

# Interaction between eye movements and adhesion of extraocular muscles

Hongmei Guo<sup>a,b,1\*</sup>, Yunfei Lan<sup>a,1</sup>, Zhipeng Gao<sup>a</sup>, Chenxi Zhang<sup>a</sup>, Liping Zhang<sup>a</sup>, Xiaona Li<sup>a</sup>,  
Jianying Lin<sup>a</sup>, Ahmed Elsheikh<sup>c</sup>, Weiyi Chen<sup>a\*</sup>

<sup>a</sup> College of Biomedical Engineering, Taiyuan University of Technology, Taiyuan 030024, China;

<sup>b</sup> Third Hospital of Shanxi Medical University (Shanxi Bethune Hospital, Shanxi Academy of Medical Sciences, Tongji Shanxi Hospital), Taiyuan 030032, China.

<sup>c</sup> School of Engineering, University of Liverpool, Liverpool, United Kingdom

\* Correspondence: [guohongmei@tyut.edu.cn](mailto:guohongmei@tyut.edu.cn); [chenweiyi@tyut.edu.cn](mailto:chenweiyi@tyut.edu.cn)

<sup>1</sup> These authors contributed equally to this work.

## Abstract

The adhesion between the extraocular muscles and the sclera affects eye movement. The contact and pull-off tests and finite element simulations were used to study the extraocular muscle-sclera adhesion and its variation with eye movement in this research. The effect of the adhesion on the eye movements was also determined using equilibrium equations of eye motion. The contact and pull-off tests were performed using quasi-static and non-quasi-static unloading velocities. Finite element models were developed to simulate these tests in cases with high unloading velocity which could not be achieved experimentally. These velocities range from the eye's fixation to saccade movement. The tests confirmed that the pull-off force is related to the unloading velocity. As the unloading velocity increases, the pull-off force increases, with an insignificant increase at the high ocular saccade velocities. The adhesion moment between the extraocular muscles and the sclera exhibited the same trend, increasing with higher eye movement velocities and higher separation angles between the two interfaces. The adhesion moment ratio to the total moment was calculated by the traditional model and the active pulley model of eye movements to assess the effect of adhesion behavior on eye movements. At the high ocular

27 saccade velocities (about 461 deg/s), the adhesion moment was found to be 0.53% and 0.50% of  
28 the total moment based on the traditional and active pulley models, respectively. The results  
29 suggest that the adhesion behavior between the extraocular muscles and the sclera has a negligible  
30 effect on eye movements. At the same time, this adhesion behavior can be ignored in eye  
31 modeling, which simplifies the model reasonably well.

32 **Keywords:** Adhesion behavior, Extraocular muscle, Eye Movement, Viscoelasticity, Finite  
33 element.

# 1. Introduction

During the eye movement, the extraocular muscle (EOM) regulates the rotation of the eyeball, leading to an inevitable contact and separation process between the surface of the sclera and the EOM, which results in adhesive interactions. Previous studies have investigated the material properties of EOM along the length direction (including strength, tangent modulus, and toughness), but have neglected the properties in the thickness direction of the EOMs and the adhesion properties between the sclera and the EOMs [1-5].

The adhesion behavior of biological tissues is commonly assessed using contact and pull-off tests, where a rigid indenter is brought into contact pressed into the test material, and subsequently separated [6-8]. Dai et al. investigated the adhesion behavior of facial skin using contact and pull-off tests, revealing variations in adhesion behavior under different moisture conditions [9]. Similarly, Zhu et al. conducted contact and pull-off tests on silicone hydrogel contact lenses while on the cornea, demonstrating that different lens materials affected the lens-cornea adhesion differently [10]. In a more recent study, contact and pull-off tests were employed to determine the adhesion behavior between the retina and the vitreous, which was identified as a significant factor contributing to rhegmatogenous retinal detachment [11].

The theoretical foundation of contact and pull-off tests can be traced back to the early research conducted by Kendall and colleagues, specifically the Johnson-Kendall-Roberts (JKR) model [12-14]. The JKR model primarily describes the contact mechanics between two elastic solids or an elastic solid and a substrate of another material, where under the influence of Hertzian contact pressure, adhesive forces are generated and result in a necking-like deformation in the contact region, thereby increasing the contact area. According to the JKR model, contact stresses

56 gradually approach infinity at the contact edge, and the resulting pull-off force during separation is  
57 given by  $P_{pull-off} = -1.5\pi R\Delta\gamma$ , where  $R$  denotes the radius of the indenter while  $\Delta\gamma$   
58 represents the work of adhesion. The elastic behavior of adhesive contacts can also be  
59 characterized by the Tabor parameter  $\mu$  [15], which can be expressed as

$$60 \quad \mu = \left[ \frac{R\Delta\gamma^2}{E^{*2}z_0^3} \right]^{1/3}$$

61 where  $E^* = \left[ (1-\nu_1^2)/E_1 + (1-\nu_2^2)/E_2 \right]^{-1}$  is the equivalent elastic modulus ( $E_1$ ,  $\nu_1$  and  $E_2$ ,  $\nu_2$   
62 denote the elastic modulus and Poisson's ratio of the two contacting elastic spheres, respectively)  
63 and  $z_0$  represents the equilibrium distance. As reported in earlier research, the JKR model is valid  
64 for cases in which  $\mu > 5$ , a condition that applies to this study [16].

65 Soft materials can be broadly categorized as either elastic or viscoelastic. The JKR theory is  
66 primarily applicable to elastic soft materials. However, the analysis becomes more complex when  
67 dealing with viscoelastic materials due to the consideration of velocity dependence.

68 In cases of viscoelastic materials, even when unloading velocity approaches zero, the JKR  
69 theory can still be utilized to evaluate their behavior. This theory gains importance when studying  
70 the adhesion between two viscoelastic materials during separation. Under specific conditions, an  
71 increase in velocity-induced adhesion is observed due to the velocity-dependent properties  
72 inherent to viscoelasticity, which are absent under quasi-static conditions [17-19]. This  
73 phenomenon has been well-documented across various viscoelastic materials, highlighting the  
74 influence of strain rate [20, 21].

75 Notably, Muller's work highlights that when viscoelastic spheres come into contact with a  
76 plane, pull-off forces can significantly exceed the thermodynamic predictions from the JKR theory,

77 and this discrepancy exists even at minimal separation velocities [22]. Steady fixation velocities  
78 are less than 2 deg/s (26 mm/min), smooth pursuit tracks moving targets at velocities below 70  
79 deg/s (911 mm/min), and the peak saccade velocity is up to 600 deg/s (7806 mm/min) [23, 24].  
80 Since the velocities of some eye movements may be outside the quasi-static velocity range (higher  
81 than 30 mm/min), these movements may surpass the applicability limits of the traditional JKR  
82 theory [24-26]. Therefore, it is necessary to adopt the JKR-like viscoelastic model in this study to  
83 accommodate the velocity dependence due to the tissue's viscoelastic behavior.

84 In this context, Afferrante and Violano conducted a significant study using a JKR-like test  
85 between an optical spherical glass lens and a viscoelastic rubber substrate [27]. They developed an  
86 analytical solution based on the JKR theory, offering insights into the detachment of a rigid sphere  
87 from a viscoelastic substrate [28]. This solution provides a nuanced understanding of viscoelastic  
88 adhesion behavior by presenting applied load and contact penetration as functions of the contact  
89 radius, thus enabling a more accurate representation of velocity dependent viscoelastic detachment.

90 In addition to theoretical analysis, the finite element method serves as a valuable tool for  
91 simulating interfacial adhesion. For instance, He conducted finite element simulations to  
92 investigate the detachment of a spherical indenter from an elastic film [29]. This study identified  
93 the key factors governing interfacial instability modes and proposed methods to hinder such  
94 instabilities. Jiang developed a finite element model to explore the contact between a  
95 polydimethylsiloxane (PDMS) stamp substrate and a spherical viscoelastic adhesive indenter [30].  
96 The study showed that the rate dependence became more pronounced at higher unloading  
97 velocities. Afferrante and Violano investigated classical Hertzian contact adhesion using a finite  
98 element approach, incorporating adhesive interactions described by the Lennard-Jones potential

99 and viscoelastic behavior described by a standard linear solid model [31, 32]. Their study revealed  
100 a significant velocity dependence of the adhesion force.

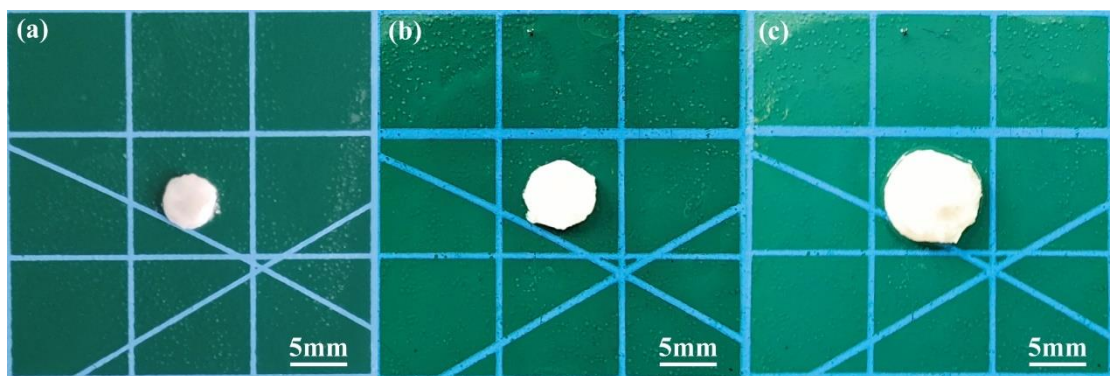
101 The effect of the adhesion behavior of the EOM to the sclera on eye movements can be  
102 assessed by modeling eye movements. In the study of eye movement models, the perception of  
103 eye movement was changed by the discovery of the pulley, a connective tissue of the EOM  
104 bonded to the orbital wall, the presence of which altered the path of force on the EOM. Currently,  
105 two common models are used in eye movement modeling: the traditional (non-pulley) model and  
106 the active pulley model. In the traditional model, the EOMs are constituted by several key points:  
107 the insertion point, the tangent point, and the origin point (the end where the EOM is attached to  
108 the bony orbit) [33]. Demer et al. proposed the active pulley hypothesis, which views the location  
109 of the pulley as a functional origin for eye movements, with the functional origin moving with the  
110 eye during eye movements [34]. Many reviews have described active pulley behavior and  
111 emphasized that pulleys are the functional origin of EOM [35-38]. In this study, the EOM  
112 behavior in the thickness direction was determined in compressive stress-relaxation tests. The  
113 study also quantified the adhesion behavior between the EOM and the sclera using experimental  
114 and finite element analysis methods. The effect of this adhesion on eye movement was then  
115 quantified by calculating the ratio between the adhesion moment, and the total moment using the  
116 traditional model and the active pulley model.

