of  $0.210g$ .

435 On the other hand, it is evident (Figured 18) that the damage accumulation induced by multiple  
436 excitations caused a more extensive reduction of the seismic resistance of the RC building, compared  
437 to mainshock and aftershock scenarios. The fragility assessment for the multiple earthquakes (Figure  
438 18), indeed, led to a further increase in the failure probability of about 6.7% for the IMs of MASI and  
439  $S_a(T1)$ , and 10% for the PGA, in contrast to the building subjected to mainshock excitations.

440 Finally, the fragility curves (black lines in the figures) obtained by using the threshold limits posed  
441 by the Eurocode 8 (EN 1998 – Part-3, 2004) were plotted against the corrosion rates for all the  
442 earthquake scenarios and depicted with black lines. The fragility analysis implied large conservative  
443 results with almost 50% overprediction of the seismic vulnerability for each examined IM. The last

444 finding is a relevant indication of the lack of conservatism in the safety of non-seismic designed RC  
445 buildings exposed to various levels of corrosion and multiple earthquakes.

446

### 447 **8.3 NEAR COLLAPSE**

448 The definition of the limit state of Near Collapse (NC) is always associated with large plastic  
449 deformations and strong inelastic behaviour of RC structures. Both the maximum inter-storey drift  
450 ratios from technical codes (4%) and non-linear static analyses (Table 2) were hereafter used to build  
451 the fragility curves.

452 Figure 19 shows the fragility assessment carried out for the testbed building subjected to aftershock  
453 motions. The outcomes obtained from the numerical simulations demonstrated that the seismic  
454 vulnerability increased over the corrosion rates for all the examined seismic IMs. For instance, for a  
455 ground motion having a PGA = 0.4g and the threshold limits from SPOs, there is 27% chance of  
456 achieving the collapse, while the values of 61% and 83% were obtained for the building with  
457 CR=10% and 20%. Conversely, the drift ratio from the Eurocode 8 (EN 1998 – Part-3, 2004) and for  
458 the same PGA, produced smaller failure probabilities, between 9.8% and 19.7% for the un-corroded  
459 and corroded building. Compared to the PGA, Sa(T1) and MASI induced a larger increase in the  
460 failure probabilities. Such values were equal to 85% at a Sa(T1) = 0.381g and 74.5% at a MASI =  
461 0.161gs for the corrosion rate of 20% and the limits from Table 2. On the contrary, an overestimation  
462 of the seismic capacity could be observed for the fragility curves obtained using the limits from the  
463 Eurocode 8 (EN 1998 – Part-3, 2004).

464 Figures 20 instead illustrate the fragility assessment of the existing building subjected to mainshock  
465 motions. In comparison with aftershock case-study, mainshocks produced a larger increase in the  
466 seismic vulnerability of the testbed building. For example, the maximum increase in the failure  
467 probability was equal to 68% at a PGA = 0.231g, compared to 53% for the aftershock scenario.  
468 Instead, the values of 92.7% and 95% were observed for MASI and Sa(T1), which caused an  
469 increment of 23% and 11.7% in contrast with the structure subjected to aftershock motions. Such  
470 results were obtained performing fragility assessment with limits from non-linear static pushover  
471 analyses.

472 Unlike mainshocks, the effects of seismic sequences (Figures 21) almost doubled the seismic fragility  
473 of the structure when exposed to highly corrosive environments (i.e. CR= 20%). For example, a PGA  
474 equal to 0.231g produced a probability of exceedance equal to 75%, compared to 68% exhibited by  
475 the structure subjected to mainshock motions. On the contrary, both MASI and Sa(T1) showed similar  
476 trends with a total increase in the failure probability of 100% for the structure at a corrosion rate of

477 20%. Finally, the fragility curves computed by using the limit states from Eurocode 8 (EN 1998 –  
478 Part-3, 2004) led to smaller failure probabilities for each examined IM, which implied an  
479 overestimation of the real seismic capacity of the corroded building.

## 480 9. CONCLUSIONS

481 This analytical study contributes to providing a comprehensive framework for the performance of  
482 existing RC buildings under multiple excitations and various level of corrosion. The probabilistic  
483 fragility analysis was carried out to assess the seismic vulnerability of an existing four-storey RC  
484 building. A new seismic intensity measure based on the modified acceleration spectral intensity is  
485 presented. The proposed intensity measure accounts for the elongation period experienced by the  
486 structure during an earthquake event. The primary outcomes of the comprehensive numerical analyses  
487 can be summarised as follows:

488

- 489 - Results from the interpolation of the pair EDP-IM of un-scaled records based on the cloud  
490 method for assessing the efficiency, proficiency, practicality and sufficiency of the three IMs  
491 (i.e. PGA,  $Sa[T_1]$  and MASI), demonstrated that the newly formulated modified acceleration  
492 spectrum intensity, herein named MASI, appeared to be accurate and reliable for the  
493 evaluation of the seismic vulnerability of corroded RC structures. Such observations can be  
494 confirmed by low values of standard errors, high values of the slope of the power fitting line  
495 and small ratios between standard error and regression slope. Furthermore, the proposed  
496 intensity measure was also sufficient as it was un-correlated to the ground motion features,  
497 which is essential for the accuracy when performing fragility analysis;
- 498 - The effects of corrosion reduced the global seismic capacity of the testbed building and  
499 increased the failure probability for each examined limit states. PGA produced the lowest  
500 increments in the probability that the RC structure could exceed such threshold limits,  
501 compared to larger values obtained by using  $Sa(T_1)$  and MASI. According to the numerical  
502 simulations, the seismic vulnerability was almost doubled (increment of 100%) when using  
503 the last two seismic intensity measures, especially when the building was subjected to  
504 mainshocks and earthquake sequences. This finding can be explained by the building  
505 information, such its natural frequencies, included in those seismic parameters;
- 506 - The damage and deterioration caused by multiple excitations induced larger inter-storey drift  
507 ratios compared to single strong ground motions. As a result, the building exhibited a further  
508 increase of the seismic vulnerability, i.e. 17% for the limit state of limited damage, in contrast  
509 with mainshock motions;

- 510 - The difference in the failure probability between CR=10% and 20% was small for the limit  
511 state of limited damaged in contrast with larger differences observed for the limit states of  
512 severe damage and near collapse. This was due to the achievement of the limited damage for  
513 low-scaled motions where corrosion produced similar effects on structural stiffness and  
514 strength;
- 515 - The fragility assessment using the limit states from non-linear static analyses contributed to  
516 indicating that current technical codes are longer conservative towards the safety of existing  
517 RC buildings exposed to multiple earthquakes and various levels of corrosion. Therefore, new  
518 provision should be provided in newly revised seismic technical codes to account for such  
519 detrimental phenomena;
- 520 - Additional investigations should also consider employing the uncertainties when analysing  
521 advanced and refined finite element models of RC structures. For instance, the probabilistic  
522 distributions of the main mechanical and geometrical properties of RC components (i.e. cover  
523 depth, position of longitudinal bars, stirrups spacing, diameter loss of steel rebars) should be  
524 included in the structural model.
- 525 - Future works should account for the time-dependency of the corrosion effects on RC buildings  
526 (i.e. statistical approach for time initiation and propagation). This allows the evaluation of the  
527 seismic vulnerability based on the lifetime of the structure rather than using the corrosion rate.

