

# High Step-Up Switched-Capacitor Active Switched-Inductor Converter with Self-Voltage Balancing and Low Stress

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**Abstract**—High step-up DC-DC converters are widely used in new energy applications such as photovoltaic cell, fuel cell, DC microgrid etc. Active switched-inductor (ASL) converter has simple operation and low stress on switches. To further increase the voltage gain, some SC (switched-capacitor)/ASL step-up converters have been proposed recently. However, these SC/ASL step-up converters have voltage oscillation on switches, which leads to the voltage stress on switches is higher than the theoretical value. In this paper, a novel high step-up SC/ASL converter is proposed. Compared with other SC/ASL step-up converters, the proposed converter has lower voltage stress on the switches, output diodes and output filter capacitors, and the efficiency is higher. In addition, the proposed converter can achieve self-voltage balancing on switches. This paper analyzes the proposed converter from operation principle, continuous conduction mode (CCM) analysis, CCM operation with unbalanced inductors, input current ripple analysis, discontinuous conduction mode (DCM) and boundary conduction mode (BCM) analysis, switches self-voltage balancing characteristic, voltage stress, current stress, comparison analysis, and design considerations. Finally, a 200W, 25-45V/380V, 50kHz experimental prototype has been established in the laboratory to evaluate the proposed converter, which reached a peak efficiency of 97.3%.

**Index Terms**—Active switched-inductor (ASL), switched-capacitor (SC), high step-up DC-DC converters, self-voltage balancing.

## I. INTRODUCTION

IN recent years, high step-up DC-DC converters have been widely used, and their applications mainly include solar photovoltaic (PV) cell, fuel cell (FC), DC microgrid, electric vehicle, uninterruptible power supply (UPS) etc. [1]-[6].

High step-up DC-DC converters are divided into two types: isolated type and nonisolated type. Isolated high step-up converters can obtain high voltage gain by adjusting the transformer turn ratio, however, high voltage spike usually could be produced during switch transition process because of the leakage inductor. In addition, isolated type converters have many shorts, such as large volume, large weight, and high costing [7]-[9]. Nonisolated high step-up converters are widely

used in the applications which electrical isolation is not required. Nonisolated converters can be mainly classified into many different categories, such as cascading, coupled inductor, SC (switched-capacitor) and SL (switched-inductor). The cascade converters achieve high voltage gain by cascading multiple boost converters. However, due to large quantities of components of the cascade converter, the system efficiency is usually low, and cascade converter requires more control circuits, which increases the complexity of the system [10], [11]. Coupled inductor high step-up converters are similar to isolated type converters, the high voltage gain can be achieved by adjusting the turn ratio of the coupled inductor. But the leakage inductor of the coupled inductor could cause voltage spikes and it may increase the voltage stress on the power semiconductor device, therefore, coupled inductor converters need more snubber circuits which increase the complexity of the converter [12], [13]. Using multiple SC cells or SL cells are the other two methods to achieve high voltage gain, however, this may reduce the efficiency of the converter because of a large number of components [14]-[17].

Active switched-inductor (ASL) is another effective boost structure, which obtains voltage gain by charging the inductors in parallel and discharging in series [18]. Compared with the above four types, ASL has the characteristics of simple structure and low voltage and current stresses on the switches. But the voltage gain of ASL converter is difficult to exceed 10 times. In order to further increase the voltage gain, the ASL converter with different types of single-stage SC cells were proposed in [19]-[21], [24]. The ASL converter with two-stage SC cells were proposed in [23], [25], [27], compare with single-stage SC/ASL converters, the two-stage SC/ASL converters have higher voltage gain and lower stresses on switches and diodes. A hybrid switched-inductor/SC converter was proposed in [22], which based on the symmetrical hybrid switched inductor (SH-SLC) in [33]. In [26], a hybrid switched-inductor/SC converter with an auxiliary switch was proposed to improve the voltage gain and efficiency. However, for these SC/ASL step-up converters, there is usually a problem of overvoltage on the switches. When the inductor values are not identical, the junction capacitors of the switches resonate with inductors, which may cause voltage oscillation on two switches. Although the theoretical value of the voltage stress on

the switches is low, the actual voltage stress on the switches is higher than the theoretical value because of the voltage oscillation on switches. In order to reduce the voltage oscillation, some snubber circuits like RC need to be added, which increases the complexity of the system. In brief, the present existing SC/ASL step-up converters still have the problem of overvoltage on switches, which needs to be solved.

A novel high step-up SC/ASL converter is proposed in this paper, named ASL-SC-2OD. The features of the proposed converter are as follows: 1) It has high voltage gain. 2) simplicity of operation (only two modes in CCM). 3) the proposed converter can achieve self-voltage balancing on two switches due to the capacitors clamp structure. 4) the switches voltage stress is reduced, which leads to lower voltage stress MOSFETs with smaller ON-resistance ( $R_{on}$ ) can be selected. 5) the output diodes voltage stress is reduced and lower voltage stress output diodes can be utilized, also the one output diode can help form a capacitor clamp loop to clamp the voltage of switch. 6) The output capacitors are not only the output filters, but also a part of the capacitors clamp structure, and the output capacitors have lower voltage stress. 7) The proposed converter has lower cost. 8) higher efficiency (peak efficiency is 97.3%).

In order to comprehensive introduce the proposed converter in detail, the remaining of this paper is organized as follows. In section II, the structure of the proposed converter is introduced, then the operation principle, CCM analysis, CCM operation with unbalanced inductors, input current ripple analysis, DCM and BCM analysis, switches self-voltage balancing characteristic, voltage stress on the power components, current stress across the power components. The comparison of the proposed converter with other similar nonisolated step-up converters is presented in section III. Design considerations are discussed in section IV. Section V presents the experimental waveforms and the experimental results. Finally, the conclusions have been drawn in Section VI.

## II. THEORETICAL ANALYSIS OF PROPOSED CONVERTER

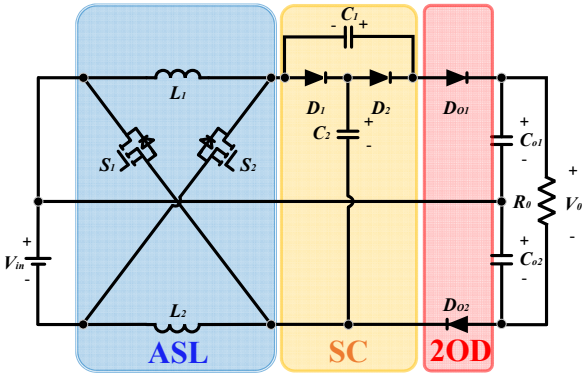


Fig. 1. Proposed converter ASL-SC-2OD.

The structure of the proposed converter is shown in Fig. 1, the proposed converter is composed of ASL network (two switches  $S_1$  &  $S_2$ , two inductors  $L_1$  &  $L_2$ ), SC cell (two capacitors  $C_1$  &  $C_2$ , two diodes  $D_1$  &  $D_2$ ), two output diodes  $D_{01}$  &  $D_{02}$  and two output capacitors  $C_{01}$  &  $C_{02}$ . So, the proposed converter can be named ASL-SC-2OD. The components position of the proposed converter is an important feature to increase the voltage gain, reduce their voltage stress and also maintain the

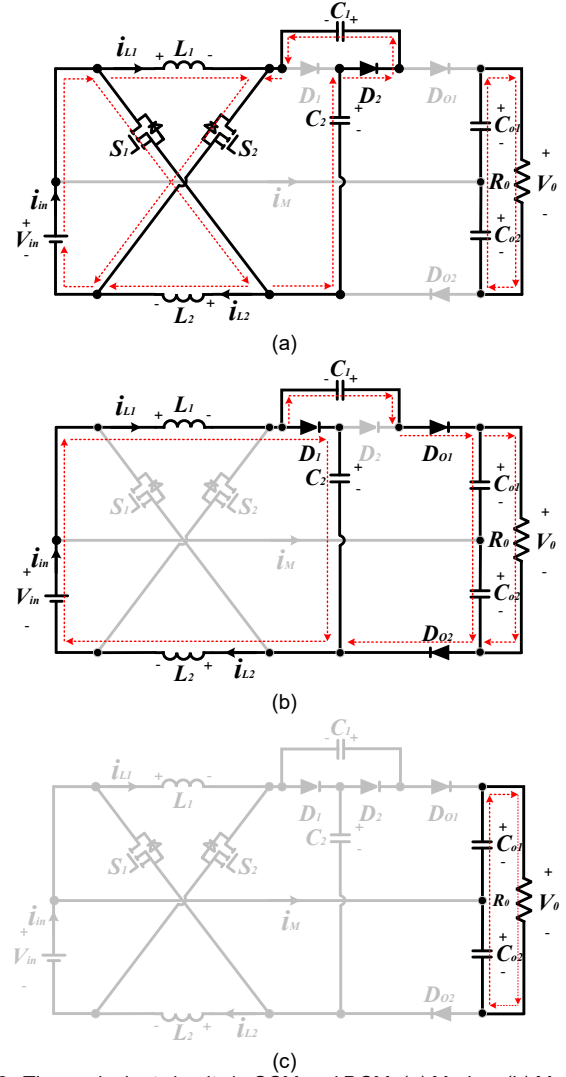


Fig. 2. The equivalent circuits in CCM and DCM. (a) Mode I. (b) Mode II. (c) Mode III.

simple operation. In addition, the ASL-SC-2OD converter can achieve self-voltage balancing on switches due to the capacitors  $C_1$ ,  $C_{01}$  and  $C_{02}$ . The voltage of  $S_1$  is clamped by  $C_{02}$  and the voltage of  $S_2$  is clamped by  $C_1$  and  $C_{01}$ . The output capacitors  $C_{01}$  and  $C_{02}$  are not only the output filters, but also a part of the capacitors clamp structure. In order to verify the above characteristics, the proposed converter is theoretically and experimentally analyzed in detail in the following sections.

### A. Operation Principle

The ASL-SC-2OD converter can be divided into two modes of operation: CCM and DCM. The equivalent circuits in CCM and DCM are shown in Fig. 2. In one switching cycle, the equivalent circuits in CCM are mode I and mode II, as shown in Fig. 2(a)&(b), and the typical waveform in CCM is shown in Fig. 3(a). In DCM, the equivalent circuits are mode I, mode II and mode III, as shown in Fig. 2(a)-(c), and the typical waveform in DCM is shown in Fig. 3(b). To simple the analysis, the following assumptions are made: all components are ideal; both input and output voltages are constant;  $L_1=L_2=L$ ; The detailed analysis of the three modes is presented in the following part.