## 117 **2. Materials & methods**

### 118 **2.1 Specimens preparation**

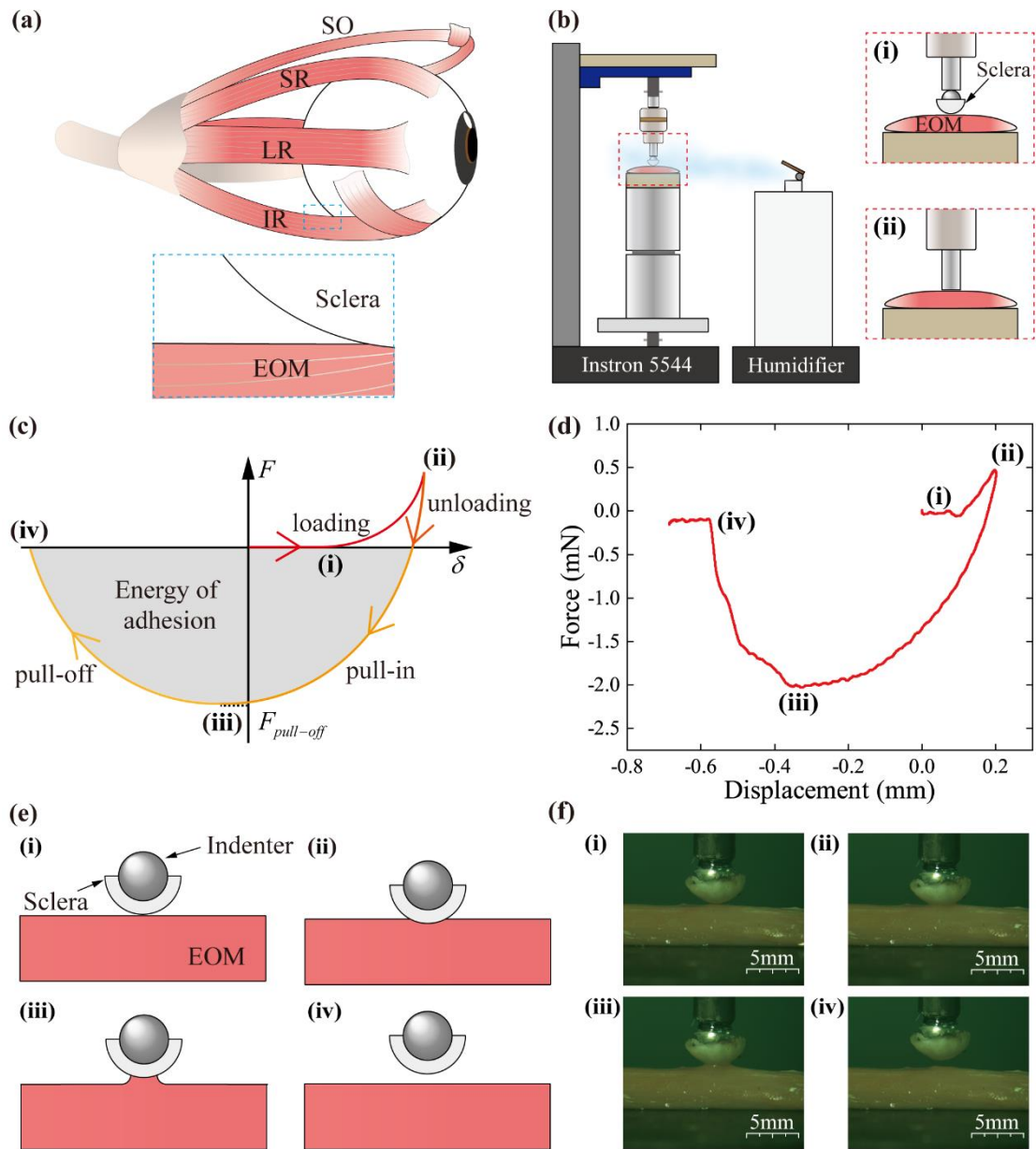
119 A total of 180 porcine eyes, of animals aged between 6 and 8 months, were procured from a

120 local slaughterhouse and promptly transported to the Laboratory of Soft Tissue Biomechanics,  
121 Taiyuan University of Technology, within 24 hours post-mortem. The eyes were placed in an ice  
122 pack during transport, preventing dehydration and tissue decay. At room temperature, the EOMs  
123 were dissected from each eye using scissors and forceps, and subsequently cut into strips with  
124 dimensions of  $(24.3 \pm 3.4 \text{ mm}) \times (10.2 \pm 2.2 \text{ mm}) \times (2.5 \pm 0.5 \text{ mm})$ . In making an EOM specimen,  
125 the fat was carefully removed and the membrane on the surface of the EOM was preserved. We  
126 chose the portion of the sclera posterior to the EOM insertion point for scleral specimen  
127 preparation, which was positioned between the anterior and equatorial portions of the sclera. The  
128 sclera was cut into a specimen twice the radius of the indenter with surgical scissors. The circular  
129 sclera specimens are shown in Fig. 1. The indenter was dipped in glue and bonded to the sclera,  
130 and the excess of the scleral specimen was cut off. Before conducting the contact and pull-off tests,  
131 the thickness at the center of the sclera specimens was measured three times using a laser  
132 displacement sensor (LK-H050, Keyence Corporation). The thickness of the sclera was recorded  
133 as  $0.55 \pm 0.23 \text{ mm}$ .



135 **Fig. 1.** The shape and size of the porcine sclera tissue specimens. Scale bars are labeled in the  
136 lower right corner of the figure. Scleral specimens bonded at indenter radii of (a) 1 mm, (b) 1.5  
137 mm, and (c) 2 mm are shown.

## 2.2 Contact and pull-off tests



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**Fig. 2.** The adhesion behavior between the sclera and the EOMs. **(a)** The EOMs responsible for controlling eye movements include the lateral rectus (LR), medial rectus (MR), superior rectus (SR), and inferior rectus (IR) muscles, as well as the superior oblique (SO) and inferior oblique (IO) muscles. The inset provides a visual representation of the adhesive interaction hypothesis between the sclera and EOMs during eye movements. **(b)** Schematic of Instron 5544 testing machine. The illustration is a partial enlargement of the specimen. **(i)** Contact between the scleral



146 tissue-wrapped indenter and the EOM in the contact and pull-off tests. **(ii)** Contact between the  
147 flat-ended indenter and the EOM in the compressive stress-relaxation tests. **(c)** A diagram outlines  
148 the contact and pull-off test procedure, including **(i)** the loading phase, **(ii)** maximum compression  
149 force, **(iii)** pull-off force, and **(iv)** separation. **(d)** The adhesion force-displacement diagram of a  
150 typical specimen, with an unloading velocity of 6 mm/min. **(e)** A schematic diagram illustrates the  
151 different phases of the contact and pull-off test. **(f)** Experimentally captured images depict the  
152 various phases of the contact and pull-off test. The scale bar is labeled in the lower right corner.

153 The EOMs responsible for controlling eye movements include the lateral rectus (LR), medial  
154 rectus (MR), superior rectus (SR), and inferior rectus (IR) muscles, as well as the superior oblique  
155 (SO) and inferior oblique (IO) muscles. Physiologically, the EOMs wrap around the sclera, with  
156 adhesive interaction between the two tissues due to their viscoelastic nature (Fig. 2.a). To  
157 investigate the adhesion behavior between the sclera and the EOMs at room temperature, contact  
158 and pull-off tests were conducted.

159 The contact and pull-off tests were performed using an Instron 5544 (Instron, Boston, USA)  
160 testing machine, equipped with a load cell with 5 N capacity and 0.001 N accuracy (Fig. 2.b). In  
161 preparation, the sclera specimens were glued onto spherical indenters with radii of 1 mm, 1.5 mm,  
162 and 2 mm. The test process then commenced as follows:

163 **(i)** The scleral tissue-wrapped indenter moved towards the EOM tissue at a velocity of 1  
164 mm/min until contact was established.

165 **(ii)** The scleral tissue-wrapped indenter was pressed into the EOM to achieve a maximum  
166 indentation of 0.1 mm. The force corresponding to this displacement is referred to as the preload  
167 force. Subsequently, the scleral tissue-wrapped indenter was pulled away from the EOM with

168 unloading velocities that included quasi-static velocities of 0.5, 1, 6, 18, and 30 mm/min; and non-  
 169 quasi-static velocities of 42 and 300 mm/min. The number of EOM specimens used in the above  
 170 experiment is shown in [Table 1](#).

171 **Table 1.** Number of EOM specimens with different unloading velocities for contact and pull-off  
 172 tests.

<b>Indenter radius</b>	<b>0.5 mm/min</b>	<b>1 mm/min</b>	<b>6 mm/min</b>	<b>18 mm/min</b>	<b>30 mm/min</b>	<b>42 mm/min</b>	<b>300 mm/min</b>
1 mm	31	28	30	29	27	31	27
1.5 mm	35	25	28	29	30	32	28
2 mm	26	30	26	27	29	28	29

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 174 (iii) As the scleral tissue-wrapped indenter detached from the EOM, peeling occurred at or  
 175 near the maximum adhesive force (Pull-off force  $F_{pull-off}$ ).

176 (iv) Finally, the scleral tissue-wrapped indenter completely separated from the EOM, and the  
 177 force measured by the sensor returned to zero.

178 The entire experimental process was carefully observed and documented using a charge-  
 179 coupled device (CCD) for image acquisition. [Fig. 2.c](#) shows a schematic diagram of the contact  
 180 and pull-off tests including the four steps described above.

181 Data collection started when the gap between the sclera and the EOM was 0.1 mm, and the  
 182 indenter was then displaced towards the EOM specimen for 0.2 mm leading to a maximum  
 183 indentation of 0.1 mm, before reversing the loading direction. [Fig. 2.d](#) shows the adhesion force-  
 184 displacement diagram of a typical specimen, with an unloading velocity of 6 mm/min.

185 Furthermore, to evaluate the effect of air exposure duration on the EOM-sclera adhesion  
 186 behavior, EOM strips were acquired and divided into two groups – with 30 specimens each – one  
 187 with 15 min exposure, and one with 30 min exposure – both groups were subjected to an  
 188 unloading velocity of 0.5 mm/min. Exposure time refers to the time from the dissection to the end  
 189 of the test, corresponding to the entire procedure of strabismus surgery. The number of EOM  
 190 specimens used in the above experiments is shown in [Table 2](#).

191 **Table 2.** Number of EOM specimens with different exposure times for contact and pull-off tests.

Indenter radius	Exposure time 15min	Exposure time 30min
1 mm	31	25
1.5 mm	35	28
2 mm	26	23

192  
 193 In all tests, two parameters were of particular interest: First, the  $F_{pull-off}$  at stage (iii), which  
 194 prevented the EOM-sclera separation; Second, the work of adhesion,  $\Delta\gamma$ , defined as the work  
 195 required per unit area to separate the two tissues from initial contact to infinite separation. This  
 196 parameter is crucial in characterizing the strength of adhesion between the two tissues. To  
 197 determine  $\Delta\gamma$ , the adhesion energy,  $U$ , was obtained first by integrating the attraction region of  
 198 the behavior curve (gray area in [Fig. 2.c](#)). Subsequently,  $U$  was divided by the contact area to  
 199 determine  $\Delta\gamma$ . [Fig. 2.e](#) presents a schematic diagram illustrating this process, while [Fig. 2.f](#)  
 200 shows images of the contact and pull-off test.

## 201 **2.3 Compressive stress-relaxation test**

202 In this study, uniaxial compressive stress-relaxation tests were conducted on porcine EOMs,  
203 where the EOMs were subjected to compressive loads along the thickness direction. The EOM  
204 specimen did not slide on the test bench during the test. A total of 14 EOM specimens were tested  
205 using an Instron 5544 tester. A flat-ended indenter with a diameter of 5 mm was used at 1 mm/min  
206 to compress the specimens with a compressive strain of 10%. The schematic diagram of a flat-  
207 ended indenter compressed into the EOM is shown in [Fig. 2.b](#). After the ramp loading phase, the  
208 compression was held constant for 500 seconds to allow the specimens to stress-relaxation. Each  
209 specimen was tested only once. Considering the elevated levels of strain, such as that applied in  
210 our tests, can result in permanent tissue deformation, no preload was applied. Additionally, a  
211 humidifier was used throughout to make sure that the tissue did not dehydrate.

## 212 **2.4 Theoretical Analysis**

### 213 **2.4.1 JKR-like viscoelastic model**

214 In the seminal work by Johnson, Kendall, and Roberts, an analytical closed-form solution  
215 was developed to characterize adhesive contact between a rigid sphere and an elastic, soft half-  
216 space [\[12\]](#). The JKR theory provides straightforward expressions that establish relationships  
217 between the applied load  $F$ , indentation displacement  $\delta$ , and contact radius  $a$ . However, in the  
218 context of viscoelastic materials, an equivalent solution does not exist, necessitating the utilization  
219 of numerical or semi-analytical methods to address the problem [\[28\]](#).

220 When the approach and retraction phases are performed under quasi-static conditions, the  
221 viscoelastic substrate behaves as an elastic medium. For an elastic substrate,  $F$  and  $\delta$  can be

222 determined in terms of  $a$  by JKR theory

$$223 \quad F = \frac{4 E^* a^3}{3 R} - \sqrt{8\pi E^* a^3 \Delta\gamma} \quad (1)$$

$$224 \quad \delta = \frac{a^2}{R} - \sqrt{\frac{2\pi a \Delta\gamma}{E^*}} \quad (2)$$

225 where  $E^*$  is the equivalent elastic modulus,  $\Delta\gamma$  is the work of adhesion, which depends on the  
226 adhesion properties of the contact interface, and  $R$  is the radius of the indenter.

227 In the presence of a viscoelastic substrate, the process of detachment involves the occurrence  
228 of viscous dissipation. Gent and Schultz introduced the concept of an equivalent work of adhesion  
229  $\Delta\gamma_{eff}$  to account for this dissipation [39]. An empirical relationship known as the Gent-Schultz  
230 law is often used to describe crack propagation, which is similar to the separation process between  
231 the sclera and the EOM. The  $\Delta\gamma_{eff}$  was found to be dependent on the velocity of loading and is  
232 typically expressed as a function of the contact line velocity  $v_c = -da/dt$  [40, 41]. This  
233 dissipation function is characteristic of viscoelastic materials and is not influenced by the  
234 geometry of the contact. These observations can be explained by the following empirical equation.

$$235 \quad \Delta\gamma_{eff} = \Delta\gamma \left[ 1 + \left( \frac{v_c}{v^*} \right)^n \right] \quad (3)$$

236 The crucial point to note is that the effective adhesion energy relies on the crack front  
237 velocity, denoted as the characteristic velocity  $v^*$  and the power-law exponent  $n$ , which can be  
238 determined through experimental measurements [19, 22, 39]. It is important to highlight that the  
239 exponent  $n$  is not a universal value but varies depending on the viscoelastic modulus [22, 42].  
240 Generally, values for  $n$  typically range from 0.1 to 0.8 [43]. However, some arguments have been  
241 put forward suggesting that it is linked to the distribution of characteristic relaxation times within

242 the viscoelastic material [44].