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705 **12. APPENDIX**

706 **List of Tables:**

707 Table 1. Seismological parameters.

708 Table 2. Main Seismological Parameters

Earthquake	Date	Event type	PGA <sub>x</sub> [g]	PGA <sub>y</sub> [g]	SD <sub>x</sub> [sec]	SD <sub>y</sub> [sec]	IA <sub>x</sub> [m/sec]	IA <sub>y</sub> [m/sec]	P <sub>x</sub> [sec]	P <sub>y</sub> [sec]
Spitak, Armenia	07/12/1988	MS	0.20	0.18	7.90	10.15	0.31	0.24	0.22	0.34
		AS	0.08	0.04	9.24	12.54	0.06	0.02	0.54	0.22
Valparaiso, Chile	24/04/2017	MS	0.39	0.68	40.88	35.96	6.81	15.07	0.14	0.22
		AS	0.18	0.19	16.86	19.59	0.68	0.73	0.52	0.18
North-West, China	12/05/2008	MS	0.27	0.19	14.38	9.90	0.49	0.61	0.14	0.36
		AS	0.13	0.14	17.62	15.60	0.19	0.21	0.20	0.22
Kalamata, Greece	13/09/1986	MS	0.25	0.14	2.70	4.11	0.28	0.08	0.32	0.30
		AS	0.15	0.27	2.82	1.87	0.11	0.30	0.30	0.34
Chamoli, India	29/03/1999	MS	0.19	0.37	14.60	8.98	0.29	0.80	0.66	0.36
		AS	0.04	0.07	8.80	5.06	0.01	0.02	0.24	0.22
Varzaghan, Iran	11/08/2012	MS	0.45	0.36	5.58	8.28	1.45	0.80	0.18	0.18
		AS	0.51	0.54	6.97	5.95	1.65	1.88	0.16	0.26
Emilia, Italy	20/05/2012	MS	0.26	0.26	5.60	5.99	0.69	0.84	0.32	0.26
		AS	0.22	0.29	7.54	6.97	0.76	1.28	0.10	0.26
Friuli, Italy	11/09/1976	MS	0.34	0.30	4.14	4.93	0.79	1.21	0.26	0.64
		AS	0.12	0.08	1.46	2.20	0.03	0.01	0.10	0.10
Irpinia, Italy	23/11/1980	MS	0.25	0.36	15.08	15.24	1.19	1.39	0.36	0.20
		AS	0.07	0.08	14.06	13.90	0.07	0.07	0.22	0.22
Nocera Umbria, Italy	26/09/1997	MS	0.56	0.49	4.95	4.35	3.29	2.80	0.16	0.38
		AS	0.52	0.31	4.73	4.10	0.86	0.70	0.18	0.16
Fukushima, Japan	11/03/2011	MS	0.39	0.42	21.30	24.41	2.44	3.40	0.62	0.64
		AS	0.14	0.13	14.55	16.28	0.14	0.14	0.20	0.16
Niigata, Japan	16/06/1964	MS	0.41	0.54	96.08	69.02	2.43	3.51	0.26	0.32
		AS	0.55	0.53	122.47	163.19	2.66	3.47	0.26	0.28
Christchurch, New Zealand	22/02/2011	MS	0.22	0.18	4.00	3.33	0.22	0.17	1.00	0.58
		AS	0.17	0.16	7.05	7.89	0.20	0.13	0.18	0.14
Edgecumbe, New Zealand	02/03/1987	MS	0.32	0.50	6.47	7.79	1.67	1.91	0.40	0.36
		AS	0.08	0.11	9.50	10.60	0.09	0.11	0.30	0.46
Weber, New Zealand	13/05/1990	MS	0.15	0.19	9.88	8.98	0.17	0.23	0.18	0.20
		AS	0.20	0.26	12.90	12.49	0.38	0.43	0.46	0.30
Chi-Chi, Taiwan	21/09/1999	MS	0.95	0.91	21.76	21.89	9.31	6.97	0.84	0.84
		AS	0.47	0.22	2.73	5.25	1.80	0.43	1.04	0.70
Duzce, Turkey	12/11/1999	MS	0.30	0.30	16.94	17.78	1.58	1.87	0.42	0.20
		AS	0.15	0.22	6.66	5.88	0.15	0.29	0.28	0.12
Chalfant, USA	21/06/1986	MS	0.45	0.40	6.17	8.12	1.94	2.00	0.20	0.74
		AS	0.27	0.24	8.48	11.50	0.53	0.54	0.36	0.40
Mammoth, USA	25/05/1980	MS	0.42	0.44	9.18	9.56	2.25	2.60	0.22	0.14
		AS	0.16	0.18	7.46	7.72	0.24	0.20	0.30	0.34
Whittier, USA	01/10/1987	MS	0.39	0.29	5.70	5.22	0.87	0.81	0.14	0.24
		AS	0.21	0.18	7.82	4.45	0.12	0.16	0.14	0.24

(*Keynote:* MS = Mainshock; AS = Aftershock; SD = Significant Duration; IA = Arias Intensity; P = Predominant Period).

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715 **List of figures:**

716 **Figure 9.** Numerical relationship between the normalized maximum inter-storey displacement (EDP)  
717 and IM (PGA, Sa(T1), MASI) for aftershock motions: (a) CR [%] =0, (b) CR [%] =10, and (c) CR  
718 [%] =20%

719  
720 **Figure 10.** Numerical relationship between the normalized maximum inter-storey displacement  
721 (EDP) and IM (PGA, Sa(T1), MASI) for mainshock motions: (a) CR [%] =0, (b) CR [%] =10, and  
722 (c) CR [%] =20%

723  
724 **Figure 11.** Numerical relationship between the normalized maximum inter-storey displacement  
725 (EDP) and IM (PGA, Sa(T1), MASI) for earthquake sequences: (a) CR [%] =0, (b) CR [%] =10, and  
726 (c) CR [%] =20%

727  
728 **Figure 12.** IM residuals versus Earthquake Magnitude: (a) CR [%] =0, (b) CR [%] = 10, and (c) CR  
729 [%] = 20

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731 **(LIMITED DAMAGE – LD)**

732 **Figure 10.** (a) Fragility Curves for aftershock records and (b) Difference of failure probability (CR  
733 [%] = 0 as benchmark, Keynotes: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)

734  
735 **Figure 11.** (a) Fragility Curves for mainshock records and (b) Difference of failure probability (CR  
736 [%] = 0 as benchmark, Keynotes: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)

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738 **Figure 12.** (a) Fragility Curves for sequence records and (b) Difference of failure probability (CR  
739 [%] = 0 as benchmark, Keynotes: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)

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741 **(SEVERE DAMAGE - SD)**

742 **Figure 13.** (a) Fragility Curves for aftershock records and (b) Difference of failure probability (CR  
743 [%] = 0 as benchmark, Keynotes: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)

744  
745 **Figure 14.** (a) Fragility Curves for mainshock records and (b) Difference of failure probability (CR  
746 [%] = 0 as benchmark, Keynotes: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)

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748 **Figure 15.** (a) Fragility Curves for sequence records and (b) Difference of failure probability (CR  
749 [%] = 0 as benchmark, Keynotes: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)

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751 **(NEAR COLLAPSE - NC)**

752 **Figure 16.** (a) Fragility Curves for aftershock records and (b) Difference of failure probability (CR  
753 [%] = 0 as benchmark, Keynotes: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)

