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Uniform and graded bed-load sediment transport in a degrading channel with non-equilibrium conditions

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1 **Uniform and graded bed-load sediment transport in a degrading channel with**
2 **non-equilibrium conditions**

3
4

5 **ABSTRACT**

6 Bed-load transport plays a critical role in river morphological change and has an important
7 impact on river ecology. Although there is good understanding of the role of the variation of
8 river bed grain size on transport dynamics in equilibrium conditions, much less is understood for
9 non-equilibrium conditions when the channel is either aggrading or degrading. In particular, the
10 relative role of different grain sizes in the promotion and hindering of the transport of coarse and
11 fine fractions in a degrading channel has yet to be investigated. The current study attempts to
12 provide new understanding through a series of flume experiments done using uniform and
13 graded sediment particles. The experiments revealed coarser grain-size fractions for a poorly-
14 sorted sediment, relative to uniform-sized sediment, reduced the transport of finer grains and
15 finer fractions enhanced the transport of coarse grains. This hindering-promotion effect, caused
16 by relative hiding and exposure of finer and coarse fractions, increased with bed slope and
17 decreased with relative submergence. In particular, as relative submergence increased, the graded
18 fractions tended towards behaving more like their uniform-sized counterparts. Also, the bed-load
19 parameter of the graded fractions increased more with a rise in bed slope than observed for the
20 uniform-sized counterparts. These results revealed, for degrading channel conditions, such as
21 downstream of a dam, bed-load equations developed for uniform bed sediment are inappropriate
22 for use in natural river systems, particularly in mountain streams. Furthermore, changes in river

23 bed composition due to activities that enhance the input of hill-slope sediment, such as fire,
24 logging, and agricultural development, are likely to cause significant changes in river
25 morphology.

26 **Keywords:** Graded sediment, Exposure, Hiding, Flume Experiments, Non-equilibrium.

27

28

29 **1. Introduction**

30 Coarse sediment transport in streams is responsible for shaping channel morphology and
31 controlling morphodynamics (Baewert & Morche, 2014; Liébault et al., 2016). Accurate
32 quantification of morphodynamic processes is needed for assessment of hazards along river
33 corridors, such as flooding and pollutant transport, and for defining water and land management
34 plans that mitigate their impact (Chien & Wan, 1999; Frey & Church, 2009; Graf, 1971; Raven
35 et al., 2010; Wilcock, 1998). Although traditional bed-load equations are often used for practical
36 reasons (e.g., Engelund & Hansen, 1967; Meyer-Peter & Muller, 1948), most of them have been
37 developed based on laboratory data, collected under simplified conditions and using uniform bed
38 sediment (Li et al., 2016). Uncertainties in predictions when using these traditional formulas are
39 in the range of orders of magnitude. Thus, bed-load assessment in rivers and streams is still one
40 of the major challenges facing fluvial hydraulics and river engineers, especially in channels with
41 heterogeneous sediment (Bagnold, 1977).

42

43 The mobility of sediment in high gradient rivers is significantly affected by grain sorting
44 (Hammond et al., 1984), hiding-protrusion effects (Ashworth & Ferguson, 1989), low relative
45 roughness (Bathurst et al., 1983), presence of an armor layer (Lenzi, 2004), and slope (Lamb et

46 al., 2008). Traditionally the movement of a single particle from a uniform bed in any flow can be
47 determined by flow velocity, sediment size, and sediment density (Allen, 1985; Leeder, 1982),
48 but in graded sediment there is a non-negligible inter-granular effect that must be considered. As
49 bed-load field measurements are often difficult to make in a range of flow and channel
50 conditions, flume experiments have long been a very powerful tool for exploring the process of
51 bed-load transport (Howard, 2008).

52

53 A large body of research has attempted to investigate these processes in graded channels under
54 equilibrium conditions (Kuhnle, 1993; Kuhnle, 1996; Kuhnle et al., 2013; Wilcock & Crowe,
55 2003; Wilcock & Kenworthy, 2002; Wilcock et al., 2001; Wilcock & McArdell, 1993). Along
56 with field-gathered data, this approach has led to the development of bedload equations for
57 graded sediment (e.g., Almedeij et al., 2006; Patel & Ranga Raju, 1996; Wilcock & Crowe,
58 2003; Wilcock & Kenworthy, 2002; Wu, 2004). However, non-equilibrium conditions, when the
59 channel is either aggrading or degrading, are more difficult to study. For aggrading conditions a
60 number of models are available (Belleudy & Sogreah, 2000; Cui, 2007; Cui et al., 1996; Hu et
61 al., 2014; Qian et al., 2015; Wu & Wang, 2008), but in the case of degrading channels, such as
62 downstream of a dam, only a few computational models are available because experimental data
63 often is insufficient to produce models that perform well over a range of flow and channel
64 conditions (e.g., Dietrich et al., 1989; Fuller, 1998; Pender et al., 2001; Willetts et al., 1998). In a
65 degrading channel, Li et al. (2016) showed that sand greatly promotes the transport of gravel,
66 whilst gravel significantly reduces the transport of sand, as others observed for equilibrium
67 conditions (e.g., Venditti et al., 2010; Wilcock & McArdell, 1997; Wilcock et al., 2001; Wilcock
68 & Crowe, 2003). However, the relative role of different grain sizes in this promotion and

69 hindering effect has yet to be investigated. For example, although Li et al. (2016) investigated
70 the promotion and hindering effect of uniform sand and gravel, no study in degrading channels
71 has considered how the mobility of grain size fractions of graded sediment differ from their
72 counterpart uniform-sized sediment. Nor has any study examined how this difference between
73 graded and uniform-sized sediment varies with key channel conditions, such as bed slope and
74 relative submergence. Such information would provide new understanding on why promotion
75 and hindering occur for graded sediment. The current study attempts to provide this new
76 understanding.

77

78 The current paper presents a series of laboratory flume experiments done using uniform and
79 graded sediment, designed to shed further light on the fractional bed-load sediment transport rate
80 for poorly-sorted beds in degrading channel conditions. The main goals are to compare transport
81 rates of uniform and poorly-sorted sediment and their variation with bed slope and relative
82 submergence under degrading conditions. In particular, the study aims to determine the mobility
83 of different graded fractions in comparison to counterpart uniform-sized sediment, and the effect
84 of fine fractions on the total transport rate of graded sediment. The current research offers insight
85 into the significance of grain size variation in governing the transport of coarse-grained river
86 beds.

87

88 **2. Experimental methods**

89 *2.1. Experimental procedure*

90 A total of 86 experiments were done in a 12-m long, 0.5-m wide, and 0.5-m deep rectangular
91 glass-wall flume channel with an adjustable slope in which water was recirculated (Fig. 1). Four
92 naturally rounded groups of uniform sediment particles of mean size 5.17, 10.35, 14, and 20.7
93 mm were used; along with a graded sediment mixture obtained using the four uniform sizes
94 mixed with equal proportions in weight (Table 1).