243 To accurately characterize the detachment behavior, it is necessary to determine the precise  
244 parameters of the contact line velocity  $v_c$  and the contact radius  $a$ . Considering that the pulling  
245 velocity is denoted as  $V = -d\delta/dt$ , the derivative  $da/d\delta$  can be numerically calculated by  
246 solving a differential equation given by Muller [22], while Violano et al. estimated  $da/d\delta$  from  
247 the JKR solution [45].

$$248 \quad v_c = V \left( \frac{2a}{R} - \sqrt{\frac{\pi\Delta\gamma}{2aE^*}} \right)^{-1} \quad (4)$$

249 Due to the difficulty of experimental measurements, Eq. (4) was used to calculate the  
250 approximate value of  $v_c$ . The  $\Delta\gamma_{eff}$  can be initially estimated by substituting  $v_c$  into Eq. (3).  
251 Inspired by a similar approach proposed by Barthel and Roux, for the effects caused by the  
252 viscoelastic energy of the EOM at different velocities in this study, the  $F$  and  $\delta$  in the  
253 viscoelastic substrate can be determined while the  $\Delta\gamma_{eff}$  was used to replace the  $\Delta\gamma$  in the Eqs. (1)  
254 and (2) [43]. For a rigid indenter wrapped with scleral tissue, the radius is  $R = r + h$ , where  $r$  is  
255 the radius of the indenter and  $h$  is the thickness of the sclera. The equivalent elastic modulus of  
256 the indenter wrapped with scleral tissue and the EOM substrate becomes  
257  $E^* = \left[ (1 - \nu_{sclera}^2) / E_{sclera} + (1 - \nu_{EOM}^2) / E_{EOM} \right]^{-1}$ . Therefore,

$$258 \quad F = \frac{4}{3} \frac{E^* a^3}{R} - \sqrt{8\pi E^* a^3 \Delta\gamma_{eff}} \quad (5)$$

$$259 \quad \delta = \frac{a^2}{R} - \sqrt{\frac{2\pi a \Delta\gamma_{eff}}{E^*}} \quad (6)$$

260 when  $v_c$  tends to 0, the above equation will change to the form applicable to quasi-static, i.e., Eqs.  
261 (1) and (2).

262 To make the results more generalizable, all dimensional parameters were converted to  
 263 dimensionless parameters. The dimensionless forms were proposed by Lin and Violano, that is,  
 264  $\hat{F} = F / (3\pi R \Delta \gamma_{eff})$ ,  $\hat{\delta} = \delta \left[ 3\pi^2 \Delta \gamma_{eff}^2 R / (2E^{*2}) \right]^{-1/3}$ ,  $\hat{a} = a / R$ ,  $\Delta \hat{\gamma}_{eff} = \Delta \gamma_{eff} / (E^* R)$ ,  
 265  $\hat{F}_{pull-off} = F_{pull-off} / (3\pi R \Delta \gamma_{eff})$ ,  $\hat{v}_c = v_c / v^*$ , and thus  $\hat{V} = V / v^*$  [28, 46].

266 Therefore, the above relationships can be rewritten as

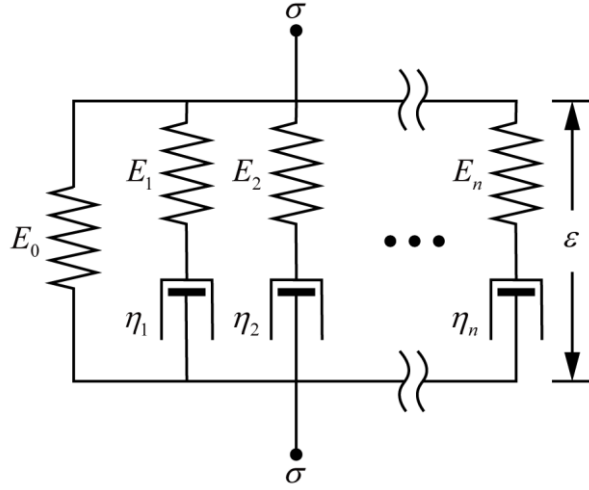
$$267 \quad \hat{F} = \frac{4}{3} \hat{a}^3 - \sqrt{8\pi \hat{a}^3 \Delta \hat{\gamma}_{eff}} \quad (7)$$

$$268 \quad \hat{\delta} = \hat{a}^2 - \sqrt{2\pi \hat{a} \Delta \hat{\gamma}_{eff}} \quad (8)$$

269 In Eq. (7), the first term is the dimensionless Hertzian contact pressure, while the second is  
 270 the dimensionless Kendall interface adhesion force.

## 271 **2.4.2 Wiechert Viscoelastic Model**

272 Most biological tissues, including the EOM, exhibit viscoelastic properties. To characterize  
 273 the viscoelastic behavior of the EOM, the Wiechert model was selected [2]. This model employs a  
 274 superposition of linear combinations of multiple spring-damper units (Fig. 3), allowing for the  
 275 separation of transient elastic behavior from long-term viscoelastic behavior. This approach  
 276 enables an accurate description of the stress-relaxation behavior of the material and facilitates the  
 277 use of finite element analysis.



278

279 **Fig. 3.** Schematic diagram of the Wiechert viscoelastic model.

280 When utilizing the Abaqus software, it becomes essential to employ the Prony series  
 281 formulation, which involves considering multiple characteristic times  $\tau_i$  ( $i = 1, 2, \dots, N$ ). In this  
 282 formulation, the time-dependent relaxation modulus  $E(t)$  is expressed in terms of the Prony  
 283 series [47]:

$$284 \quad E(t) = E_\infty \frac{1 - \sum_{i=1}^n g_i (1 - e^{-t/\tau_i})}{1 - \sum_{i=1}^n g_i} \quad (9)$$

285 The relaxation modulus of the EOM in the time-dependent relaxation modulus  $E(t)$ ,  
 286 normalized by the initial modulus  $E_0 = E_\infty / (1 - \sum_{i=1}^n g_i)$ , can be expressed using the Prony  
 287 series  $E(t)/E_0 = 1 - \sum_{i=1}^n g_i (1 - e^{-t/\tau_i})$ .

288 For the Abaqus software, when a viscoelastic model is defined in the time domain, the  
 289 following parameters need to be provided as input:  $g_i$  (normalized Prony coefficients for shear  
 290 behavior),  $k_i$  (normalized Prony coefficients for volumetric behavior), and  $\tau_i$  (relaxation times of  
 291 the Prony series). Abaqus assumes that  $g_i$  and  $k_i$  are independent of each other. In this particular  
 292 study, the volume changes in the material are not taken into account, so the  $k_i$  values will be



293 omitted [48]. The specific values for  $g_i$  and  $\tau_i$  are presented in Table 3.

294 **Table 3.** The relevant parameters of the finite element model.

Model	Material model	Density	Material parameters
Indenter	Elastic	7.85 g/cm <sup>3</sup>	$E = 200$ GPa, $\nu = 0.3$
Sclera	Elastic	1.076 g/cm <sup>3</sup> [49]	$E = 11.2$ kPa, $\nu = 0.47$ [This work]
EOM	Elastic Prony	1.060 g/cm <sup>3</sup> [50]	$E = 4.34$ kPa, $\nu = 0.47$
			$g_1 = 0.25$ , $\tau_1 = 1.72$ s
			$g_2 = 0.23$ , $\tau_2 = 23.94$ s
			$g_3 = 0.27$ , $\tau_3 = 276.17$ s [This work]

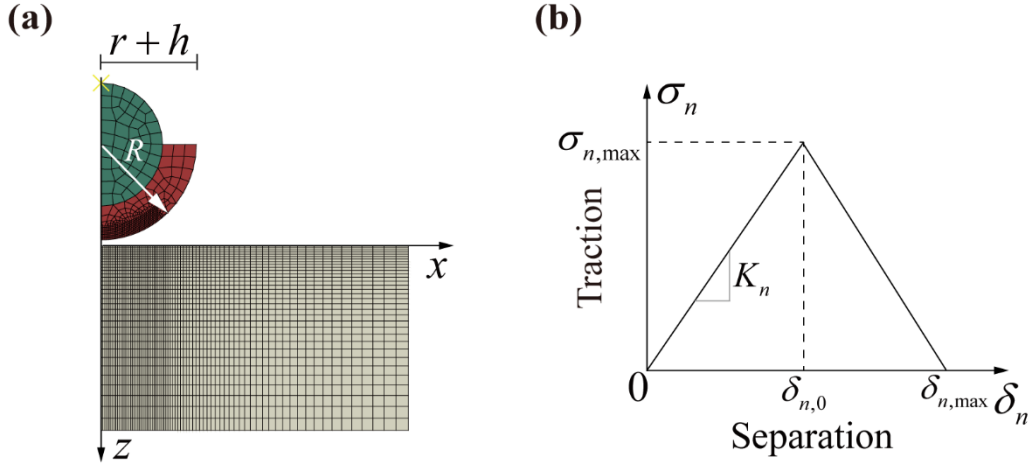
295

## 296 2.5 Finite element model

297 Based on the experiments in the previous sections, a finite element model was constructed  
 298 using the commercial Abaqus software, as illustrated in Fig. 4.a. The radius of the spherical rigid  
 299 indenter is  $r$  and the thickness of the sclera is  $h$ . The total radius of the scleral tissue-wrapped  
 300 indenter is  $R = r + h$ . The indenter was set as a rigid body according to the experiment, and then  
 301 the "Tie" was used to bind the indenter to the scleral tissue. The scleral tissue was characterized by  
 302 a linear elastic model, while the EOM was assumed to follow both a linear elastic constitutive  
 303 model and a viscoelastic constitutive model based on the Prony series. Specific parameters are  
 304 shown in Table 3. The model was created using axisymmetric four-node elements (CAX4RH).  
 305 The indenter radius was set to 1 mm, and the thickness of the sclera model was assumed to equal  
 306 the average experimental value of 0.55 mm. In the EOM model, the dimension along the x-axis is  
 307 half the width of the experimental EOM with a size of 5 mm, and the dimension along the z-axis is  
 308 the thickness of the experimental EOM with a size of 3 mm.

309 The descent of the indenter continued for 0.2 mm, resulting in  $\delta$  of approximately 0.1 mm.

310 Upon reaching this value of the  $\delta$ , the indenter reversed its direction of travel while adopting the  
 311 bilinear cohesive zone model (CZM) depicted in Fig. 4.b [51, 52].



312  
 313 **Fig. 4.** Schematic diagram of the contact model between the scleral tissue-wrapped indenter and  
 314 the EOM. (a) Finite element meshing diagram. (b) Model of the bilinear cohesive zone between  
 315 the two contact surfaces used to simulate the finite element model.

316 In the finite element simulations, the scleral compressive elastic modulus in the thickness  
 317 direction was derived from the results of the uniaxial compression test on porcine sclera in vitro,  
 318 which are presented in Table 3. The details of this experiment are described in the [Supplementary](#)  
 319 [Material](#). The compressive elastic modulus of the EOM in the thickness direction was obtained  
 320 from the indentation phase of the compressive stress-relaxation test, specifically before the  
 321 relaxation occurs. This elastic modulus was determined by analyzing the experimental results  
 322 using the model proposed by Sneddon and shown in Eq. (10) [53].

$$323 \quad E = \frac{F(1-\nu^2)}{2a\delta}, \quad (10)$$

324 where  $F$  is the applied load,  $\nu$  is the Poisson's ratio,  $a$  is the contact radius, and  $\delta$  is the

325 indentation displacement.

326 To simulate the adhesion behavior between the sclera and the EOM at different separation  
327 velocities, the unloading velocities in the finite element simulation were set to the experimental  
328 values of 0.5, 1, 6, 18, 30, and 42 mm/min, as well as eye saccade velocities of 300, 3000 and  
329 6000 mm/min. The adhesion behavior was primarily determined by the bilinear criterion of the  
330 work of adhesion, specifically the area under the cohesion zone model curve (Fig. 4.b). However,  
331 the exact shape of the cohesive zone model has negligible influence on the overall adhesive  
332 response as long as the area under the cohesive zone model curve remains constant [54].