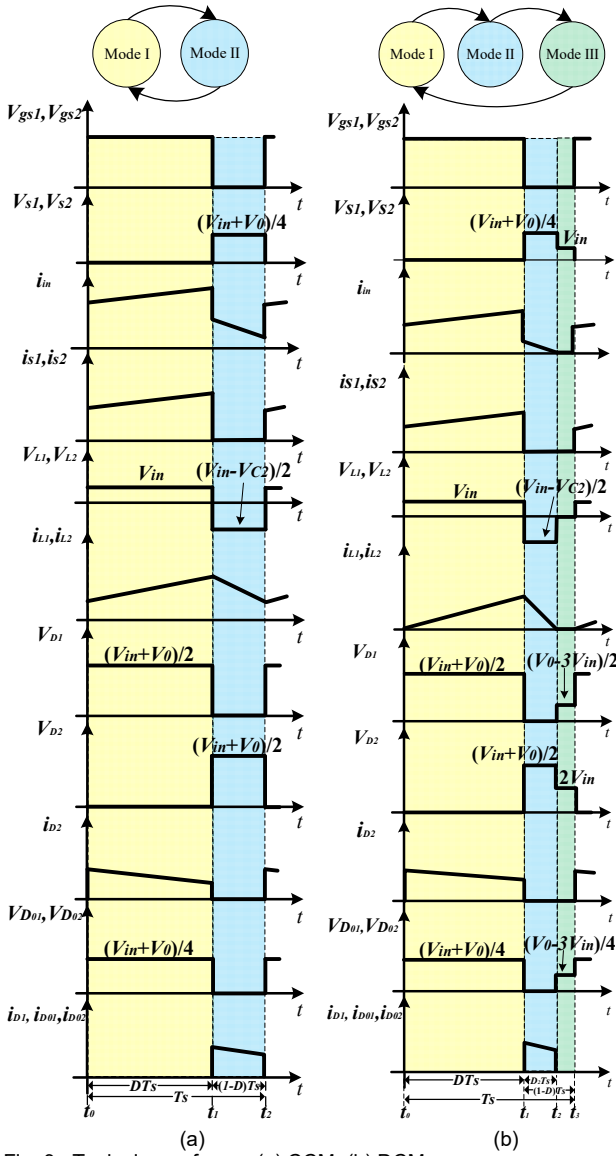


Fig. 3. Typical waveforms. (a) CCM. (b) DCM.

1) Mode I [ $t_0-t_1$ , Fig. 2(a)]: In mode I, the two switches  $S_1$  and  $S_2$  are turned on simultaneously. Two inductors  $L_1$  &  $L_2$  are connected in parallel and charged by input voltage  $V_{in}$ , the currents of two inductors  $i_{L1}$  and  $i_{L2}$  are increased linearly, the peak value of inductor current  $i_L$  can be expressed as

$$i_{L1(t)} = i_{L2(t)} = i_{L(t_0)} + \frac{V_{in}}{L}(t_1 - t_0) \quad (1)$$

where  $i_{L(t_0)}$  is value of  $i_L$  at  $t_0$ .

The diodes  $D_1$ ,  $D_{O1}$ ,  $D_{O2}$  are reverse-biased, the diode  $D_2$  is forward-biased. The DC source and  $C_2$  charge  $C_1$ , and the capacitor  $C_2$  is discharged. The energy stored in capacitors  $C_{o1}$  and  $C_{o2}$  is released to the load  $R_0$ . According to Kirchhoff Voltage Law (KVL), the relationship between the voltage on the capacitor  $C_1$  and the capacitor  $C_2$  is given by

$$V_{in} + V_{C2} = V_{C1} \quad (2)$$

2) Mode II [ $t_1-t_2$ , Fig. 2(b)]: In mode II, the two switches  $S_1$  and  $S_2$  are turned off altogether, the two inductors  $L_1$  and  $L_2$  are connected in series and discharged to post-stage circuit. The

currents of two inductors  $i_{L1}$  and  $i_{L2}$  are decreased linearly, the peak value of inductor current  $i_L$  can be expressed as

$$i_{L1(t)} = i_{L2(t)} = i_{L(t_0)} + \frac{V_{C2} - V_{in}}{2L}(t_2 - t_1) \quad (3)$$

The diode  $D_2$  is reverse-biased, the diodes  $D_1$ ,  $D_{O1}$ ,  $D_{O2}$  are forward-biased. The capacitor  $C_1$  is discharged and the capacitor  $C_2$  is charged. According to KVL, the relationship between the voltage across the capacitor  $C_1$  and the capacitor  $C_2$  is given by

$$V_{C1} + V_{C2} = V_0 \quad (4)$$

3) Mode III [ $t_2-t_3$ , Fig. 2(c)]: In mode III, the two switches  $S_1$  and  $S_2$  are turned off, the inductor current is always zero and this mode is only for DCM. The diodes  $D_1$ ,  $D_2$ ,  $D_{O1}$ ,  $D_{O2}$  are all reverse-biased, all semiconductors of the proposed converter are blocked. The energy stored in capacitors  $C_{o1}$  and  $C_{o2}$  is released to the load  $R_0$ .

### B. CCM Analysis

In CCM, the ASL-SC-2OD converter is divided into mode I and mode II. According to the equivalent circuits in CCM, as shown in Fig. 2(a) and Fig. 2(b), in mode I, the voltage across the inductors can be expressed as

$$V_{L1}^I = V_{L2}^I = V_{in} \quad (5)$$

In mode II, the voltage across the inductors can be expressed as

$$V_{L1}^{II} = V_{L2}^{II} = (V_{in} - V_{C2}) / 2 \quad (6)$$

Combining (2) and (4), the voltages across the capacitors  $C_1$  &  $C_2$  are given by

$$V_{C1} = (V_0 + V_{in}) / 2 \quad (7)$$

$$V_{C2} = (V_0 - V_{in}) / 2 \quad (8)$$

According to (6) and (8), in mode II, the voltage across the inductors can be derived as

$$V_{L1}^{II} = V_{L2}^{II} = \frac{3}{4}V_{in} - \frac{1}{4}V_0 \quad (9)$$

The voltage-second balance principle on the inductors is shown in (10).

$$\begin{cases} \int_{t_0}^{t_1} V_{L1}^I dt + \int_{t_1}^{t_2} V_{L1}^{II} dt = 0 \\ \int_{t_0}^{t_1} V_{L2}^I dt + \int_{t_1}^{t_2} V_{L2}^{II} dt = 0 \end{cases} \quad (10)$$

Combining (5), (6) and (10), the voltage gain of the proposed converter in CCM is derived as

$$G_{CCM} = \frac{V_0}{V_{in}} = \frac{3+D}{1-D} \quad (11)$$

The charge balance principle on the capacitors is shown below

$$\int_{t_0}^{t_2} i_C(t) dt = 0 \quad (12)$$

So, in one switching cycle, according to Kirchhoff's Current Law (KCL), the average current of diodes is given by

$$I_{D1} = I_{D2} = I_{D_{O1}} = I_{D_{O2}} = I_0 = \frac{V_0}{R_0} \quad (13)$$

Because the diode  $D_2$  is only forward-biased in mode I, the diodes  $D_1$ ,  $D_{O1}$ ,  $D_{O2}$  are only forward-biased in mode II, the average current of diode  $D_2$  in mode I is given by

$$I_{D_2}^I = \frac{I_0}{D} \quad (14)$$

The average current of diodes  $D_1$ ,  $D_{O1}$ ,  $D_{O2}$  in mode II is

$$I_{D_1}^{II} = I_{D_{O1}}^{II} = I_{D_{O2}}^{II} = \frac{I_0}{1-D} \quad (15)$$

The inductor current  $I_L$  is equal to the sum of the average current of diodes  $D_1$  and  $D_{O1}$  in mode II, as shown in Fig. 2(b), so

$$I_L = I_{D_1}^{II} + I_{D_{O1}}^{II} = \frac{2I_0}{1-D} \quad (16)$$

### C. CCM Operation with Unbalanced Inductors

In practice, it is difficult to keep the two inductors consistent, this paper assumes that  $L_1$  is less than  $L_2$ . In CCM with unbalanced inductors, the operation of mode I will not change, the main difference is mode II. Fig. 4 shows the operation of mode II with unbalanced inductors, and the key waveforms in the condition of unbalance inductors are shown in Fig. 5. Due to the values of two inductors are different, the rising slope and decreasing slope of both two inductor currents are not the same. In mode II, during  $t_1 - t'$ , the current flowing path is shown in Fig. 4 and the direction of  $i_M$  is from the output side to the input side; during  $t' - t_2$ , the direction of  $i_M$  is from the input side to the output side.

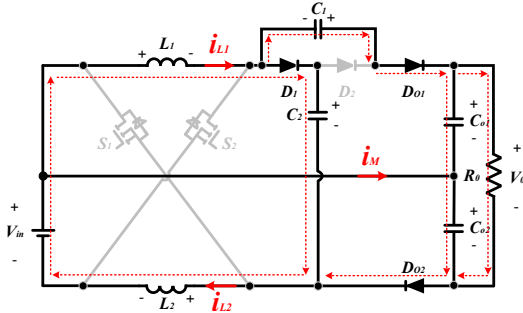


Fig. 4. The operation of mode II with unbalanced inductors.

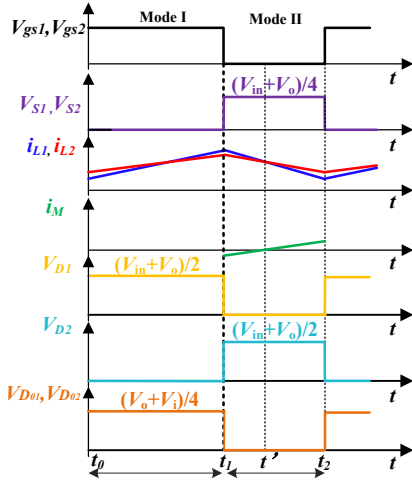


Fig. 5. Key waveforms in the condition of unbalance inductors.

When the values of two inductors are slightly different, their slopes are also slightly different, and the middle line current is very small. Under high frequency, the current in the middle line only affects the voltage ripple of the input and output capacitors, the voltage ripple is very small, and it has very little impact on the average voltage of the input and output capacitors.

Therefore, the voltage balance of the input and output capacitors can be remained, and the voltage stress of the switches can be derived as

$$\begin{cases} V_{S1} = V_{C_{O2}} \\ V_{S2} = V_{in} + V_{C_{O1}} - V_{C_1} \end{cases} \quad (17)$$

### D. DCM and BCM Analysis

In DCM, the ASL-SC-2OD converter is divided into mode I, mode II and mode III, as shown in Fig. 2(a)-(c), and the operation principles of the three modes are analyzed in detail in section A. According to (1), the peak inductor current in mode I is given by

$$i_{L1p} = i_{L2p} = i_{L(t_0)} + \frac{V_{in}}{L} DT_s \quad (18)$$

According to (2) and Fig. 3(b), the peak inductor current in mode II is given by

$$i_{L1p} = i_{L2p} = i_{L(t_0)} + \frac{V_0 - 3V_{in}}{4L} D_2 T_s \quad (19)$$

where  $D_2 T_s$  is the duration time between  $t_1$  and  $t_2$ .