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755 **Figure 20.** (a) Fragility Curves for mainshock records and (b) Difference of failure probability (CR  
756 [%] = 0 as benchmark, Keynotes: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)

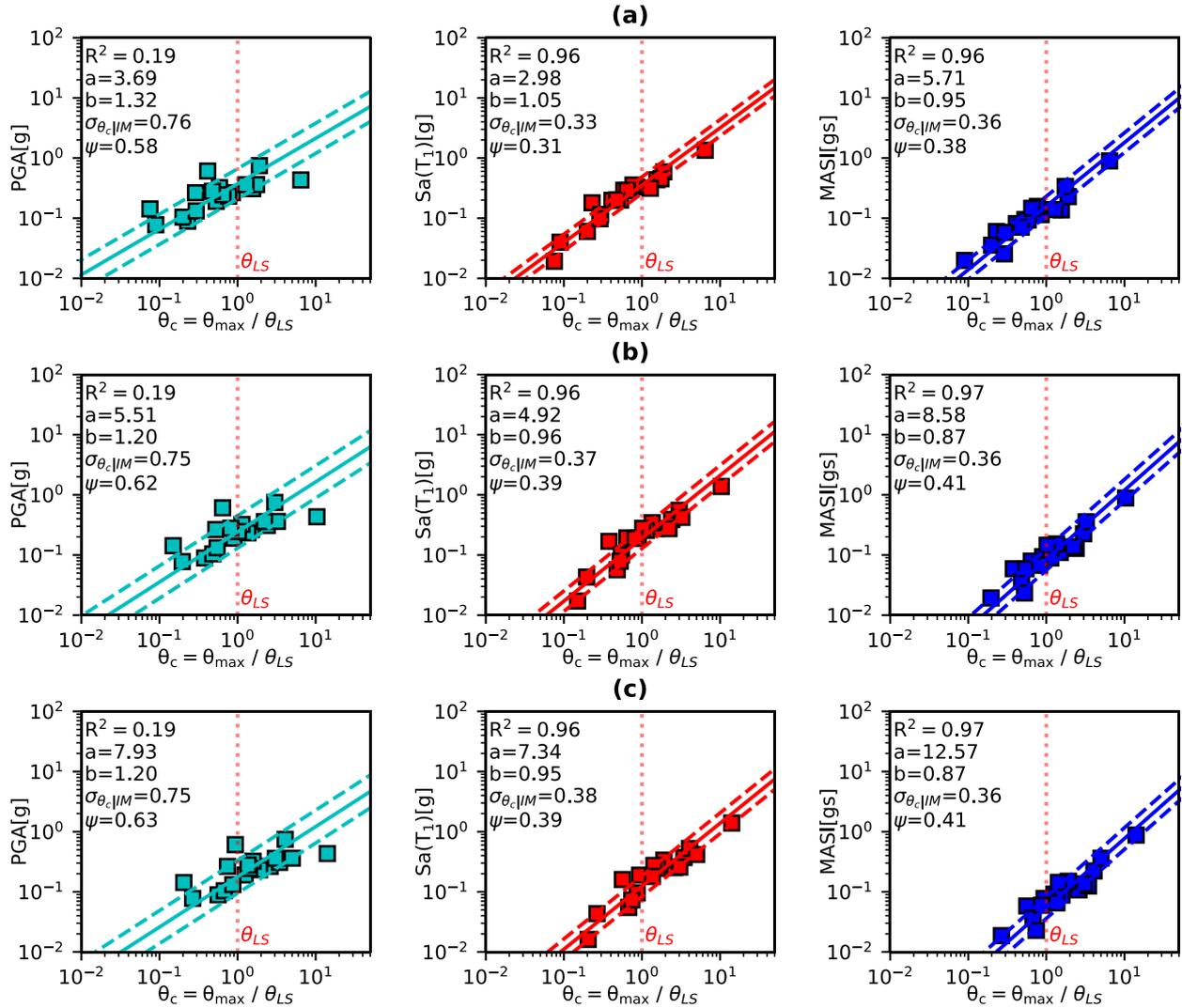
757  
758 **Figure 21.** (a) Fragility Curves for sequence records and (b) Difference of failure probability (CR  
759 [%] = 0 as benchmark, Keynotes: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)

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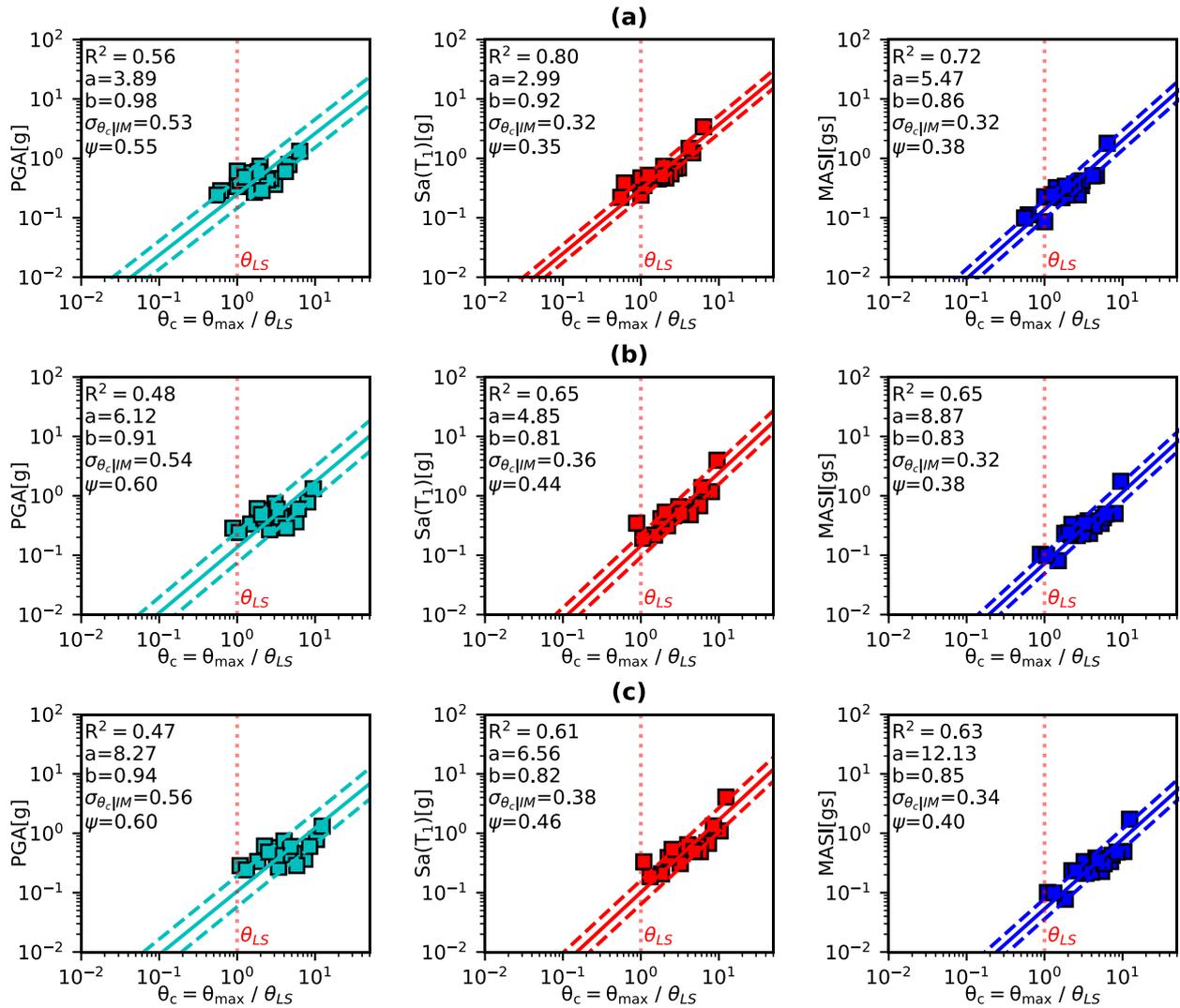
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Figure 17. Numerical relationship between the normalized maximum inter-storey displacement (EDP) and IM (PGA,  $Sa(T_1)$ , MASI) for aftershock motions: (a) CR [%]=0, (b) CR [%]=10, and (c) CR [%]=20%