95

96

Fig.1.

97

Table 1.

98

99 The slopes used in the experimental runs varied from 0.005 to 0.035 m/m depending on the grain
100 sizes used (Table 2). Nets were installed at the upstream end of the flume to straighten and
101 smooth the flow into the channel. The first 4 m and the last 2.8 m contained fixed bed sections
102 that were artificially roughened to prevent local scour and back-water effects (see Fig.1). In
103 between, the flume was filled with mobile sediment particles.

104

Table 2.

105

106 These mobile sediment particles were level flat to a depth of $\sim 5-6 d_{50}$ (where d_{50} is the median
107 particle size). These sediment particle were re-screeded and completely re-mixed (for graded
108 sediment) after each run. A 0.5 m x 0.2 m trap was used to collect the transported sediment at the
109 downstream end of the flume. Whenever the trap was filled, another trap was immediately
110 substituted. The flow was controlled using a tailgate at the downstream end of the flume and the
111 water depth was measured using two moving point gauges and three ultrasonic sensors operating

112 at 25 Hz (see Fig.1). The first ultrasonic sensor was positioned in the upstream fixed bed section
113 and the second and third in the movable bed section. The first and second point gauges were
114 located in the first and last parts of the movable bed.

115 Prior to each experiment, the slope of the flume was set, the tailgate was raised, the flume was
116 slowly filled with water at the downstream end to prevent disruption of the initial bed, the pump
117 was turned on, and the inlet valve and tailgate slowly opened to create a low, steady initial flow
118 condition. This initial inflow was set such that no sediment transport took place. Finally, the flow
119 was gradually increased to the desired value and held constant. Uniform flow was then
120 established by adjusting the tailgate and sediment transport sampling began. The duration of each
121 run depended on the sediment transport rate, the larger transport rate, the shorter the duration,
122 which varied between 1 to 30 min, and the duration of bed-load sampling was several seconds to
123 several minutes. This sampling allowed the temporal change in the transport rate and transported
124 bed-load composition to be determined. The bed slope, flow velocity flow depth, and sediment
125 transport rate were measured continuously during all experimental runs. Mean flow velocity was
126 estimated using the travel time of a tracer (potassium permanganate). Due to the short duration
127 of the experiments, no sediment feeding was done. The effect of not-feeding sediment in the
128 short duration experiments, only affected the upstream-end of the channel, and did not affect the
129 morphology in the downstream sections of the stream nor the sediment transport rates
130 determined at the channel outline (Binns & Da Silva, 2009). Thus, all experiments were done for
131 a degrading bed. All flows were fully turbulent and supercritical except for tests 1 and 2 in which
132 the Froude number, Fr , was 0.97 and 1, respectively (Table 2).

133

134 The flume experiments were designed to test the influence of bed slope and relative submergence
 135 on the sediment transport rate, bed-load composition, and mobility of the uniform-sized and
 136 graded bed sediment. Relative submergence was defined as $RS = y/d$, where y is the flow depth
 137 and d is the bed grain size (equal to the mean particle diameter for uniform sediment and d_{50} for
 138 graded sediment). To determine the impact of bed slope, runs were done in which the flow depth
 139 was held constant and the bed slope was increased, meaning that the discharge, shear stress, and
 140 sediment transport rate increased with each run but the relative submergence remained constant
 141 for a given sediment size (Table 2) (For example, see the bold and highlighted rows in table 2).
 142 To test the effect of both relative submergence and bed slope, runs were done for in which the
 143 discharge was held constant and the bed slope increased, causing the flow depth and relative
 144 submergence to decrease, and the shear stress, and, therefore, the sediment transport rate to
 145 increase.

146

147 2.2. Sediment transport rate estimation

148 The collected sediment samples were dried and weighed after each run and the sediment
 149 transport rate [kg/m/s] during each run was estimated (Shvidchenko & Pender, 2000) according
 150 to:

$$151 \quad q = \frac{G}{b * T} \quad (1)$$

152 where G is the collected and dried mass of sediment [kg], T is the sampling time [s], and b is
 153 width of the flume [0.5 m]. The bed-load transport intensity I [s^{-1}] rate, defined as the relative
 154 number of transported particles in a time unit, was estimated as follows:

$$155 \quad I = \frac{m}{NT} \quad (2)$$

156 where m is the number of particles transported [-] during a time interval T [s] over an area of A
 157 [m^2], and N is the number of surface particles in this area [-]. Thus, the intensity is defined as the
 158 fraction of all particles transported every second. The number of particles in a bed-load sample
 159 was estimated by dividing the total dried mass of the sample by the mass of one particle. The
 160 value of N , which is the number of surface particles in the area, was estimated by assuming a
 161 surface layer with a thickness equal to one grain diameter, d :

$$162 \quad N = \frac{Ad(1-\alpha)}{\frac{\pi d^3}{6}} \quad (3)$$

165 where α is bed material porosity [-] and d for uniform bed sediment is equal to the mean grain
 166 size [m] and for graded sediments is equal to d_{50} [m]. The transport intensity can be also
 167 interpreted as the probability that a particle in a bed area with length L and unit width is
 168 transported every second. The area of the movable bed was estimated as follows:

$$169 \quad A = b * l \quad (4)$$

171 where l is the effective length of the movable bed [m], which was determined using different
 172 colored sediment set at a downstream interval of 1 m along the flume (Fig. 1). The length of
 173 transport was estimated by the presence of these colors within the bed-load samples. The
 174 Einstein bed load parameter was calculated as (Shvidchenko & Pender, 2000):

$$175 \quad q^* = \frac{q}{f_i \rho_s \sqrt{(s-1)gd}^3} \quad (5)$$

177

178 where s is specific gravity of sediment [-], ρ_s is sediment density [kg/m], g is gravitational
 179 acceleration [m/s], d for uniform bed sediment is equal to the mean grain size [m] and for graded
 180 sediments is equal to d_{50} [m], and f_i for uniform bed sediment [-] is equal to 1 and for graded
 181 sediment is equal to the proportion of size fraction i in the bed surface [-]. For graded beds q^* is
 182 equal to the fractional sediment transport rate. The Shields stress, τ^* [-], was estimated as:

183

$$184 \quad \tau^* = \frac{\tau}{g(\rho_s - \rho)} = \frac{R_b S}{(s-1)d} \quad (6)$$

185

186 where $\tau = \rho g R_b S$ is the mean bed shear stress [N/m], ρ is fluid density [kg/m³], R_b is the
 187 hydraulic radius of the bed [m], and S is bed slope [-].