Because the peak currents in two modes are equal, combining (18) and (19), the relationship between  $D_2$  and  $D$  can be derived as

$$D_2 = \frac{4V_{in}}{V_0 - 3V_{in}} D \quad (20)$$

Combining (13), (18) and (20), the voltage gain in DCM is derived as

$$G_{DCM} = \frac{V_0}{V_{in}} = \frac{3}{2} + \frac{1}{2} \sqrt{9 + \frac{4D^2}{\tau}} \quad (21)$$

where

$$\tau = \frac{Lf_s}{R_0} \quad (22)$$

The ASL-SC-2OD converter can be operated in Boundary Conduction Mode (BCM) when the voltage gain in CCM and DCM is equal. Combining (11) and (21), the boundary condition between CCM and DCM can be derived as

$$\tau_B = \frac{D(1-D)^2}{4D+12} \quad (23)$$

The boundary condition is shown in Fig. 6. The ASL-SC-2OD converter is operated in CCM when  $\tau$  is larger than  $\tau_B$ , the ASL-SC-2OD converter is operated in DCM when  $\tau$  is less than  $\tau_B$ .

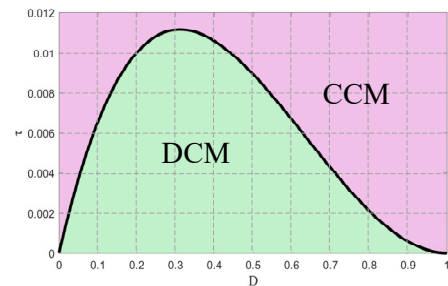


Fig. 6. Boundary condition.

### E. Input current ripple analysis

The diagram of input current  $i_{in}$ , inductor current  $i_{L1}$  &  $i_{L2}$ , midline current  $i_M$  is shown in Fig. 2. And the current

waveforms of the proposed converter are shown in Fig. 7.

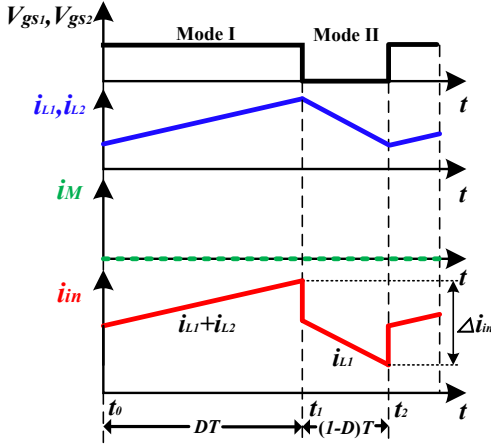


Fig. 7. Current waveforms of the proposed converter.

According to the current waveforms of the proposed converter. The current through inductors  $L_1$ ,  $L_2$  can be expressed as

$$i_{L1} = i_{L2} = \begin{cases} i_L(t_0) + \frac{V_{in}}{L}(t - t_0) & t_0 \leq t < t_1 \\ i_L(t_1) + \frac{3V_{in} - V_0}{4L}(t - t_1) & t_1 \leq t < t_2 \end{cases} \quad (24)$$

The midline current is given by

$$i_M = 0 \quad (25)$$

The input current is given by

$$i_{in} = \begin{cases} i_{L1} + i_{L2} & t_0 \leq t < t_1 \\ i_{L1} & t_1 \leq t < t_2 \end{cases} \quad (26)$$

From (24) and (26), the input current can be obtained

$$i_{in} = \begin{cases} \frac{4I_0}{1-D} - \frac{V_o(1-D)D}{f_s L(3+D)} + \frac{2V_o(1-D)}{L(3+D)}(t - t_0) & t_0 \leq t < t_1 \\ \frac{2I_0}{1-D} + \frac{V_o(1-D)D}{2f_s L(3+D)} - \frac{DV_0}{(3+D)L}(t - t_1) & t_1 \leq t < t_2 \end{cases} \quad (27)$$

And then, the ripple of input current can be expressed as:

$$\Delta i_{in} = \frac{2I_0}{1-D} + \frac{3V_o(1-D)D}{2Lf_s(3+D)} \quad (28)$$

#### F. Switches self-voltage balancing characteristic

Several high step-up DC-DC converters which combining ASL structure with SC cell were introduced in literature [19]-[21], [23]-[25], [27]. These SC/ASL step-up converters can be classified into the structure which is shown in Fig. 8. In actual conditions, the parallel parasitic capacitor exists in the MOSFET. So,  $V_{in}$ ,  $L_1$ ,  $C_{p2}$  and  $V_{in}$ ,  $L_2$ ,  $C_{p1}$  forms a resonant circuit respectively when the two switches are turned off, the resonant voltage will cause unbalance voltage stress across the switches when the values of the two inductors  $L_1$  &  $L_2$  are unequal, which results in overvoltage stress across the switches. However, this problem does not appear in the proposed converter. Considering the existence of parasitic capacitors, the equivalent circuit of the proposed converter in mode II is shown in Fig. 9 and Fig. 10.

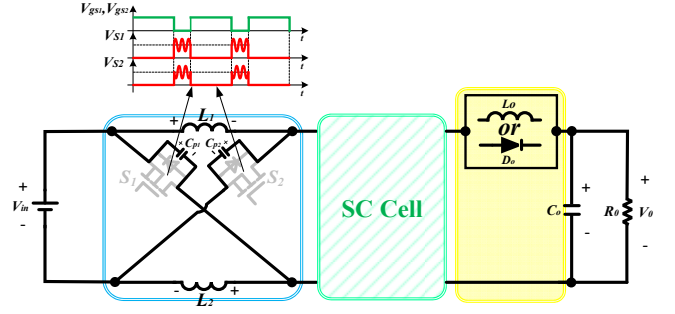


Fig. 8. Voltage unbalance problem on switches  $S_1$  &  $S_2$  of the converters in [19]-[21], [23]-[25], [27].

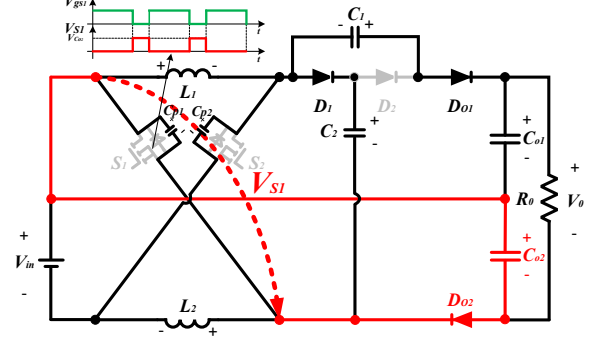


Fig. 9. The principle of voltage balance on switch  $S_1$ .

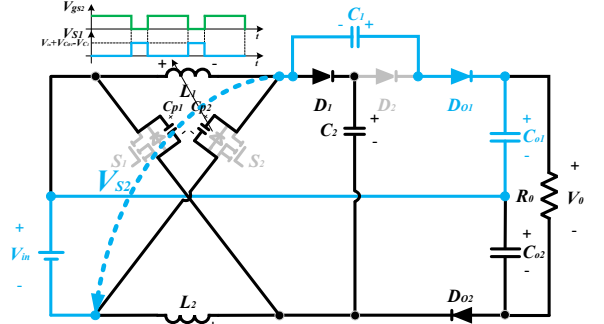


Fig. 10. The principle of voltage balance on switch  $S_2$ .

Because the voltage of the capacitors cannot be changed suddenly, the voltage of  $S_1$  is clamped by  $C_{02}$  when the two switches are turned off, which is shown in the red circuit loop of Fig. 9. The principle of voltage balance on switch  $S_2$  is shown in Fig. 10 (blue circuit loop), the voltage of  $S_2$  is clamped by  $C_1$  and  $C_{01}$  when the two switches are turned off. So, the voltages of  $S_1$  and  $S_2$  in mode II are given by

$$\begin{cases} V_{S1} = V_{C_{02}} \\ V_{S2} = V_{in} + V_{C_{01}} - V_{C_1} \end{cases} \quad (29)$$

In addition, due to the capacitors clamping structure, whether the values of the two inductors  $L_1$  and  $L_2$  are the same or not, the voltages of the two inductors in two modes can be written as

$$\begin{cases} V_{L1}^I = V_{in}, & V_{L1}^{II} = V_{C_1} - V_{C_{01}} \\ V_{L2}^I = V_{in}, & V_{L2}^{II} = V_{in} - V_{C_{02}} \end{cases} \quad (30)$$

Combining (10) and (30), the voltage-second balance principles on two inductors are given by

$$\begin{cases} V_{in} \cdot D + (V_{C_1} - V_{C_{01}}) \cdot (1-D) = 0 \\ V_{in} \cdot D + (V_{in} - V_{C_{02}}) \cdot (1-D) = 0 \end{cases} \quad (31)$$

By simplifying (31)

$$V_{C_{o2}} = V_{in} + V_{C_{o1}} - V_{C_1} \quad (32)$$

According to (29) and (32), the relationship between the voltage of  $S_1$  and the voltage of  $S_2$  can be derived as

$$V_{S_1} = V_{S_2} \quad (33)$$

Also, as shown in Fig. 9 and Fig. 10, the voltages of junction capacitors  $C_{p1}$  and  $C_{p2}$  are given by

$$\begin{cases} V_{C_{p1}} = V_{C_{o2}} \\ V_{C_{p2}} = V_{in} + V_{C_{o1}} - V_{C_1} \end{cases} \quad (34)$$

The voltages of inductors  $L_1$  and  $L_2$  are given by

$$V_{L_1} = V_{L_2} = (V_{in} - V_{C_2}) / 2 \quad (35)$$

Due to the voltages of capacitors  $C_1$ ,  $C_2$ ,  $C_{o1}$ ,  $C_{o2}$  and input voltage are constant, according to (34) and (35), the voltages of two inductors and two capacitors are constant. Therefore, there is no resonance occur between junction capacitors and inductors, the voltages of two switches are constant in mode II and there is no voltage oscillation on two switches.

Therefore, in CCM, the proposed converter has the characteristic of voltage balance on two switches whether the two inductors are the same or not.

In DCM, according to the equivalent circuit of the proposed in mode III, it can be concluded that the theoretical voltage of the two switches is equal to  $V_{in}$ , and equivalent circuit of the proposed converter is similar to the converter in [21]. In mode III, the switches voltage will not be clamped by the capacitors clamp structure, the source voltage, inductor and the parasitic capacitor across the switch will be in resonance and spikes will occur. However, although the self-balancing will be lost in mode III, the voltage oscillation amplitude will not exceed the voltage of the switch  $[(V_{in} + V_0)/4]$  of mode II, this is because the output diode will turn on when the switches voltage is higher than the switch voltage  $[(V_{in} + V_0)/4]$  of mode II, and the capacitors clamp loop can be worked, which leads to the voltage of switches can be clamped again. The switches voltage stress depends on the maximum voltage, due to the voltage oscillation amplitude will not exceed the voltage stress value in mode II, so the voltage stress of switches in CCM and DCM are the same. In DCM, the switches voltage stress is not affected by the voltage oscillation in mode III, the switches voltage stress is also equal to  $(V_{in} + V_0)/4$ .