333 In this study, it was assumed that the adhesion between the scleral tissue-wrapped indenter  
334 and the EOM specimen was simultaneously and independently present in the normal and  
335 tangential directions. Under the interaction module, the cohesive behavior was selected in the  
336 contact property option. The stiffness value of  $K_n$  was set to 20 MPa/mm in the normal direction  
337 and the other two tangential directions, respectively, with the "any slave nodes experiencing  
338 contact" option.

339 The damage criterion adopted in the interaction module was set to "maximum separation",  
340 with values of  $\delta_{n,0}$  was set to  $9 \times 10^{-5}$  mm. Evolution of specify damage was controlled by energy,  
341 and the fracture energy parameter was calculated using Eq. (3) to determine the equivalent work of  
342 adhesion at velocities of 300, 3000, and 6000 mm/min. At a velocity of 0.5 mm/min, the  
343 equivalent work of adhesion was set to  $1.3 \times 10^{-7}$  J/mm<sup>2</sup>. Other parameter settings are shown in the  
344 [Supplementary Material](#).

345 The contact area was meshed using a local seed size of 0.01 mm, while other areas of the  
346 EOM were meshed using unidirectional encrypted seeds with a minimum size of 0.01 mm and a

347 maximum size of 0.2 mm. The sclera was also locally seeded in the contact area with a size of  
348 0.01 mm, while other areas used global seeds with a size of 0.2 mm. When the number of  
349 elements in the finite element model was tripled, the error caused by increasing the number of  
350 elements was 3.6%. From the above results, it is indicated that the finite element meshing is  
351 reasonable and the resulting error can be accepted.

352 The models assumed that the nodes at the bottom boundary of the EOM were completely  
353 fixed, while the nodes on the symmetry axis were restricted in the perpendicular direction of the  
354 symmetry axis. Two analysis steps were defined for the model, both of which were defined as  
355 viscous steps. The contact and pull-off process observed experimentally between the scleral tissue-  
356 wrapped indenter and the EOM was simulated using the displacement control methods.

## 357 **2.6 Eye Movement Model**

358 During eye abduction, both the active contraction force of the LR and the passive force of  
359 MR are essential in maintaining the mechanical balance of the eye [55]. Therefore, this study  
360 focuses on calculating the active moment of the LR ( $M_{ac}$ ) and the passive moment of the MR  
361 ( $M_{pa}$ ) by using the traditional model and the active pulley model. The active pulley model differs  
362 from the traditional model by considering the pulley of the EOMs. Setting the center of the eye at  
363 point O as the (0, 0) point, OXYZ was defined as the stationary coordinate system, and OX'Y'Z'  
364 was defined as the body axes system of the eye. Fig. 5.a illustrates the initial position of the key  
365 points for the LR, with the origin point  $M_1$  (-34.00, -13.00, 0.60), tangent point  $T_1$  (-8.12, 9.39,  
366 0.58), pulley  $P_1$  (-11.00, 10.02, -0.50), and insertion point  $I_1$  (6.50, 10.08, 0.00). Similarly, the  
367 initial position of the key points for MR are  $M_2$  (-30.00, -17.00, 0.60),  $T_2$  (1.82, -12.30, 0.12),

368  $P_2$  (-5.00, -14.40, -0.60), and  $I_2$  (8.42, -9.65, 0.00) [33, 55-57]. Capital letter subscripts are used  
 369 to differentiate the different EOMs. The corresponding translation relations for the coordinates of  
 370 the active pulley can be derived from the study of Demer et al [34]. The coordinate points on the  
 371 eye before and after the eye rotation can be converted by Eq. (11).

$$372 \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} \cos \theta \cos \varphi & \sin \theta \cos \varphi & -\sin \varphi \\ \cos \theta \sin \varphi \sin \psi - \sin \theta \cos \psi & \cos \theta \cos \psi + \sin \theta \sin \varphi \sin \psi & \cos \varphi \sin \psi \\ \sin \theta \sin \psi + \cos \theta \sin \varphi \cos \psi & \sin \theta \sin \varphi \cos \psi - \cos \theta \sin \psi & \cos \varphi \cos \psi \end{bmatrix} \begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} \quad (11)$$

373 Where the rotation angles  $\theta$ ,  $\varphi$ , and  $\psi$  represent the rotation angles around the OZ, OY, and OX  
 374 axes, respectively. During eye abduction, the rotation angles  $\varphi$  and  $\psi$  are equal to  $0^\circ$ . The  
 375 updated geometry of the LR is related to the abduction angle  $\theta$  (Fig. 5.b). In the traditional model,  
 376 the new tangent point  $S_1$  was obtained by substituting the coordinates of the new insertion point  
 377  $I'_1$  and origin point  $M_1$  into Eq. (12). In the active pulley model, the new tangent point was  
 378 obtained by substituting the coordinates of the new insertion point  $I'_1$  and the new pulley  $P'_1$  into  
 379 Eq. (12).

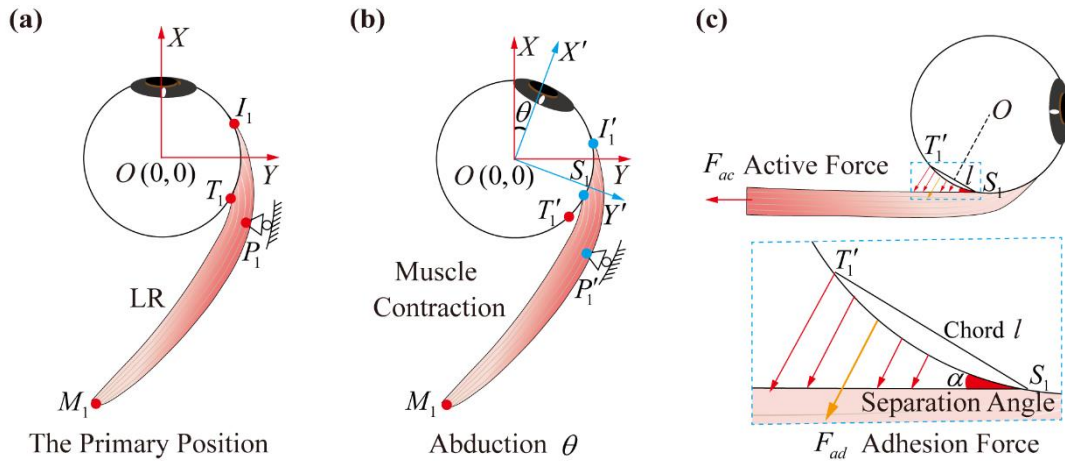
$$380 \begin{cases} x_T^2 + y_T^2 + z_T^2 = R_e^2 \\ x_T x_M + y_T y_M + z_T z_M = R_e^2 \\ (y_M z_I - z_M y_I) x_T + (y_M x_I - x_M z_I) y_T + (x_M y_I - y_M x_I) z_T = 0 \end{cases} \quad (12)$$

381 Where  $R_e$  represents the radius of the eye, with a mean value of 12.43 mm used in this study.

382 When the LR actively contracts, the abduction of the eye will occur. Based on the hypothesis  
 383 proposed by our research group, the separation of the EOM from the sclera during eye abduction  
 384 can be likened to the crack propagation in the adhesion region between the sclera and the EOM  
 385 towards the muscle insertion point on the sclera. This propagation occurs at an equivalent  
 386 separation angle of  $\alpha$ , which corresponds to the eye abduction angle  $\theta$ . Different eye movement

387 velocities correspond to different velocities of crack propagation, and the separation between the  
 388 sclera and the EOM occurs more rapidly during rapid eye movements. The adhesion region during  
 389 eye movement is the area between the tangent points on the sclera and the EOM before and after  
 390 movement. Consequently, in the JKR model, the contact arc length between the sclera and the  
 391 EOM is approximately represented by  $l$  that corresponds to the arc length between the tangent  
 392 points on the sclera. Furthermore, the adhesion force between the sclera and the EOM was  
 393 assumed perpendicular to  $T_1S_1$  (Fig. 5.c). The separation angle  $\alpha$  can be approximately  
 394 described as

$$395 \quad \alpha = (l / R_e) / (180 / \pi) \quad (13)$$



397 **Fig. 5.** Adhesion influences eye motion. (a) The reference coordinate system  $OXY$  depicts the  
 398 primary position of the eye, where  $O$  represents the center of the eye, and  $M_1, T_1, P_1$ , and  $I_1$   
 399 correspond to the origin, tangent, pulley, and insertion points of the LR, respectively. Detailed  
 400 coordinates of the EOM are provided in [Supplementary Material](#). (b) Schematic diagram  
 401 illustrating the EOM in contact with the sclera after the abduction. The rotated coordinate system  
 402 is denoted as  $OX'Y'$ , with  $I_1, P_1$ , and  $T_1$  transformed into  $I_1', P_1'$ , and  $T_1'$ , respectively, as the  
 403 eye is rotated by an angle of  $\theta$ .  $S_1$  represents the new tangent point. (c) Illustration of adhesion

404 between the sclera and the EOM. The active force  $F_{ac}$  separates the EOM from the sclera at an  
 405 angle of  $\alpha$ , creating an adhesion region between the two separated interfaces. The resultant force  
 406 within the adhesion region is denoted as the adhesion force  $F_{ad}$ . The chord  $l$  represents the  
 407 distance between the old tangent point  $T_1'$  and the new tangent point  $S_1$ . The adhesion force acts  
 408 perpendicular to  $T_1'S_1$ , and the length of the arm for the adhesion moment created by this force is  
 409 approximately one-sixth of  $l$ .

410 The mechanical equilibrium within the intraocular system relies on the characteristics of  
 411 orbital tissues and EOMs. The balance of the eye is maintained by the passive moment of MR  
 412 denoted as  $M_{pa}$ , the active moment of the LR denoted as  $M_{ac}$ , the adhesive moment of the  
 413 sclera and the EOM denoted as  $M_{ad}$ , and the resistive moment provided by other tissues in the  
 414 orbit denoted as  $M_t$ . Based on previous studies conducted by our research group, the coordinates  
 415 of each key point of the EOMs before and after eye movement are combined with the equivalent  
 416 rotation angle of the eye [56, 58]. Subsequently, the force exerted by each EOM during the three-  
 417 dimensional movement of the eye can be determined using Eq. (14), which governs the balance of  
 418 eye movement.

$$419 \quad M_{ac} - M_{ad} - M_{pa} - M_t = 0 \quad (14)$$

420 According to a previous study, in Eq. (14), the resistance moment  $M_t = 12.43\theta K_t R_e$ , the  
 421 limiting stiffness  $K_t = 1.245$  mN/deg and the active moment  $M_{ac} = F_{ac} \times R_e$ , where  $F_{ac}$  denotes  
 422 the active force of the LR [59, 60]. The adhesion moment  $M_{ad} = F_{ad} \times l / 6$ , where  $F_{ad}$  denotes  
 423 the adhesion force. We use the maximum adhesion force (pull-off force) when calculating the  
 424 adhesion moment. In addition, to calculate the effect of the adhesion moment on eye movements,  
 425 we calculated the adhesion moment ratio to the total moment, which can be expressed as the ratio

426 of  $M_{ad}$  to the summation of  $M_{ac}$ ,  $M_{pa}$ ,  $M_{ad}$ , and  $M_t$ .

427 According to the relevant literature, The formula for the passive moment is  $M_{pa} = F_{pa} \times R_e$ ,

428 where  $F_{pa}$  can be obtained from Eq. (15) [61].

$$429 \quad F_{pa} = b \frac{A_0}{L_0^3} \Delta L^3 + c \frac{A_0}{L_0^2} \Delta L^2 + d \frac{A_0}{L_0} \Delta L \quad (15)$$

430 In Eq. (15), the MR cross-sectional area  $A_0=17.4\text{mm}^2$ , the initial length  $L_0=39.4\text{mm}$ , the

431 length change  $\Delta L = L - L_0$ ,  $L$  is the length of the MR after the corresponding eye rotation. The

432  $b$ ,  $c$ , and  $d$  are constants, where  $b=23.9$ ,  $c=8.4$ , and  $d=0.8$ , respectively [56].

## 433 2.7 Velocity Conversion Relationship

434 Different units of velocity were used to describe the corresponding results. The specific

435 velocity conversion relationship is shown in Table 4.

436 **Table 4.** Velocity conversion relationship.