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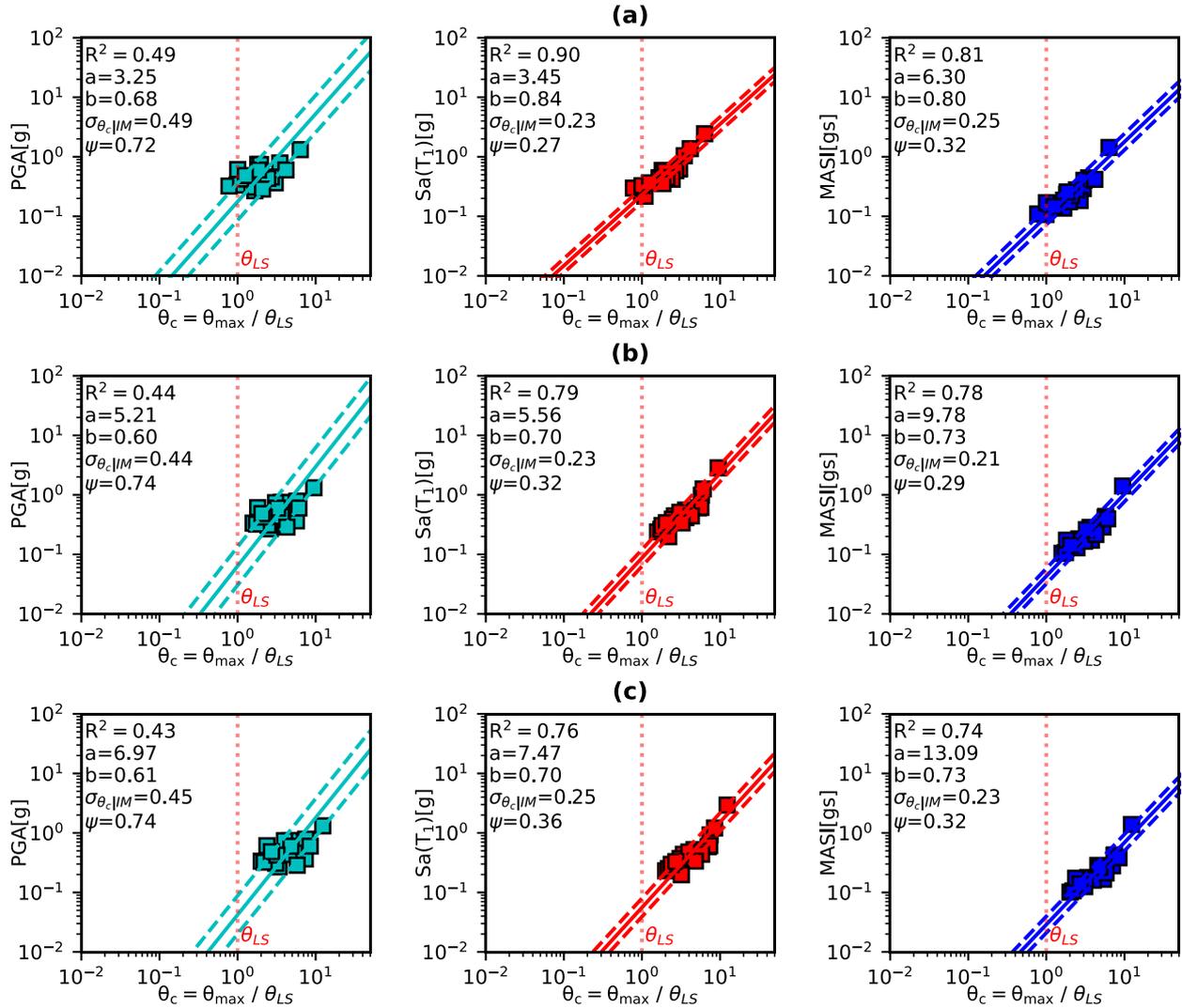


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Figure 18. Numerical relationship between the normalized maximum inter-storey displacement (EDP) and IM (PGA, Sa( $T_1$ ), MASI) for mainshock motions: (a) CR [%] = 0, (b) CR [%] = 10, and (c) CR [%] = 20%