#### G. Voltage stress on the power components

Based on the analysis of the operation principle in section A, the voltage stresses on two switches  $S_1$  and  $S_2$  are given by

$$V_{S_1} = V_{S_2} = \frac{V_{in}}{1-D} = \frac{V_0}{3+D} \quad (36)$$

The voltage stresses on two diodes  $D_1$  and  $D_2$  are given by

$$V_{D_1} = V_{D_2} = \frac{2V_{in}}{1-D} = \frac{2V_0}{3+D} \quad (37)$$

The voltage stresses on two output diodes  $D_{o1}$  and  $D_{o2}$  are given by

$$V_{D_{o1}} = V_{D_{o2}} = \frac{V_{in}}{1-D} = \frac{V_0}{3+D} \quad (38)$$

From (36)-(38), we can deduce that the voltage stresses on all the power components in the proposed converter are much lower than output voltage  $V_0$ .

#### H. Current stress across the power components

In order to facilitate the analysis and calculation, internal resistors of all components and the current ripple are neglected. According to the analysis of CCM operation, the rms current value of power components can be approximately written as

$$I_{rms} \approx \sqrt{\frac{1}{T_s} \left( \int_0^{DT_s} (I_{avg}^I)^2 dt + \int_{DT_s}^{T_s} (I_{avg}^{II})^2 dt \right)} \quad (39)$$

Combining (14), (16) and (39), the rms current values across the switches  $S_1$  and  $S_2$  are given by

$$\begin{aligned} I_{S_1(rms)} = I_{S_2(rms)} &\approx \sqrt{\frac{1}{T_s} \int_0^{DT_s} (I_L + I_{D_2}^I)^2 dt} \\ &= \sqrt{\frac{1}{T_s} \int_0^{DT_s} \left( \frac{2I_0}{1-D} + \frac{I_0}{D} \right)^2 dt} = I_0 \sqrt{D} \left( \frac{2}{1-D} + \frac{1}{D} \right) \end{aligned} \quad (40)$$

The detailed calculation process for the rms current value of the switch is given in Appendix A.

Combining (14) and (39), the rms current value across the diode  $D_2$  is given by

$$I_{D_2(rms)} \approx \sqrt{\frac{1}{T_s} \int_0^{DT_s} (I_{D_2}^I)^2 dt} = \sqrt{\frac{1}{T_s} \int_0^{DT_s} \left( \frac{I_0}{D} \right)^2 dt} = I_0 \sqrt{\frac{1}{D}} \quad (41)$$

Combining (15) and (39), the rms current values across the diode  $D_1$  and output diodes  $D_{o1}$  &  $D_{o2}$  are given by

$$I_{D_1(rms)} = I_{D_{o1}(rms)} = I_{D_{o2}(rms)} \approx \sqrt{\frac{1}{T_s} \int_{DT_s}^{T_s} \left( \frac{I_0}{1-D} \right)^2 dt} = I_0 \sqrt{\frac{1}{1-D}} \quad (42)$$

### III. COMPARISON ANALYSIS

Table. II shows the comparison of the proposed converter with other similar nonisolated step-up converters in the aspects of voltage gain, ideal switches voltage stress, output diodes voltage stress, components count and voltage oscillation on switches. As can be seen in Table. II and Fig. 11(a)&(b)&(c), the voltage gain of the proposed converter is the highest among these similar nonisolated step-up converters for the whole duty cycle range and the proposed converter has the lowest voltage stress on switches and lowest output diodes voltage stress.

As shown in Table. II, for traditional ASL converter [18] and its derivative hybrid SL/ASL converters [33], SC/ASL converters [19-21], [24], when the values of inductors  $L_1$  and  $L_2$  are different, resonant voltage occurs across two switches, which results in unbalanced voltage stress across the switches and voltage oscillations on the switches appear. The switches voltage stress values are higher than their ideal theoretical values. However, the proposed converter has no voltage oscillations on two switches due to the capacitors clamp structure composed of its own input and output capacitors. The resonant can be suppressed and the switches voltage stress of the proposed converter is equal to the ideal theoretical value. Therefore, although the switches voltage stress of the proposed converter, the SC-ANC converter [20] and ASL-SU2C-VO converter [21] are all the lowest, in practice, the proposed converter has lower voltage stress on switches.

It should be noted that the SC-ANC [20] and ASL-SU2C-VO [21] converters have the same voltage gain as the proposed converter. However, these two converters have voltage oscillation on switches, which leads to the voltage stress on switches is higher than proposed converter. Also, the output



diodes voltage stress of the proposed converter is half of that of these two converters.

In the aspect of cost comparison, the costs of the inductors, diodes and capacitors the proposed converter are similar to that of converter [21]. However, due to the proposed converter has lower voltage stress on switches, so, a lower voltage stress MOSFETs with smaller ON-resistance ( $R_{on}$ ) can be used in the proposed converter, which leads to the switches cost of the proposed converter is less than that of the converter [21]. Also, to reduce the switches voltage oscillation in converter [21], the RC snubber circuits are needed, however, the RC snubber circuits are not used in the proposed converter, the proposed converter uses its own input and output capacitors to suppress the voltage oscillation. Because of this, the proposed converter reduces the cost of using the snubber circuits. Due to the voltage stress on switches and output diodes are reduced, the created heat is decreased, and the cost of radiator is reduced.

The proposed converter has one more output capacitor than converter [21], but in general, because the output voltage is high, two low voltage stress capacitors in series can be used in place of one high voltage stress capacitor. Therefore, the capacitor count of both two converters is similar. Also, the two output capacitors of the proposed converter are not only the output filters, but also a part of the capacitors clamp structure. The switches voltage can be clamped by the input voltage and the voltages of two output capacitor, the capacitor clamp structure is composed of its own input and output capacitors without adds additional capacitors. Therefore, the stacked capacitor architecture in the proposed converter will not affect the controller of the converter, the proposed converter can use the same digital controller as the converter [21].

In brief, the merits of the proposed converter are high voltage gain, lower voltage stress on switches, lower voltage stress on output diodes, and lower costs.

#### IV. DESIGN CONSIDERATIONS

In order to verify the performance of the proposed converter accurately in the experiment, some design considerations need to be discussed. The proposed converter is designed to operate in CCM operation, and the detailed designs of all components are as follows.

(1) Selection of Duty cycle: according to the CCM voltage gain expression (11), the selection of duty cycle is given by

$$D = \frac{G_{CCM} - 3}{G_{CCM} + 1} \quad (43)$$

(2) Inductors Design: the inductor current ripple  $\Delta i_L$  can be written as

$$\Delta i_L = \frac{V_{in} D}{L f_s} = \frac{V_0 (1-D) D}{(3+D) L f_s} \quad (44)$$

where  $f_s$  is switching frequency.

Therefore, the inductor values of  $L_1$  and  $L_2$  are given by

$$L_1 = L_2 \geq \frac{V_0 (1-D) D}{(3+D) \Delta i_L f_s} \quad (45)$$

(3) Capacitors Design: according to the theoretical analysis in section II, the capacitors voltage stresses are given by

$$\begin{cases} V_{C_{o1}} = \frac{(2+D)V_0}{3+D}, V_{C_{o2}} = \frac{V_0}{3+D} \\ V_{C_1} = \frac{2V_0}{3+D}, V_{C_2} = \frac{(1+D)V_0}{3+D} \end{cases} \quad (46)$$

According to ref. [34], the power loss of the switched-capacitor can be reduced when the current level is decreased. Also, the two capacitors of SC cell are charged and discharged in two operation modes, therefore, the switched capacitors should be designed in the operation of partial charge.

In mode I, the capacitor  $C_1$  is charged, according to the analysis in ref. [34], the capacitor  $C_1$  can be calculated by

$$C_1 \geq \frac{0.1}{R_{eq1} f_s} \quad (47)$$

where  $R_{eq1}$  is the sum of resistor of switches, capacitors and diodes in mode I.

In mode II, the capacitor  $C_2$  is charged, the capacitor  $C_2$  can be calculated by

$$C_2 \geq \frac{0.18}{R_{eq2} f_s} \quad (48)$$

where  $R_{eq2}$  is the sum of resistor of capacitors and diodes in mode II.

Finally, the output capacitors can be given by

$$\begin{cases} C_{o1} \geq \frac{I_0 (1-D)}{\Delta v_{C_{o1}} f_s} \\ C_{o2} \geq \frac{I_0 (1-D)}{\Delta v_{C_{o2}} f_s} \end{cases} \quad (49)$$

where  $\Delta v_{C_{o1}}$ ,  $\Delta v_{C_{o2}}$  are capacitors voltage ripples.

(4) Selection of power components: the voltage stresses on power components are discussed in section G, the current stresses across power components are discussed in section H. Therefore, power components can be selected according to expression (36)-(42).

Based on the above analysis, the values of storage components and the selection of power components are shown in Table. I.

TABLE I  
EXPERIMENT PARAMETERS

Components	Parameters
Input voltage $V_{in}$	25-45V
Output voltage $V_o$	380V
Rated power $P_o$	200W
Switching frequency $f_s$	50kHz
Inductors $L_1, L_2$	240 $\mu$ H (both two converters)
MOSFETs $S_1, S_2$	150V-SE150180GTS (proposed converter) 200V-NCE0275T (converter in ref. [21])
Diodes $D_1, D_2$	300V-SFAF805GC0G (both two converters)
Output diodes $D_{o1}, D_{o2}$	150V-MBR20H150CTG (proposed converter)
Output diodes $D_o$	300V-SFAF805GC0G (converter in ref. [21])
Input capacitors	820 $\mu$ F/50V & CBB 2 $\mu$ F (both two converters)
Capacitors $C_1, C_2, C_{o1}, C_{o2}$	22 $\mu$ F (film capacitor, proposed converter)
Capacitors $C_1, C_2, C_o$	22 $\mu$ F (film capacitor, converter in ref. [21])

TABLE II  
COMPARISON WITH OTHER SIMILAR NONISOLATED STEP-UP CONVERTERS

Converters	Voltage Gain ( $G_{CCM}$ )	Ideal Switches voltage Stress ( $V_S/V_0$ )	Output Diodes voltage Stress ( $V_D/V_0$ )	Switches Count	Diodes Count	Inductors Count	Capacitors Count	Voltage Oscillation on Switches
Proposed	$\frac{3+D}{1-D}$	$\frac{1}{3+D}$	$\frac{1}{3+D}$	2	4	2	4	No
Converter I in [18]	$\frac{1+D}{1-D}$	$\frac{1}{1+D}$	$\frac{1}{1+D}$	2	2	2	4	Yes
Converter III in [18]	$\frac{3-D}{1-D}$	$\frac{1}{3-D}$	$\frac{2}{3-D}$	2	3	2	3	Yes
ASL-SU2C-CO [19]	$\frac{1+3D}{1-D}$	$\frac{1}{1+3D}$	—	2	2	3	3	Yes
SC-ANC [20]	$\frac{3+D}{1-D}$	$\frac{1}{3+D}$	$\frac{2}{3+D}$	2	3	3	3	Yes
ASL-SU2C-VO [21]	$\frac{3+D}{1-D}$	$\frac{1}{3+D}$	$\frac{2}{3+D}$	2	3	2	3	Yes
Converter [24]	$\frac{1+3D}{1-D}$	$\frac{1}{1+3D}$	—	2	2	3	3	Yes
SC-Boost [28]	$\frac{2}{1-D}$	$\frac{1}{2}$	$\frac{1}{2}$	2	3	2	3	No
SL-Boost [29]	$\frac{1+D}{1-D}$	1	1	1	4	2	1	No
HBC [30]	$\frac{3-D}{1-D}$	$\frac{1}{3-D}$	—	1	4	1	4	No
Group E (N=2) in [31]	$\frac{3}{1-D}$	$\frac{1}{3}$	$\frac{1}{3}$	2	3	2	3	No
Converter in [32]	$\frac{2}{1-D}$	$\frac{1}{2}$	—	4	0	2	4	No
SH-SLC [33]	$\frac{1+3D}{1-D}$	$\frac{1+D}{1+3D}$	$\frac{2+2D}{1+3D}$	2	7	4	1	Yes
AH-SLC [33]	$\frac{1+2D}{1-D}$	$\frac{1+D}{1+2D}$	$\frac{2+D}{1+2D}$	2	4	3	1	Yes
		$\frac{1}{1+2D}$						