Unloading velocity (mm/min)	Dimensionless velocity $\hat{V}$	Eye movement velocity (deg/s)
0.5	4	0.04
1	7	0.08
6	42	0.5
18	127	1.4
30	212	2.3
42	297	3.2
300	2119	23
3000	21186	231
6000	42373	461

437



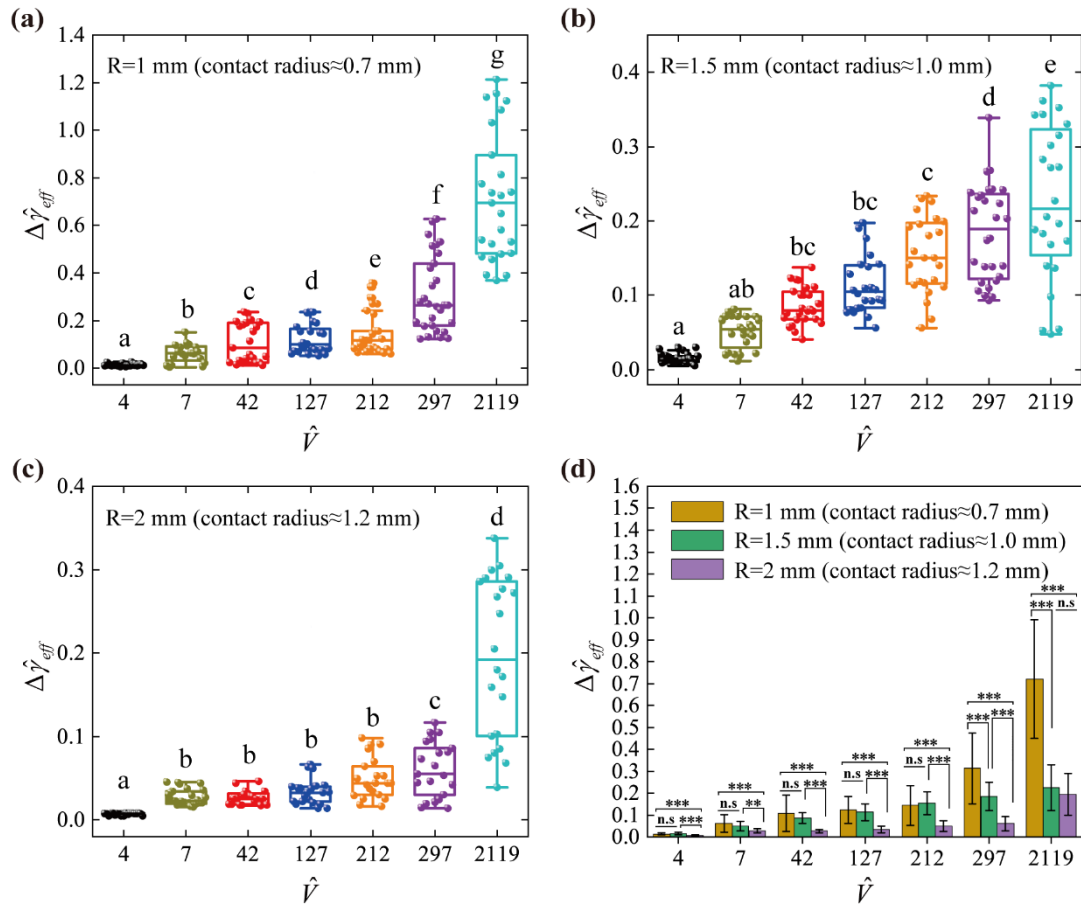
## 438 **2.8 Statistics**

439 The experimental data obtained in this study were presented as mean  $\pm$  standard deviation  
440 (s.d.). The statistical analysis was evaluated using a one-way analysis of variance (ANOVA)  
441 subjected to an LSD test using SPSS v.26.0 (SPSS Inc., Chicago, IL, USA). For experimental  
442 groups with different velocities, Tukey's *post-hoc* test was used to distinguish the differences. A  
443 probability value (**p**) of less than 0.05 was considered indicative of statistical significance.

## 444 **3. Results**

### 445 **3.1 Experimental results of adhesion behavior between** 446 **EOMs and sclera**

447 **Fig. 6** shows the analysis of the dimensionless equivalent work of adhesion  $\Delta\hat{\gamma}_{eff}$  as a  
448 function of the dimensionless unloading velocity  $\hat{V}$ . The figure shows the indenter radius and the  
449 average contact radius. The results show that  $\Delta\hat{\gamma}_{eff}$  is velocity dependent at contact radii at the  
450 sub-millimeter level with an indenter radius of 1 mm. With an indenter radius of 1.5 mm, the  
451 contact radius is between sub-millimeter and millimeter-level thresholds, and  $\Delta\hat{\gamma}_{eff}$  is some  
452 velocity dependent. In addition, the results showed that there is velocity dependence between  
453 quasi- and non-quasi-static velocities (e.g.,  $\hat{V} = 212$  and  $\hat{V} = 297$ ), regardless of whether the  
454 contact radius is sub-millimeter or millimeter. In the subsequent analysis, we took the case with  
455 the indenter radius of 1 mm as an example.



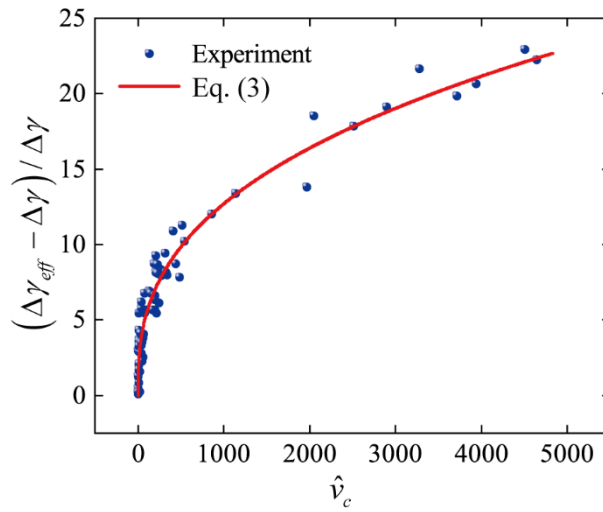
456

457 **Fig. 6.** Analysis of the dimensionless equivalent work of adhesion  $\Delta\hat{\gamma}_{eff}$  as a function of the  
 458 dimensionless unloading velocity  $\hat{V}$ . The experimental data and their dispersion are presented  
 459 through box plots.  $\Delta\hat{\gamma}_{eff}$  were measured at each  $\hat{V}$  using a one-way ANOVA (\*\* indicates  $p <$   
 460  $0.01$  and \*\*\* indicates  $p < 0.001$ , respectively; and signed by n.s indicate no statistical differences  
 461 among the groups with  $p > 0.05$ ). Differences between values with different lowercase letters were  
 462 significant ( $p < 0.05$ ). Identical letters on the same box plots are statistically similar. The figure  
 463 represents experimental results with an indenter radius of (a) 1mm (contact radius is 0.7 mm), (b)  
 464 1.5mm (contact radius is approximately 1.0 mm), and (c) 2mm (contact radius is approximately  
 465 1.2 mm). (d) Significance analysis of different radius indenter.

466

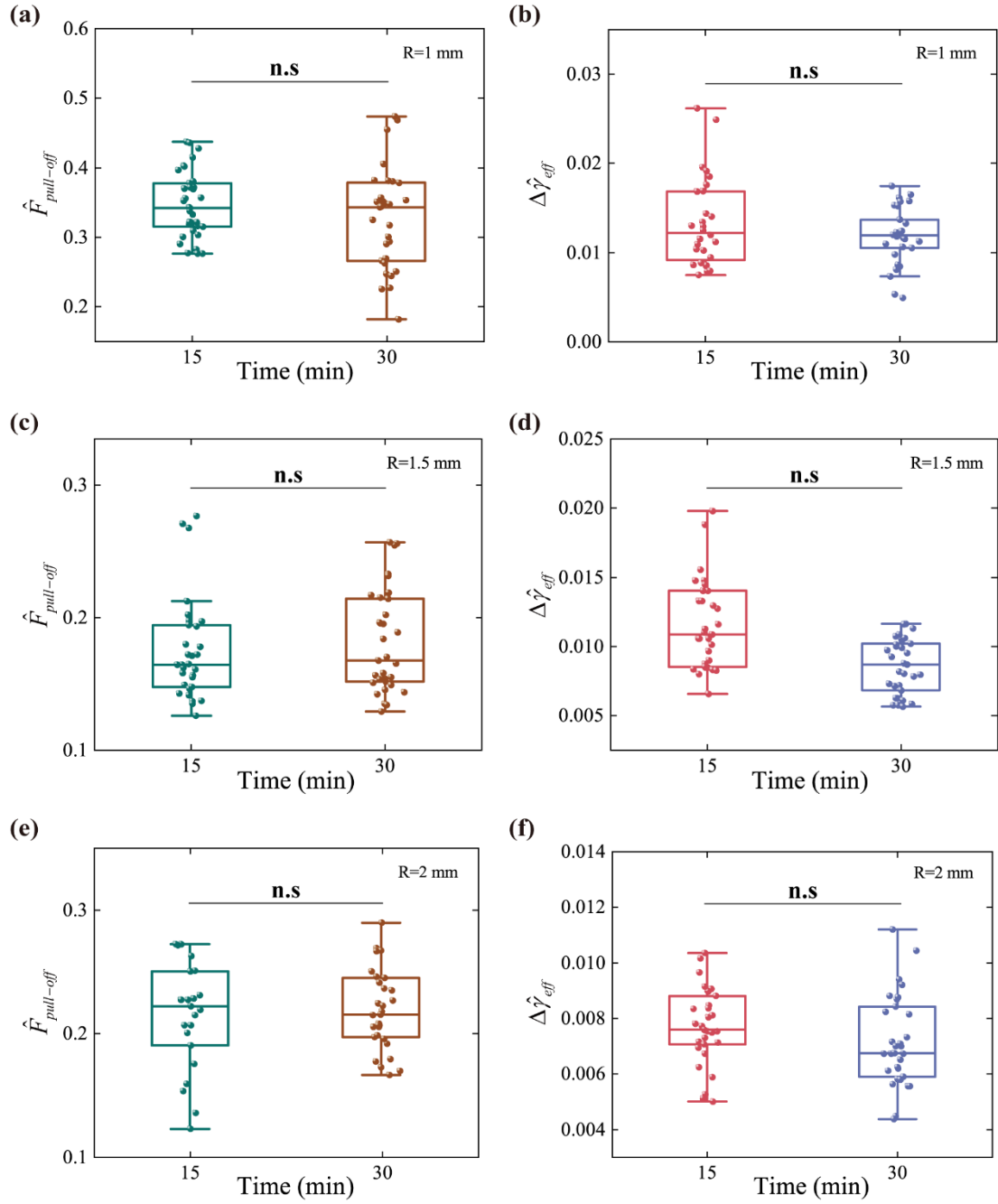
To enhance the generalizability of the results, all important parameters were transformed into  
 467 dimensionless parameters. Fig. 7 illustrates the experimental dimensionless contact line velocity

468  $\hat{v}_c$  plotted against the relative increase in the work of adhesion  $(\Delta\gamma_{eff} - \Delta\gamma) / \Delta\gamma$ . The best fit  
 469 trend curve by Eq. (3), whose parameters were  $n = 0.368$  and  $v^* = 0.00236$  mm/s, will then be  
 470 normalized, indicated by the red line. The results demonstrate a correlation between  
 471  $(\Delta\gamma_{eff} - \Delta\gamma) / \Delta\gamma$  and  $\hat{v}_c$ , suggesting that the velocity dependence cannot be neglected in  
 472 considering the adhesion of viscoelastic materials.



473  
 474 **Fig. 7.** Experimental dimensionless contact line velocity  $\hat{v}_c$  versus relative increase in the work of  
 475 adhesion  $(\Delta\gamma_{eff} - \Delta\gamma) / \Delta\gamma$ . The blue dots were obtained from the experimental contact radius  
 476  $a$ , while the red line was theoretical predictions based on Eq. (3), where the parameters of the  
 477 fitted curve are chosen as  $n = 0.368$  and  $v^* = 0.00236$  mm/s.

478 In addition to the aforementioned results, the adhesion behavior of the EOM was examined  
 479 under various durations of air exposure, with a velocity of 0.5 mm/min. The analysis revealed no  
 480 significant difference ( $p > 0.05$ ) between the specimen groups exposed to air for 15 and 30  
 481 minutes (Fig. 8).



482

483 **Fig. 8.** The relationship between dimensionless pull-off force  $\hat{F}_{pull-off}$  and exposure times of  
 484 EOM and the relationship between equivalent work of adhesion  $\Delta\hat{\gamma}_{eff}$  and exposure times of  
 485 EOM. The radius of the indenter is labeled in the upper right corner of each figure. (The **n.s.**  
 486 indicates no statistically significant difference between groups, representing  $p > 0.05$ ).