188

189 In graded mixtures, there is a relative hindering and promotion effect on the transport of fine and
 190 coarse fractions, respectively, that has a significant impact on the sediment transport rate of these
 191 sediment particles (Einstein, 1950; Parker & Klingman, 1982; Wu, 2004). To examine this
 192 effect, fractional bed-load mobility was estimated as follows (Parker & Klingman, 1982):

193

$$194 \quad \Psi_i = \frac{P_i}{F_i} \quad (7)$$

195

196 where P_i [-] and F_i [-] are the fractional proportions by weight in the collected bed-load sample
 197 and within the bed sediment in the flume, respectively. The mobility can be less than 1 (reduced
 198 mobility), equal to 1 (equal mobility), or higher than 1 (enhanced mobility). Reduced/enhanced

199 mobility takes place whenever the mobility of a fraction is lower/higher than what is anticipated
 200 for its uniform-sized counterpart, due to hiding/protrusion effects.

201 The critical shear stress for incipient motion in the equilibrium condition has previously been
 202 used for assessing the role of exposure and hiding on bed-load transport rates (e.g., Wilcock &
 203 Kenworthy, 2002). However, as it proves challenging to assess precisely the critical shear stress,
 204 the effect of hindering and promotion in graded sediment can also be tested using the fractional
 205 sediment transport rate. Here F_{mn} [-] is calculated, representing the impact of a fraction with
 206 diameter m [m] on sediment transport of fraction n [-] in graded sediment in comparison to its
 207 counterpart in uniform-sized sediment. The F_{mn} impact factor can be estimated as proposed by Li
 208 et al. (2016):

$$F_{mn} = \left(\frac{q_n}{f_n} \right) / \left(\frac{q_{n-uni}}{f_{n-uni}} \right) \quad (8)$$

213 where q_n is unit-width volumetric transport rate [kg/m] for fraction n , uni is for uniform-sized
 214 sediment, f_n is volumetric proportion of fraction n in the bed surface [-], and, thus, f_{n-uni} for
 215 uniform-sized bed sediment is equal to 1. If the finer fractions impact on the mobility of the
 216 coarser fractions, the impact factor is greater than 1. On the contrary, if the coarser fractions
 217 impact the finer fractions, the impact factor is less than 1.

218 3. Results and discussion

219

220 3.1. Effect of bed slope and relative submergence on the sediment transport rate

221 For tests at the same relative submergence, the sediment transport rate of the uniform-sized
222 sediment increased with bed slope (Fig. 2a-d). For example, for bed material of 5.17 mm at $RS =$
223 13.9, an increase in bed slope from 0.0075 to 0.015 resulted in a 98% increase in the transport
224 rate. This increase is associated with an increase in discharge, and, therefore, shear stress. The
225 effect of bed slope on the Einstein bed load parameter for a constant flow depth of 9 cm is
226 compared between the different uniform-sized and graded sediment in Fig. 2e. The figure shows
227 that for a given bed sediment, the bed-load parameter increased with an increase in bed slope,
228 more so for the graded fractions, except for the coarsest fraction of 20.7 mm.

229

230

Fig. 2.

231

232 A comparison between the effect of bed slope on the bed-load parameter of graded fractions of
233 5.17, 10.35, 14, and 20.7 mm and their uniform-sized sediment counterpart is shown in Fig. 3.
234 The finer fractions were more stable than the counterpart uniform-sized sediment. For example,
235 at a bed slope of 0.015 m/m and a flow depth of 10 cm, the bed-load parameter of uniform bed
236 sediment of 5.17 and 10.35 mm was 380 and 310 times higher than that of the counterpart graded
237 fractions (Fig. 3a, b). However for sediment of a size of 14 mm, the bed-load parameter was
238 almost equal for the uniform-sized and graded sediment (Fig. 3c). Also, at a grain size of 20.7
239 mm the bed-load parameter of the graded fraction was 5.2 times greater than its uniform-sized
240 counterpart at a bed slope of 0.03 m/m and a flow depth of 10 cm (Fig. 3d). This difference in
241 mobility of the finer and coarser fractions between the uniform-sized and graded sediment can be
242 attributed to the greater hiding and protrusion that occurs in the later (Li et al., 2016; Wang et al.,

243 2015). Despite this difference, the transport rate of the graded fractions and their uniform-sized
244 material counterpart increased at a similar rate with bed slope.

245

246

Fig. 3.

247 Figure 4 shows an example of the change in the sediment transport rate with bed slope and
248 relative submergence for the tests done at the same flow discharge. In these tests an increase in
249 bed slope corresponded to a decrease in relative submergence. The figure shows that the bed-
250 load transport rate increased with bed slope and decreased with relative submergence. For
251 example, for bed material of 5.17 mm, an increase in bed slope from 0.005 to 0.015 mm^{-1} ,
252 corresponding with a decrease in RS from 17.4 to 11.6, and caused a 99% increase in the
253 transport rate. This result occurred because the shear stress was higher at the steeper slopes and
254 lower submergences. A comparison between the graded fractions and their uniform counterparts
255 (Fig. 4c) shows that the finer fractions than d_{50} (e.g., 5.17 and 10.35 mm) had a lower transport
256 rate, the 14 mm fraction had an equal transport rate and the coarsest fraction of 20.7 mm had a
257 higher transport rate, than their uniform-sized counterparts.

258

259

Fig. 4.

260

261 The transport rate increased with relative submergence because higher submergences were
262 related to higher shear stress (Fig. 5). For example, for uniform sizes of 5.17, 10.35, 14, 20.7
263 mm, and the graded sediment, a 1.6, 1.3, 1.3, 1.5, and 1.2 times increase in RS at a constant bed
264 slope of 0.01 m/m, caused 15, 41, 52, 5 and 16 times increases in transport rate, respectively.

265

266 Fig.5.

267

268 *3.2. Effect of relative submergence on the Einstein bed-load parameter and inter-granular effects*

269 Figure 6a shows the relation between the Einstein bed-load parameter and relative submergence
270 at a fixed bed slope of 0.015 m/m for uniform bed materials of 5.17, 10.35, 14 mm, and the
271 graded sediment. There was a clear increase in the bed-load parameter with relative
272 submergence, and the rate of increase was fairly invariant with sediment size. In contrast,
273 relative submergence had a much greater impact on the sediment transport rate of the coarser
274 fractions within the graded mixture (Fig. 6b).