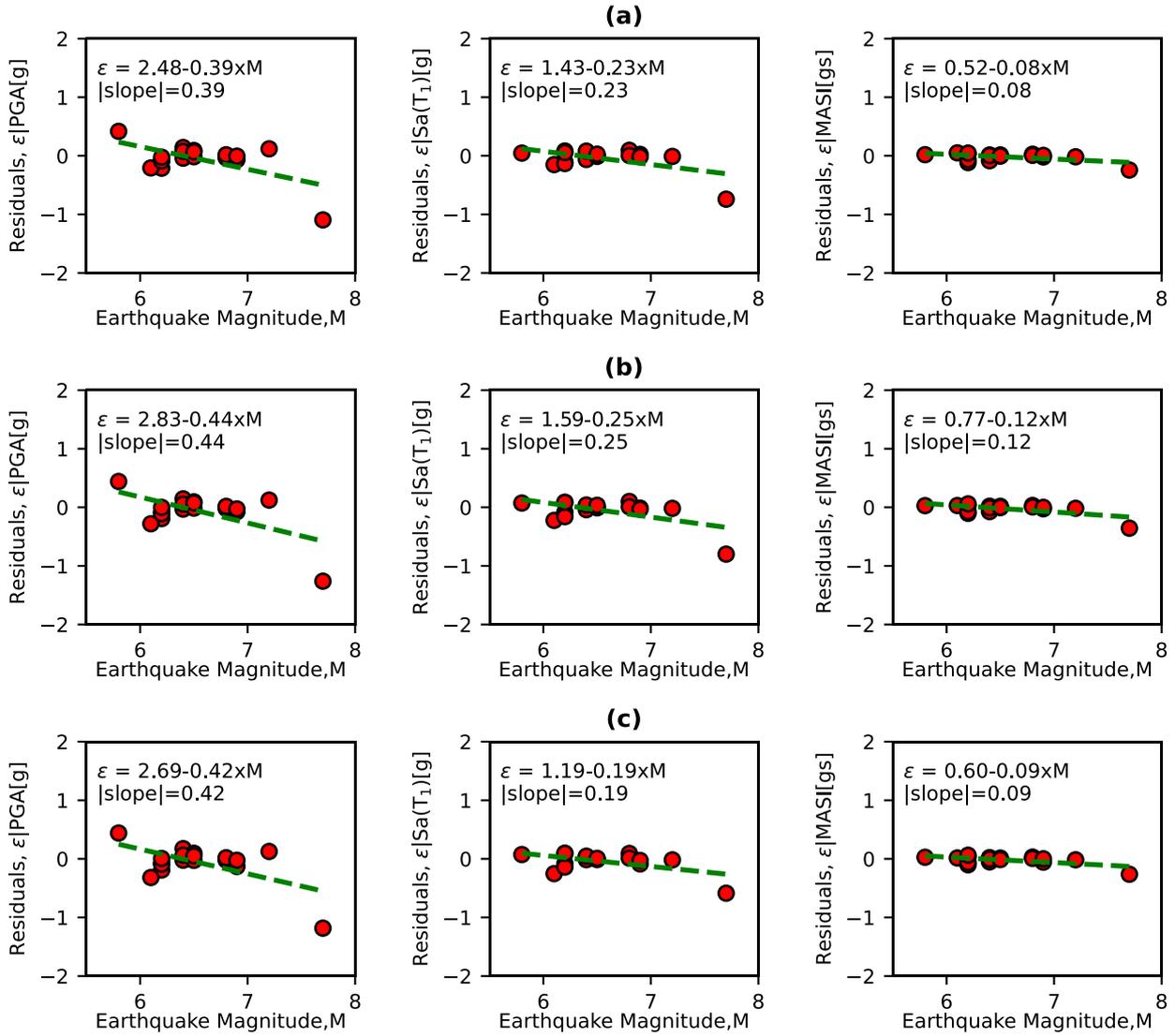
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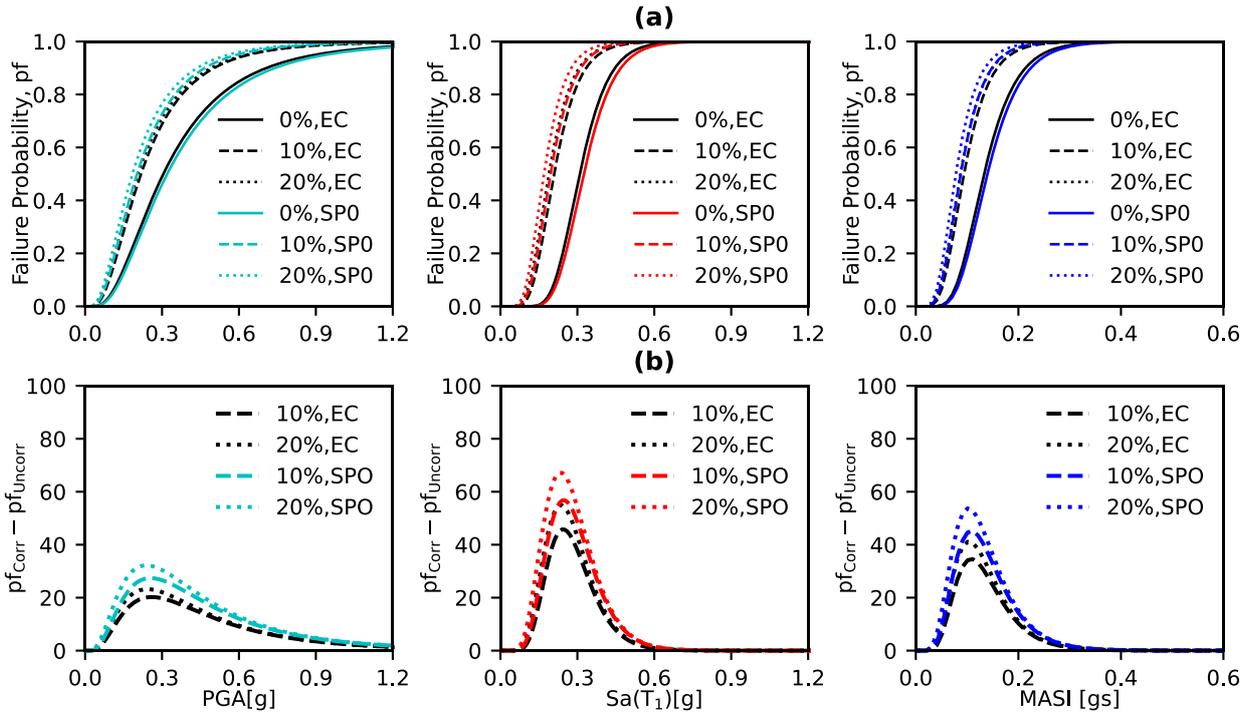
Figure 19. Numerical relationship between the normalized maximum inter-storey displacement (EDP) and IM (PGA,  $Sa(T_1)$ , MASI) for earthquake sequences: (a) CR [%]=0, (b) CR [%]=10, and (c) CR [%]=20%



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Figure 20. IM residuals versus Earthquake Magnitude: (a) CR [%] = 0, (b) CR [%] = 10, and (c) CR [%] = 20



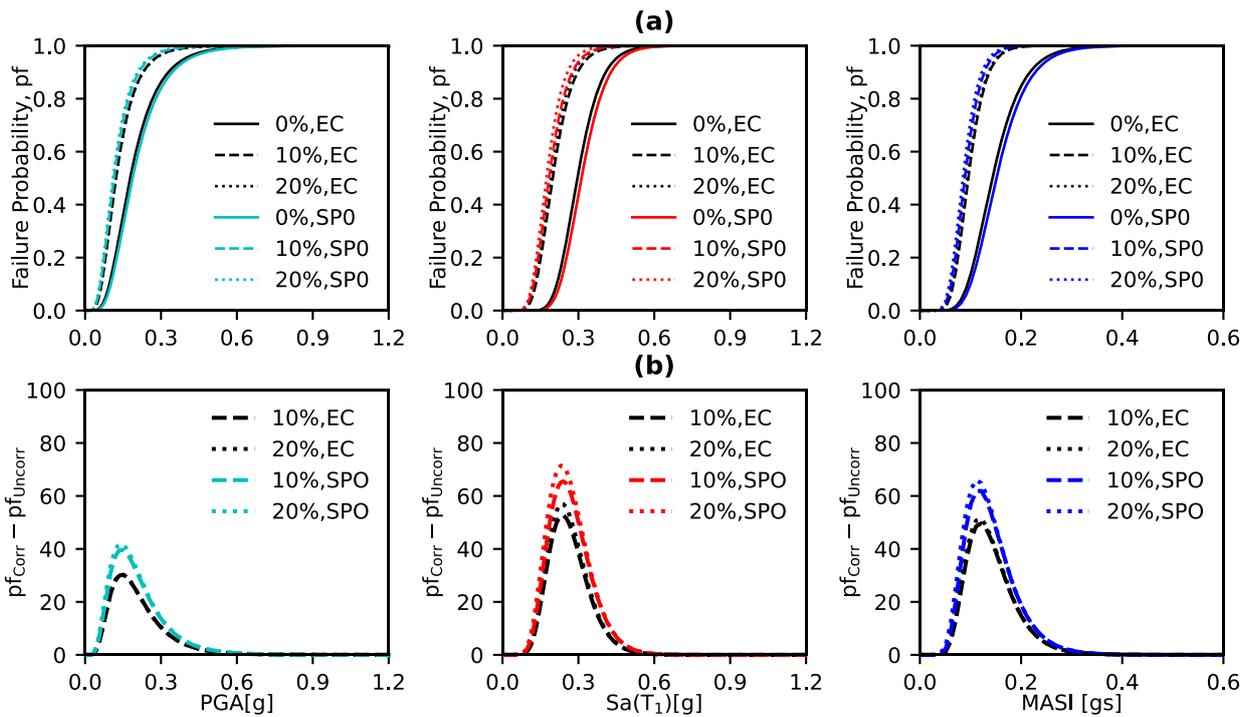
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Figure 21. (a) Fragility Curves for aftershock records and (b) Difference of failure probability (CR [%] = 0 as benchmark, *Keynotes*: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)