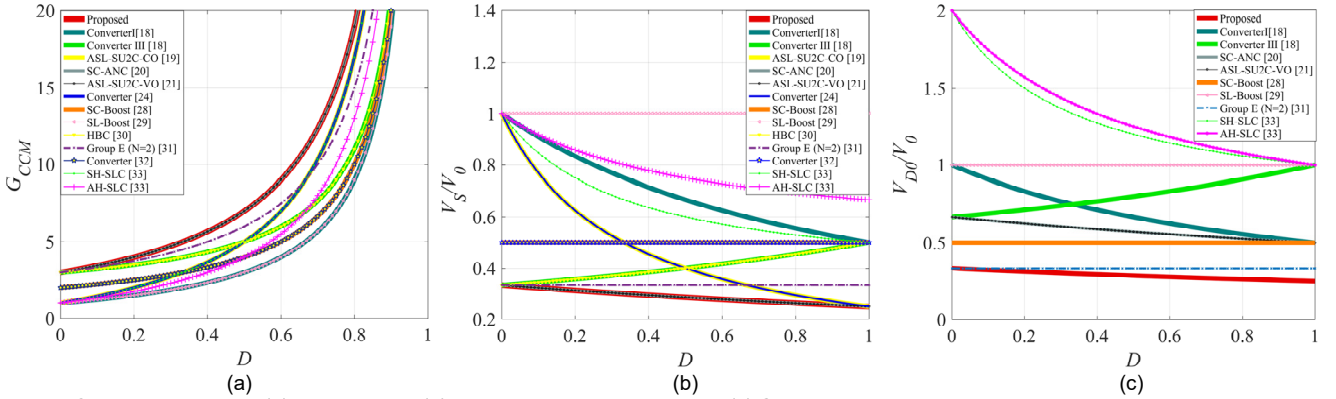


Fig. 11. Comparison curves. (a) Voltage gain. (b) Ideal switches voltage stress. (c) Output diodes voltage stress.

## V. EXPERIMENTAL RESULTS

To evaluate the performance of the proposed ASL-SC-2OD converter, an experimental prototype (Fig. 12) was built in the laboratory, and the experimental prototype of ASL-SU2C-VO converter in [21] was also built to compare with the proposed converter. The two experimental prototypes were tested in the same experimental conditions: input voltage  $V_{in}$  that ranges from 25 to 45V, the output voltage  $V_0$  is 380V, the switching

frequency  $f_s$  is 50 kHz, and the rated power is 200W. According to the analysis in section II, both two converters have the same voltage gain and the same voltage stress on SC diodes, the switches voltage stress and output diodes voltage stress of both two converters are different. So, 150V MOSFET SE150180GTS and 150V output diodes MBR20H150CTG are utilized for the proposed converter, 200-V MOSFET NCE0275T and 300V output diode SFAF805GC0G are utilized for the ASL-SU2C-VO converter in [21]. 300V SC diodes SFAF805GC0G are utilized for both two converters. The main



components and parameters of the converters are summarized in Table I.

The proposed converter has simple operation and the ability to realize self-balance on switches. Therefore, the proposed converter does not need complicated closed loop control logic. The proposed converter adopts the closed-loop control strategy of single voltage loop, as shown in Fig. 13, the voltage  $V_o$  is controlled by the voltage controller with the reference voltage  $V_{ref}$  in the voltage loop, and the digital signal is transmitting to the PI regulator, then output the synchronous PWM gate signals of  $S_1$  and  $S_2$  by PWM generator.

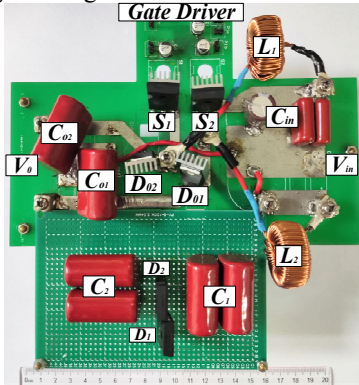


Fig. 12. Experimental prototype.

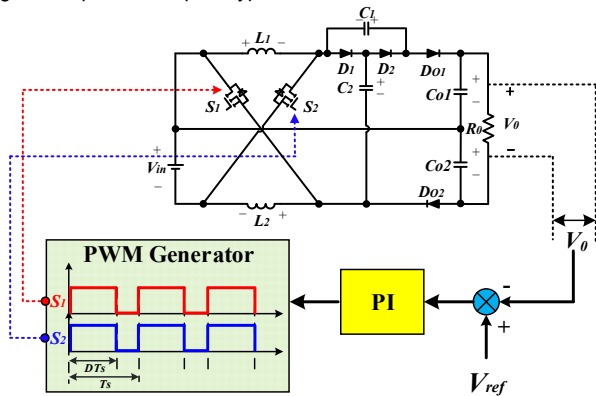
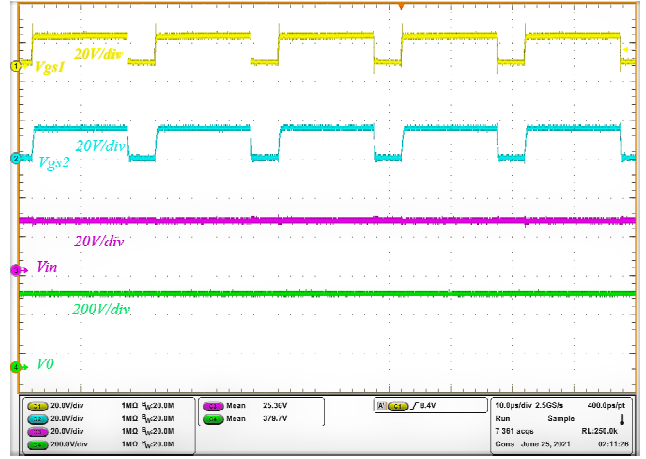


Fig. 13. Control strategy of the proposed converter.

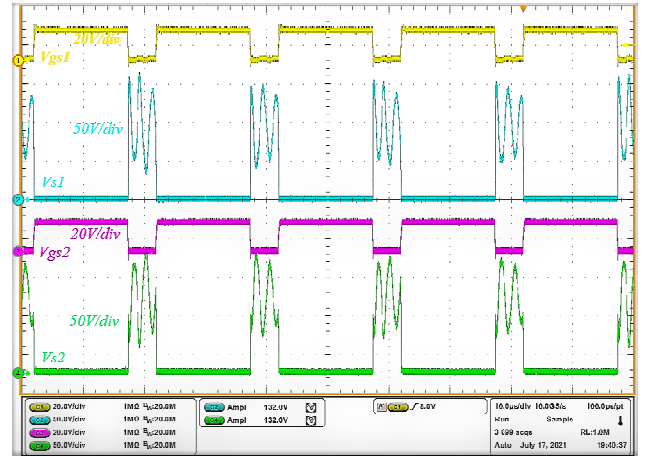


(a)

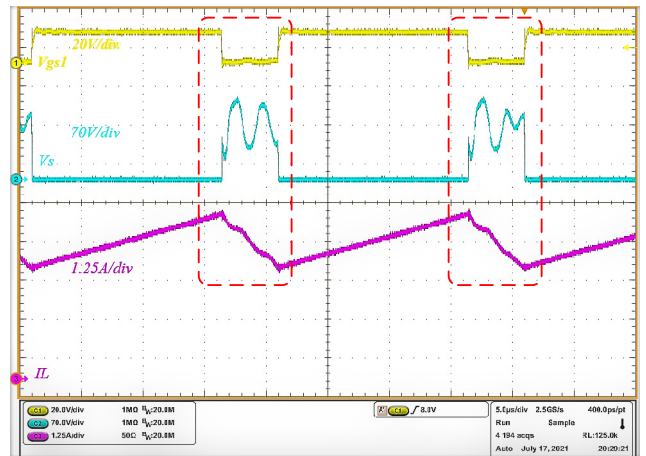


(b)

Fig. 14. (a) Gate-source signals ( $V_{gs1}$ ,  $V_{gs2}$ ) and input and output voltage ( $V_{in}$  and  $V_o$ ) of the converter in [21]. (b)  $V_{gs1}$ ,  $V_{gs2}$  and input and output voltage ( $V_{in}$  and  $V_o$ ) of the proposed converter. Time (10  $\mu$ s/div).

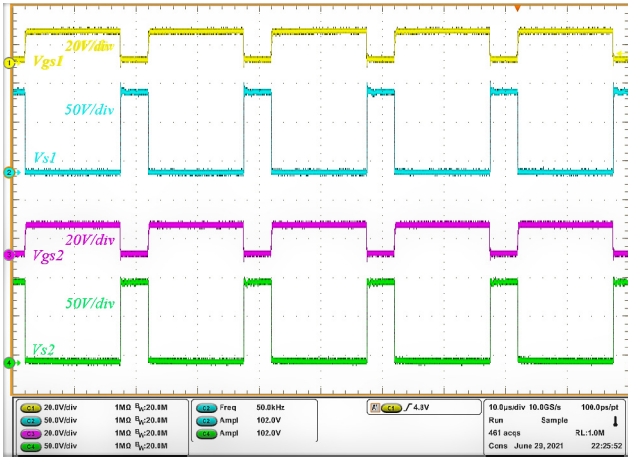


(a)



(b)

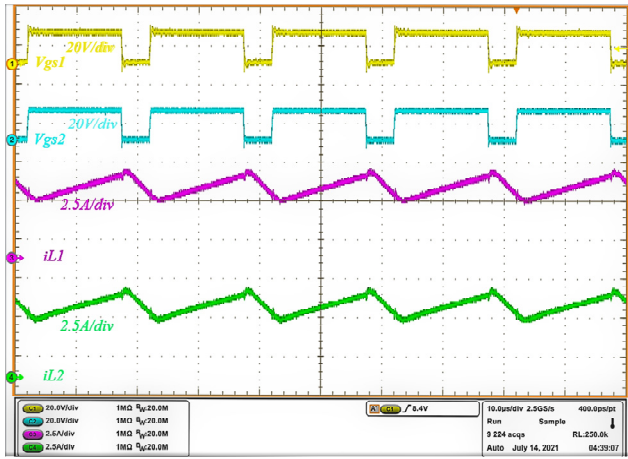
Fig. 15. (a) Gate-source signals ( $V_{gs1}$ ,  $V_{gs2}$ ) and Drain-source voltages ( $V_{ds1}$  and  $V_{ds2}$ ) of the converter in [21]. (b)  $V_{gs1}$ ,  $V_{ds}$  and inductor current  $i_L$  of the converter in [21].