275 Fig. 6.

276

277 Figure 7 shows the degree to which the impact factor (IF) changed with relative submergence.
278 For example, F_{20} represents the impact of three fractions (5.17, 10.35, and 14 mm) on the
279 sediment transport behavior of fraction 20.7 mm. Results show that for F_{20} and F_{14} , IF was
280 higher than 1 meaning finer fractions caused an increase in the transport rate of fractions of 20.7
281 and 14 mm in comparison to their uniform-sized counterparts. For F_{10} , the IF values at both
282 slopes of 0.015 and 0.03 m/m were lower than 1 indicating that the other fractions (5.17, 14, and
283 20.7 mm) caused a relative decrease in the sediment transport rate of fraction of 10 mm in
284 comparison to the uniform counterpart. These observations show that fine fractions enhanced the
285 sediment transport rate of the coarser fractions and the total sediment transport rate, and that
286 coarser fractions reduced the transport rate of finer fractions. This result is in accordance with
287 results for equilibrium (e.g., Venditti et al., 2010; Wilcock & Crowe, 2003; Wilcock et al., 2001;

288 Wilcock & McArdell, 1997) and degrading conditions (Li et al., 2016). This behavior occurred
289 because finer fractions tended to hide between or behind coarser fractions, whilst the coarser
290 fractions were more exposed to the higher hydrodynamic forces further up in the flow (Einstein,
291 1950). Fig. 7 also reveals that the IF values for the coarser fraction decreased with a rise in
292 relative submergence and that the opposite trend occurred for the finer fractions. In other words,
293 as relative submergence increased the graded fractions tended towards behaving more like their
294 uniform-sized counterparts. This change is likely to have occurred because at high relative
295 submergences there was a larger shear stress, and, thus, the hydrodynamic exposure of the
296 different fractions differed less than at lower submergences, acting to reduce the promotion-
297 hindering effect on transport rates.

298

299 Fig. 7.

300 *3.3. Effect of Shields stress on the bed-load parameter*

301 A comparison between the effect of Shields stress on the bed-load parameter for the graded
302 fractions and their uniform-sized counterparts is shown in Fig. 8. In the case of 10.35 mm, the
303 Shields stress and the Einstein bed load parameter for uniform sediment was higher than the
304 graded fraction (Fig. 8a). But for sizes of 14 and 20.7 mm, these parameters were lower (Fig. 8b,
305 c). This hindering and promotion effect is in accordance with the results of Li et al. (2016) for
306 mixtures of sand and gravel, and attributed to the elevated hiding and protrusion of fine and
307 coarse fractions within a graded mixture.

308

309 Fig.8.

310 3.4. Effect of bed slope on fractional bed load mobility

311 Generally the mobility of the coarser fractions, (coarser than d_{50}), was higher than 1 but the
312 mobility of finer fractions (finer than d_{50}) was lower than 1 (Fig. 9), as one might expect from the
313 results in Fig. 8. The highest relative mobility belongs to the 20.7 mm fraction, followed by 14,
314 10.35, and 5.17 mm. These differences are reflected in the bed-load grain size distribution; in all
315 experimental runs the transported sediment of the graded mixture was coarser than the bed
316 surface composition. An example is shown in Fig. 10 for the run done at a bed slope of 0.03 m/m
317 and $RS = 6.4$.

318 The results in Fig. 8 also reveal that an increase in bed slope caused the mobility of the coarser
319 fractions to increase from 1 at a slope of 0.015 m/m to 1.8 at a slope of 0.03 m/m, but the finest
320 fraction reduced from 0.3 to 0.13 (Fig. 9). This change with bed slope occurred because at higher
321 slopes there is a larger shear stress, and, thus, greater hydrodynamic exposure of the coarser
322 grains than would occur at lower slopes, making their relative mobility higher at steeper slopes.
323 Thus, the finer fractions at higher slopes became relatively less exposed than would occur at
324 lower slopes, in comparison to the coarser fractions.

325 Fig 9.

326 Fig 10.

327

328 3.5. Implications and recommendations

329 The results have a number of implications. First, under degrading channel conditions, such as
330 downstream of a dam, coarser grain-size fractions in a poorly-sorted sediment, relative to

331 uniform-sized sediment, reduce the transport of finer grains and finer fractions enhance the
332 transport of coarse grains. This result confirms that bed-load equations developed for uniform
333 bed sediment are inappropriate for use in natural river systems. Second, this hindering-promotion
334 effect, caused by relative hiding and exposure of finer and coarse fractions, increased with bed
335 slope and decreased with relative submergence. Thus, the errors in the use of these equations are
336 likely to be most critical in mountain streams. Third, the large difference in the transport rates of
337 the fine and coarse fractions of the poorly-sorted sediment in comparison to their uniform-sized
338 counterparts also indicates that changes in bed composition could lead to significant changes in
339 river morphology. Such changes could be caused by natural or human activities, such as fire,
340 logging, flow diversion, road construction, and agricultural development. Thus, measures that
341 control the input of catchment-stored sediment that differ to those of river bed sediment, such as
342 soil conservation techniques, grass-planting, afforestation, buffer strips, and check-dams, will
343 play a useful role in reducing river morphological change.

344 Future studies should consider a wider range of poorly-sorted sediment than studied here, and a
345 wider range of non-equilibrium conditions, such as in the case of an upstream sediment supply.
346 Also, information on the changes in bed surface composition and topography, and in the near-
347 bed flow field, would further elucidate the impact of bed slope and relative submergence on the
348 effect of hiding and exposure on the mobility of poorly-sorted sediment.

349

350 **4. Conclusions**

351 Laboratory experiments in a recirculating flume have quantified the effect of bed grain size
352 variation on bed-load transport. A comparison between of the sediment transport behavior of

353 fractions in a graded mixture with their counterpart uniform-sized sediment revealed that finer
354 fractions had a lower Shields stress and Einstein bed load parameter. In contrast, the coarser
355 fractions had a higher Shields stress and Einstein bed load parameter. This difference in mobility
356 was attributed to hiding and protrusion effects, and was most pronounced at higher slopes and
357 lower relative submergences. In particular, as relative submergence increased the graded
358 fractions tended towards behaving more like their uniform-sized counterparts. Also, the bed-load
359 parameter of the graded fractions increased more with an increase in bed slope than observed for
360 the uniform sized counterparts. These results reveal, under degrading channel conditions, such as
361 downstream of a dam, bed-load equations developed for uniform bed sediment are inappropriate
362 for use in natural river systems, particularly in mountain streams. The large difference in the
363 transport rates of the fine and coarse fractions of the poorly-sorted sediment in comparison to
364 their uniform-sized counterparts also indicates that changes in bed composition could lead to
365 significant changes in river morphology. Thus, measures that control the input of hill-slope
366 erosion, due to activities such as fire, logging, and agricultural development, could play an
367 important role in reducing river morphological change.

368

369 **References**

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Figure captions

Fig. 1. Experimental flume set-up (not to scale).

Fig. 2. Effect of bed slope on sediment transport rate at a constant flow depth for uniform-sized bed sediment of (a) 5.17 mm, (b) 10.35 mm, (c), 14 mm and (d), 20.7 mm for uniform-sized and (e) graded sediment.

Fig. 3. A comparison between the effect of bed slope on the bed load parameter for uniform-sized and graded sediment.