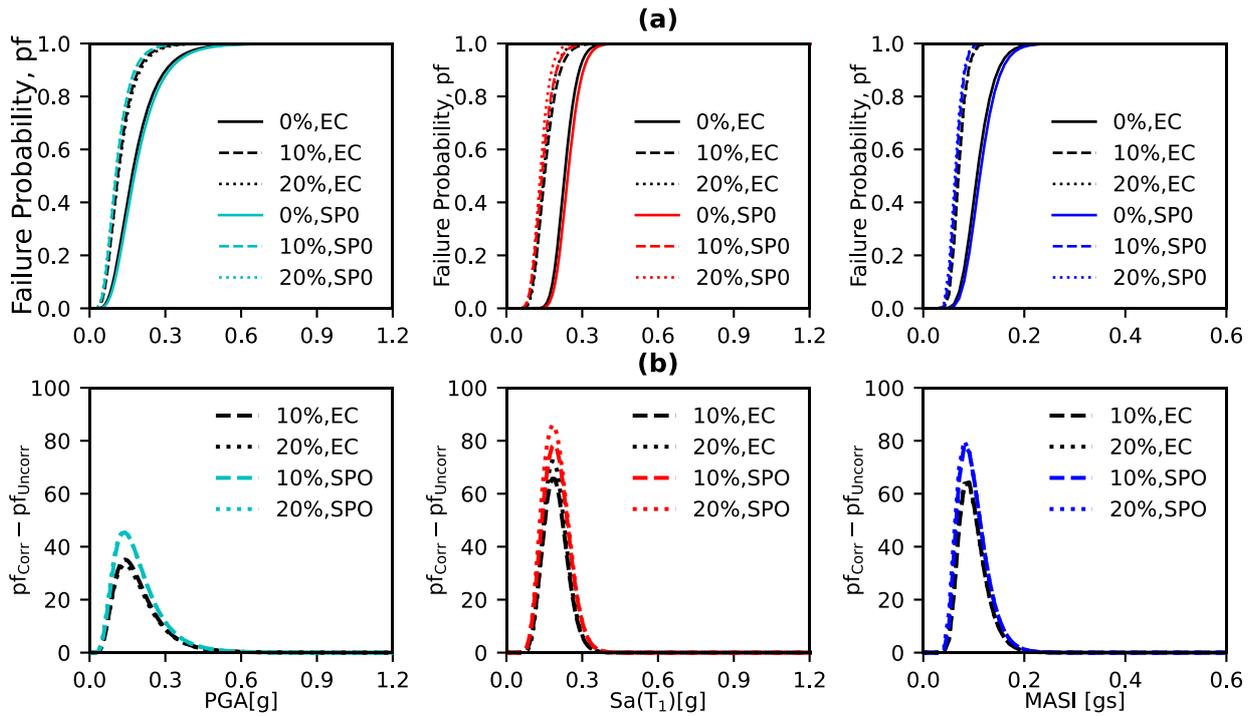
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Figure 22. (a) Fragility Curves for mainshock records and (b) Difference of failure probability (CR [%] = 0 as benchmark, *Keynotes*: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)



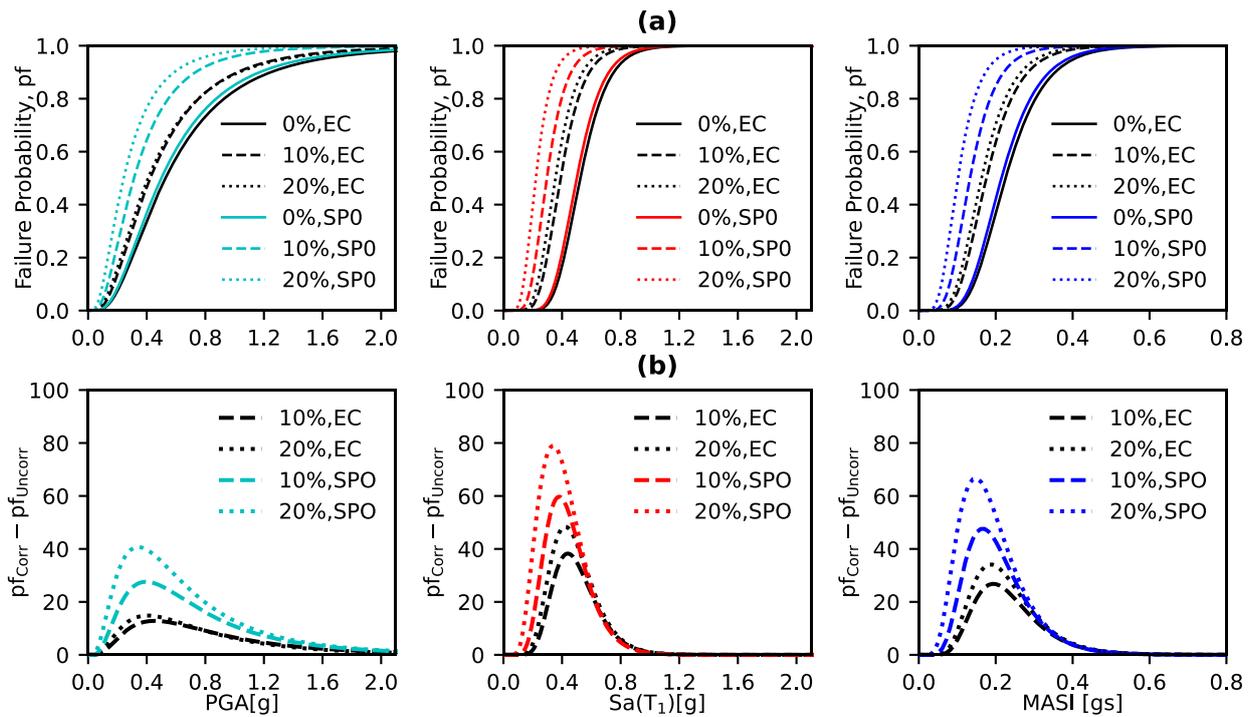
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Figure 23. (a) Fragility Curves for sequence records and (b) Difference of failure probability (CR [%] = 0 as benchmark, *Keynotes*: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)