(a)



Fig. 18. Gate-source signals ( $V_{gs1}$ ,  $V_{gs2}$ ) and output diodes voltages ( $V_{D1}$  and  $V_{D2}$ ) of the proposed converter. Time ( $10 \mu\text{s}/\text{div}$ ).



(b)

Fig. 16. (a) Gate-source signals ( $V_{gs1}$ ,  $V_{gs2}$ ) and drain-source voltages ( $V_{S1}$  and  $V_{S2}$ ) of the proposed converter. (b)  $V_{gs1}$ ,  $V_{gs2}$  and inductor currents ( $i_{L1}$  and  $i_{L2}$ ) of the proposed converter.

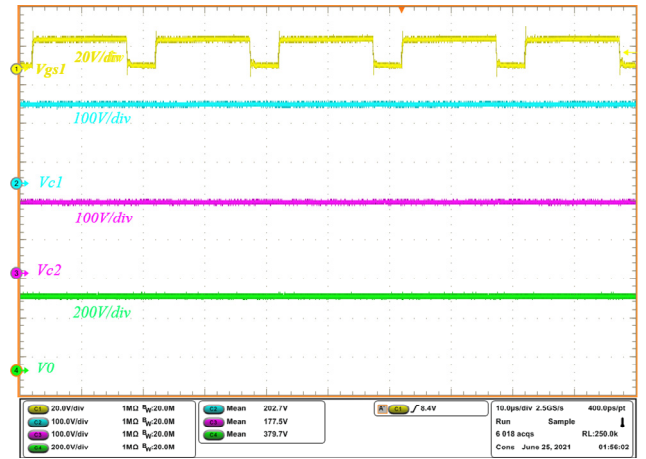


Fig. 19. Gate-source signal  $V_{gs1}$ , capacitors voltages ( $V_{C1}$  and  $V_{C2}$ ) and output voltage  $V_0$  of the proposed converter. Time ( $10 \mu\text{s}/\text{div}$ ).

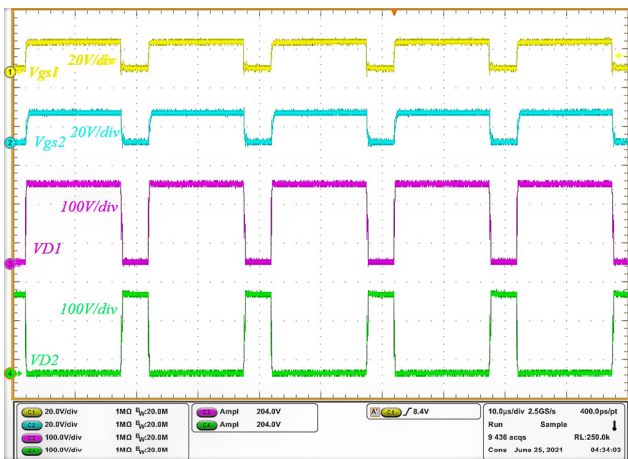


Fig. 17. Gate-source signals ( $V_{gs1}$ ,  $V_{gs2}$ ) and diodes voltages ( $V_{D1}$  and  $V_{D2}$ ) of the proposed converter. Time ( $10 \mu\text{s}/\text{div}$ ).



Fig. 20. Gate-source signal  $V_{gs1}$ , capacitors voltages ( $V_{CO1}$  and  $V_{CO2}$ ) and output voltage  $V_0$  of the proposed converter. Time ( $10 \mu\text{s}/\text{div}$ ).

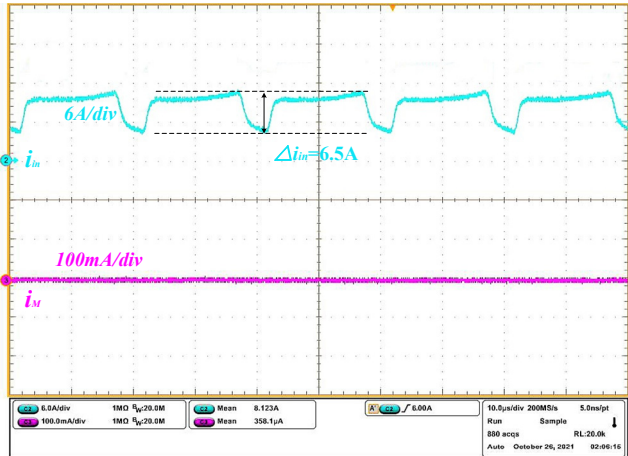


Fig. 21. The experiment waveforms of input current  $i_{in}$  and the middle line current  $i_M$ .

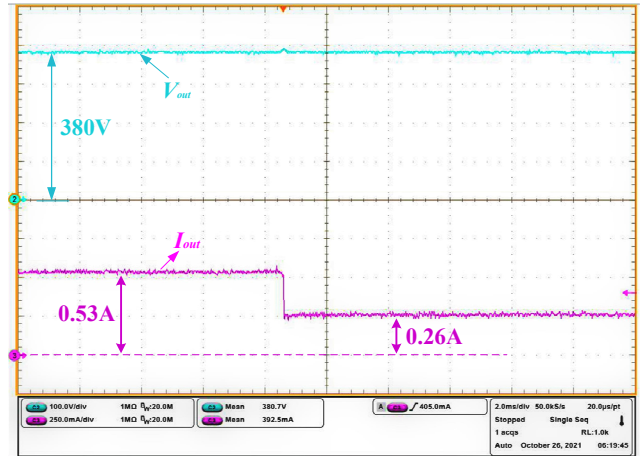


Fig. 24. The dynamic response of the output voltage for changes in load from 200W to 100W.

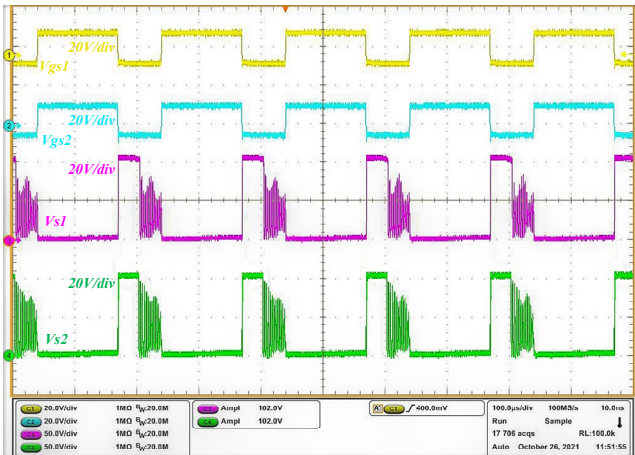


Fig. 22. Gate-source signals ( $V_{gs1}$ ,  $V_{gs2}$ ) and drain-source voltages ( $V_{s1}$  and  $V_{s2}$ ) of the proposed converter in DCM.

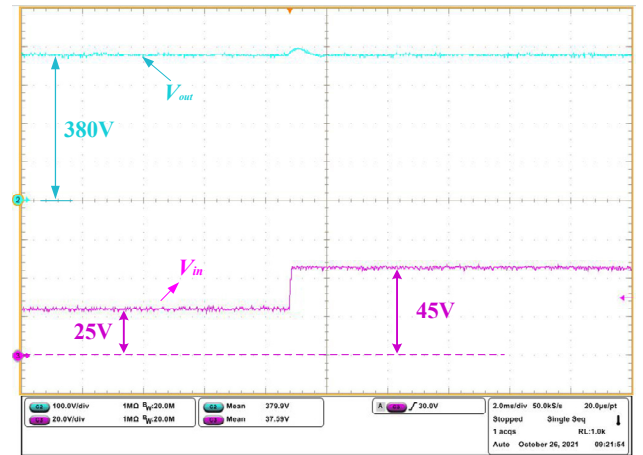


Fig. 25. The dynamic response of the output voltage for changes in load from input voltage 25V to 45V.

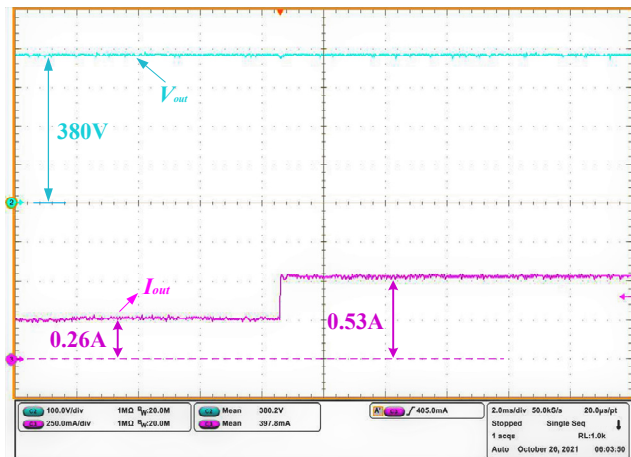


Fig. 23. The dynamic response of the output voltage for changes in load from 100W to 200W.

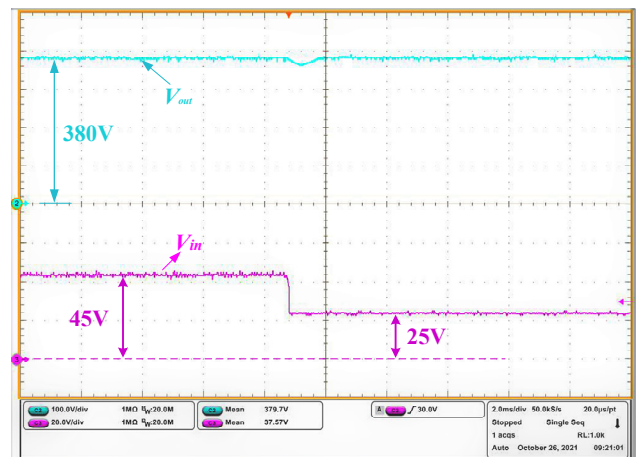


Fig. 26. The dynamic response of the output voltage for changes in load from input voltage 45V to 25V.



As shown in Fig. 14(a)&(b), the converter in [21] and the proposed converter were tested in the same duty cycle, and the two switches are turned on and off simultaneously. The output voltage  $V_o$  of both converters is 380V when the input voltage is 25V, so both converters have the same voltage gain.

Fig. 15(a) shows gate source signals ( $V_{gs1}$  and  $V_{gs2}$ ) and drain source voltages ( $V_{S1}$  and  $V_{S2}$ ) of the converter in [21]. The experimental conditions are the input voltage is 25V and the output voltage is 380V. Obviously, the converter in [21] has voltage oscillation on switches, and the voltage stress on switches is 132V, which is higher than 102V (ideal switches voltage stress is  $(V_{in}+V_o)/4$ ). Fig. 15(b) shows gate source signals  $V_{gs1}$ , drain source voltages  $V_S$ , and the inductor current  $i_L$  of the converter in [21], the inductor current is also in the resonance obviously.