Fig. 4. Effect of (a) bed slope and (b) relative submergence on the sediment transport rate for uniform sediment of 5.17 mm, and (c) effect of bed slope on sediment transport rate for all uniform-sized and counterpart fractions.

Fig. 5. A comparison between the effect of relative submergence on sediment transport for uniform-sized and graded sediment.

Fig. 6. Effect of relative submergence on (a) the Einstein bed load parameter for graded and uniform-sized sediment at a bed slope of 0.015 m/m and (b) total and fractional sediment transport rate of the graded mixture at a bed slope of 0.015 m/m.

Fig. 7. Effect of relative submergence on the impact factor.

Fig. 8. Effect of Shields stress on the Einstein bed load parameter for uniform-sized and counterpart graded fractions of (a) 10.35 mm, (b), 14 mm, and (c) 20.7 mm.

Fig. 9. Effect of bed slope on fractional bed load mobility.

Fig. 10. Size distribution of transported sediment and the bed surface at a bed slope of 0.03 m/m and a relative submergence of 6.4.

Table 1. Bed sediment properties

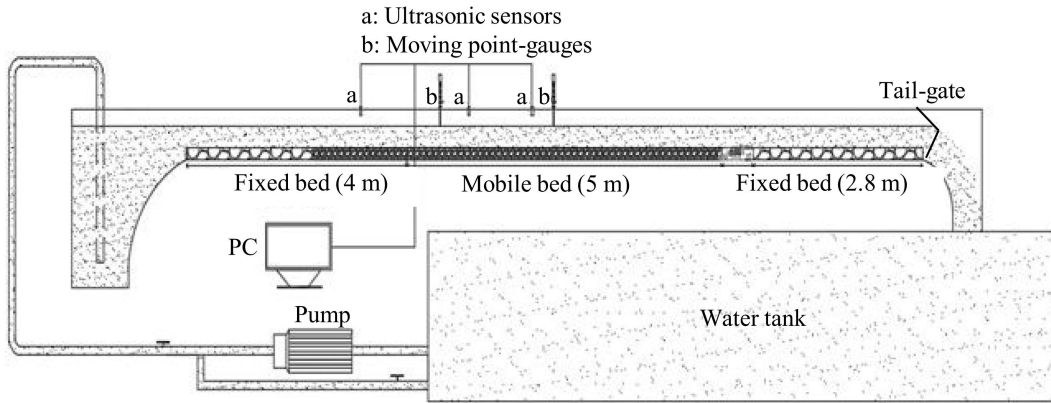
Sediment	Fractions (mm)	Mean size, d (mm)	Median size, d_{50} (mm)	σ_g [-]	Density, (kg/m ³)	Porosity [-]	Grain shape [-]
Fine gravel	4.8-5.5	5.17	-	-	2,391	0.4	Rounded
Medium gravel 1	9.5-11	10.35	-	-	2,375	0.4	Rounded
Medium gravel 2	13-15	14	-	-	2,900	0.45	Rounded
Coarse gravel	19-22.4	20.7	-	-	2,552	0.43	Rounded
Graded (mixture)	4.8-22.4	13.5	12.5	1.7	2,567	0.37	Rounded

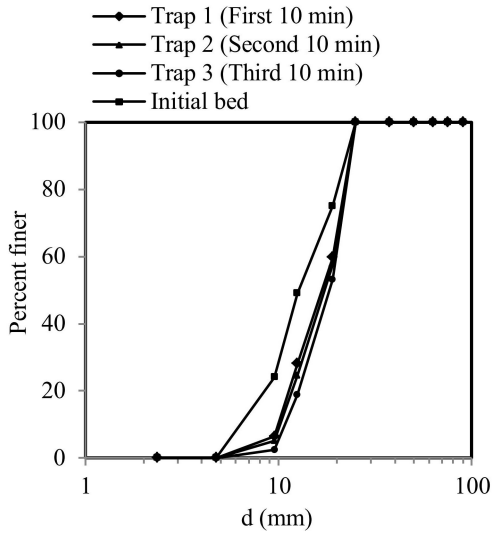
Table 2. Summary of the experimental conditions