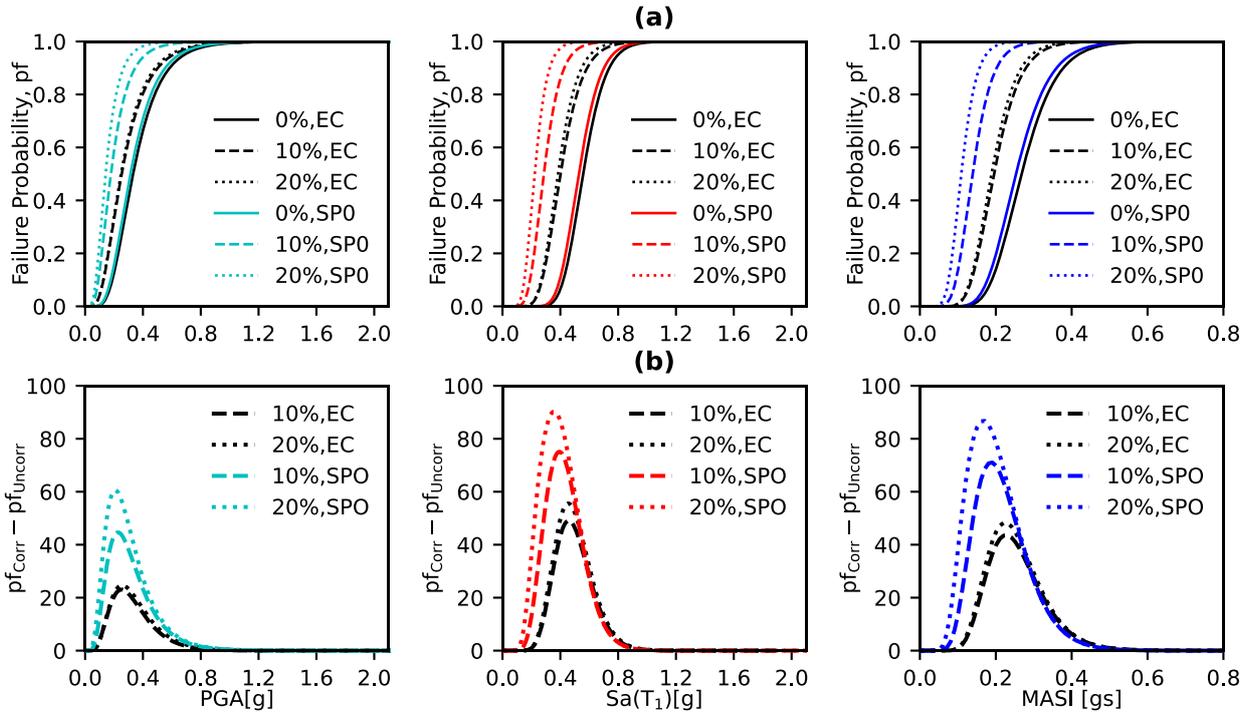


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Figure 24. (a) Fragility Curves for aftershock records and (b) Difference of failure probability (CR [%] = 0 as benchmark, *Keynotes*: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)

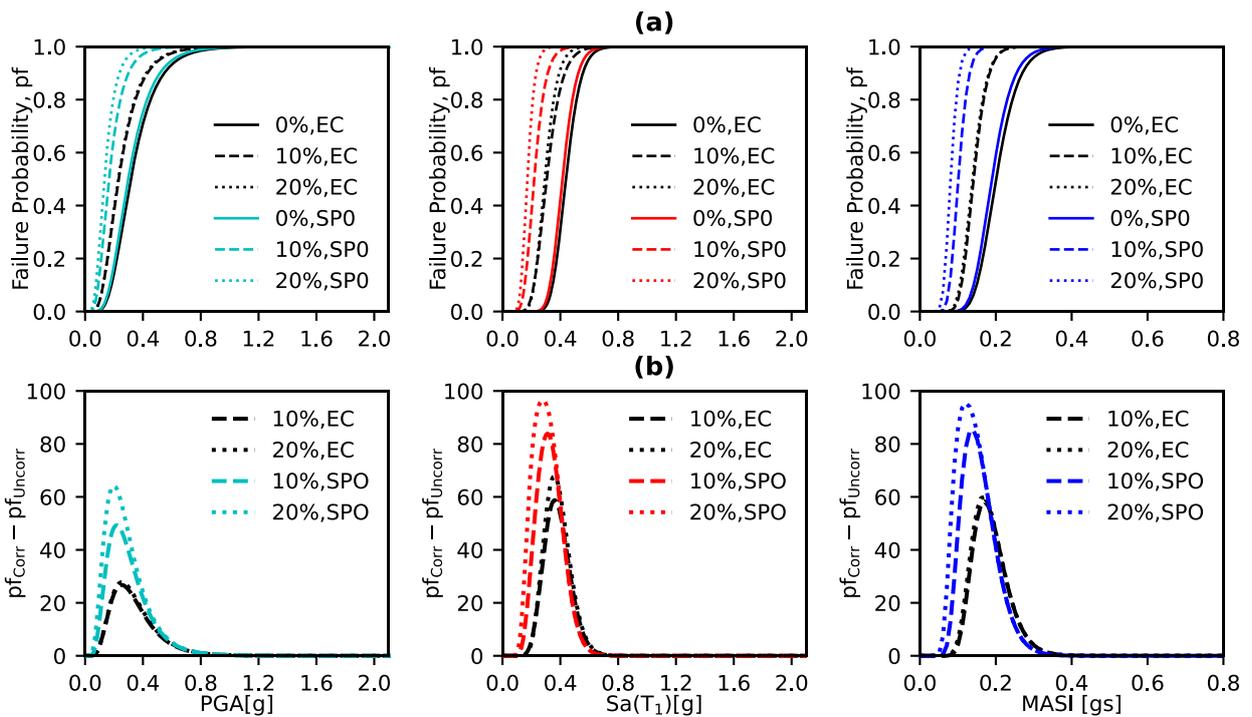


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Figure 25. (a) Fragility Curves for mainshock records and (b) Difference of failure probability (CR [%] = 0 as benchmark, *Keynotes*: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)



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Figure 26. (a) Fragility Curves for sequence records and (b) Difference of failure probability (CR [%] = 0 as benchmark, *Keynotes*: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)