Fig. 16(a) shows gate source signals ( $V_{gs1}$  and  $V_{gs2}$ ) and drain source voltages ( $V_{S1}$  and  $V_{S2}$ ) of the proposed converters. The proposed converter has no voltage oscillation on switches, the switches voltage stress  $V_{S1}=V_{S2}=102V$ , which is equal to ideal switches voltage stress  $((V_{in}+V_o)/4)$ . So, the voltage stress on switches is lower and the proposed converter can achieve self-voltage balance on two switches. Fig. 16(b) shows  $V_{gs1}$  and  $V_{gs2}$ , the inductor currents ( $i_{L1}$  and  $i_{L2}$ ) of the proposed converter. Obviously, the resonance of inductor currents is also suppressed. It should be noted that the shown resonance frequency in ref. [21] is lower than the resonance frequency in this paper. We have analyzed the resonance frequency values mathematically and the mathematical procedures are shown in Appendix B.

Fig. 17 shows  $V_{gs1}$  and  $V_{gs2}$  and the diodes voltages ( $V_{D1}$  and  $V_{D2}$ ),  $V_{D1}=V_{D2}=204V$ . Fig. 18 shows  $V_{gs1}$  and  $V_{gs2}$  and the output diodes voltages ( $V_{D01}$  and  $V_{D02}$ ),  $V_{D01}=V_{D02}=102V$ . Fig. 19 shows  $V_{gs1}$ , capacitors voltages ( $V_{C1}$  and  $V_{C2}$ ) and output voltage  $V_o$ ,  $V_{C1}=203V$ ,  $V_{C2}=177V$  and  $V_o=380V$ . Fig. 20 shows  $V_{gs1}$ , capacitors voltages ( $V_{CO1}$  and  $V_{CO2}$ ) and output voltage  $V_o$ ,  $V_{CO1}=278V$ ,  $V_{CO2}=102V$  and  $V_o=380V$ , so the voltage stresses on two output capacitors are lower than output voltage.

As can be seen in Fig. 21, the input current waveform is consistent with the theoretical analysis in section E, the input current ripple value is 6.5A, and the middle line current is approximately zero.

Fig. 22 shows the waveforms of two gate-source signals and the voltage of two switches in DCM operation in the condition of input voltage is 25V and output voltage is 380V. The voltage stress on the two switches is  $V_{S1}=V_{S2}=102V$ , which is equal to switches voltage stress in CCM. Although the self-balancing is lost in mode III, the voltage oscillation amplitude will not exceed the voltage of the switch 102V  $[(V_{in}+V_o)/4]$  of mode II, so the voltage oscillation in DCM will not affect the switch voltage stress value.

The dynamic response of the output voltage for changes in load from half load 100W to the nominal load 200W is shown in Fig. 23. The dynamic response of the output voltage for changes in load from nominal load 200W to the half load 100W is shown in Fig. 24. As can be seen from the waveforms of output current and output voltage, the output current changes in a step wise manner and the output voltage can be maintained at 380V when the load sudden changes under the designed voltage closed-loop control.

The dynamic response of the output voltage for changes from input voltage 25V to 45V is shown in Fig. 25, the output

voltage for changes from input voltage 45V to 25V is shown in Fig. 26. Also, the output voltage can be maintained at 380V when the input voltage sudden changes under the designed voltage closed-loop control. Therefore, the proposed converter has good dynamic characteristics.

The experimental waveforms are all similar to the theoretical waveforms and the experimental values are equal to the theoretical values, which verifies the correctness of theoretical analysis in section II.

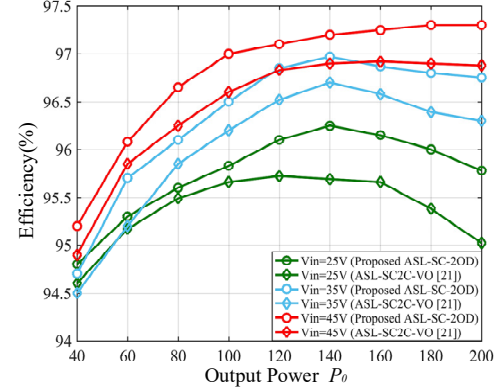


Fig. 27. Experimental efficiency curves.

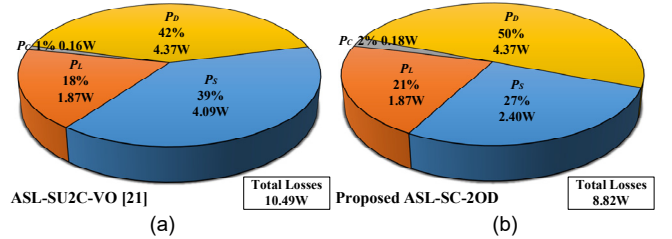


Fig. 28. Losses distribution ( $P_o=200W$ ). (a) ASL-SU2C-VO [21], efficiency=95.02%. (b) Proposed ASL-SC-2OD, efficiency=95.78%.

Fig. 27 shows the experimental efficiency curves in the condition that input voltage is 25V, 35V, or 45V, output voltage is 380V. The experimental efficiency is measured by a Yokogawa power analyzer WT1800. The peak efficiency value of the ASL-SU2C-VO converter [21] is 96.92%, while the peak efficiency value of the proposed ASL-SC-2OD converter is 97.3%. The efficiency of ASL-SU2C-VO [21] at rated power 200W is 95.02%, 96.30% and 96.88% for input voltages of 25 V, 35 V and 45V, respectively, while for the proposed ASL-SC-2OD, these values are 95.78%, 96.75% and 97.30%.

Fig. 28 shows the calculated losses distribution for both converters in the condition that  $V_{in}=25V$ ,  $V_o=380V$  and  $P_o=200W$ . The theoretical calculation method of the loss distribution is shown in Appendix. C. Although the proposed converter has one more capacitor and one more output diode than the ASL-SU2C-VO converter, the capacitor loss value is very low, and the output diode voltage stress (102V) of the proposed converter is half of that (204V) of the converter [21], so a lower forward voltage Schottky diodes MBR20H150CTG ( $v_f=0.45V$ ) can be utilized in the proposed converter, the diodes loss for both converters is approximately equal. Compared with the ASL-SU2C-VO converter, the switches loss of the proposed converter is reduced by 1.69W, this is because the switches voltage stress (102V) of the proposed converter is lower than that (132V) of ASL-SU2C-VO converter, and lower voltage stress MOSFETs with smaller ON-resistance ( $R_{on}$ ) are utilized in the proposed converter.

## VI. CONCLUSION

In this paper, a novel high step-up SC/ASL converter was proposed (named ASL-SC-2OD). The proposed ASL-SC-2OD converter was analyzed in detail from operation principle, CCM analysis, CCM operation with unbalanced inductors, input current ripple analysis, DCM and BCM analysis, switches self-voltage balancing characteristic, voltage stress, current stress, comparison analysis, and design consideration. Finally, the correctness of the theoretical analysis was verified by experiments.

The proposed ASL-SC-2OD converter has high voltage gain (more than 15 times), and the operation principle is also simple. Compared with other similar nonisolated step-up converters, the proposed converter has lower voltage stresses on switches and output diodes, which leads to MOSFETs with smaller ON-resistance  $R_{ds(on)}$  and lower voltage stress output diodes can be utilized, and the efficiency of the proposed converter can be improved. Also, the one output diode can help form a capacitor clamp loop to clamp the voltage of switch. In addition, unlike other SC/ASL step-up converters [19]-[21], the proposed converter can suppress the resonance and achieve self-voltage balancing on two switches due to the capacitors clamp structure. Meanwhile, the output capacitors are not only the output filters, but also a part of the capacitors clamp structure, and the output capacitors have lower voltage stress. The proposed converter also has the advantage of lower cost.

Based on the above merits, the proposed converter is more suitable for high step-up applications.

### APPENDIX A. CALCULATION OF RMS VALUE OF SWITCH CURRENT

The inductor  $L_1$  current, diode  $D_2$  current and switch  $S_2$  current of mode I is shown in Fig. 29. The simplified key waveforms in switching period are shown in Fig. 30.

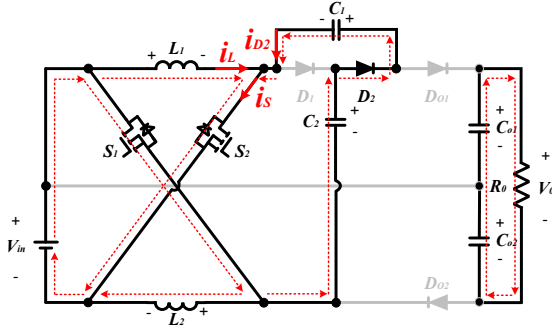


Fig. 29. Inductor  $L_1$  current, diode  $D_2$  current and switch  $S_2$  current in mode I.

#### (1) The calculation of average current of diodes

In one switching cycle, the avg current of capacitor  $C_1$ ,  $C_1$ ,  $C_{o1}$ ,  $C_{o2}$  is zero. Through the analysis of mode I and mode II, according to Kirchhoff's Current Law (KCL), the average currents of four diodes are equal and can be given by

$$I_{D_1} = I_{D_2} = I_{D_{o1}} = I_{D_{o2}} = I_0 \quad (50)$$

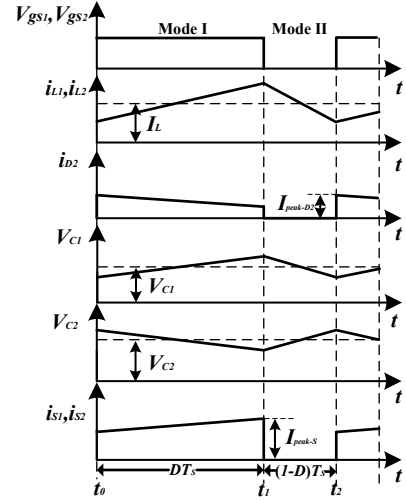


Fig. 30. Key waveforms in switching period.

#### (2) The calculation of rms current of the switches

According to Fig. 29, the switches current can be given by

$$i_S = i_L + i_{D_2} \quad (51)$$

From the analysis of Fig. 29 and Fig. 30, the current of  $D_2$  reaches its maximum at  $t=nT_s$  ( $n$  is an integer), and the peak current of  $D_2$  is given by

$$\begin{aligned} i_{peak-D_2} &= i_{D_2(DT_s)} \\ &= \frac{V_{C_1} + \Delta V_{C_1} - (V_{C_2} - \Delta V_{C_2}) + V_{in} - V_d}{R} = \frac{\Delta V_{C_1} + \Delta V_{C_2} - V_d}{R} \end{aligned} \quad (52)$$

where  $V_d$  is the forward voltage of  $D_2$ ;  $R$  is the resistor of the circuit loop which is formed of  $V_{in}$ ,  $S_1$ ,  $S_2$ ,  $C_1$ ,  $D_2$ , and  $C_2$ . Compared with the internal resistance of the diode and the switches, the resistance of the capacitor is small and can be ignored, so the resistor of the circuit loop can be given by

$$R = 2R_{ds} + R_d \quad (53)$$

where  $R_{ds}$  is the resistor of the switches and  $R_d$  is the resistor of the diodes. From (50) and (52), we can deduce  $i_{D_2}$  during the time interval  $[nT_s \sim (n+D)T_s]$ .

$$i_{D_2} = i_{D_2(nT_s)} - 2 \cdot \frac{i_{D_2(nT_s)} - I_0}{DT_s} \cdot (t - nT_s) \quad (54)$$

The inductor current during the time interval  $[nT_s \sim (n+D)T_s]$  can be given by

$$i_{D_2} = I_L - \frac{1}{2} \Delta i_L + \frac{\Delta i_L}{DT_s} (t - nT_s) \quad (55)$$

In mode I, the current pass the switches, and from (51) and (55), the rms switches current is given by (56) as shown at the top of the next page.