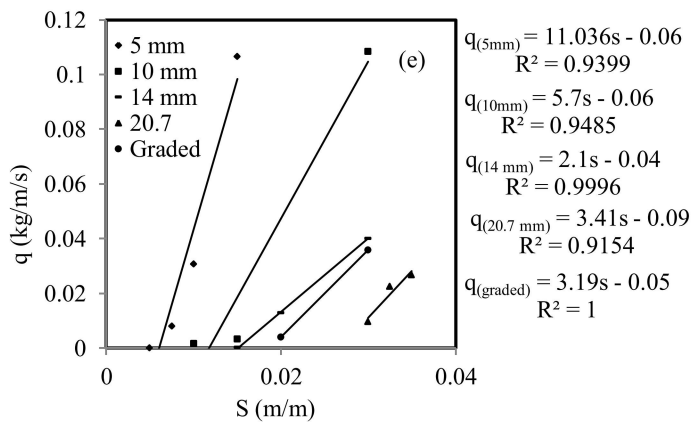
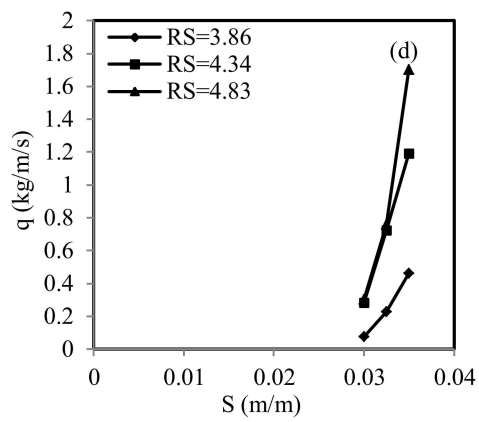
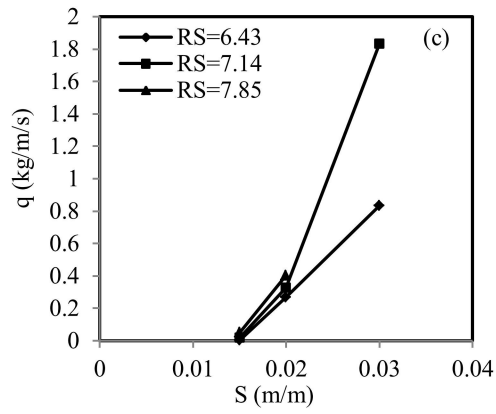
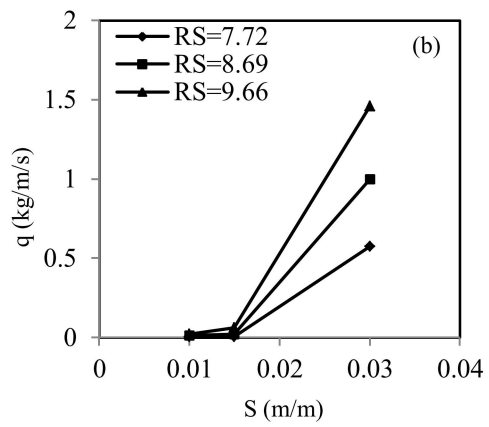
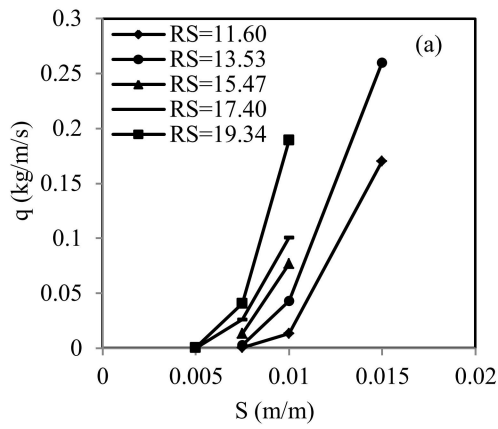
ID	d (mm)	Slope, S (m/m)	y (cm)	Mean velocity, V (m/s)	Relative submergence, RS [-]	Fr [-]	Re [-]	τ^* [-]	V^* [-]
1	5.17	0.005	9	0.92	17.4	0.97	60,882	0.055	0.062
2			10	1	19.3	1	71,428	0.060	0.065
3			11	1.1	21.2	1.05	84,027	0.065	0.068
4			12	1.2	23.2	1.1	97,297	0.070	0.071
5		0.0075	6	0.83	11.6	1.08	40,161	0.057	0.064
6			7	0.96	13.5	1.15	52,500	0.066	0.068
7			8	1.1	15.4	1.24	66,666	0.074	0.073
8			9	1.2	17.4	1.27	79,411	0.082	0.076
9			10	1.27	19.3	1.28	90,714	0.090	0.080
10			11	1.33	21.2	1.29	101,597	0.098	0.083
11			12	1.4	23.2	1.3	113,513	0.106	0.087
12			0.01	4	0.75	7.0	1.19	25,862	0.052
13		5		0.94	9.6	1.24	39,166	0.065	0.067
14		6		1.08	11.6	1.31	52,258	0.076	0.073
15		7		1.13	13.5	1.37	61,796	0.088	0.079
16		8		1.25	15.4	1.44	75,757	0.099	0.084
17		9		1.3	17.4	1.38	86,029	0.110	0.088
18		10		1.35	19.3	1.36	96,428	0.121	0.092
19		0.015		4	1	7.0	1.58	34,482	0.078
20			5	1.11	9.6	1.59	46,296	0.096	0.083
21			6	1.25	11.6	1.61	60,483	0.114	0.090
22			7	1.3	13.5	1.58	71,093	0.130	0.097
23			8	1.4	15.4	1.59	84,848	0.149	0.103
24			9	1.5	17.4	1.6	99,264	0.165	0.108
25	10.35	0.01	8	1.11	7.7	1.25	67,340	0.051	0.084
26			9	1.2	8.6	1.27	79,411	0.056	0.089
27			10	1.3	9.6	1.3	92,857	0.062	0.093
28			11	1.42	10.6	1.36	108,472	0.067	0.097
29		0.015	7	1.1	6.7	1.32	60,156	0.067	0.097
30			8	1.2	7.7	1.35	72,727	0.076	0.103
31			9	1.31	8.6	1.39	86,691	0.085	0.109
32			10	1.42	9.6	1.43	101,428	0.093	0.114
33			11	1.52	10.6	1.46	116,111	0.101	0.119
34		0.03	4	1.05	3.8	1.67	36,206	0.080	0.106
35			5	1.25	4.8	1.78	52,083	0.098	0.118
36			6	1.5	5.7	1.95	72,580	0.117	0.128
37			7	1.62	6.7	1.96	88,867	0.135	0.138
38			8	1.75	7.7	1.97	106,060	0.153	0.146
39			9	1.85	8.6	1.96	122,426	0.170	0.154
40			10	2	9.6	2.00	142,857	0.187	0.162
41	14	0.015	8.5	1.3	6.0	1.42	82,462	0.044	0.107
42			9	1.4	6.4	1.48	92,647	0.045	0.109
43			10	1.5	7.1	1.40	74,230	0.050	0.115
44			11	1.65	7.8	1.58	126,041	0.055	0.120
45			12	1.75	8.5	1.61	141,891	0.059	0.125
46			0.02	6.5	1.19	4.6	1.49	61,388	0.045
47		7		1.3	5	1.56	71,093	0.048	0.113
48		8		1.4	5.7	1.58	84,848	0.054	0.120
49		9		1.6	6.4	1.7	105,882	0.061	0.126
50				10	1.8	7.1	1.81	128,571	0.067