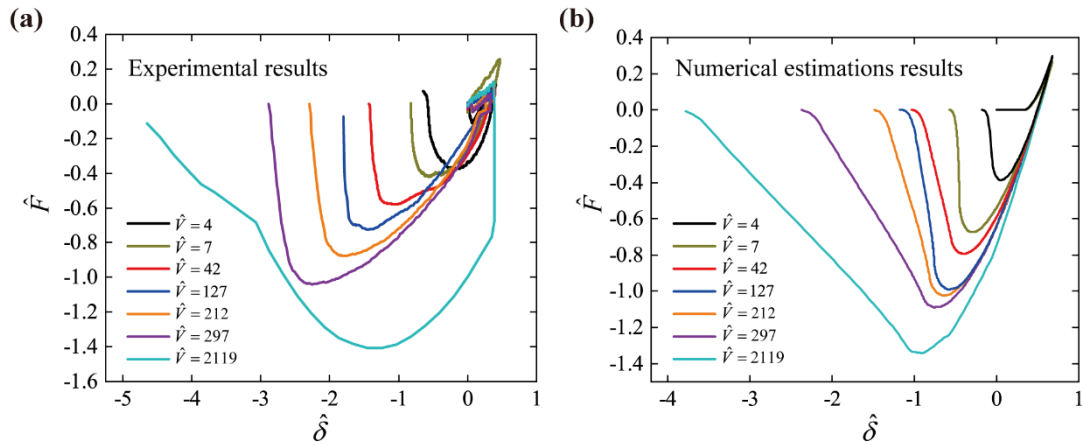
## 487 **3.2 Numerical estimations of adhesion behavior between** 488 **EOMs and sclera**

### 489 **3.2.1 Model validation**

490 The finite element setup was the same as in the experiments. The finite element results were  
491 compared with the experimental results to validate models. Fig. 9.a illustrates the relationship  
492 between the dimensionless penetration depth  $\hat{\delta}$  and adhesion force  $\hat{F}$  for the tests at various  
493 velocities ( $\hat{V}=4, 7, 42, 127, 212, 297,$  and  $2119$ ), while Fig. 9.b displays the relationship between  
494  $\hat{\delta}$  and  $\hat{F}$  obtained using the finite element simulations at different velocities. The force-  
495 displacement curves during unloading differ from those during loading due to viscoelastic energy  
496 dissipation during the separation of the sclera from the EOM. As the unloading velocity increases,  
497 the pull-off force between the sclera and EOM increases, along with an increase in the pull-off  
498 force corresponding to the separation displacement. From Fig. 9.a, it is observed that  
499 dimensionless pull-off force  $\hat{F}_{pull-off}$  increases by 135% when  $\hat{V}$  increases from 4 to 212 in the  
500 experiments. Moreover, when  $\hat{V}$  increases from 212 to 297, the corresponding increase in  
501  $\hat{F}_{pull-off}$  is 18%. As  $\hat{V}$  further increases from 297 to 2119 (614% increase),  $\hat{F}_{pull-off}$  only  
502 increases by 37%.

503 Fig. 9.b also shows that in the finite element simulation, as  $\hat{V}$  increases from 4 to 212,  
504  $\hat{F}_{pull-off}$  increases by 166%. Similarly, when  $\hat{V}$  increases further from 212 to 297, the  
505 corresponding increase in  $\hat{F}_{pull-off}$  is 7%, which is similar to the increase observed experimentally.  
506 According to the FEM prediction, when  $\hat{V}$  increases from 297 to 2119 (614% increase),  $\hat{F}_{pull-off}$   
507 only increases by 23%. A further inspection of the  $\hat{\delta}$  -  $\hat{F}$  behavior obtained numerically and

508 experimentally shows trend consistency in most values considered of  $\hat{V}$ , Fig. 9.



509

510 **Fig. 9.** Model validation of adhesion behavior between sclera and EOM at different unloading

511 velocities. (a) Contact and pull-off test of dimensionless indentation displacement  $\hat{\delta}$  and adhesion

512 force  $\hat{F}$  curves between the sclera and EOM at different unloading velocities, where the different

513 color curves correspond to  $\hat{V}=4, 7, 42, 127, 212, 297,$  and  $2119$ . (b) Finite element simulation of

514  $\hat{\delta}$  and  $\hat{F}$  profiles between the sclera and EOM at different unloading velocities.

### 515 3.2.2 Numerical estimations results

516 In this section, finite element results on the adhesion between the sclera and the EOMs were

517 presented. A loading scheme, resembling the experimental setup, was implemented in the finite

518 element model. The nephograms of normal stress corresponding to  $\hat{V}=42$  were selected for visual

519 representation (Fig. 10). The deformation pattern of the EOM model is very similar to the

520 experimentally captured images.

521 The analysis involved four steps:

522 (i) Initially, the axisymmetric scleral tissue-wrapped indenter gradually approached the EOM.

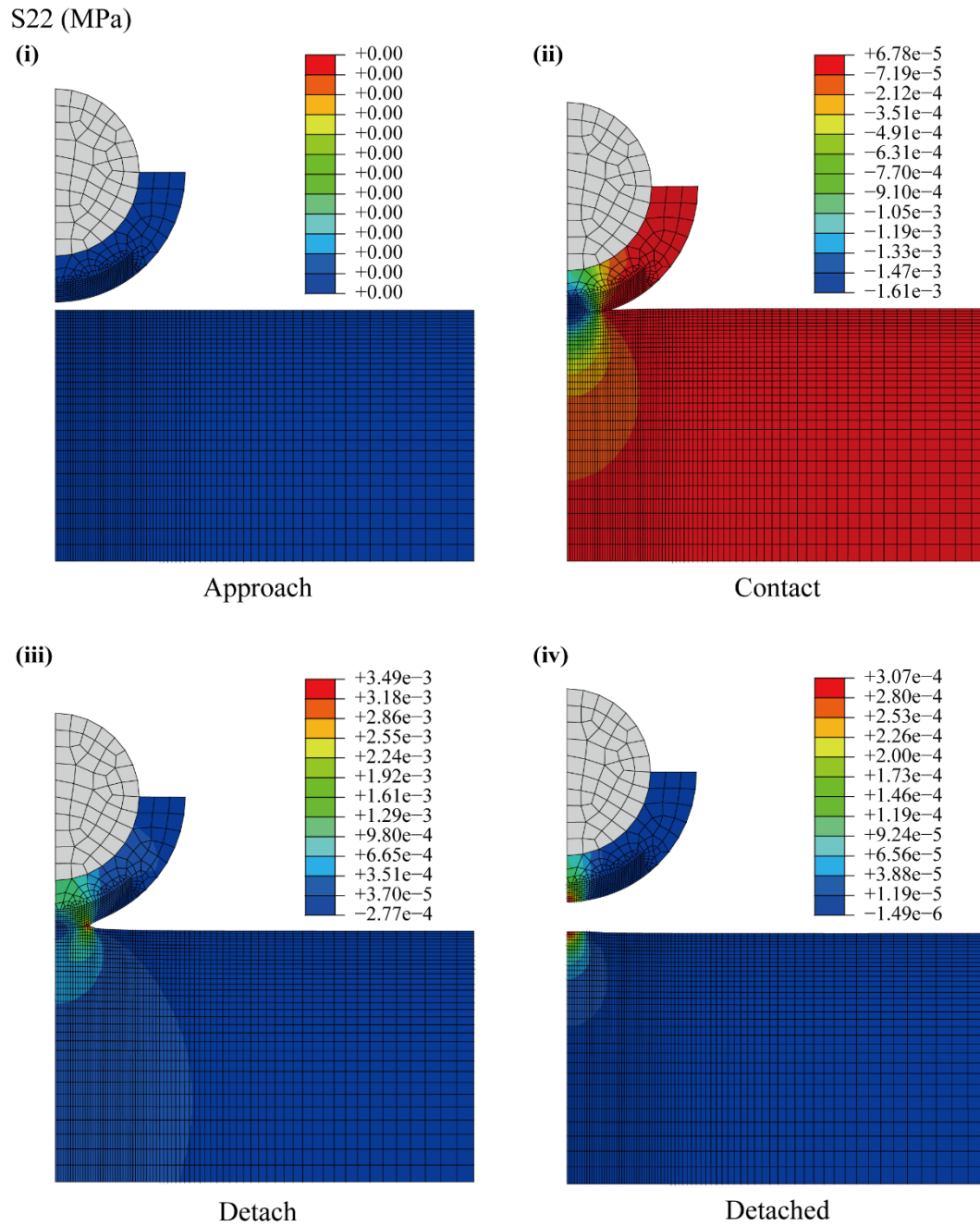
523 At this stage, the two interfaces were not in contact, resulting in no generation of normal stress on

524 the surface of the EOM.

525           (ii) The indenter was then pressed to a predefined maximum value of 0.1mm, leading to the  
526 generation of the maximum negative normal stress on the EOM.

527           (iii) While maintaining the contact area, the indenter was lifted upwards at different velocities.  
528 This means that the previously contacted area was not allowed to separate until the pull-off force  
529 was reached. Once the pull-off force was reached, the separation of the EOM from the scleral  
530 interface began.

531           (iv) The indenter continued to be lifted until the two surfaces were completely separated.  
532 However, due to the viscoelastic nature of the EOM substrate, residual stresses persisted for some  
533 time even after the separation was achieved.



534

535 **Fig. 10.** Normal stress results for the EOM near the contact area in each stage of the finite element

536 simulation, showing only the results for the axisymmetric system in the x-z plane.

537 [Fig. 11](#) shows the contact stress pressure distribution between the sclera and the EOM at

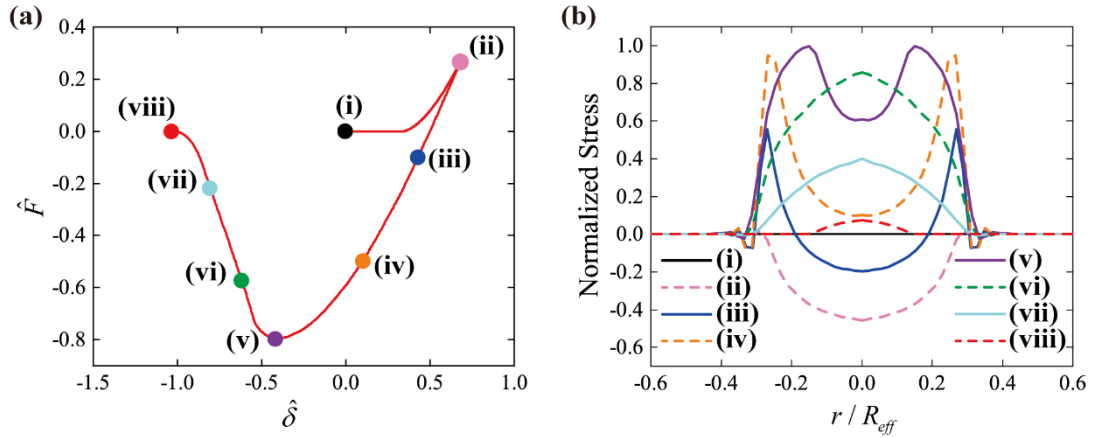
538 different phases of loading and unloading. [Fig. 11.a](#) illustrates the dimensionless force-

539 displacement curve between the sclera and the EOM. [Fig. 11.b](#) presents the normalized stress

540 distribution on the surface of the EOM, with the horizontal axis representing  $r/R_{eff}$  and the



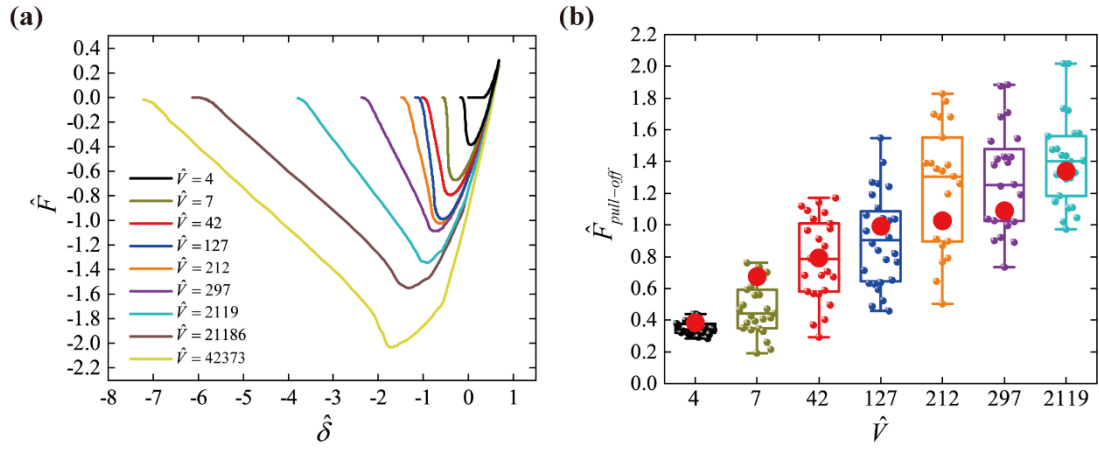
541 vertical axis representing the normalized normal stress  $\sigma_n / \sigma_{n,\max}$ . The phases of loading and  
 542 unloading represented by the roman numerals in Fig. 11.a and Fig. 11. b correspond to each other.  
 543 The  $\sigma_{n,\max}$  is observed at the edge of the contact region between the sclera and the EOM, with a  
 544 value of  $3.49 \times 10^{-3}$  MPa. Fig. 11.b reveals that as the interface gradually separates, the maximum  
 545 normal stress shifts from the edge towards the center of the contact area. The stress distribution on  
 546 the EOM surface aligns with the findings from previous finite element simulations and is  
 547 consistent with the assumptions of classical theory [12, 31].