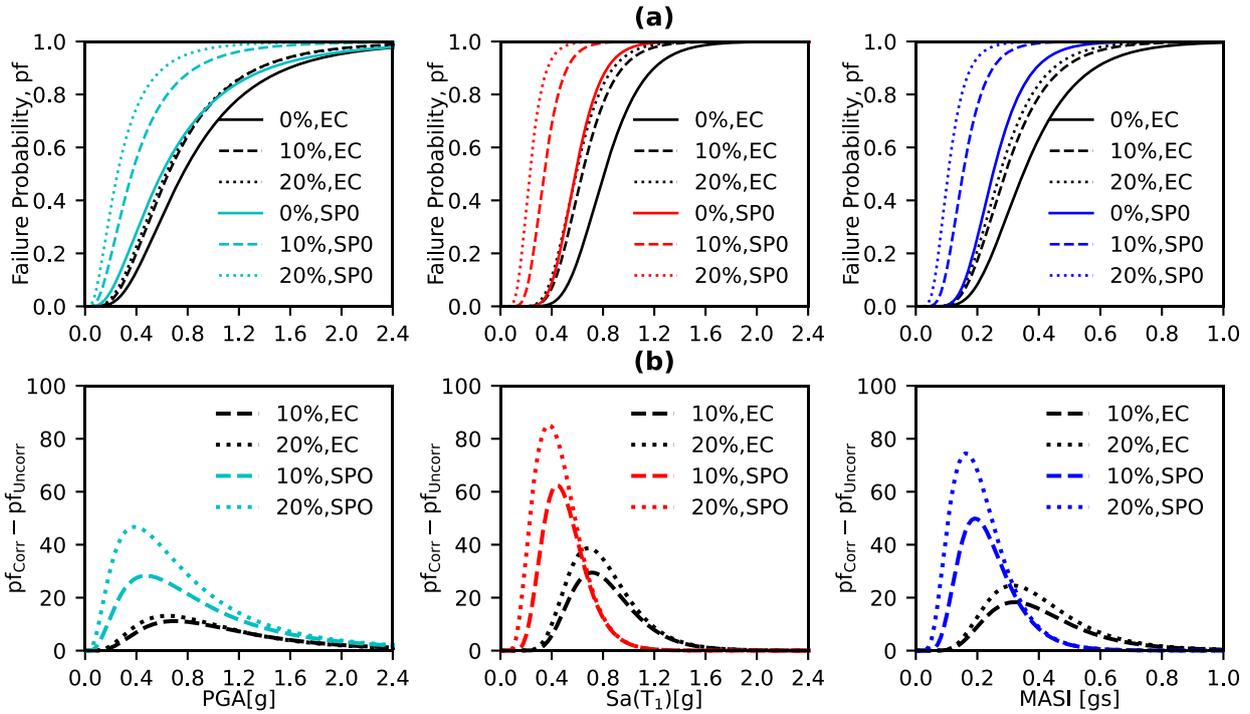


Figure 27. (a) Fragility Curves for aftershock records and (b) Difference of failure probability (CR [%] = 0 as benchmark, *Keynotes*: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)

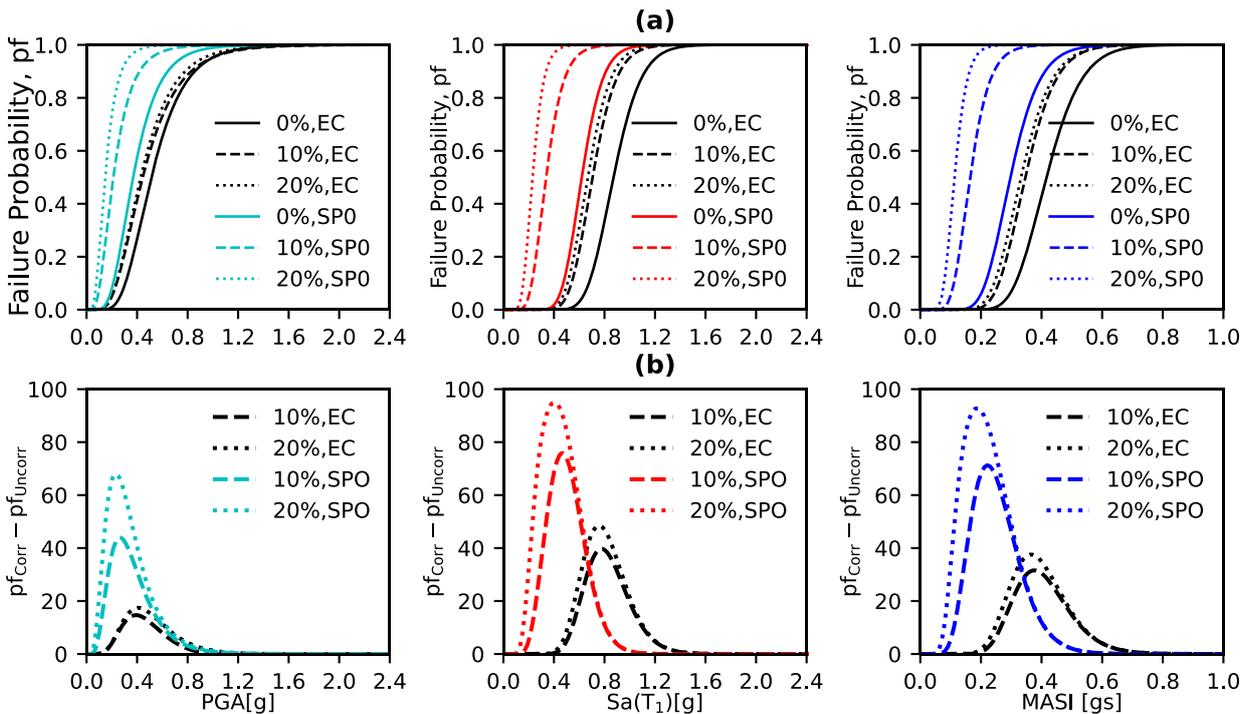
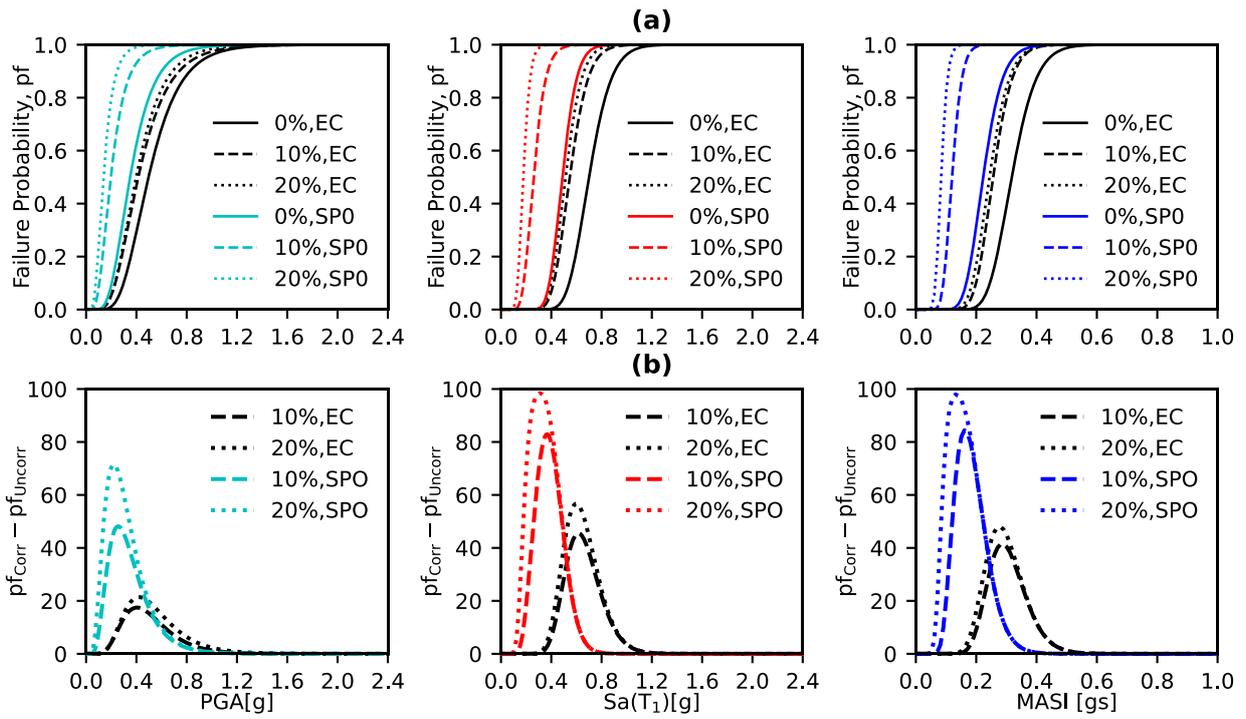


Figure 28. (a) Fragility Curves for mainshock records and (b) Difference of failure probability (CR [%] = 0 as benchmark, *Keynotes*: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)



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Figure 29. (a) Fragility Curves for sequence records and (b) Difference of failure probability (CR [%] = 0 as benchmark, *Keynotes*: EC – Eurocode; SPO – Non-Linear Static Pushover Analysis)