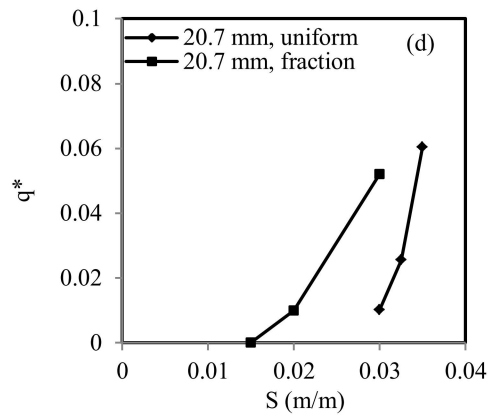
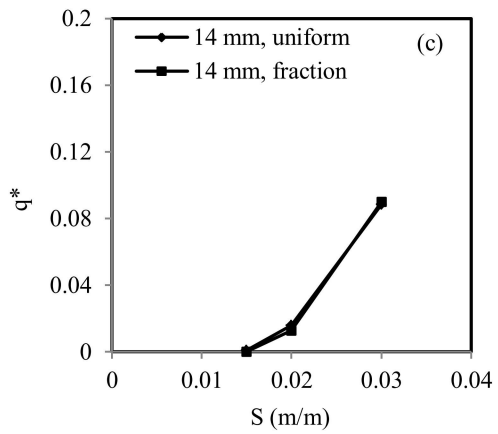
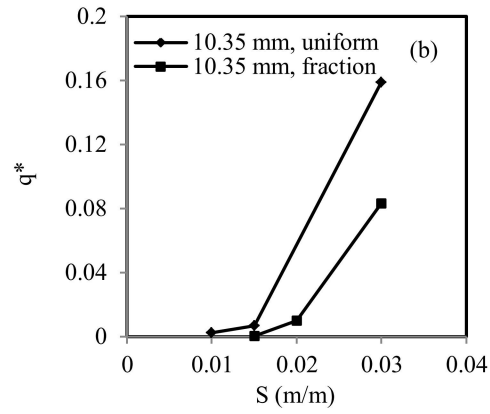
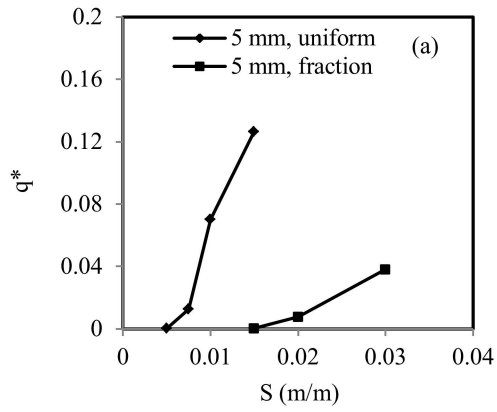
51	20.7	0.03	11	2	7.8	1.92	152,777	0.073	0.138		
52			4.5	1.1	3.2	1.63	42,736	0.049	0.113		
53			5	1.3	3.5	1.85	54,166	0.053	0.118		
54			6	1.55	4.2	2.00	75,000	0.063	0.128		
55			7	1.67	5	2.00	91,328	0.072	0.138		
56			8	1.75	5.7	1.97	106,060	0.082	0.148		
57			9	1.9	6.4	2.02	125,735	0.091	0.155		
58			10	2.1	7.1	2.12	150,000	0.101	0.162		
59			11	2.4	7.8	2.25	157,145	0.108	0.165		
60			20.7	0.03	8	1.66	3.8	1.87	100,606	0.068	0.147
61					9	2.08	4.3	2.21	137,647	0.076	0.155
62	10	2.17			4.8	2.19	155,000	0.084	0.163		
63	0.0325	6		1.42	2.9	1.85	68,709	0.056	0.134		
64		7		1.61	3.3	1.92	88,046	0.065	0.144		
65		8		1.76	3.8	1.99	106,666	0.074	0.153		
66		9		1.92	4.3	2.06	127,058	0.083	0.162		
67	10	2.2		4.8	2.22	157,142	0.091	0.170			
68	0.035	5		1.35	2.4	1.92	56,250	0.051	0.128		
69		6		1.5	2.9	1.95	72,580	0.061	0.139		
70		8	1.8	3.8	2.03	109,090	0.080	0.159			
71		9	2	4.3	2.12	132,353	0.089	0.168			
72	10	2.3	4.8	2.32	164,285	0.098	0.176				
73	Graded	0.015	10	1.51	8	1.52	107,857	0.068	0.115		
74			11	1.65	8.8	1.58	126,041	0.075	0.120		
75			12	1.8	9.6	1.65	145,945	0.080	0.124		
76		0.02	7	1.25	5.6	1.50	68,359	0.065	0.112		
77			8	1.33	6.4	1.50	80,606	0.074	0.120		
78			9	1.56	7.2	1.66	103,235	0.082	0.126		
79			10	1.7	8	1.71	121,428	0.091	0.132		
80		11	1.82	8.8	1.75	139,027	0.099	0.138			
81		0.03	5	1.25	4.0	1.78	52,083	0.072	0.118		
82			6	1.5	4.8	1.95	72,580	0.085	0.128		
83			7	1.67	5.6	2.01	91,328	0.098	0.138		
84			8	1.72	6.4	1.94	104,242	0.111	0.147		
85			9	1.85	7.2	1.96	122,426	0.124	0.155		
86			10	2	8	2.01	142,857	0.136	0.162		

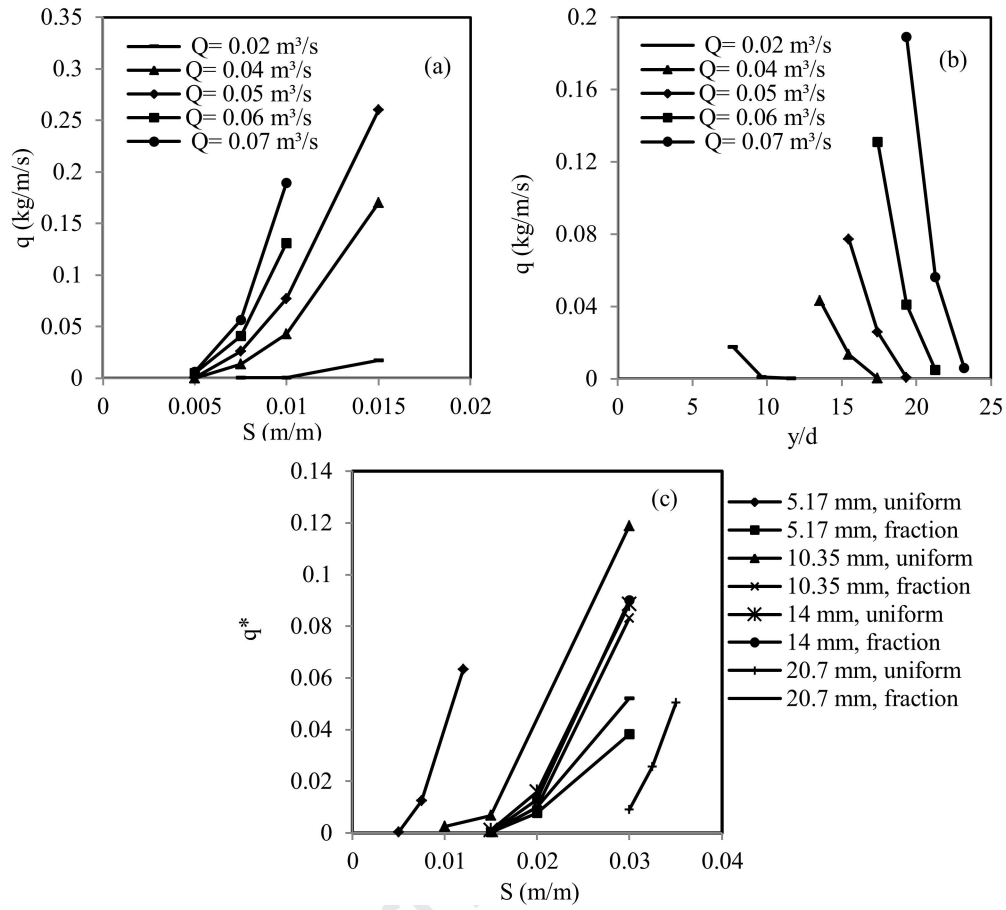
(Froude number (Fr), Reynolds number (Re), Shields stress (τ^*), and shear velocity (V^*)).