548  
 549 **Fig. 11.** Analysis of the results of the adhesion behavior between the sclera and the EOM. (a)  
 550 Dimensionless adhesion force-displacement plots for specimens with an unloading velocity of 6  
 551 mm/min in the experiment, in which the roman serial numbers indicate the different stages of the  
 552 adhesion process in the finite element simulation. (b) The contact pressure distribution over the  
 553 contact area of the EOM at different stages of the finite element simulation.

554 Fig. 12.a illustrates the relationship between  $\hat{\delta}$  and  $\hat{F}$  for the finite element simulations at  
 555 different velocities, which additionally predict velocities of  $\hat{V} = 2119, 21186, \text{ and } 42373$ . From  
 556 the figure, it is evident that as  $\hat{V}$  increases from 2119 to 42373 (1900% increase),  $\hat{F}_{\text{pull-off}}$   
 557 increases 51% times, indicating a relatively inconsiderable increase. Fig. 12.b presents the  
 558 variation of the experimental and finite element  $\hat{F}_{\text{pull-off}}$  with  $\hat{V}$ . Box line plots show the

559 experimental data and their scattering, and big red dots indicate the finite element results using the  
 560 average work of adhesion calculated by Eq. (3) as the input parameter.



561  
 562 **Fig. 12.** Analysis of adhesion behavior between sclera and EOM at different unloading velocities.

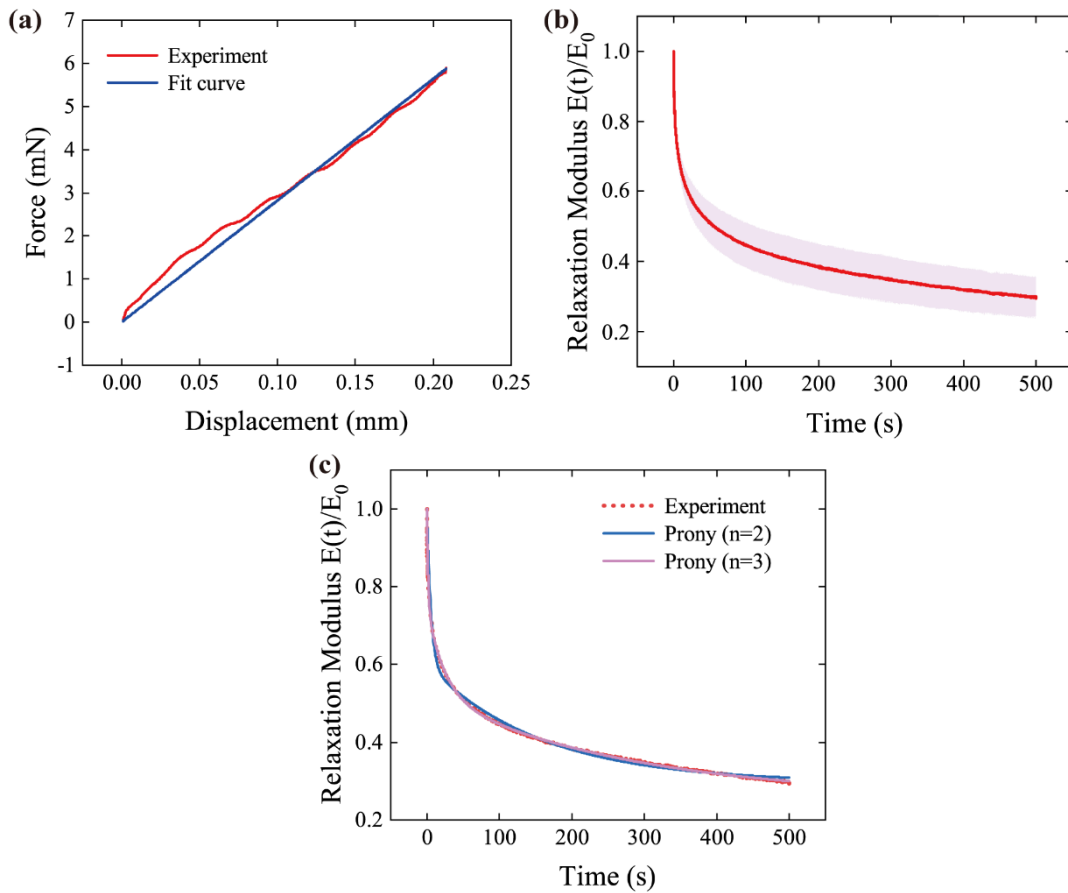
563 **(a)** Finite element simulation of dimensionless indentation displacement  $\hat{\delta}$  and adhesion force  $\hat{F}$   
 564 curves between the sclera and EOM at different unloading velocities, where the different color  
 565 curves correspond to  $\hat{V} = 4, 7, 42, 127, 212, 297, 2119, 21186,$  and  $42373$ . **(b)** Variation of  
 566 experimental and finite element dimensionless pull-off force  $\hat{F}_{pull-off}$  with dimensionless  
 567 unloading velocity  $\hat{V}$ . Box line plots show the experimental data and their scattering, and big red  
 568 dots indicate the finite element results using the average work of adhesion calculated by Eq. (3) as  
 569 the input parameter.

### 570 **3.3 Biomechanical properties of the EOM along the** 571 **thickness direction**

572 The force-displacement curves obtained from compressive stress-relaxation tests conducted  
 573 on the EOM along the thickness direction are presented in Fig. 13.a, and the plot of normalized  
 574 relaxation modulus against time is depicted in Fig. 13.b. The mean value is represented by the red  
 575 line, while the shaded region corresponds to the standard deviation of measurements. The

576 elasticity modulus of the EOM along the thickness direction was determined through fitting using  
 577 Eq. (10), resulting in a value of  $4.34 \pm 2.34$  kPa (average fit  $R^2 = 0.934$ ).

578 To generate data applicable in the finite element software Abaqus, the Prony series was fitted  
 579 to the normalized relaxation modulus curves (Fig. 13.c). The parameters of the second-order Prony  
 580 series (curve fit  $R^2 = 0.989$ ) were obtained as follows:  $g_1=0.40$ ,  $\tau_1=5.39$ s,  $g_2=0.30$ ,  $\tau_2 =$   
 581  $156.60$ s. Additionally, the parameters of the third-order Prony series (curve fit  $R^2 = 0.999$ ) were  
 582 determined as follows:  $g_1=0.25$ ,  $\tau_1=1.72$ s,  $g_2=0.23$ ,  $\tau_2=23.94$ s,  $g_3=0.27$ , and  $\tau_3=276.17$ s.  
 583 The above material parameters are organized in Table 3. Fig. 13.c shows the results of the least  
 584 squares regression method used to fit the EOM specimens to the Prony series at a 10% strain level,  
 585 indicating that the third-order Prony series provides a better fit.



586

587 **Fig. 13.** Analysis of EOM compressive stress-relaxation tests. The red line represents the mean

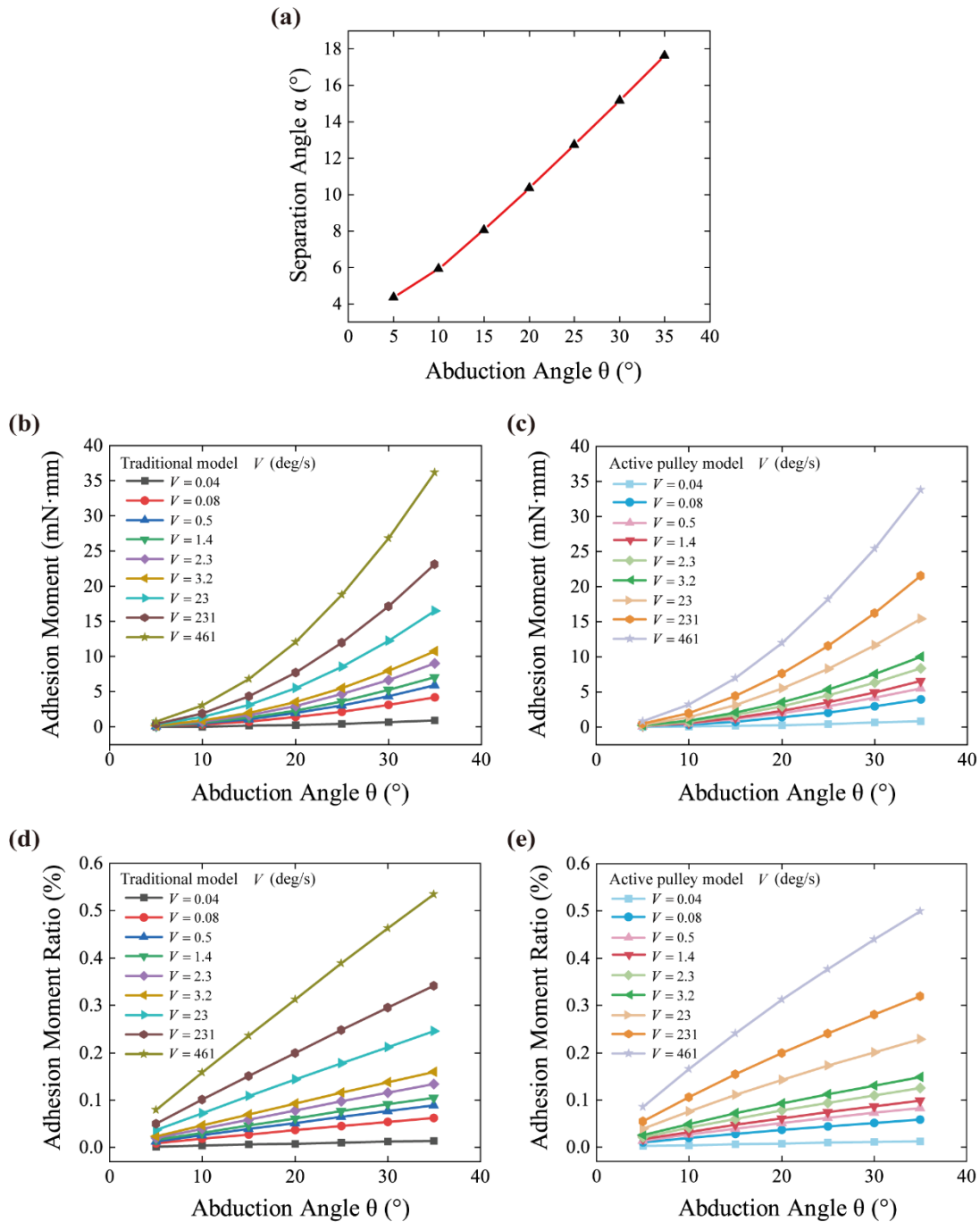
588 value of the experimental curve, and the shaded area indicates the standard deviation. (a)  
589 Compressive stress-relaxation tests were conducted on EOM specimens along the thickness  
590 direction. (b) Variation of normalized relaxation modulus with time for EOM specimens at a 10%  
591 strain level. (c) Least-squares regression fitting of Prony series to EOM specimens at a 10% strain  
592 level.

### 593 **3.4 Adhesion moment**

594 Through the calculation of the equilibrium equation of eye motion, it becomes evident that  
595 the separation angle  $\alpha$  exhibits a linear increase with the increment of the eye abduction angle  $\theta$   
596 (Fig. 14.a). The results show the adhesion moments for the traditional model and the active pulley  
597 model, as well as the adhesion moment ratio to the total moment for both models. The adhesion  
598 moment also shows an increase in correlation with both the eye abduction angle and the velocity  
599 of separation of the EOM from the sclera (Fig. 14.b and Fig. 14.c). Additionally, the adhesion  
600 moment between the sclera and the EOM experiences an augmentation as the eye undergoes  
601 abduction, resulting in a corresponding rise in the adhesion moment ratio to the total moment (Fig.  
602 14.d and Fig. 14.e). In the traditional model, the adhesion moment ratio to the total moment was  
603 0.002% to 0.01% at  $V = 0.04$  deg/s for eye abduction angles within the range of  $5^\circ$  to  $35^\circ$ .  
604 However, the adhesion moment ratio to the total moment in the range of  $5^\circ$  to  $35^\circ$  of eye  
605 abduction was approximately 0.08% to 0.53% when  $V = 461$  deg/s. The maximum adhesion  
606 moment increased from 0.76 mN·mm to 36.2 mN·mm. In the active pulley model, the adhesion  
607 moment ratio to the total moment was 0.002% to 0.01% at  $V = 0.04$  deg/s for eye abduction angles  
608 within the range of  $5^\circ$  to  $35^\circ$ . However, the adhesion moment ratio to the total moment in the

609 range of  $5^\circ$  to  $35^\circ$  of eye abduction was approximately 0.09% to 0.50% when  $V = 461$  deg/s. The

610 maximum adhesion moment increased from 0.83 mN·mm to 33.8 mN·mm.