Assuming the values of  $C_1$ ,  $C_2$ , and  $L$  are large enough, the voltage and current ripples are small. According to (52) and (53), the current through  $D_2$  during the time  $[nT_s \sim (n+D)T_s]$  can be considered as a constant value, and the current value of  $D_2$  can be simplified in (57).

$$\begin{aligned}
I_{S1(rms)} = I_{S2(rms)} &= \sqrt{\frac{1}{T_s} \int_0^{T_s} i_s^2 dt} = \sqrt{\frac{1}{T_s} \int_0^{T_s} (i_L + i_{D2})^2 dt} \\
&= \sqrt{D \left[ \frac{4I_0^2}{(1-D)^2} + \frac{1}{12} \Delta i_L^2 + \frac{1}{3} \Delta i_L i_{D2(T_s)} - \frac{1}{3} \Delta i_L \frac{I_0}{D} + 2 \frac{2I_0 I_0}{1-D} + \frac{1}{3} i_{D2(T_s)}^2 - \frac{2}{3} i_{D2(T_s)} \frac{I_0}{D} + \frac{4}{3} \frac{I_0^2}{D^2} \right]} \\
&= \sqrt{D \left[ 4I_0^2 \frac{D^2 + D + 1}{3D^2(1-D)^2} + \frac{1}{12} \frac{D^2(1-D)^2 V_0^2}{(3+D)^2 L^2 f_s^2} + \frac{1}{3} \frac{D(1-D)V_0}{(3+D)Lf_s} i_{D2(T_s)} - \frac{1}{3} \frac{D(1-D)V_0}{(3+D)Lf_s} \frac{I_0}{D} + \frac{1}{3} i_{D2(T_s)}^2 - \frac{2}{3} i_{D2(T_s)} \frac{I_0}{D} \right]}
\end{aligned} \quad (56)$$

$$i_{peak-D2} = i_{D2(nT_s \sim (n+D)T_s)} = \frac{I_0}{D} \quad (57)$$

Therefore, from above, the rms current of switches is given by

$$\begin{aligned}
I_{S1(rms)} = I_{S2(rms)} &= \sqrt{\frac{1}{T_s} \int_0^{T_s} i_s^2 dt} = \sqrt{\frac{1}{T_s} \int_0^{DT_s} (i_L + i_{D2})^2 dt} \\
&\approx \sqrt{\frac{1}{T_s} \int_0^{DT_s} \left( I_L + \frac{I_0}{D} \right)^2 dt} = I_0 \sqrt{D} \left( \frac{2}{1-D} + \frac{1}{D} \right)
\end{aligned} \quad (58)$$

## APPENDIX B. CALCULATION OF THE RESONANT FREQUENCY OF THE CONVERTER [21]

The experimental resonance frequency in ref. [21] is lower than the resonance frequency in this paper. We have analyzed the resonance frequency values mathematically and the mathematical procedures are as follows.

### (1) The resonance frequency of converter [21] in this paper

In this paper, the inductors and switches junction capacitors values are shown below.

$$\begin{cases} L_1 = L_2 = 240 \mu\text{H} \\ C_{p1} = C_{p2} = 476 \text{pF} \end{cases}$$

According to the formula of resonance frequency, the calculated resonance frequency of converter [21] which is shown in this paper is given by

$$f_{calculated} = \frac{1}{2\pi} \sqrt{\frac{1}{LC}} = \frac{1}{2\pi} \sqrt{\frac{1}{C_{p1} + C_{p2}} \cdot \frac{L_1 + L_2}{L_1 L_2}} = 4.71 \times 10^5 \text{ Hz} \quad (59)$$

According to Fig. 15(a), as can be seen, the resonant period is 2.1  $\mu\text{s}$ , so the resonance frequency is given by

$$f_{experimental} = \frac{1}{T} = \frac{1}{2.1 \times 10^{-6}} = 4.71 \times 10^5 \text{ Hz} \quad (60)$$

Therefore, the mathematical calculated value of resonant frequency is equal to the experimental resonant frequency value.

### (2) The resonance frequency of converter [21] in ref. [21]

In ref. [21], the voltage waveforms of switches  $S_1$  and  $S_2$  are shown in Fig. r6, the resonant period is about 3  $\mu\text{s}$ . Therefore, the experimental resonant frequency is given by

$$f_{experimental} = \frac{1}{T} = \frac{1}{3 \times 10^{-6}} = 3.33 \times 10^5 \text{ Hz} \quad (61)$$

So, compare with (60), the shown resonance frequency in ref. [21] is lower than the resonance frequency in this paper. In ref. [21], the experiment parameters of the inductors and junction capacitors values are

$$\begin{cases} L_1 = L_2 = 223 \mu\text{H} \\ C_{p1} = C_{p2} = 390 \text{pF} \end{cases}$$

The calculated resonance frequency of converter [21] which is shown in ref. [21] is given by

$$f_{calculated} = \frac{1}{2\pi} \sqrt{\frac{1}{LC}} = \frac{1}{2\pi} \sqrt{\frac{1}{C_{p1} + C_{p2}} \cdot \frac{L_1 + L_2}{L_1 L_2}} = 5.40 \times 10^5 \text{ Hz} \quad (62)$$

From (61) and (62), it can be deduced that the calculated resonance frequency is higher than the experimental resonant frequency. This is because the RC snubber circuit may be added in converter [21] in ref. [21], the actual equivalent capacitor is larger than junction capacitor, therefore, the calculated resonance frequency is higher than the experimental resonant frequency in ref. [21]

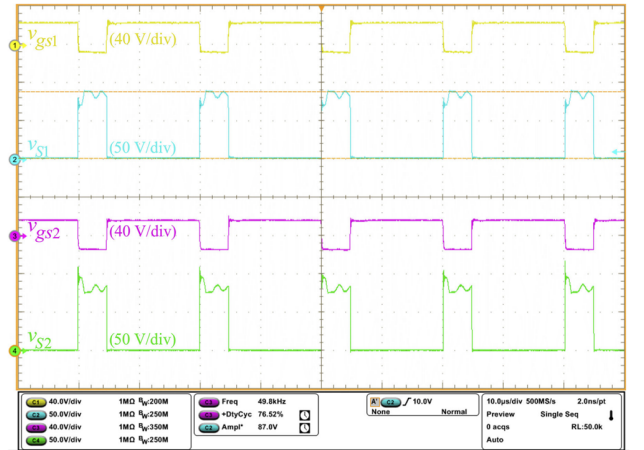


Fig. 31. Gate-source signals ( $V_{gs1}$ ,  $V_{gs2}$ ) and Drain-source voltages ( $V_{s1}$  and  $V_{s2}$ ) of the converter in [21] in ref. [21].

## APPENDIX C. THEORETICAL CALCULATION METHOD OF THE LOSS DISTRIBUTION

### ① Losses distribution analysis of the converter in ref. [21]

1) The losses of the switches can be divided into switching loss and conduction loss, and they can be calculated by:

$$P_s = 2[I_{s(rms)}^2 R_{on} + \frac{1}{2} f_s V_s I_s (t_{on} + t_{off})] \quad (63)$$

where  $I_s(rms)$  is the RMS current of the switches and  $R_{on}$  is on-state resistor of the switches;  $f_s$  is switching frequency;  $t_{on}$  and  $t_{off}$  are Turn-on time and Turn-off time, respectively;  $V_s$  is voltage stress of the switches and  $I_s$  is the current of the switches during switching time.

2) The diodes loss distribution can be divided into conduction loss and reverse recovery loss. The diodes losses are given by



$$P_D = 2 \left( I_{D_1(\text{avg})} v_{D_1f} + Q_{rD_1} V_{rD_1} f_s \right) + \left( I_{D_0(\text{avg})} v_{D_0f} + Q_{rD_0} V_{rD_0} f_s \right) \quad (64)$$

where  $I_D$  is the average current of the diodes and  $v_{Df}$  is the diode forward voltage,  $Q_r$  is the diode reverse recovery charge,  $V_r$  is the diode reverse turn-off voltage, and  $f_s$  is the switching frequency.

3) The inductors losses are given by

$$P_L = 2[r_L I_{L(\text{rms})}^2 + (aB_{pk}^b f_s^c) A_e l_e] \quad (65)$$

where  $I_{L(\text{rms})}$  is the RMS current of the inductor;  $r_L$  is copper resistance;  $B_{pk}$  is the AC magnetic flux density of the magnetic core; a, b, c are constants determined from the curve fitting of the core;  $l_e$  is the core medium path length and  $A_e$  is the transversal core area.

4) The capacitors losses can be given by

$$P_C = 2I_{C_1(\text{rms})}^2 \cdot \text{ESR} + I_{C_0(\text{rms})}^2 \cdot \text{ESR} \quad (66)$$

where  $I_{C(\text{rms})}$  is the RMS current of the capacitor and ESR is the resistor of capacitors.

So, the total losses  $P_{\text{loss}}$  can be written as

$$P_{\text{loss}} = P_S + P_D + P_L + P_C \quad (67)$$

## ② Losses distribution analysis of the proposed converter

Similarly, the loss calculation process of the proposed converter is shown below.

1) The losses of the two switches are given by

$$P_S = 2[I_{S(\text{rms})}^2 R_{DS(\text{on})} + \frac{1}{2} f_s V_S I_S (t_{\text{on}} + t_{\text{off}})] \quad (68)$$

2) The diodes losses are given by

$$P_D = \left( I_{D_1(\text{avg})} v_{D_1f} + Q_{rD_1} V_{rD_1} f_s \right) + \left( I_{D_2(\text{avg})} v_{D_2f} + Q_{rD_2} V_{rD_2} f_s \right) + 2I_{D_{01}(\text{avg})} v_{D_{01}f} \quad (69)$$

3) The inductors losses are given by

$$P_L = 2[r_L I_{L(\text{rms})}^2 + (aB_{pk}^b f_s^c) A_e l_e] \quad (70)$$

4) The capacitors losses can be given by

$$P_C = 2I_{C_1(\text{rms})}^2 \cdot \text{ESR} + 2I_{C_0(\text{rms})}^2 \cdot \text{ESR} \quad (71)$$

The total losses  $P_{\text{loss}}$  can be written as

$$P_{\text{loss}} = P_S + P_D + P_L + P_C \quad (72)$$

The efficiency ( $\eta$ ) can be determined as follows:

$$\eta = \frac{P_0}{P_0 + P_{\text{loss}}} \quad (73)$$

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