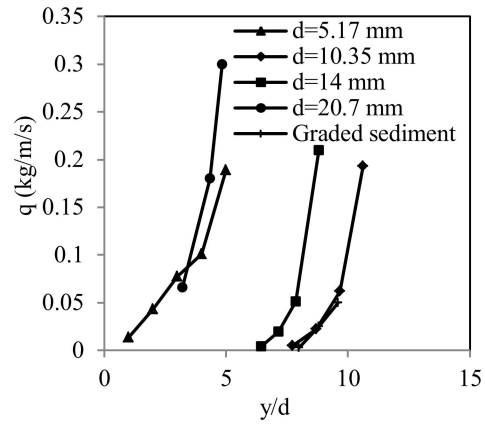




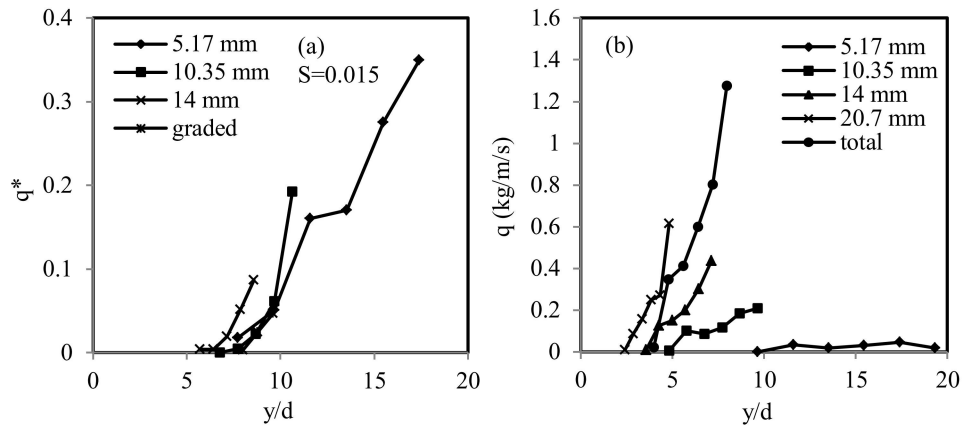


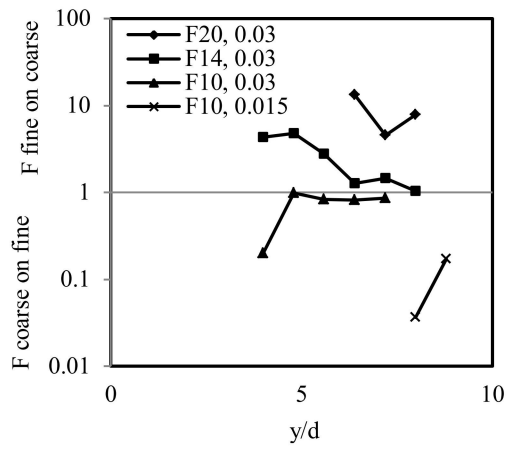




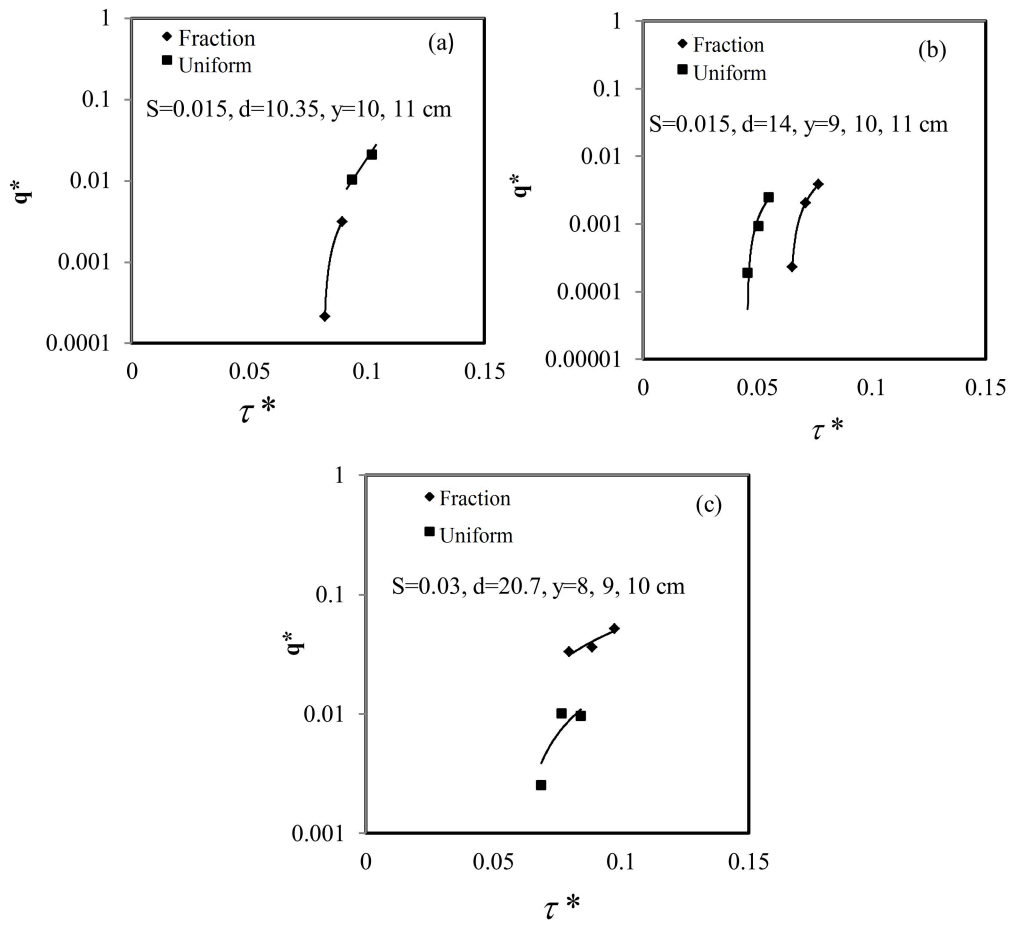


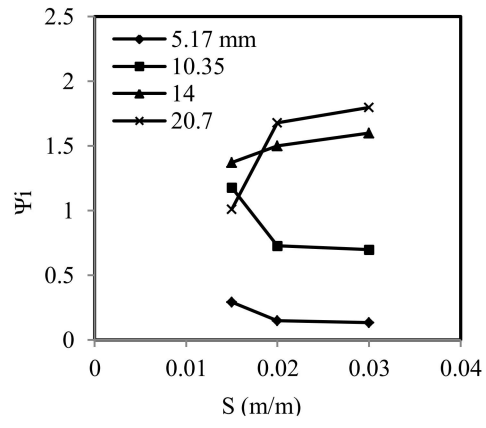
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There isn't any conflict of interest

- All authors have participated in (a) conception and design, or analysis and interpretation of the data; (b) drafting the article or revising it critically for important intellectual content; and (c) approval of the final version.
- This manuscript has not been submitted to, nor is under review at, another journal or other publishing venue.
- The authors have no affiliation with any organization with a direct or indirect financial interest in the subject matter discussed in the manuscript
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