611

612 **Fig. 14.** Analysis results of the adhesion moment between the sclera and the EOM. (a)

613 Relationship between the separation angle  $\alpha$  of the sclera and the EOM and the abduction angle

614  $\theta$ . Relationship between the adhesion moment and the abduction angle  $\theta$  for different velocities

615 of the sclera and EOM separation in (b) traditional model and (c) active pulley model.  
616 Relationship between the percentage of adhesion moment and the abduction angle  $\theta$  at different  
617 velocities of the sclera and EOM separation in (d) traditional model and (e) active pulley model.

## 618 4. Discussion

619 Previous studies often neglected the contact behavior between the sclera and the EOMs.  
620 However, the adhesion behavior between the scleral tissue-wrapped indenter and the EOMs was  
621 observed in the contact and pull-off tests conducted in this paper. The adhesion force-displacement  
622 trend of EOM-scleral tissue adhesion (Fig. 9.a) aligns with the adhesion force-displacement curve  
623 observed in facial adhesion experiments conducted by Dai et al. [9]. According to Muller's  
624 description, the pull-off force varies with the unloading velocity, with higher unloading velocities  
625 resulting in higher pull-off forces [22]. Moreover, the area enclosed under the force-displacement  
626 curve increases as the unloading velocity increases, indicating that the work of adhesion also  
627 increases with the unloading velocity.

628 Furthermore, contact and pull-off tests were performed using indenters with radii of 1 mm,  
629 1.5 mm, and 2 mm at various unloading velocities (Fig. 6). In a previous study, it was also  
630 observed that variations in indenter radius at the sub-millimeter and millimeter levels caused  
631 differences in the work of adhesion [62]. This sensitivity of the sub-millimeter contact radius to  
632 size may be the source of the difference in results. In addition to the differences caused by indenter  
633 size, between quasi-static and non-quasi-static velocities, the dimensionless equivalent work of  
634 adhesion  $\Delta\hat{\gamma}_{eff}$  for the indenters is also statistically different. Therefore, if adhesion behavior  
635 under the high eye movement velocity is to be considered, the viscoelasticity of the tissue should

636 be taken into account.

637 To investigate the impact of the duration of EOM exposure to air on adhesion behavior,  
638 experiments were performed with different exposure times. Clinicians typically perform EOM  
639 surgery for approximately 30 minutes [63]. The exposure time was divided into 15-minute and 30-  
640 minute groups, and the results in Fig. 8 showed no significant differences between these two  
641 groups.

642 In combination with the results of the experiments and the finite element model in this study,  
643 it was observed that the pull-off force between the sclera and the EOM gradually increased with  
644 the increase of unloading velocities (Fig. 9). However, the rate of increase in the pull-off force  
645 diminished at higher unloading velocities. Despite the different materials studied, Jiang et al.  
646 found similar trends in their finite element simulations of contact between viscoelastic stamps and  
647 spherical transfer elements [30]. Han et al. effectively revealed the adhesion rates of articular  
648 cartilage tissues at various unloading velocities through experimental studies [21]. Naraghi et al.  
649 report a simple method for extending the range of controlled adhesion of a stamp, which can be  
650 achieved by adjusting the thickness of the elastic layer and the separation rate [64]. Das et al.  
651 conducted a comprehensive investigation on the adhesion behavior of polyacrylonitrile nanofibers,  
652 focusing specifically on its dependence on the velocity of unloading [65]. Their findings revealed  
653 a consistent and progressive improvement in the apparent adhesion as the unloading velocity  
654 increased. These findings are in line with the results obtained in this study.

655 In this study, we determined the elastic modulus and viscoelastic parameters of the EOMs  
656 along the thickness direction through compressive stress-relaxation tests. When the EOMs  
657 regulate eye movements by active contraction and passively stretched, and the force direction of

658 the EOM is mainly along the length direction. For this reason, many scholars have focused on the  
659 tensile elastic modulus of the EOM along the length direction, for example, Jeong et.al set the  
660 elastic modulus of the EOMs to 0.09 MPa in finite element modeling [66]; Schutte et al. used a  
661 value of 40 kPa as the elastic modulus of the EOMs input into the finite element model [60]. The  
662 EOM wraps around the eyeball, causing the EOM and sclera to squeeze against each other.  
663 Therefore, the elastic modulus of the EOM along the thickness direction is particularly important  
664 in analyzing the adhesion between the sclera and the EOMs in this work. Up to now, there are few  
665 reports about the compressive modulus of the EOM. Therefore, the compressive modulus of the  
666 EOMs was tested in this study and was found to be 4.34 kPa.

667 When considering the viscoelastic properties of the EOM itself, there are two fundamental  
668 linear viscoelastic modeling approaches: the Maxwell model and the Voigt model [67]. The  
669 Maxwell model predicts relaxation behavior and describes how a material returns to equilibrium  
670 after being deformed by external disturbances. However, it is unable to accurately predict creep,  
671 which refers to the tendency of a material to undergo permanent deformation under a constant  
672 force. On the other hand, the Voigt model effectively describes creep but is less proficient in  
673 predicting relaxation [2]. Nonetheless, neither of these models adequately captures the viscoelastic  
674 properties of the EOMs. To address these limitations, we ultimately opted for the Wiechert model,  
675 which is constructed as a linear combination of multiple springs and buffers, offering a more  
676 comprehensive representation of the EOM's viscoelastic behavior.

677 The elastic modulus of the sclera has been reported a lot recently, but not what was needed in  
678 this study. Many researchers focused on the tensile elastic modulus of the sclera. For example,  
679 Nguyen et.al measured the tensile modulus of the human sclera to be 2.5 MPa in 2020 [68]. In



680 2021, Park et.al found that the tensile elastic modulus of the human sclera varied in the anterior,  
681 equatorial, and posterior portions of the sclera, which resulted in a tensile modulus of  
682 approximately 30.8 MPa in the anterior sclera, 17.7 MPa in the equatorial portion of the sclera,  
683 and 13.3 MPa in the posterior portion of the sclera [69]. In the same year, Hatami-Marbini et al.  
684 reported that the equilibrium tensile modulus of the porcine sclera was 3-7 MPa [70]. Although  
685 several researchers had also measured the compressive elastic modulus of the sclera along the  
686 thickness, not about the sclera between the anterior and equatorial position of the eye, mainly  
687 studying the posterior sclera. For example, in 2009, Mortazavi et.al determined the compressive  
688 modulus of the human and porcine peripapillary sclera to be 1.1 kPa and 3.9 kPa, respectively [71].  
689 In 2014, Worthington et al. measured the compressive modulus of the posterior porcine sclera to  
690 be approximately 35 kPa [72]. In 2021, Brown et al. derived from unconfined compression  
691 experiments that the average compressive stiffness of the porcine sclera near the optic nerve head  
692 was 10 kPa [73]. The scleral compressive modulus between the anterior and equatorial portions  
693 measured in this study was approximately 11.2 kPa, which is in the same order of magnitude as  
694 previously reported compressive moduli.

695 In this study, a 2D axisymmetric finite element model was developed to simulate the  
696 interaction between a scleral tissue-wrapped indenter and the EOM. The model considered the  
697 viscoelastic properties of the substrate and employed the JKR-like viscoelastic model to calculate  
698 the equivalent work of adhesion in the 2D simulation. However, it should be noted that the JKR-  
699 like viscoelastic model assumes the substrate to be a half-space, whereas the EOM is not of  
700 infinite thickness. To address this, we set a very small indentation displacement and concluded,  
701 based on Shull's description of finite thickness, that the substrate thickness does not significantly

702 impact the experimental results under the conditions of this study [74].

703 By comparing the finite element results with the experimental data, it is found that the  
704 dimensionless indentation displacement  $\hat{\delta}$  and adhesion force  $\hat{F}$  of both have the same trend.  
705 The dimensionless pull-off force  $\hat{F}_{pull-off}$  of finite element calculations were within the range of  
706 experimental scatter, confirming the accuracy of the model in describing the interfacial bond and  
707 the viscoelastic properties of the EOM (Fig. 12.b).

708 In this study, the approximation of the indenter's unloading velocity was based on the  
709 separation velocity between the sclera and the EOM. This unloading velocity was then utilized to  
710 determine the magnitude of the equivalent work of adhesion, which was subsequently  
711 incorporated into the equilibrium equation of eye movement to calculate the adhesion moment  
712 (Fig. 14.b and Fig. 14.c). The analysis aimed to assess the impact of the adhesion moment on eye  
713 movement.

714 Since there is no previous report about the in vivo measurement of the adhesion behavior  
715 between the LR and the sclera, we chose to verify the active force of the LR. Collins et al.  
716 measured the active force of the LR in humans during surgery and reported values of 316.5 mN  
717 when the right eye was abducted at an angle of 15° and 487.4 mN at 30° of eye abduction [59]. In  
718 our study, the calculated active force of the LR at quasi-static velocities was within the range of  
719 234.8 mN to 236.9 mN at 15° of eye abduction and 473.9 mN to 482.4 mN at 30° of eye abduction.  
720 The consistency between our calculated values and the previous reports verifies the accuracy of  
721 our results.

722 In this paper, several limitations need to be addressed in future studies. Firstly, due to the  
723 difficulty in obtaining human tissues, parameters obtained from porcine eyes were used to analyze

724 the human oculomotor model. This results in a potential bias in the obtained results.

725       Furthermore, it is important to acknowledge that the adhesion area between the sclera and the  
726 EOM contains other tissues such as body fluids and fat in actual oculomotor processes. These  
727 additional factors may potentially influence the measurement of adhesion work and could be  
728 considered in future investigations. Additionally, in the finite element modeling process, a 2D  
729 axisymmetric model was used to improve the computing efficiency.

730       Lastly, for the contact and pull-off tests, we used in vitro EOMs. However, in the physical  
731 situation, the muscle would remain active and the muscle tension would counteract some of the  
732 adhesion forces. Also, the dryness and humidity of the muscle differed from the in vitro conditions.  
733 The adhesive behavior between the sclera and the EOM in the physical situation is not fully  
734 understood and requires further study.

735       Addressing these shortcomings will contribute to a more comprehensive understanding of the  
736 oculomotor system and the adhesion behavior between the sclera and the EOM in realistic  
737 physiological conditions.

## 738 **5. Conclusion**

739       During eye movements, adhesion between the sclera and the EOMs occurs. This study aimed  
740 to understand the adhesion between the porcine sclera and the EOMs at different velocities. At the  
741 saccade velocities, the adhesion moment was found to be 0.53% and 0.50% of the total moment  
742 based on the traditional and active pulley models, respectively. Although the adhesion effect is  
743 increasing at high eye movement velocities, the effect on eye movements remains minimal.  
744 According to the results of the study, the effect of adhesions between the sclera and the EOMs on

745 eye movement can be ignored. Knowledge of the adhesion behavior between the sclera and the  
746 EOMs can supplement a portion of the unknown quantities in the equations of eye movement,  
747 resolving the contradiction between the number of equations and the mismatch of unknown  
748 quantities. Furthermore, when this adhesion behavior is considered in eye modeling, it can be  
749 ignored, thus simplifying the model reasonably well.

### 750 **Declaration of Competing Interest**

751 The authors declare that they have no known competing financial interests or personal  
752 relationships that could have influenced the work reported herein.

### 753 **Author Statement**

754 **Hongmei Guo:** Conceptualization, Investigation, Writing-review & editing, Funding acquisition,  
755 Supervision, Project administration. **Yunfei Lan:** Formal analysis, Investigation, Writing-original  
756 draft, Visualization, Software, Methodology. **Zhipeng Gao:** Resource, Funding acquisition,  
757 Methodology. **Chenxi Zhang:** Investigation, Software. **Liping Zhang:** Formal analysis,  
758 Investigation. **Jianying Lin:** Supervision. **Xiaona Li:** Investigation, Funding acquisition. **Ahmed**  
759 **Elsheikh:** Writing-review & editing. **Weiyi Chen:** Supervision, Funding acquisition.

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